baseline fluxes : SIBYLL$(\pi, K, c)$, $\mathcal{L}_{\mathrm{pp}} = 3$ ab$^{-1}$ FASER$\nu$ Run $4+5$