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Taller 05: Mínimos Cuadrados

GR1CC

FECHA DE ENTREGA 15 DE DICIEMBRE DEL 2025

```
In [1]: # Derivadas parciales para regresión lineal
#####
# derivadas_parciales_lineal(x: list, ys: list) => tuple[float, float, float, float]:
#   Devuelve las derivadas parciales de la ecuación de la derivada parcial con respecto al parámetro 1 al reemplazar los valores "xs" y "ys". La ecuación es de la forma:
#   c_0 + c_1*x + c_2*x^2 + ... + c_n*x^n
#   xs = lista de valores de x.
#   ys = lista de valores de y.
#
#   Returns
#   c_1: coeficiente del parámetro 1.
#   c_0: coeficiente del parámetro 0.
#   c_1*ind: coeficiente del término independiente.
#
#   ...
#   # coeficiente del término independiente
#   c_n*ind = sum(ys)
#
#   # coeficiente del parámetro 1
#   c_1*ind = sum(xs)
#
#   # coeficiente del parámetro 0
#   c_0 = len(xs)
#
#   return (c_1, c_0, c_1*ind)

def derivadas_parciales_0(xs: list, ys: list) => tuple[float, float, float, float]:
    ##### Devuelve los coeficientes de la ecuación de la derivada parcial con respecto al parámetro 0 al reemplazar los valores "xs" y "ys". La ecuación es de la forma:
    c_0 + c_1*x + c_2*x^2 + ... + c_n*x^n
    xs = lista de valores de x.
    ys = lista de valores de y.
    #
    # Returns
    #   c_0: coeficiente del parámetro 0.
    #   c_0*ind: coeficiente del parámetro 0.
    #   c_0*ind: coeficiente del término independiente.
    #
    #   ...
    #   # coeficiente del término independiente
    #   c_n*ind = sum(ys)
    #
    #   # coeficiente del parámetro 1
    #   c_1*ind = sum(xs)
    #
    #   # coeficiente del parámetro 0
    #   c_0 = len(xs)
    #
    #   return (c_1, c_0, c_0*ind)

def derivadas_parciales_1(xs: list, ys: list) => tuple[float, float, float, float]:
    ##### Devuelve los coeficientes de la ecuación de la derivada parcial con respecto al parámetro 1 al reemplazar los valores "xs" y "ys". La ecuación es de la forma:
    c_0 + c_1*x + c_2*x^2 + ... + c_n*x^n
    xs = lista de valores de x.
    ys = lista de valores de y.
    #
    # Returns
    #   c_1: coeficiente del parámetro 1.
    #   c_0: coeficiente del parámetro 0.
    #   c_1*ind: coeficiente del término independiente.
    #
    #   ...
    #   # coeficiente del término independiente
    #   c_n*ind = sum(ys)
    #
    #   # coeficiente del parámetro 1
    #   c_1*ind = sum(xs)
    #
    #   # coeficiente del parámetro 0
    #   c_0 = len(xs)
    #
    #   return (c_1, c_0, c_1*ind)

In [2]: from arc import ajustar_min_cuadrados

# UTILIZAR:
# ajustar_min_cuadrados((3,4,9,5,12,3), (3,2,0.7,-3.4), (der_parcial_1, der_parcial_0))
# 12-15 17:27:57[77131, 8.78397454] Se ajustarán 2 parámetros.
Out[2]: array([4.05232559, 8.78397454])
```

```
In [3]: import numpy as np
import matplotlib.pyplot as plt

from arc import ajustar_min_cuadrados
```

```
# Datos
xs = [3.4, 9.5, 12.3]
ys = [3.2, 0.7, -3.4]
```

```
# Ajuste por mínimos cuadrados
al, ab = ajustar_min_cuadrados(xs, ys, (der_parcial_1, der_parcial_0))

# Función ajustada
def f(x):
    return al * x + ab
```

Valores para la recta

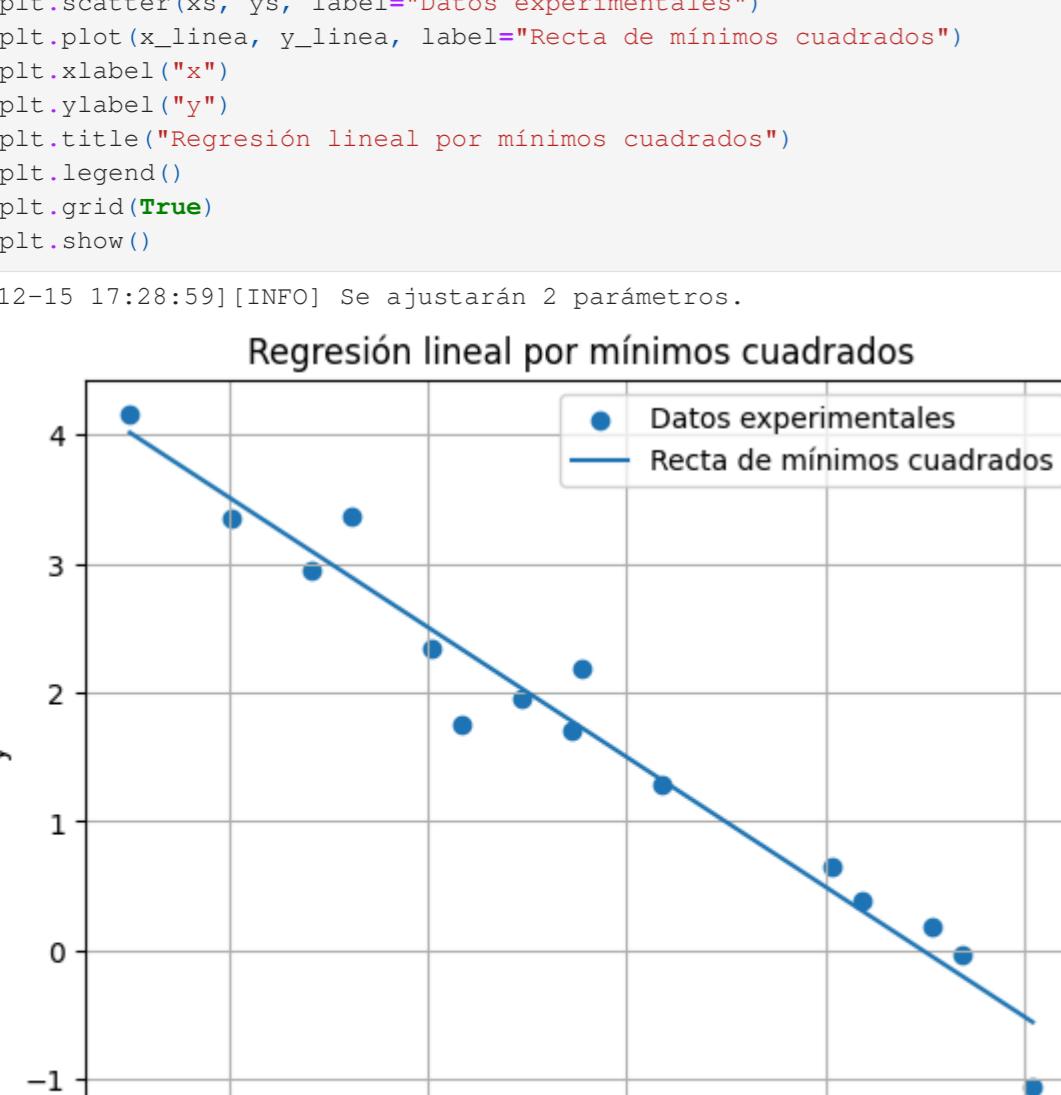
y_linea = np.linspace(min(xs), max(xs), 100)

Gráfica

```
plt.figure()
plt.scatter(xs, ys, label="Datos")
plt.plot(x_linea, y_linea, label="Recta ajustada")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Regresión lineal por mínimos cuadrados")
plt.legend()
plt.show()
```

12-15 17:28:05[77131] Se ajustarán 2 parámetros.

Regresión lineal por mínimos cuadrados



```
In [5]: from arc import ajustar_min_cuadrados
```

```
# UTILIZAR:
```

```
# ajustar_min_cuadrados((3,38, 0.35, -0.45, -0.55, -1.06, -2.78, 3.08, 3.09, -3.98, -5, -3.18, -1.96, 2.37, -1.67, 4.09, -4.09, -5.00, -3.18, -1.96, 2.37, -1.67, 4.09, -4.65, 2.68, 2.78, -3.79, -1.87))
```

```
# Ajuste por mínimos cuadrados
al, ab = ajustar_min_cuadrados(xs, ys, (der_parcial_1, der_parcial_0))

# Función ajustada
def f(x):
    return al * x + ab
```

Valores para la recta

x_linea = np.linspace(min(xs), max(xs), 100)

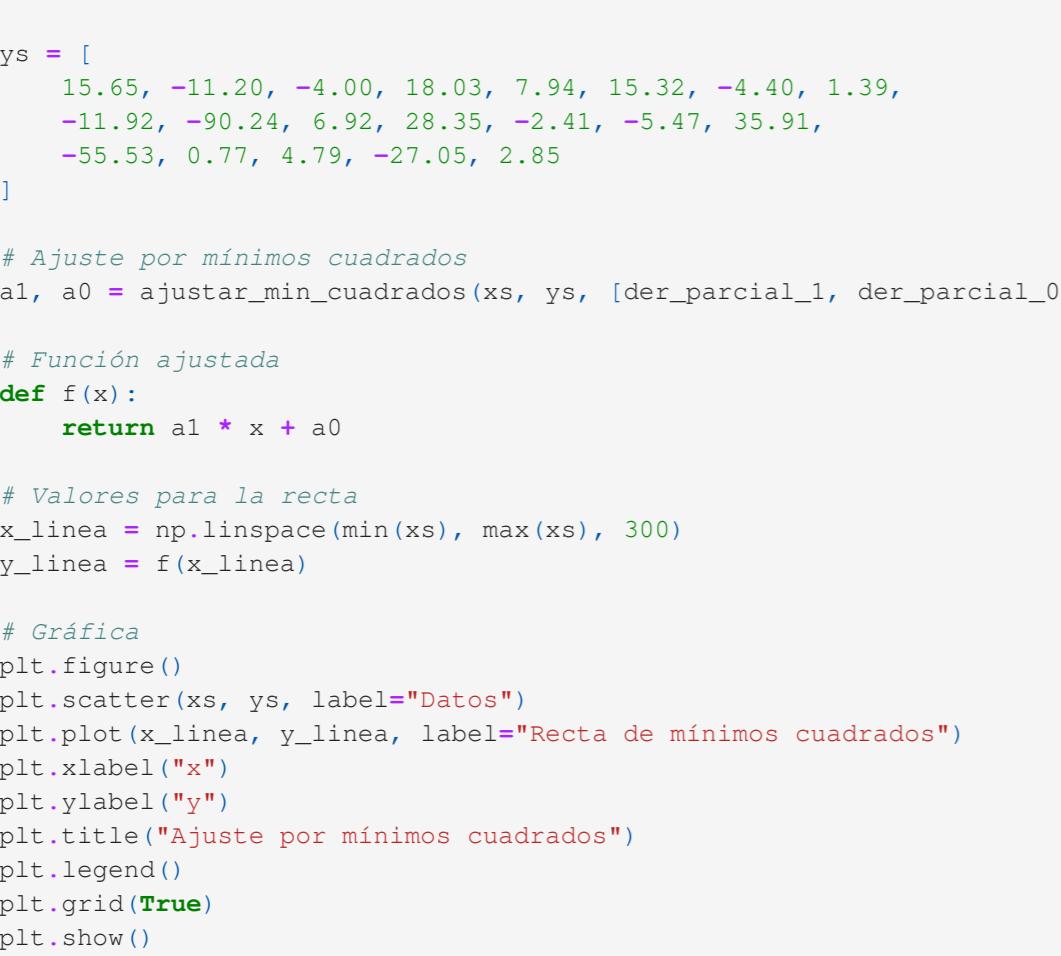
y_linea = f(x_linea)

Gráfica

```
plt.figure()
plt.scatter(xs, ys, label="Datos experimentales")
plt.plot(x_linea, y_linea, label="Recta de mínimos cuadrados")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Ajuste por mínimos cuadrados")
plt.legend()
plt.show(True)
```

12-15 17:28:15[77131] Se ajustarán 2 parámetros.

Regresión lineal por mínimos cuadrados



```
In [7]: from arc import ajustar_min_cuadrados
```

```
# UTILIZAR:
```

```
# ajustar_min_cuadrados((3.38, 0.35, -0.45, -0.55, -1.06, -2.78, 3.08,
```

```
-3.09, -3.98, -5, -3.18, -1.96, 2.37, -1.67, 4.09,
```

```
-4.09, -5.00, -3.18, -1.96, 2.37, -1.67, 4.09,
```

```
-4.65, 2.68, 2.78, -3.79, -1.87))
```

```
# Ajuste por mínimos cuadrados
al, ab = ajustar_min_cuadrados(xs, ys, (der_parcial_1, der_parcial_0))

# Función ajustada
def f(x):
    return al * x + ab
```

Valores para la recta

x_linea = np.linspace(min(xs), max(xs), 100)

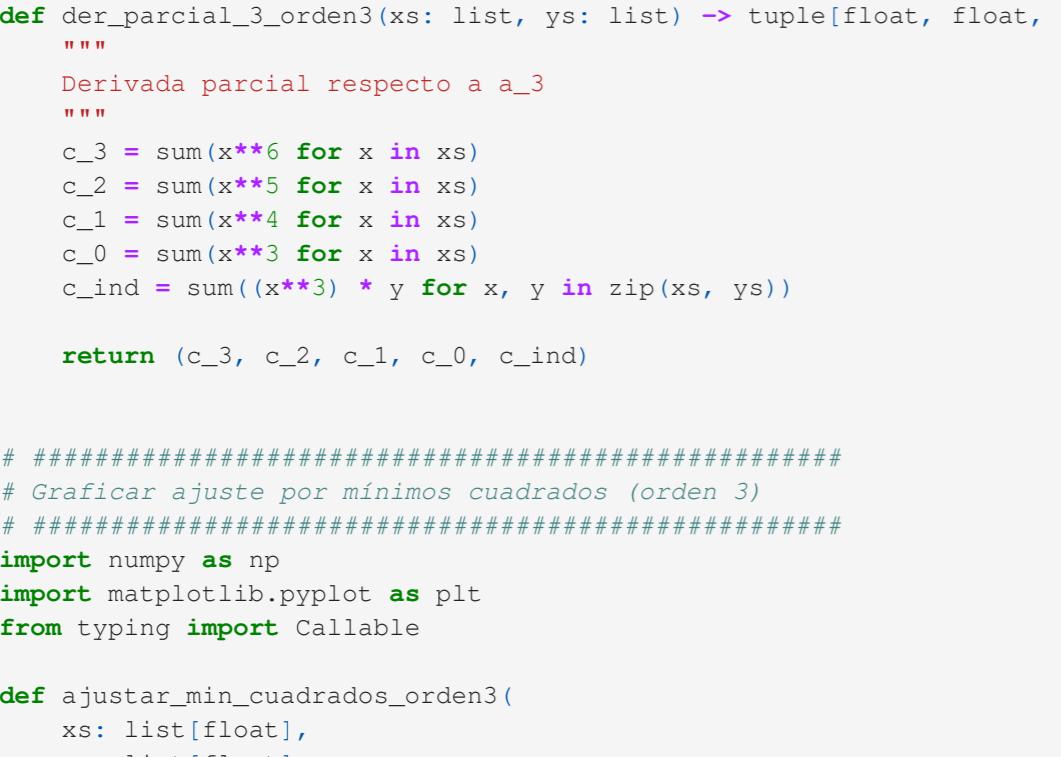
y_linea = f(x_linea)

Gráfica

```
plt.figure()
plt.scatter(xs, ys, label="Datos")
plt.plot(x_linea, y_linea, label="Recta de mínimos cuadrados")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Ajuste por mínimos cuadrados")
plt.legend()
plt.show()
```

12-15 17:28:15[77131] Se ajustarán 2 parámetros.

Ajuste por mínimos cuadrados



Para una función de orden 3

```
In [8]: # Regresión polinómica de orden 3 (mínimos cuadrados)
```

```
# Derivadas parciales y ecuaciones normales
```

```
#####
# derivadas_parciales_0_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
#   Devuelve la derivada parcial respecto a x_0
#   Derivada parcial respecto a x_0
#   c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
#   ...
#   c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
#   xs = lista de valores de x.
#   ys = lista de valores de y.
#
#   Returns
#   c_3: sum(x**4) for x in xs
#   c_2: sum(x**3) for x in xs
#   c_1: sum(x**2) for x in xs
#   c_0: len(xs)
#   c_0*ind: sum(ys)
```

```
return (c_3, c_2, c_1, c_0, c_0*ind)

def derivadas_parciales_1_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_1
    # Derivada parcial respecto a x_1
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_1*ind: sum(x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_1*ind)

def derivadas_parciales_2_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_2
    # Derivada parcial respecto a x_2
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_2*ind: sum(x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_2*ind)

def derivadas_parciales_3_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_3
    # Derivada parcial respecto a x_3
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_3*ind: sum(x*x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_3*ind)

def derivadas_parciales_0_xsorden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_0
    # Derivada parcial respecto a x_0
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_0*ind: sum(ys)
```

```
return (c_3, c_2, c_1, c_0, c_0*ind)

def derivadas_parciales_1_xsorden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_1
    # Derivada parcial respecto a x_1
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_1*ind: sum(x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_1*ind)

def derivadas_parciales_2_xsorden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_2
    # Derivada parcial respecto a x_2
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_2*ind: sum(x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_2*ind)

def derivadas_parciales_3_xsorden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_3
    # Derivada parcial respecto a x_3
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_3*ind: sum(x*x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_3*ind)

def derivadas_parciales_0_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a a_0
    # Derivada parcial respecto a a_0
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_0*ind: sum(ys)
```

```
return (c_3, c_2, c_1, c_0, c_0*ind)

def derivadas_parciales_1_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a a_1
    # Derivada parcial respecto a a_1
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_1*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_1*ind: sum(x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_1*ind)

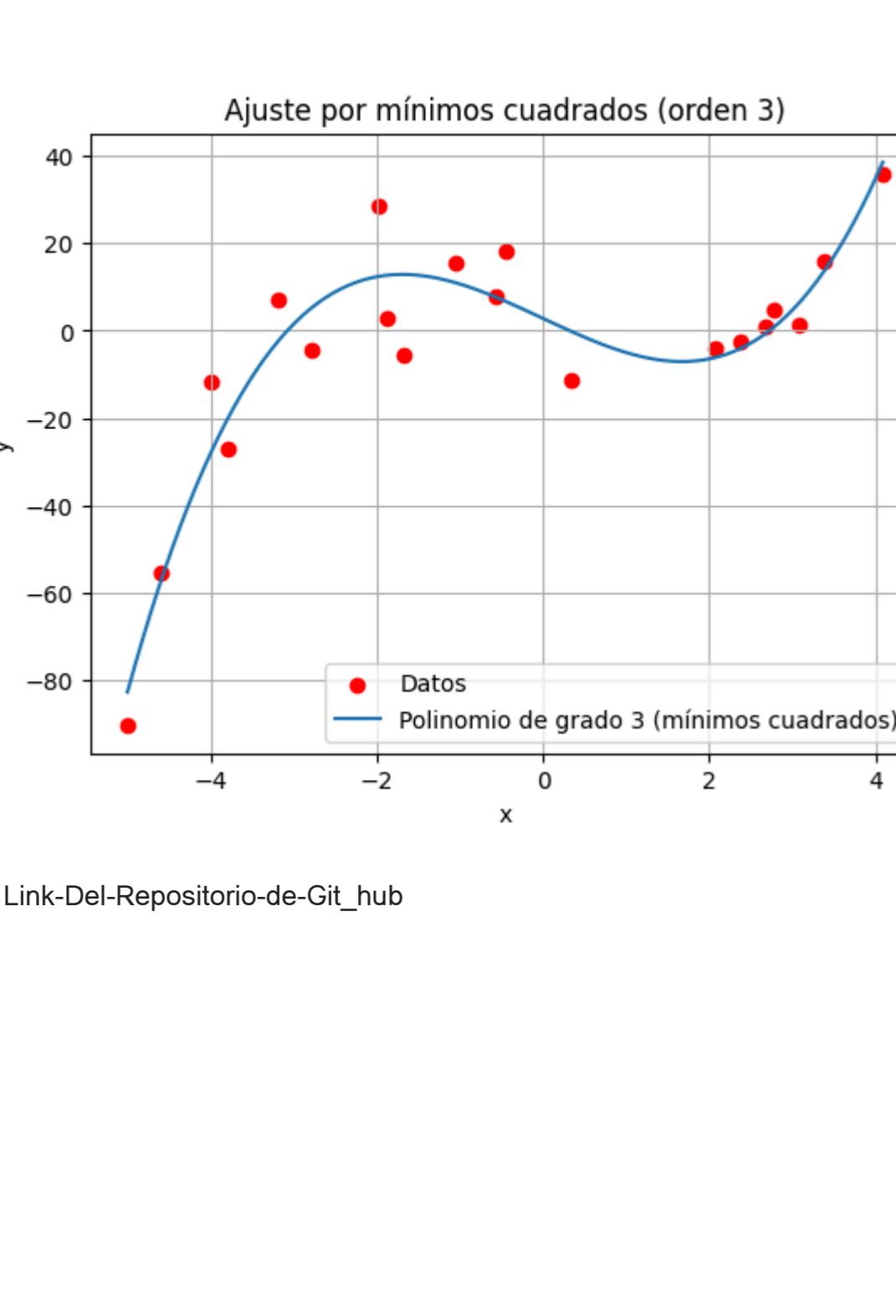
def derivadas_parciales_2_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a a_2
    # Derivada parcial respecto a a_2
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_2*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_2*ind: sum(x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_2*ind)

def derivadas_parciales_3_orden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a a_3
    # Derivada parcial respecto a a_3
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_3*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4) for x in xs
    #   c_2: sum(x**3) for x in xs
    #   c_1: sum(x**2) for x in xs
    #   c_0: len(xs)
    #   c_3*ind: sum(x*x*x*y) for x, y in zip(xs, ys)
```

```
return (c_3, c_2, c_1, c_0, c_3*ind)

def derivadas_parciales_0_xsorden3(xs: list, ys: list) => tuple[float, float, float, float, float]:
    #####
    # Devuelve la derivada parcial respecto a x_0
    # Derivada parcial respecto a x_0
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # ...
    # c_3*x^3 + c_2*x^2 + c_1*x + c_0*x^0 = c_0*ind
    # xs = lista de valores de x.
    # ys = lista de valores de y.
    #
    # Returns
    #   c_3: sum(x**4)
```



Link-Del-Repositorio-de-Git_hub