# Assignment 6

# Due BEFORE 8:00AM on Monday 10/15/2018

On time / 20% off / no credit

Total points: 40

You are allowed to work with a partner on this assignment. If you decide to form a pair, make sure to include both names above, but submit only one zip file to D2L.

This assignment will develop your algorithmic design skills. More specifically, it will make you more comfortable with the divide-and-conquer paradigm. You must write up your solutions to this assignment IN THIS FILE using LaTeX by filling in all of the boxes below. If your submitted .tex file does not compile, then you will receive 0 points. You should NOT add any LaTeX packages to your .tex file.

Since this assignment includes a programming component, you must also complete and submit the SLIT. java file.

## Submission procedure:

- 1. Complete this file, called a6.tex, with your full name(s) and answers typed up below.
- 2. Compile this file to produce a file called a6.pdf. Make sure that this file compiles properly and that its contents and appearance meet the requirements described in this handout.
- 3. Create a directory called a6 and copy exactly three files into this directory, namely:
  - a6.tex (this file with all of your answers added)
  - a6.pdf (the compiled version of the file above)
  - SLIT. java (your completed Java code file)
- 4. Zip up this directory to yield a file called a6.zip
- 5. Submit this zip file to the D2L dropbox for A6 before the deadline above.
- 6. BEFORE the beginning of class on the due date above, submit a single-sided, hard copy of your:
  - a6.pdf file
  - completed SLIT.java file, making sure that your name(s) are in the top documentation block and that you stated whether or not each algorithm works as expected. For FULL credit, your hard copy of the code MUST be properly indented, contain no lines that wrap around (i.e., with a length greater than the page width), and be fully legible and easily understandable.

#### Problem statement

In this assignment, you will implement two solutions to the following problem:

## **SLIT** problem

**Input:** An  $n \times n$  matrix m whose elements come from the set  $\{'A', 'C', 'G', 'T'\}$ 

**Output:** The size s of the largest imbalance in Thymine within any slit window in m, where:

- a slit window is a rectangular sub-matrix of m with height 2 and any positive width, and
- s is computed as the total number of 'T' elements minus the total number of 'A', 'C', and 'G' elements in the window.

The first solution you will implement is given to you in pseudocode format, as follows:

# Algorithm 1 Brute-force SLIT algorithm

```
1: function COUNT(m, r, c, w)
           This is a helper function that returns the total number of non-T bases subtracted from the total
         \triangleright number of T bases within the sub-matrix of m whose top-left corner is at r \times c, whose width is
           equal to w columns, and whose height is equal to two rows
 2: end function
3: function BF_SLIT(m, n)
                                                                                                   ⊳ m: 2D matrix
                            \triangleright n: # of top rows and left columns of m that are part of this problem instance
4:
        slit \leftarrow 0
5:
       for each row \in [0..(n-2)] do
                                                 \triangleright row is the index of the row in the top-left corner of the slit
           for each col \in [0..(n-1)] do \triangleright col is the index of the column in the top-left corner of the slit
6:
               for each w \in [1..(n-col)] do
                                                                        \triangleright w is the number of columns in the slit
 7:
                   slit \leftarrow max(slit, count(m, row, col, w))
 8:
               end for
9:
           end for
10:
11:
        end for
       return slit
13: end function
```

You will have to design another algorithm that has a better asymptotic running time than the bruteforce algorithm given above. Here are the detailed requirements for this assignment.

1. (5 points) What is the big-theta bound on the worst-case running time of the brute-force algorithm?

Answer:  $\Theta( | \text{Your answer goes here} | )$ 

Prove your answer by computing the exact worst-case running time.

Your proof goes here

2. (6 points) Implement the brute-force algorithm, that is, the two methods called count and algorithm1 in the file SLIT. java. For this question, you may NOT modify any other part of the code handout besides the BODY OF THESE TWO METHODS.

Your answer to this problem will be fully contained in the SLIT. java file that you submit

- 3. (8 points) Design an algorithm whose worst-case running time is asymptotically better than your answer to the previous question. Your algorithm must use the divide-and-conquer approach. You must describe in precise and concise English prose the main idea(s) behind your algorithm by filling in the following four descriptions.
  - a. Divide step

Your description of the divide step goes here

b. Conquer step

Your description of the conquer step goes here

c. Combine step

Your description of the combine step goes here

d. Base case(s)

Your definition of the base case(s) goes here, as well as what processing must be done in this case(s)

4. (7 points) Fully specify your algorithm in pseudocode format using the LaTeX packages included in this file (just like in earlier assignments). Each recursive call of your algorithm must use O(1) additional space.

Your pseudocode goes here

5. (2 points) What is the FULL DEFINITION of the recurrence that describes your algorithm?

Answer: Your answer goes here

6. (2 points) What is the solution to the recurrence you gave as an answer to Question 5 above?

Answer:  $\Theta(|\text{Your answer goes here}|)$ 

7. (8 points) Implement your algorithm, that is, the body of the method called algorithm2 in the file SLIT. java as well as any helper methods that you need (these, MUST be added just below the algorithm2 method). For this question, you may NOT modify any other part of the code handout. Recall that each recursive call of your algorithm must use O(1) additional space.

Your answer to this problem will be fully contained in the SLIT. java file that you submit

8. (2 points) Run the driver code provided in A6. java without modifying it. You MUST use the seed value of 1 in the output that you include below. You may interrupt the execution of the driver once the brute-force algorithm takes more than five minutes to complete. Include the output of this run below.

Delete this box; then copy and paste the full output of your code below within a verbatim environment.

<your output must replace this line>