

Pointing error correction

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1 Attitude of a Satellite

Fig. 46

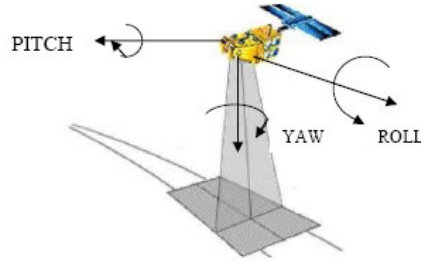


FIGURE 1 – Roll, pitch and yaw angles.

2 Satellite attitude error effects on stereo images

3 Correction of Relative Pointing Error

[1]

A simple way to correct the relative pointing error is thus to transform one of the two images, in such a way that the corresponding points fall on the respective epipolar curves : given two images u, v and a set of correspondences $(\mathbf{x}_i, \mathbf{x}'_i)_{i=1\dots N}$, we search for a translation f such that, for all i , the transformed point $f(\mathbf{x}'_i)$ lies on the epipolar curve $epi_{uv}^{\mathbf{x}_i}(R)$. The desired transformation f^* minimises the relative pointing error defined by :

$$f^* = \underset{f}{\operatorname{argmin}} \frac{1}{N} \sum_{i=1}^N d(f(\mathbf{x}'_i), epi_{uv}^{\mathbf{x}_i}(R)) \quad (1)$$

From [1], we know that the epipolar curve $epi_{uv}^{\mathbf{x}_i}(R)$ is approximated up to 0.05 pixels by the straight line $F\mathbf{x}_i$, where F is the affine fundamental matrix between the two views for the considered tile. As this fundamental matrix is an *affine* fundamental matrix, all the lines $F\mathbf{x}_i$ are parallel. Without any additional restriction, we may assume that these lines are horizontal (otherwise just

do a change of coordinates). The horizontal line $F\mathbf{x}_i$ can be written, in homogeneous coordinates, as

$$F\mathbf{x}_i = [0 \ 1 \ c_i]$$

With these notations, for each point correspondence $(\mathbf{x}_i, \mathbf{x}'_i)$, we have

$$e(\mathbf{x}_i, \mathbf{x}'_i) = d(\mathbf{x}'_i, \text{epi}_{uv}^{\mathbf{x}_i}(R)) = d(\mathbf{x}'_i, F\mathbf{x}_i) = |y'_i + c_i|$$

3.1 Roll and Pitch Angles

Because of sensitivity issues, we can take only roll and pitch error into account. Therefore according to section 2, we search for a transformation f such that

$$f(\mathbf{x}) = T\mathbf{x}$$

where T is a translation.

Here the error e is invariant to any horizontal translation, thus the search for a translation minimizing the relative pointing error of formula (1) can be restricted to vertical translations only. With a vertical translation of parameter t , the error becomes

$$\frac{1}{N} \sum_{i=1}^N d(T\mathbf{x}'_i, F\mathbf{x}_i) = \frac{1}{N} \sum_{i=1}^N |y'_i + t + c_i|$$

The translation that minimizes this sum is given by the geometric median (Weiszfeld, 1937) of the vector $(-y'_i - c_i)_{i=1 \dots N}$. The relative pointing error can thus be minimized in a tile by applying a translation to one of the images. Note that the median is robust against outliers, thus this correction procedure works well even in the presence of false matches.

3.2 Roll, Pitch and Yaw Angles

If we assume that the scene is located at infinity with respect to the satellite, an error in the sensor attitude measurement can be modeled in image space as a translation composed with a rotation. Therefore we have

$$f(\mathbf{x}) = RT\mathbf{x}$$

where R is a rotation and T a translation.

Références

- [1] Carlo De Franchis, Enric Meinhardt-Llopis, Julien Michel, Jean-Michel Morel, and Gabriele Facciolo. An automatic and modular stereo pipeline for pushbroom images. *ISPRS Annals of the Photogrammetry, Remote Sensing and Spatial Information Sciences*, 2(3) :49, 2014.