## ECE/CS/ME 539 - Fall 2024 — Activity 5

1.

Consider a bunch of eggs. The length (cm) of an egg is used as a feature to classify the eggs into either Large (L) or Jumbo (J). The distributions of eggs in each category (length and label) are as follows:

Label\Length (cm)	1	2	3	4	5
Large	3	8	6	2	0
Jumbo	0	1	5	9	6

- (a) Total number of eggs in this bunch, N =
- (b) Class distribution:  $Pr\{Large\} = \underline{\hspace{1cm}}$ ,  $Pr\{Jumbo\} = \underline{\hspace{1cm}}$
- (c) Likelihood that the length of a large egg is longer than 3 cm:  $Pr\{x > 3 \mid Large\} =$ \_\_\_\_\_\_
- (d) The posterior probability that an egg is a jumbo egg given that its length is shorter than 4 cm:  $\Pr{\text{Jumbo} \mid x < 4} = \underline{\hspace{1cm}}$
- (e)  $Pr\{x < 4\} =$ \_\_\_\_\_
- (f)  $Pr{Jumbo, x < 4} =$ \_\_\_\_\_
- (g) Find the likelihood  $Pr\{x < 4 \mid Jumbo\} =$ \_\_\_\_\_
- (h) Using the above results, verify the Bayesian equation

$$\Pr{\text{Jumbo} \mid x < 4} = \frac{\Pr{x < 4 \mid \text{Jumbo}} \cdot \Pr{\text{Jumbo}}}{\Pr{x < 4}}$$

(i) Consider the Bayesian decision rule (a.k.a. Maximum a Posterior, MAP decision rule)

$$g(x) = \begin{cases} \text{Large} & \text{if } \Pr\{\text{Large} \mid x\} > \Pr\{\text{Jumbo} \mid x\} \\ \text{Jumbo} & \text{otherwise} \end{cases}$$

Evaluate g(x) for  $x \in \{1, 2, 3, 4, 5\}$  (unit: cm)

(j) Using the classifier developed in part (i), evaluate the probability of correct classification:

Outlook	Temperature	Humidity	Wind	Played football (yes/no)
Sunny	Hot	High	Weak	No
Sunny	Hot	High	Strong	No
Overcast	Hot	High	Weak	Yes
Rain	Mild	High	Weak	Yes
Rain	Cool	Normal	Weak	Yes
Rain	Cool	Normal	Strong	No
Overcast	Cool	Normal	Strong	Yes
Sunny	Mild	High	Weak	No
Sunny	Cool	Normal	Weak	Yes
Rain	Mild	Normal	Weak	Yes
Sunny	Mild	Normal	Strong	Yes
Overcast	Mild	High	Strong	Yes
Overcast	Hot	Normal	Weak	Yes
Rain	Mild	High	Strong	No

Table 1: Weather conditions and football playing decision

## **2**.

Table 1 lists the weather outlook, temperature, humidity, and wind conditions of 14 days and the outcome of whether a junior league will play footfall or not. Calculate the following empirical probabilities based on given weather conditions and junior league play outcomes:

- (a)  $Pr.\{Humidity = High\} = \underline{\hspace{1cm}}$
- (b) Pr.{Outlook = Sunny AND Humidity = Normal} = \_\_\_\_\_
- (c) Pr.{Temperature = Cool OR Wind = Weak} = \_\_\_\_\_
- (d)  $Pr.{Play = Yes \mid Humidity = High} = \underline{\hspace{1cm}}$
- (e)  $Pr.{Humidity = High \mid Play = Yes} = \underline{\hspace{1cm}}$
- (f) Entropy of the outcome of Play = \_\_\_\_\_