Final Project Submission

Please fill out:

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• Scheduled project review date/time: 28.02.2023

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Blog post URL:

Setup preparation

In [1]:

```
# loading basic packages for data manipulation
import pandas as pd
import numpy as np
import re
from sklearn.preprocessing import StandardScaler
import math
# Loading basic packages for visualisation
import matplotlib.pyplot as plt
%matplotlib inline
import plotly.express as px
import seaborn as sns
# Loading basic packages for statistics
import statsmodels.api as sm
from scipy import stats
from sklearn.metrics import mean_absolute_error, mean_squared_error
from sklearn.linear_model import LinearRegression
```

In [2]:

%cd data

 ${\tt C:\Wsers\mullerju\Documents\Flatiron\Course_Material\Phase_2\dsc-phase-2-project-v2-5\data}$

Data preparation

In this section, the data will be loaded and inspected. I will decide what to do with missing values, duplicates and outliers. I will also see if any variables will have to be scaled and do one-hot-encoding with categorical variables.

In [3]:

```
df = pd.read_csv("kc_house_data.csv") #read csv
df.info() #inspect and see only few NAs
df.dropna(inplace = True) #drop all rows with nas
df = df.drop_duplicates() #drop duplicate rows
df.drop(["id"], axis = 1, inplace = True) #drop too detailed information
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 30155 entries, 0 to 30154
Data columns (total 25 columns):
#
    Column
                   Non-Null Count Dtype
а
     id
                   30155 non-null
                                   int64
 1
                   30155 non-null
     date
                                   object
     price
                   30155 non-null float64
 3
                    30155 non-null int64
     bedrooms
 4
     hathrooms
                    30155 non-null float64
 5
     sqft_living
                   30155 non-null int64
                    30155 non-null
 6
     sqft_lot
                                   int64
    floors
                   30155 non-null float64
 8
                    30155 non-null object
    waterfront
     greenbelt
 9
                   30155 non-null object
 10
    nuisance
                   30155 non-null object
                   30155 non-null
 11
    view
                                   object
    condition
                   30155 non-null object
 12
     grade
 13
                   30155 non-null
                                   object
 14
     heat_source
                    30123 non-null
                                   object
                   30141 non-null
 15
     sewer_system
                                   object
     sqft_above
                   30155 non-null
 16
                                   int64
     sqft_basement 30155 non-null int64
 17
 18
    sqft_garage
                    30155 non-null int64
 19
     sqft_patio
                    30155 non-null
                                   int64
 20
    yr_built
                   30155 non-null int64
 21
    yr_renovated
                   30155 non-null int64
                    30155 non-null object
 22
    address
 23
    lat
                    30155 non-null float64
 24
    long
                    30155 non-null float64
dtypes: float64(5), int64(10), object(10)
memory usage: 5.8+ MB
```

We have overall more than 30.000 data points with almost no missing values. Therefore, we will drop all the rows where there are missing values. We have several categorical values and numerical values. Later, we will decide if we transform them or not.

```
#For all variables, I want to see the values distribution
for column in df.columns:
     print(f"Unique values in column '{column}': \n{df[column].unique()}")
     print(f"Values distribution '{column}': \n{df[column].value counts()}\n")
Unique values in column 'date':
['5/24/2022' '12/13/2021' '9/29/2021' '12/14/2021' '8/24/2021' '7/20/2021'
  '11/17/2021' '4/28/2022' '3/17/2022' '6/21/2021' '6/1/2022' '6/11/2021'
  '6/25/2021' '11/15/2021' '8/26/2021' '3/28/2022' '6/16/2021' '3/23/2022'
  '3/24/2022' '9/28/2021' '10/19/2021' '2/28/2022' '12/28/2021'
  '11/19/2021' '11/4/2021' '10/8/2021' '5/4/2022' '2/26/2022' '9/7/2021' '9/13/2021' '8/18/2021' '8/20/2021' '8/16/2021' '4/11/2022' '11/3/2021'
  '3/2/2022' '6/29/2021' '4/1/2022' '11/20/2021' '8/25/2021' '3/16/2022' '7/9/2021' '3/22/2022' '6/14/2021' '11/12/2021' '11/5/2021' '6/23/2021'
  '7/22/2021' '6/2/2022' '5/19/2022' '5/3/2022' '9/10/2021' '2/15/2022'
  '8/31/2021' '4/13/2022' '12/7/2021' '4/19/2022' '5/31/2022' '7/29/2021' '6/18/2021' '9/16/2021' '6/20/2021' '10/21/2021' '10/29/2021' '7/21/2021'
  '12/8/2021' '12/11/2021' '12/6/2021' '12/20/2021' '8/2/2021' '1/14/2022' '3/7/2022' '11/29/2021' '11/30/2021' '4/2/2022' '5/2/2022' '8/13/2021'
  '9/14/2021' '1/21/2022' '7/6/2021' '7/2/2021' '9/21/2021' '7/16/2021'
 '8/4/2021' '4/14/2022' '4/18/2022' '11/24/2021' '8/5/2021' '10/11/2021' '3/29/2022' '11/2/2021' '7/30/2021' '11/26/2021' '12/15/2021' '7/19/2021' '4/5/2022' '3/25/2022' '2/14/2022' '5/9/2022' '10/22/2021' '7/12/2021'
  '6/22/2021' '2/16/2022' '11/13/2021' '11/10/2021' '1/20/2022'
```

There are two findings: there are houses with no bedrooms and houses with 0 or 0.5 bathrooms. We would expect every house to at least have 1 bedroom and at least 1 bathroom with shower or bathtub.

In [5]:

```
# I will drop the objects with 0 or 0.5 bathrooms.
#And I'll round up the bathrooms to have complete bathrooms
df = df[df["bathrooms"] >= 1]
df = df[df["bedrooms"] >= 1]
# rounding bathrooms and bedrooms
df['bathrooms'] = df['bathrooms'].apply(lambda x: math.ceil(x))
df['bedrooms'] = df['bedrooms'].apply(lambda x: math.ceil(x))
```

In [6]:

```
#I want to calculate from the two date columns how old the house
#was when it was sold. for this i will subtract
#the date it was built from the date it was sold and
#get a new column with the age.

df["date"] = df["date"].str[-4:].apply(int) #extracting the year

delta = df["date"] - df["yr_built"] #calculating date

df["age"] = delta
#drop too detailed information

df.drop(["date", "yr_built"], axis=1, inplace=True)
```

Regarding the location, there seem to be objects outside of King County. I will remove all objects outside King County

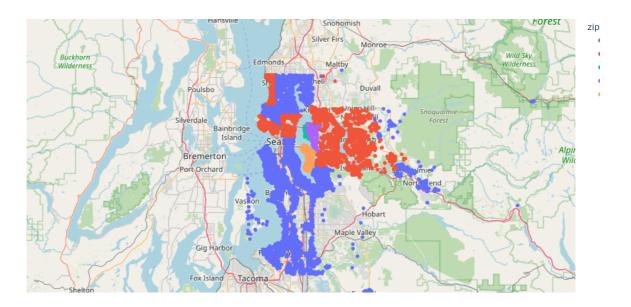
In [7]:

```
# define zip code pattern
zip code pattern = r'' b d{5}(?:-d{4})?b''
# create new column with extracted zip codes
df['Zip Code'] = df['address'].apply(
    lambda x: re.search(zip_code_pattern, x).group(
    ) if re.search(zip_code_pattern, x)else None)
url = 'https://www.zipcode.com.ng/2022/12/king-county-zip-codes-wa.html'
# read html table into a list of dataframes
tables = pd.read_html(url)
# extract the first dataframe from the list
zips = tables[1]
# drop unnecessary columns
zips = zips.drop(['State', 'County'], axis=1)
zips.rename(columns={"ZIP Code": "Zip Code"}, inplace=True)
zips["Zip Code"] = zips["Zip Code"].astype(str)
df = pd.merge(df,zips, on="Zip Code", how="left")
#drop all outside of king county
df = df.dropna(subset=["City"])
```

Let's next look at the price difference per zip code to combine them into categories of inexpensive/expensive neighbourhoods

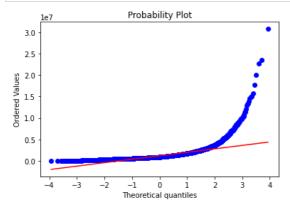
In [8]:

In [9]:



In [10]:

```
#check distribution of the price
res = stats.probplot(df['price'], plot=plt)
```



We can see that there are heavy outliers in certain areas on the map and confirmed this with the qq plot. I will try to log transform the price

In [11]:

```
df["price_log"] = np.log(df["price"]) #Log transforming price
```

In [12]:

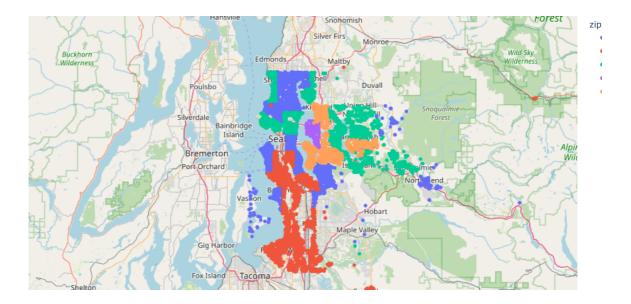
```
from scipy.stats import skew
data_skewness = skew(df["price_log"])
print("Skewness of the data: ", data_skewness)
```

Skewness of the data: 0.12381872198073594

The skew looks good now.

In [13]:

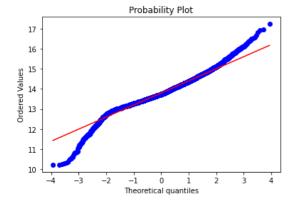
In [14]:



Looking at the map, we can see the distribution of zip codes depending on the average price per zip code. It looks like the south of King County has low house prices. It's surprising that many neighbourhoods close to the water have low house prices.

In [15]:

```
#looking again at distribution
res = stats.probplot(df['price_log'], plot=plt)
```



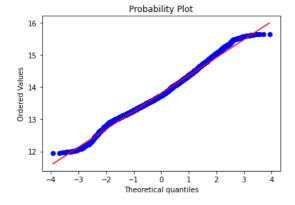
Still has quite some outliers. I will try to remove them with the IQR.

In [16]:

```
# Compute the IQR
q1, q3 = np.percentile(df["price_log"], [25, 75])
iqr = q3 - q1

# Set the bounds for outlier detection
lower_bound = q1 - 2*iqr
upper_bound = q3 + 2*iqr

# Drop the outliers
df = df[(df["price_log"] >= lower_bound) & (df["price_log"] <= upper_bound)]
res = stats.probplot(df['price_log'], plot=plt)</pre>
```

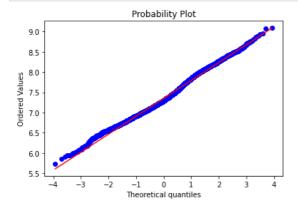


In [17]:

```
#sqft log has a lot of outliers.
#The information seems unreliable so I will drop the column
df.drop(["sqft_lot"], axis=1, inplace=True) #drop sqft lot
#Also, I will transform the price and sqft_living
#to a logarithm to work against outliers
df["sqft_living_log"] = np.log(df["sqft_living"])
df["sqft_above_log"] = np.log(df["sqft_above"])
```

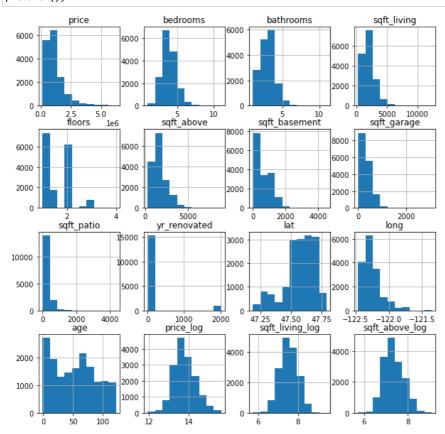
In [18]:

```
#checking distribution of sqft above Log
res = stats.probplot(df['sqft_above_log'], plot=plt)
```



In [19]:

df.hist(figsize=(10,10)) #Looking at histogram of variables
plt.show();

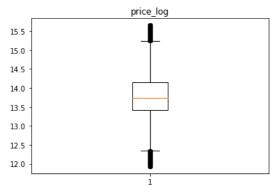


In [20]:

```
# Check continuous predictors for outliers using Boxplot

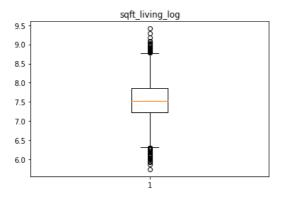
outliers = [
    "price_log", 'bedrooms', 'bathrooms', "sqft_living_log", 'sqft_above_log']

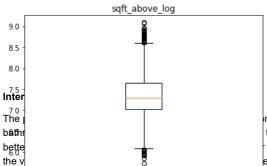
for outlier in outliers:
    plt.boxplot(df[outlier])
    plt.title(outlier)
    plt.show()
```











r the bedrooms, houses have between 1 and 10 bedrooms while the majority have 3. For the the majority have 2. For sqft living, we had a slight positive skew. After log transforming it, it looks 1 or 2 floors. waterfront only has few yes. greenbelt only has few yes. nuisance only has few yes. e grade as well. the most common heat source is gas. the sewer system is either public or private.

sqft above and sqft basement and positively skewed. sqft garage and patio have outliers that may have to be removed. year built starts in 1900 and has its peak in 2020, year renovates seems to have a lot of missing values which we will have to remove.

For Waterfront, greentbelt, nuisance, view, condition, grade, heat source and sewer system, we can create categorical dummy variables. Looking at the values distribution and the most common values, an average house would consist of the following attributes:

Waterfront: no Greenbelt: no Nuisance: no View: None Condition: Average Grade: Avaerage Heat source: Gas Sewer System: Public

I will change the grade of the house and the condition to a numerical column. Also, I will summarize small categories from the variables heat source and sewer system. I will also create categorical columns for objects if they have a basement, garage and patio

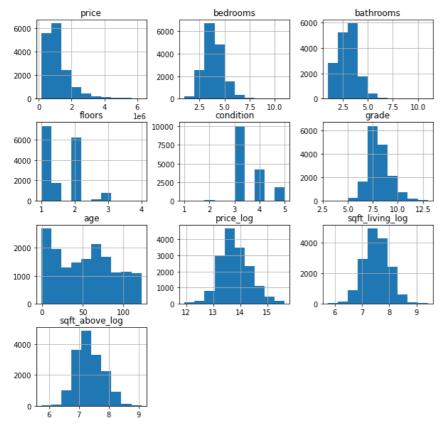
The log transformation for the price and sqft living helped. The log price and sqft living is now normally distributed so we can remove the old price indication.

In [21]:

```
# I will make a categorical column out of the garage, basement, patio and year renovated
# define a custom function that maps the values to 'yes' or 'no
def map_to_category(value):
   if value > 0:
       return 'YES
    else:
       return 'NO'
# apply the function
df['garage'] = df['sqft_garage'].apply(map_to_category)
df['basement'] = df['sqft_basement'].apply(map_to_category)
df['patio'] = df['sqft patio'].apply(map to category)
df['renovated'] = df['yr_renovated'].apply(map_to_category)
\#also I will make a numeric variable out of the grade, condition and remap some
df['grade'] = df['grade'].str.split().str[0].astype(int)
df["sewer_system"] = df["sewer_system"].replace(
   {'PRIVATE RESTRICTED': "PRIVATE", "PUBLIC RESTRICTED": "PUBLIC"})
  = df.drop([
   "lat", "long", "address", 'sqft_garage', 'sqft_basement',
"sqft_living", "sqft_above", 'sqft_patio', 'yr_renovated'], axis=1)
```

In [22]:

```
#showing a histogram of numeric columns
df.hist(figsize=(10,10))
plt.show();
```



Based on the histogram, I will further remove floors from the model, condition and age as it's not normally distributed.

Feature selection & One hot encoding

In this section, I'm looking at which features to include in the regression model. I will create dummy variables for the categorical columns so that we can evaluate if we include them in the linear regression model.

In [23]:

```
y = df["price_log"] #my dependent variable is the log price
#my independent variables are the following
X = df.drop(["price_log", "price", "City"], axis=1)
#next, I will create dummy variables for the categorical variables
X = pd.get_dummies(X, columns=[
    "waterfront", "basement", "garage", "patio", "greenbelt",
    "nuisance", "view", "heat_source", "sewer_system",
    "renovated", "zip_category"], drop_first=False)
#finally, I will drop irrelevant columns
X = X.drop([
    "waterfront_NO", "greenbelt_NO", "patio_NO",
    "garage_NO", "nuisance_NO", "basement_NO", "view_NONE", "heat_source_Gas",
    "sewer_system_PUBLIC", "renovated_NO", "zip_category_Medium"], axis=1)
```

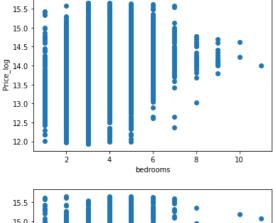
In [24]:

```
#I want to look at the correlation matrix first
corrmat = pd.concat([y,X], axis=1)
corrmat.corr()["price_log"]
Out[24]:
price_log
                           1.000000
                            0.392566
bedrooms
bathrooms
                            0.532535
                            0.229950
floors
condition
                            0.039605
                           0.642347
grade
age
                           -0.100998
sqft_living_log
                            0.646227
sqft_above_log
                           0.576039
waterfront_YES
                            0.127733
basement_YES
                           0.161561
garage_YES
                            0.180585
patio_YES
                            0.208180
greenbelt_YES
                           0.099136
                            0.009483
nuisance_YES
view_AVERAGE
                           0.131677
view_EXCELLENT
                            0.199011
view_FAIR
                            0.072661
view_GOOD
                           0.156557
heat_source_Electricity
                           -0.167931
heat_source_Oil
                           -0.082453
heat_source_Other
                           0.017766
sewer_system_PRIVATE
                           -0.037957
                           0.093616
renovated_YES
zip_category_High
                           0.354898
zip_category_Low
                           -0.092235
zip_category_Very High
                           0.254201
                           -0.502121
zip_category_Very low
```

In [25]:

Name: price_log, dtype: float64

```
#and at the scatter plots
for col in X.columns:
   plt.scatter(X[col], y)
   plt.xlabel(col)
   plt.ylabel("Price_log")
   plt.show()
```



There are some high correlations in the correlation matrix. Sqft Living and sqft above seem to be a good indicator and the grade of the construction. I will exclude nuisance and condition from the model due to the low correlations with price log. I will also drop age from the model due to the scatter plot. Before, I will check for multicollinearity

In [26]:

```
#checking for multicollinearity
cormat=X.corr().abs().stack().reset_index().sort_values(0, ascending=False)
# zip the variable name columns (Which were only named level_0 and level_1 by default) in a new column named "pairs"
cormat['pairs'] = list(zip(cormat.level_0, cormat.level_1))
# set index to pairs
cormat.set_index(['pairs'], inplace = True)
#d rop level columns
cormat.drop(columns=['level_1', 'level_0'], inplace = True)
# rename correlation column as cc rather than 0
cormat.columns = ['cc']
# drop duplicates.
cormat.drop_duplicates(inplace=True)
cormat[(cormat.cc>.75) & (cormat.cc <1)]</pre>
```

Out[26]:

| cc | pairs | | (sqft_above_log, sqft_living_log) | 0.868738 | (sqft_living_log, bathrooms) | 0.759589 |

Besides dropping age, condition, nuisance and floors due to their scatter plot or correlation values, I will also drop the sqft_living column due to high correlation with sqft above and the number of bathrooms.

In [27]:

```
#dropping variables
X = X.drop(["sqft_living_log","condition","nuisance_YES","age","floors"], axis=1)
```

In [28]:

```
#creating the first model
model_base = sm.OLS(y, sm.add_constant(X))
results_base = model_base.fit()
print(results_base.summary())

OLS Regression Results
```

	OL3 Regires	SSTOIL KES	arcs			
Dep. Variable: Model: Method: Date: Time: No. Observations: Df Model: Dep. Variable: Df Model:	price_log	Adj. R F-stat: Prob (I	-squared:		0.701 0.700 1722. 0.00 -3820.2 7686. 7863.	
Covariance Type:	nonrobust					
=======================================	coef	std err	t	P> t	[0.025	-
const bedrooms	10.5605 0.0233	0.064 0.003	165.266 7.198	0.000 0.000	10.435 0.017	
bathrooms	0.0261	0.004	6.681	0.000	0.018	

	coef	std err	t	P> t	[0.025	0.975]
const	10.5605	0.064	165.266	0.000	10.435	10.686
bedrooms	0.0233	0.003	7.198	0.000	0.017	0.030
bathrooms	0.0261	0.004	6.681	0.000	0.018	0.034
grade	0.1022	0.003	30.202	0.000	0.096	0.109
sqft_above_log	0.3349	0.011	31.652	0.000	0.314	0.356
waterfront_YES	0.1891	0.026	7.227	0.000	0.138	0.240
basement_YES	0.1395	0.006	23.523	0.000	0.128	0.151
garage_YES	-0.0538	0.006	-9.735	0.000	-0.065	-0.043
patio_YES	0.0029	0.006	0.475	0.634	-0.009	0.015
greenbelt_YES	-0.0526	0.016	-3.299	0.001	-0.084	-0.021
view_AVERAGE	0.0941	0.009	10.246	0.000	0.076	0.112
view_EXCELLENT	0.3847	0.021	18.174	0.000	0.343	0.426
view_FAIR	0.1411	0.026	5.442	0.000	0.090	0.192
view_GOOD	0.1562	0.014	11.374	0.000	0.129	0.183
heat_source_Electricity	-0.0204	0.006	-3.200	0.001	-0.033	-0.008
heat_source_Oil	0.0162	0.008	1.982	0.047	0.000	0.032
heat_source_Other	0.0003	0.028	0.010	0.992	-0.055	0.056
sewer_system_PRIVATE	-0.0439	0.010	-4.236	0.000	-0.064	-0.024
renovated_YES	0.0721	0.011	6.763	0.000	0.051	0.093
zip_category_High	0.2162	0.010	21.025	0.000	0.196	0.236
zip_category_Low	-0.2261	0.007	-34.591	0.000	-0.239	-0.213
zip_category_Very High	0.5847	0.019	29.999	0.000	0.547	0.623
zip_category_Very low	-0.6086	0.008	-78.530	0.000	-0.624	-0.593
=======================================					======	

zip_category_Very low	-0.6086	0.008 -78.530	0.000 -0.624
Omnibus: Prob(Omnibus): Skew: Kurtosis:	2787.048 0.000 -0.523 9.391	Durbin-Watson: Jarque-Bera (JB): Prob(JB): Cond. No.	1.947 28316.363 0.00 312.

Notes

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Interpretation of the baseline model

The model explains around 70% of the variance and is significant. If all features are 0, the house would sell for around 22000 USD (exp(10). Some variables are not significant (garage, renovated, sewer system, heat source).

Improvement of the model

Next, I will improve the model by dropping variables that are not significant or that do not make sense based on the coefficient or based on the scatter plot.

In [29]:

```
X2 = X.drop(["patio_YES"], axis=1) #dropping patio due non signifcance
model_v2 = sm.OLS(y, sm.add_constant(X2))
results_v2 = model_v2.fit()
print(results_v2.summary())
```

	OLS Regres	sion Resu	lts			
Dep. Variable:	price_log	 R-squar	ed:	======	0.701	
Model:	OLS	Adj. R-	squared:		0.700	
Method:	Least Squares	F-stati	stic:		1804.	
Date:	ue, 28 Feb 2023	Prob (F	<pre>-statistic):</pre>		0.00	
Time:	16:19:53	Log-Lik	elihood:		-3820.3	
No. Observations:	16207	AIC:			7685.	
Df Residuals:	16185	BIC:			7854.	
Df Model:	21					
Covariance Type:	nonrobust					
		std err	t	P> t	[0.025	0.975]
const	10.5582	0.064	165.716	0.000	10.433	10.683
bedrooms	0.0232	0.003	7.187	0.000	0.017	0.030
bathrooms	0.0262	0.004	6.726	0.000	0.019	0.034
grade	0.1023	0.003	30.247	0.000	0.096	0.109
sqft_above_log	0.3354	0.011	31.868	0.000	0.315	0.356
waterfront_YES	0.1891	0.026	7.228	0.000	0.138	0.240
basement_YES	0.1398	0.006	23.663	0.000	0.128	0.151
garage_YES	-0.0538	0.006	-9.751	0.000	-0.065	-0.043
greenbelt_YES	-0.0525	0.016	-3.291	0.001	-0.084	-0.021
view_AVERAGE	0.0943	0.009	10.275	0.000	0.076	0.112
view_EXCELLENT	0.3849	0.021	18.185	0.000	0.343	0.426
view_FAIR	0.1411	0.026	5.445	0.000	0.090	0.192
view_GOOD	0.1563	0.014	11.385	0.000	0.129	0.183
heat_source_Electricit	y -0.0204	0.006	-3.191	0.001	-0.033	-0.008
heat_source_Oil	0.0160	0.008	1.953	0.051	-5.67e-05	0.032
heat_source_Other	0.0004	0.028	0.015	0.988	-0.055	0.056
sewer_system_PRIVATE	-0.0437	0.010	-4.226	0.000	-0.064	-0.023
renovated_YES	0.0722	0.011	6.770	0.000	0.051	0.093
zip_category_High	0.2161	0.010	21.022	0.000	0.196	0.236
zip_category_Low	-0.2261	0.007	-34.597	0.000	-0.239	-0.213
zip_category_Very High	n 0.5845	0.019	29.996	0.000	0.546	0.623
zip_category_Very low	-0.6086	0.008	-78.531 	0.000	-0.624 =====	-0.593
Omnibus:	2788.071	 -Durbin		======	1.947	
Prob(Omnibus):	0.000	Jarque-	Bera (JB):		28285.360	
Skew:	-0.523	Prob(JB):		0.00	
Kurtosis:	9.387	Cond. N	0.		311.	

Notes

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

I will drop some more variables due to their insignificance

In [30]:

OLS Regression Results						
Dep. Variable: Model: Method: Date: Time: No. Observations:	price_log OLS Least Squares Tue, 28 Feb 2023 16:19:53 16207	R-squared: Adj. R-squared: F-statistic: Prob (F-statistic): Log-Likelihood: AIC:	0.700 0.700 2102. 0.00 -3829.0 7696.			
Df Residuals: Df Model: Covariance Type:	16188 18 nonrobust	BIC:	7842.			
covar farice Type.	nom obasc					

=======================================	.========		.=======			=======
	coef	td err	t	P> t	[0.025	0.975]
const	10.5079	0.062	168.581	0.000	10.386	10.630
bedrooms	0.0237	0.003	7.334	0.000	0.017	0.030
bathrooms	0.0229	0.004	6.069	0.000	0.015	0.030
grade	0.1014	0.003	30.043	0.000	0.095	0.108
sqft_above_log	0.3433	0.010	33.165	0.000	0.323	0.364
waterfront_YES	0.1857	0.026	7.101	0.000	0.134	0.237
basement_YES	0.1444	0.006	24.936	0.000	0.133	0.156
garage_YES	-0.0522	0.005	-9.506	0.000	-0.063	-0.041
greenbelt_YES	-0.0521	0.016	-3.266	0.001	-0.083	-0.021
view_AVERAGE	0.0949	0.009	10.342	0.000	0.077	0.113
view_EXCELLENT	0.3859	0.021	18.234	0.000	0.344	0.427
view_FAIR	0.1421	0.026	5.480	0.000	0.091	0.193
view_GOOD	0.1562	0.014	11.377	0.000	0.129	0.183
sewer_system_PRIVATE	-0.0456	0.010	-4.413	0.000	-0.066	-0.025
renovated_YES	0.0709	0.011	6.656	0.000	0.050	0.092
zip category High	0.2171	0.010	21.114	0.000	0.197	0.237
zip category Low	-0.2268	0.007	-34.820	0.000	-0.240	-0.214
zip_category_Very High	0.5878	0.019	30.196	0.000	0.550	0.626
zip_category_Very low	-0.6099	0.008	-78.758	0.000	-0.625	-0.595
Omnibus:		 Durbir	======== n-Watson:	=======	1.947	
Prob(Omnibus):	0.000	Jarque	e-Bera (JB):		28187.966	
Skew:	-0.526	Prob(` '		0.00	
Kurtosis:	9.375	Cond.	•		304.	
=======================================			.=======		=======	

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

In [31]:

```
#dropping greenbelt because of negative coefficient
X4 = X3.drop(["greenbelt_YES"], axis=1)
model_v4 = sm.OLS(y, sm.od_constant(X4))
results_v4 = model_v4.fit()
print(results_v4.summary())
```

OLS Regression Results						
Dep. Variable:	price_log	R-squ	R-squared: 0.7			
Model: Method:			R-squared:		0.700 2224.	
	Least Squares Tue, 28 Feb 2023		(F-statistic):		0.00	
Time:	•		ikelihood:		-3834.4	
No. Observations:	16207	AIC:	ikeiinoou.		7705.	
Df Residuals:	16189	BIC:			7843.	
Df Model:	10189	bic.			7043.	
Covariance Type:	nonrobust					
======================================						
		td err	t	P> t	[0.025	0.975]
const	10.5163	0.062	168.813	0.000	10.394	10.638
bedrooms	0.0239	0.003	7.389	0.000	0.018	0.030
bathrooms	0.0227	0.004	6.012	0.000	0.015	0.030
grade	0.1013	0.003	30.012	0.000	0.095	0.108
sqft_above_log	0.3418	0.010	33.045	0.000	0.322	0.362
waterfront_YES	0.1868	0.026	7.141	0.000	0.136	0.238
basement_YES	0.1451	0.006	25.050	0.000	0.134	0.156
garage_YES	-0.0532	0.005	-9.710	0.000	-0.064	-0.042
view_AVERAGE	0.0955	0.009	10.401	0.000	0.077	0.113
view_EXCELLENT	0.3863	0.021	18.247	0.000	0.345	0.428
view_FAIR	0.1438	0.026	5.546	0.000	0.093	0.195
view_GOOD	0.1567	0.014	11.411	0.000	0.130	0.184
sewer_system_PRIVATE	-0.0445	0.010	-4.308	0.000	-0.065	-0.024
renovated_YES	0.0719	0.011	6.745	0.000	0.051	0.093
zip_category_High	0.2177	0.010	21.166	0.000	0.198	0.238
zip_category_Low	-0.2250	0.006	-34.658	0.000	-0.238	-0.212
zip_category_Very Hig	gh 0.5909	0.019	30.382	0.000	0.553	0.629
zip_category_Very low	-0.6073	0.008	-78.818	0.000	-0.622	-0.592
=======================================					=======	
Omnibus:	2786.217	Durbi	n-Watson:		1.947	
Prob(Omnibus):	0.000		e-Bera (JB):		28138.644	
Skew:	-0.524	Prob(0.00	
Kurtosis:	9.369	Cond.	No.		304.	
=======================================					========	

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

In [32]:

```
#finally also dropping the renovated column
X5 = X4.drop(["sewer_system_PRIVATE"], axis=1) #dropping sqft_living due to high correlation with sqft_living and bathrooms
model_v5 = sm.OLS(y, sm.add_constant(X5))
results_v5 = model_v5.fit()
print(results_v5.summary())
```

	OLS Regres	ssion Res	sults			
Dep. Variable:	price_log	R-squa	 ared:		0.700	
Model:	OLS		R-squared:		0.700	
Method:	Least Squares	F-stat	tistic:		2359.	
Date:	Tue, 28 Feb 2023	Prob	(F-statistic):		0.00	
Time:	16:19:53	Log-L:	ikelihood:		-3843.6	
No. Observations:	16207	AIC:			7721.	
Df Residuals:	16190	BIC:			7852.	
Df Model:	16					
Covariance Type:	nonrobust					
	coef	std err	t	P> t	[0.025	0.975]
const	10.5213	0.062	168.829	0.000	10.399	10.643
bedrooms	0.0240	0.003	7.431	0.000	0.018	0.030
bathrooms	0.0233	0.004	6.178	0.000	0.016	0.031
grade	0.1020	0.003	30.214	0.000	0.095	0.109
sqft_above_log	0.3396	0.010	32.854	0.000	0.319	0.360
waterfront_YES	0.1764	0.026	6.769	0.000	0.125	0.228
basement_YES	0.1465	0.006	25.329	0.000	0.135	0.158
garage_YES	-0.0539	0.005	-9.837	0.000	-0.065	-0.043
view_AVERAGE	0.0948	0.009	10.324	0.000	0.077	0.113
view_EXCELLENT	0.3873	0.021	18.287	0.000	0.346	0.429
view_FAIR	0.1446	0.026	5.573	0.000	0.094	0.195
view_GOOD	0.1561	0.014	11.357	0.000	0.129	0.183
renovated_YES	0.0715	0.011	6.709	0.000	0.051	0.092
zip_category_High	0.2187	0.010	21.266	0.000	0.199	0.239
zip_category_Low	-0.2225	0.006	-34.390	0.000	-0.235	-0.210
zip_category_Very Hig	gh 0.5950	0.019	30.614	0.000	0.557	0.633
zip_category_Very low	-0.6068	0.008	-78.719	0.000	-0.622	-0.592
Omnibus:	2799.316	 Durbir	 n-Watson:	:======	1.948	
Prob(Omnibus):	0.000	Jarque	e-Bera (JB):		28088.427	
Skew:	-0.531	Prob(` '		0.00	
Kurtosis:	9.361	Cond.	,		303.	
					=======	

Notes

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Looking at the coefficients, the garage coefficient does not make sense. Why should a house with a garage be lower in price than a house without one. Zip categories look good. Bathrooms and bedrooms don't have a lot of impact. I might drop them to avoid overfitting.

In [33]:

OLS Regression Res	:u1	Lts
--------------------	-----	-----

============			
Dep. Variable:	price_log	R-squared:	0.687
Model:	OLS	Adj. R-squared:	0.687
Method:	Least Squares	F-statistic:	3947.
Date:	Tue, 28 Feb 2023	<pre>Prob (F-statistic):</pre>	0.00
Time:	16:19:53	Log-Likelihood:	-4186.7
No. Observations:	16207	AIC:	8393.
Df Residuals:	16197	BIC:	8470.
Df Model:	9		
Covariance Type:	nonrobust		
=======================================		.==========	=============
	coef st	d err t	P> t [0.025

	coef s	td err	t	P> t	[0.025	0.975]
const	10.0961	0.049	204.468	0.000	9.999	10.193
grade	0.1083	0.003	34.162	0.000	0.102	0.115
sqft_above_log	0.4044	0.008	49.478	0.000	0.388	0.420
waterfront_YES	0.4280	0.023	18.663	0.000	0.383	0.473
basement_YES	0.1893	0.005	35.002	0.000	0.179	0.200
renovated_YES	0.0985	0.011	9.136	0.000	0.077	0.120
zip_category_High	0.2230	0.010	21.271	0.000	0.202	0.244
zip_category_Low	-0.2222	0.007	-33.703	0.000	-0.235	-0.209
zip_category_Very High	0.5922	0.020	29.844	0.000	0.553	0.631
zip_category_Very low	-0.6086	0.008	-77.555	0.000	-0.624	-0.593
	=========				=======	
Omnibus:	2560.250	Durbir	n-Watson:		1.946	
Prob(Omnibus):	0.000	Jarque	e-Bera (JB):		24737.794	
Skew:	-0.462	Prob(J	IB):		0.00	
Kurtosis:	8.981	Cond.	No.		218.	

Notes

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Interpretation of my model

Dropping the variables resulted in a slightly lower explained variance but at least all variables are significant and meaningful. The model explains around 68% of the variance and is significant. My target variable is in log dollars so if all features are 0, the house would sell for around 22000 USD (exp(10)). For my categorical values, my reference values are: zip_category medium, basement no, waterfront no. For the most impactful numerical values, we can say that with each grade increase, the price will increase by 11%. Also, for 10% increase in sqft above, the price will increase by 4%.

The location of a property depending on the zip code also has an impact on price. Compared to zip codes with medium average house prices, the prices drop significantly for low and very low zip code categories and rise significantly for high and higher zip codes. This fits to what we have seen in the zip code map where there are significant differences based on the region.

In [34]:

```
#calculating grade increase
print("For each grade increase, price increases by ",
      np.exp(10.0961+0.1083)/np.exp(10.0961))
print("For 10% increase in sqft, price increases by ",
      1.1**0.4044)
print("For waterfront house, geom mean of price increases by ",
      np.exp(10.0961+0.4044)/np.exp(10.0961))
print("For house w basement, geom mean of price increases by ",
      np.exp(10.0961+0.1893)/np.exp(10.0961))
print("For house w renovation, geom mean of price increases by ",
      np.exp(10.0961+0.0985)/np.exp(10.0961))
print("For house w zip category very low compared to medium, geom mean of price decreases by ",
      np.exp(10.0961-0.6086)/np.exp(10.0961))
print("For house w zip category low compared to medium, geom mean of price decreases by ",
      np.exp(10.0961-0.2222)/np.exp(10.0961))
print("For house w zip category high compared to medium, geom mean of price increases by ",
      np.exp(10.0961+0.2230)/np.exp(10.0961))
print("For house w zip category very high compared to medium, geom mean of price increases by ",
      np.exp(10.0961+0.5922)/np.exp(10.0961))
```

```
For each grade increase, price increases by 1.1143820098472454

For 10% increase in sqft, price increases by 1.0392958709738869

For waterfront house, geom mean of price increases by 1.498403188377217

For house w basement, geom mean of price increases by 1.2084034191359254

For house w renovation, geom mean of price increases by 1.103514404394391

For house w zip category very low compared to medium, geom mean of price decreases by 0.5441120930236357

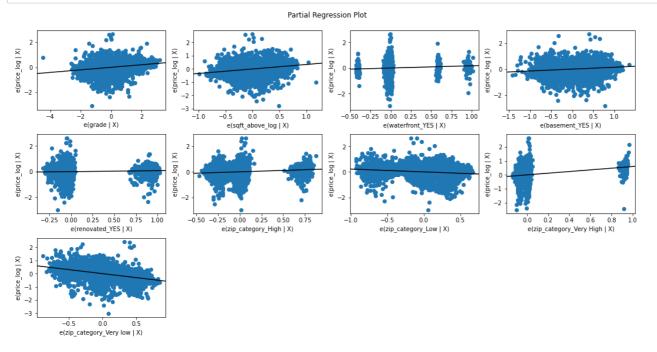
For house w zip category low compared to medium, geom mean of price decreases by 0.8007551972790311

For house w zip category high compared to medium, geom mean of price increases by 1.2498205737359849

For house w zip category very high compared to medium, geom mean of price increases by 1.8079615587669373
```

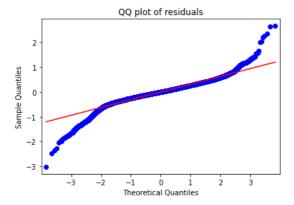
In [35]:

```
#inspecting the residuals
fig = plt.figure(figsize=(15,15))
sm.graphics.plot_partregress_grid(
    results_v5,
    exog_idx=list(X6.columns.values),
    grid=(6,4),
    fig=fig)
plt.show()
```



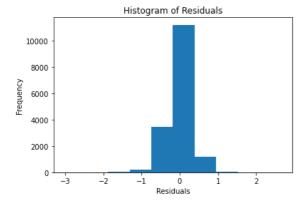
In [36]:

```
residuals = results_v6.resid
sm.qqplot(residuals, line="s")
plt.title("QQ plot of residuals")
plt.show()
```



In [37]:

```
plt.hist(residuals, bins=10)
plt.xlabel('Residuals')
plt.ylabel('Frequency')
plt.title('Histogram of Residuals')
plt.show()
```



In [38]:

```
from scipy.stats import shapiro
# Perform the Shapiro-Wilk test on residuals
stat, p = shapiro(residuals)
print('Shapiro-Wilk test statistic: {:.3f}, p-value: {:.3f}'.format(stat, p))
if p > 0.05:
    print('Residuals are normally distributed')
else:
    print('Residuals are not normally distributed')
```

Shapiro-Wilk test statistic: 0.941, p-value: 0.000 Residuals are not normally distributed

 $\label{lem:c:Users} C: \label{lem:c:Users} I earn-env\lib\site-packages\scipy\stats\morestats.py: 1681: User \warning: \line \line \line \morestats.py: 1681: User \warning: \line \morestats.py: \more$

p-value may not be accurate for N > 5000.

My residuals are not normally distributed. Looking at a confidence interval, my model is great at predicting values within 2 standard deviations of the mean so for 95% of the objects, the model will work well. For anything outside of this range it will underestimate the price of expensive objects and overestimate the price of cheap houses.

Calculating the MAE

The MAE is more appropriate for models with a log-transformed dependent variable because it measures the absolute difference between the predicted and actual values on the original scale of the data. When both the dependent and independent variables are log-transformed, the Mean Absolute Error (MAE) can be interpreted as the average absolute difference between the actual and predicted values, expressed as a percentage of the geometric mean of the actual and predicted values.

The geometric mean is used because the log transformation converts multiplication to addition, so the geometric mean of the actual and predicted values is the exponential of the mean of the log-transformed values.

In [39]:

```
model = LinearRegression()
model.fit(X6,y)
yhat = model.predict(X6)
```

In [40]:

```
# use the scikit-learn library's mean_absolute_error function
mae = mean_absolute_error(np.exp(y), np.exp(yhat))
geom_mean = np.sqrt(np.exp(y) * np.exp(yhat))
mae_percent = mae / np.mean(geom_mean) * 100
print("MAE (as percentage of geometric mean): {:.2f}%".format(mae_percent))
```

MAE (as percentage of geometric mean): 23.04%

In [41]:

```
# use the scikit-learn library's mean_absolute_error function
mae = mean_absolute_error(np.exp(y), np.exp(yhat))
geom_mean = np.sqrt(np.exp(y) * np.exp(yhat))
mae_percent = mae / np.mean(geom_mean) * 100
print("MAE (as percentage of geometric mean): {:.2f}%".format(mae_percent))
```

MAE (as percentage of geometric mean): 23.04%

On average, my model's prediction is off by 23% of the geometric mean of the actual and predicted values. This should be improved with future models.

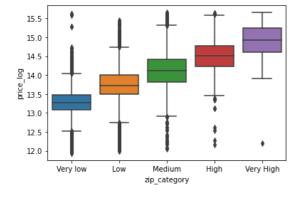
Further testing

I will now again look at the boxplots of the categorical values and confirm with a ttest or ANOVA

Testing Hypothesis 1: H1: The price is different depending on the neighbourhood you live in. H0: There is no difference depending on where you live.

In [42]:

```
#Visualising with a box plot
sns.boxplot( x=df["zip_category"], y=df["price_log"], order=[
    "Very low", "Low", "Medium", "High", "Very High"] );
plt.show()
```



In [43]:

```
#preparing the groups for my ANOVA
Very_low = df[df["zip_category"]=="Very low"]["price_log"]
Low = df[df["zip_category"]=="Low"]["price_log"]
Medium = df[df["zip_category"]=="Medium"]["price_log"]
High = df[df["zip_category"]=="High"]["price_log"]
Very_high = df[df["zip_category"]=="Very High"]["price_log"]
```

In [44]:

```
#Conducting ANOVA
from scipy.stats import f_oneway
f_oneway(Very_low, Low, Medium, High, Very_high)
print("Mean very low: ", Very_low.mean())
print("Mean very high: ", Very_high.mean())
```

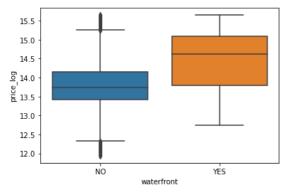
Mean very low: 13.278613131321137 Mean very high: 14.894837664514732

ANOVA shows that there is indeed a price difference depending on the neighbourhood you are in. Therefore, rejecting the null hypothesis. The prices vary from a mean of 580.0000 USD in the very low zipcodes and 2.9 mio USD in the very high zipcodes

Testing Hypothesis 2: The price of a house is higher if you have a waterfront H0: The price is less or equal when you have a waterfront

In [45]:

```
#visualising with boxplot
sns.boxplot( x=df["waterfront"], y=df["price_log"] );
plt.show()
```



In [46]:

```
#conducting t.test
from scipy.stats import ttest_ind
waterfront = df[df["waterfront"]=="YES"]["price_log"]
no_waterfront = df[df["waterfront"]=="NO"]["price_log"]
t_stat, p_value = ttest_ind(waterfront, no_waterfront)
print("T-statistic value: ", t_stat)
print("P-Value: ", p_value)
print("Mean No waterfront: ", no_waterfront.mean())
print("Mean waterfront: ", waterfront.mean())
```

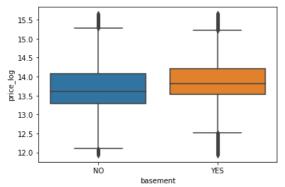
T-statistic value: 16.394556349400133 P-Value: 6.350296717606978e-60 Mean No waterfront: 13.79572730987044 Mean waterfront: 14.458361520828648

Rejecting the null hypothesis. If you have no waterfront, the mean price is exp(13.79) which are 974000 USD. If you have a waterfront, the mean price is exp(14.45) which is 1.88 Mio USD. In the boxplot you can see, that even with no waterfront, you have a lot of outliers on both sides.

Testing Hypothesis 3: The price of a house is higher if you have a basement H0: The price is less or equal when you have a basement

In [47]:

```
#visualising with boxplot
sns.boxplot( x=df["basement"], y=df["price_log"] );
plt.show()
```



In [48]:

```
#conducting t-test
basement = df[df["basement"]=="YES"]["price_log"]
no_basement = df[df["basement"]=="NO"]["price_log"]
t_stat, p_value = ttest_ind(basement, no_basement)
print("T-statistic value: ", t_stat)
print("P-Value: ", p_value)
print("Mean No basement: ", no_basement.mean())
print("Mean basement: ", basement.mean())
```

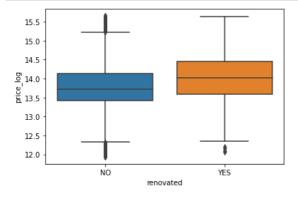
T-statistic value: 20.84027400630386 P-Value: 3.301642077452239e-95 Mean No basement: 13.696640588525463 Mean basement: 13.88006691220265

Rejecting the null hypothesis. If you have no basement, the mean price is exp(13.69) which are 882000 USD. If you have a basement, the mean price is exp(13.88) which is 1.06 Mio USD. Compared to the waterfront, the price difference is not that large which makes sense.

Testing Hypothesis 4: The price of a house is higher if you have renovated H0: The price is less or equal when you have renovated

In [49]:

```
#visualising with boxplot
sns.boxplot( x=df["renovated"], y=df["price_log"] );
plt.show()
```



In [50]:

```
#conducting t-test
renovated = df[df["renovated"]=="YES"]["price_log"]
no_renovated = df[df["renovated"]=="NO"]["price_log"]
t_stat, p_value = ttest_ind(renovated, no_renovated)
print("T-statistic value: ", t_stat)
print("P-Value: ", p_value)
print("Mean No renovated: ", no_renovated.mean())
print("Mean renovated: ", renovated.mean())
```

T-statistic value: 11.969789579744424 P-Value: 7.039674909192125e-33 Mean No renovated: 13.790768445808618 Mean renovated: 14.018666512045364

Rejecting the null hypothesis. If you have not renovated, the mean price is exp(13.79) which are 974000 USD. If you have renovated, the mean price is exp(14.01) which is 1.2 Mio USD.

Recommendation

For the customer, the real estate company, who is advising both selling and buying clients, my model enables them to properly advise them in how much difference in price a certain feature of a house will result in. My model has an R² of .68 which is solid but not perfect. They will be able to talk in actual price ranges and inform their clients about price increases or decreased dependent on a certain feature. They can apply the following information from the model dependent on the specific house:

For each grade increase, price increases by 1.11 For 10% increase in sqft, price increases by 1.03 For waterfront house, geom mean of price increases by 1.49 For house w basement, geom mean of price increases by 1.20 For house w renovation, geom mean of price increases by 1.10 For house w zip category very low compared to medium, geom mean of price decreases by 0.54 For house w zip category low compared to medium, geom mean of price decreases by 0.80 For house w zip category high compared to medium, geom mean of price increases by 1.24 For house w zip category very high compared to medium, geom mean of price increases by 1.80

Summary

The model is a good start but requires further improving. We could look next at some other variables which might have an influence on the price. In general, it is understandable that you are not able to predict all house prices. There will always be exceptions so my model which is between 2 standard deviations predicts actually quite well.