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Memo/garbage part

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M, N ::= x; \lambda x.M; MN
(\lambda x.M)N \to_{\beta} M[N/x]
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terms tend to get bigger

If $C[\]$ is a context, and $M \to_{\beta} N$ then $C[M] \to_{\beta} C[N]$

 $\begin{array}{l} P,Q ::= u(xy).P; \bar{u}xy.P; P|Q; (\nu x)P|!P \\ u(xy).P|\bar{u}ab.Q \rightarrow P[a/x,b/y]|Q \end{array}$

If
$$P \to Q$$
 then $C[P] \to C[Q]$
If $P \equiv P' \to Q \equiv Q'$ then $P \to Q$

(with necessary hypothesis on context C)

Krivine Abstract Machine (KAM) $M \star \Pi \star \mathcal{E}$

$$MN \star \Pi \star \mathcal{E} \to M \star (N, \mathcal{E}).\Pi \star \mathcal{E}$$
$$\lambda x.M \star (N, \mathcal{E}).\Pi \star \mathcal{F} \to M \star \Pi \star \mathcal{F}, s \mapsto (N, \mathcal{E})$$
$$x \star \Pi \star \mathcal{E}, x \mapsto (M, \mathcal{F}) \to M \star \Pi \star \mathcal{F}$$

For exponentials:

 $|P \simeq |P| |P|$ $(\nu u) |u(x).P \simeq 0$

idea : $!P|Q \simeq !P|!P|Q \ \forall Q$

We want $M \star \Pi \star \mathcal{E} \to M' \star \Pi' \star \mathcal{E}'$ iff $[\![M, \mathcal{E}]\!]_u | [\![\Pi]\!]_u \to [\![M', \mathcal{E}']\!]_v | [\![\Pi']\!]_v$

- equiv \simeq bisimulation
- the traduction goes well

Definition

A binary relation S is a reduction bisimulation if, for all $(P,Q) \in S$

- (1) $P \xrightarrow{\tau} P'$ implies $Q \xrightarrow{\tau} Q'$ for some Q' with $(P', Q') \in S$
- (2) $Q \xrightarrow{\tau} Q'$ implies $P \xrightarrow{\tau} P'$ for some P' with $(P', Q') \in S$

Definition (Observability:)

 $P \downarrow_x$ if P can make an input action of subject x

 $P\downarrow_{\bar{x}}$ if P can make an output action of subject x.

Definition (Image-finite process:)

P is image-finite if, for all derivative Q of P and any action $\alpha, \exists n \geq 0$ and Q_1, \dots, Q_n such that $Q \stackrel{\alpha}{\Rightarrow} Q'$ implies $Q' = Q_i$ for some i.

where \Rightarrow is the reflexive transitive closure of $\stackrel{\tau}{\rightarrow}$ and $\stackrel{\alpha}{\Rightarrow}$ is $\Rightarrow \stackrel{\alpha}{\rightarrow} \Rightarrow$ for some action α .

Rules for base- π

Value-typing TV-BASVAL TV-NAME

Process typing

T-PAR T-SUM
T-MAT T-NIL
T-REP T-RES T-TAU
T-INP T-OUT

Types : S, T ::=V value type |L| link type $| \diamond \text{ behaviour type} |$

Value types : V ::= B basic type Link types : $L ::= \sharp V$ connexion type Environments : $\Gamma ::= \Gamma, x : L|\Gamma, x : V|\emptyset$

Transitions for base- π

OUT INP
TAU MAT
SUM-L PAR-L
COMM-L
RES REP-ACT

OPEN

REP-COMM

OUTERR INPERR MATERR

simply-typed π -calculus : same but with value types V ::= B basic type |L| link type

i/o types

 $\frac{\text{Grammar:}}{\text{Subtyping rules}} + L ::= iV|oV$

(input and output capabilities)

SUB-REFL SUB-TRANS

SUB-#I SUB-#O

SUB-II SUB-OO

SUB-BS

Typing rules

T-INPS

T-OUTS

SUBSUMPTION

replaces T-INP replaces T-OUT

Linear types

fill this in later