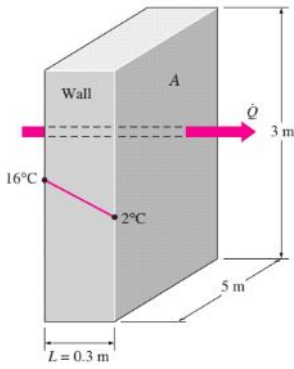


Find the rate of heat transfer through the wall if $k=0.9 \text{ W/m}^\circ\text{C}$



$$\dot{Q} = \frac{K \times A}{L} \times \Delta T = 0.9 * 15 * \frac{16 - 2}{0.3} = 630 \text{ W}$$

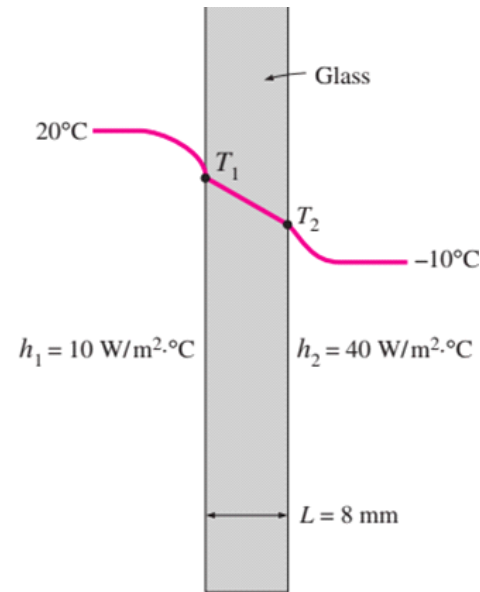
Let's use the equivalent network !

$$R_{\text{wall}} = \frac{L}{K \times A} = \frac{0.3}{0.9 * 15} = 0.0222$$

$$\dot{Q} = \frac{\Delta T}{R_{\text{wall}}} = \frac{14}{0.0222} = 630 \text{ W}$$

Example A: Heat loss through a single pane window

Consider a 0.8 m high and 1.5 m wide glass window, shown above with a thermal conductivity of $k = 0.78 \text{ W/m} \cdot ^\circ\text{C}$. Determine the steady rate of heat transfer through this glass window and the temperature of its inner surface



$$\Delta T = 20 - (-10) = 30 \text{ } ^\circ\text{C}$$

$$R_{\text{glass}} = \frac{L}{k \times A} = \frac{0.008}{0.78 \times 0.8 \times 1.5} = 0.0085 \frac{\text{ } ^\circ\text{C}}{\text{W}}$$

$$R_1 = \frac{1}{h_1 \times A} = \frac{1}{10 \times 0.8 \times 1.5} = 0.0833 \frac{\text{ } ^\circ\text{C}}{\text{W}}$$

$$R_2 = \frac{1}{h_2 \times A} = \frac{1}{40 \times 0.8 \times 1.5} = 0.0208 \frac{\text{ } ^\circ\text{C}}{\text{W}}$$

$$R_{\text{tot}} = R_1 + R_{\text{glass}} + R_2 = 0.0833 + 0.0085 + 0.0208 = 0.1126 \frac{\text{ } ^\circ\text{C}}{\text{W}}$$

$$\dot{Q} = \frac{(\Delta T)}{R_{\text{tot}}} = \frac{30}{0.1126} = 266.4 \text{ W}$$

$$\dot{Q} = \frac{T_{\text{inff1}} - T_{s1}}{R_1} \rightarrow T_{s1} = T_{\text{inff1}} - \dot{Q} \times R_1 = -2.2 \text{ } ^\circ\text{C}$$

Example B: Heat loss through a double pane window

Consider a 0.8-m-high and 1.5-m-wide double-pane window consisting of two 4-mm-thick layers of glass ($k = 0.78 \text{ W/m} \cdot ^\circ\text{C}$) separated by a 10-mm-wide stagnant air space ($k = 0.026 \text{ W/m} \cdot ^\circ\text{C}$). Determine the steady rate of heat transfer through this double-pane window and the temperature of its inner surface.

Take the convection heat transfer coefficients on the inner and outer surfaces of the window to be $h_1 = 10 \text{ W/m}^2 \cdot ^\circ\text{C}$ and $h_2 = 40 \text{ W/m}^2 \cdot ^\circ\text{C}$, which includes the effects of radiation.



$$\Delta T = 20 - (-10) = 30 \text{ } ^\circ\text{C}$$

$$R_{g1} = R_{g2} = \frac{L_g}{k_g \times A} = \frac{0.004}{0.78 \times 0.8 \times 1.5} = 0.0043 \frac{\text{ } ^\circ\text{C}}{\text{W}}$$

$$R_1 = \frac{1}{h_1 \times A} = \frac{1}{10 \times 0.8 \times 1.5} = 0.0833 \text{ } ^\circ\text{C/W}$$

$$R_2 = \frac{1}{h_2 \times A} = \frac{1}{40 \times 0.8 \times 1.5} = 0.0208 \text{ } ^\circ\text{C/W}$$

$$R_{gap} = \frac{L_{gap}}{k_{gap} \times A} = \frac{0.01}{0.026 \times 1.2} = 0.3205 \text{ } ^\circ\text{C/W}$$

$$R_{tot} = R_1 + 2 \times R_{glass} + R_{Gap} + R_2 = 0.0833 + 0.0208 + 2 \times 0.0043 + 0.3205 = \frac{0.4332 \text{ } ^\circ\text{C}}{\text{W}}$$

$$\dot{Q} = \frac{(\Delta T)}{R_{tot}} = \frac{30}{0.4332} = 69.2 \text{ W}$$

$$\dot{Q} = \frac{T_{inff1} - T_{s1}}{R_1} \rightarrow T_{s1} = T_{inff1} - \dot{Q} \times R_1 = 14.2 \text{ } ^\circ\text{C}$$

