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title: "Assignment 6: GLMs (Linear Regressions, ANOVA, & t-tests)"  
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output: pdf\_document  
geometry: margin=2.54cm  
dvi\_options:  
chunk\_output\_type: console

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## OVERVIEW

This exercise accompanies the lessons in Environmental Data Analytics on generalized linear models.

## Directions

1. Change "Student Name" on line 3 (above) with your name.
2. Work through the steps, **creating code and output** that fulfill each instruction.
3. Be sure to **answer the questions** in this assignment document.
4. When you have completed the assignment, **Knit** the text and code into a single PDF file.
5. After Knitting, submit the completed exercise (PDF file) to the dropbox in Sakai. Add your last name into the file name (e.g., "Fay\_A06\_GLMs.Rmd") prior to submission.

The completed exercise is due on Monday, February 28 at 7:00 pm.

## Set up your session

1. Set up your session. Check your working directory. Load the tidyverse, agricolae and other needed packages. Import the *raw* NTL-LTER raw data file for chemistry/physics (NTL-LTER\_Lake\_ChemistryPhysics\_Raw.csv). Set date columns to date objects.
2. Build a ggplot theme and set it as your default theme.

```
#1
getwd()

## [1] "/Users/juliaweinberg/Desktop/github repos/Environmental_Data_Analytics_2022/Assignments"
library(tidyverse)

## -- Attaching packages ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5      v purrr  0.3.4
## v tibble  3.1.6      v dplyr  1.0.7
## v tidyr   1.1.3      v stringr 1.4.0
## v readr   2.1.1      v forcats 0.5.1

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()

library(agricolae)
library(lubridate)

##
## Attaching package: 'lubridate'

## The following objects are masked from 'package:base':
##
##     date, intersect, setdiff, union
```

```

NTL_LTER <- read.csv("../Data/Raw/NTL-LTER_Lake_ChemistryPhysics_Raw.csv", stringsAsFactors = TRUE, head = FALSE)

NTL_LTER$sampldate <- as.Date(NTL_LTER$sampldate, format = "%m/%d/%y")
#format as date function
#2

my.theme <- theme_gray(base_size = 14) + #set base theme and size
  theme(axis.text = element_text(color = "darkblue"), #color text dark blue
        legend.position = "bottom") #align legend on bottom
theme_set(my.theme) #set theme

```

## Simple regression

Our first research question is: Does mean lake temperature recorded during July change with depth across all lakes?

3. State the null and alternative hypotheses for this question: > Answer: H0: There is no relationship between depth and lake temperature recorded in July. Ha: There is a relationship between lake temperature and depth recorded in July.
4. Wrangle your NTL-LTER dataset with a pipe function so that the records meet the following criteria:
  - Only dates in July.
  - Only the columns: lakename, year4, daynum, depth, temperature\_C
  - Only complete cases (i.e., remove NAs)
5. Visualize the relationship among the two continuous variables with a scatter plot of temperature by depth. Add a smoothed line showing the linear model, and limit temperature values from 0 to 35 °C. Make this plot look pretty and easy to read.

```

#4

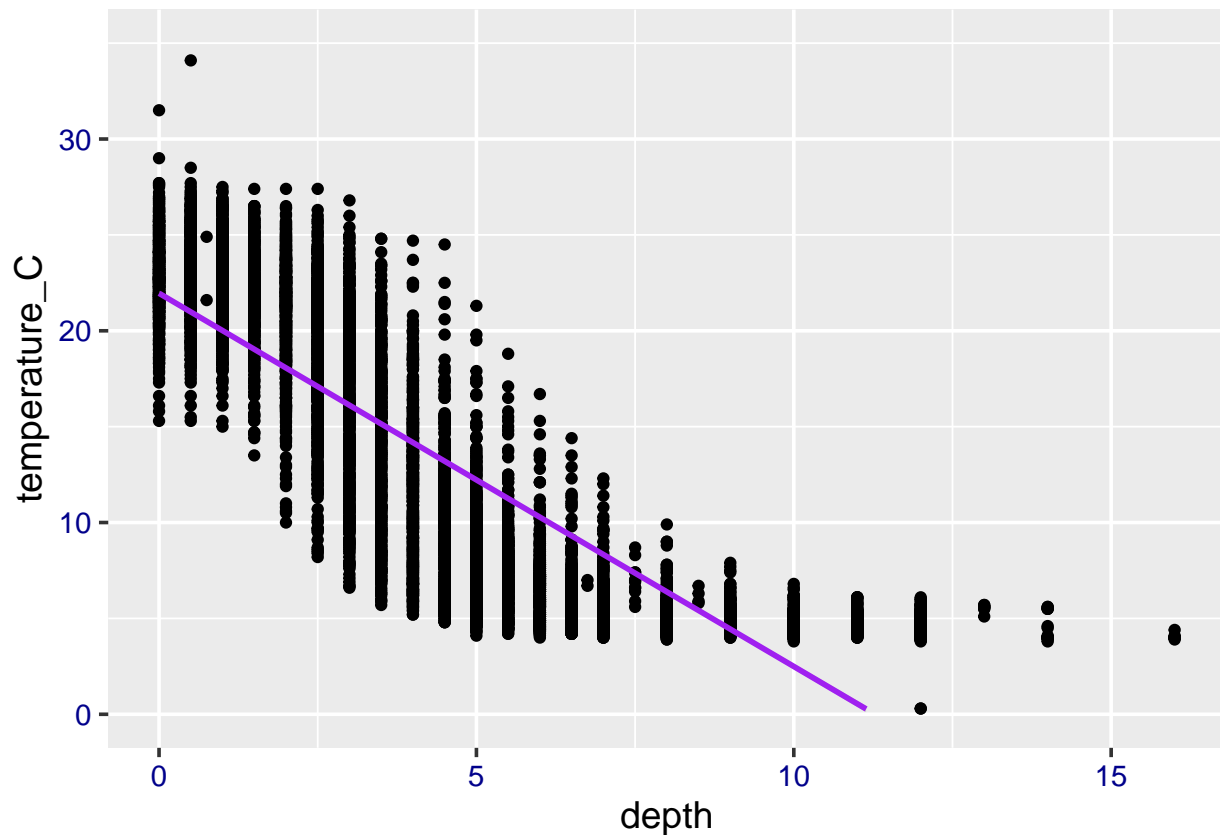
July.Temps <- NTL_LTER %>%
  mutate(month = month(sampldate))%>% #add column for month
  filter(month == "7") %>% #only include dates with July as month
  select(lakename, year4, daynum, depth, temperature_C)%>% #select variables
  filter(!is.na(temperature_C)) #filter out NA's

#5

temp.by.depth <- ggplot(July.Temps, aes(x = depth, y = temperature_C)) +
  #plot temp by depth
  geom_point()+
  ylim(0, 35)+ #limit data plotted
  geom_smooth(method = "lm", color = "purple")+ #add best fit line
  my.theme #include my theme
print(temp.by.depth) #print graph

## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 24 rows containing missing values (geom_smooth).

```



6. Interpret the figure. What does it suggest with regards to the response of temperature to depth? Do the distribution of points suggest about anything about the linearity of this trend?

Answer: This plot shows that as depth increases, temperature tends to decrease, therefore pointing to an inverse relationship between the two variables. However, this relationship is not entirely linear as temperature decreases begin to level off as depth continues to increase.

7. Perform a linear regression to test the relationship and display the results

```
#7
temp.depth.reg <- lm(data = July.Temps, temperature_C ~ depth)
#linear regression of july temperature by lake depth
summary(temp.depth.reg) #summary of regrerssion

##
## Call:
## lm(formula = temperature_C ~ depth, data = July.Temps)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.5173  -3.0192   0.0633   2.9365  13.5834
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  21.95597    0.06792   323.3  <2e-16 ***
## depth        -1.94621    0.01174  -165.8  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 3.835 on 9726 degrees of freedom
## Multiple R-squared:  0.7387, Adjusted R-squared:  0.7387
## F-statistic: 2.75e+04 on 1 and 9726 DF,  p-value: < 2.2e-16
```

8. Interpret your model results in words. Include how much of the variability in temperature is explained by changes in depth, the degrees of freedom on which this finding is based, and the statistical significance of the result. Also mention how much temperature is predicted to change for every 1m change in depth.

Answer: The R-squared value is 0.7387, which is closer to one, which would mean that the two variables are perfectly correlated. The p-value is 2.2e-16, which is much smaller than 0.05, therefore meaning that we should reject the null hypothesis, showing that there is some relationship between temperature and depth. The estimate for depth is -1.95, meaning that for every increase in depth of 1m, temperature decreased by 1.95 degrees C.

---

## Multiple regression

Let's tackle a similar question from a different approach. Here, we want to explore what might the best set of predictors for lake temperature in July across the monitoring period at the North Temperate Lakes LTER.

9. Run an AIC to determine what set of explanatory variables (year4, daynum, depth) is best suited to predict temperature.
10. Run a multiple regression on the recommended set of variables.

```
#9
library(dplyr)

TEMP.regression <- lm(data = July.Temps, temperature_C ~ depth +
                      year4 + daynum)
#create regression of temperature with chosen variables

step(TEMP.regression) #get step values

## Start:  AIC=26065.53
## temperature_C ~ depth + year4 + daynum
##
##           Df Sum of Sq    RSS   AIC
## <none>             141687 26066
## - year4      1         101 141788 26070
## - daynum     1        1237 142924 26148
## - depth      1       404475 546161 39189
##
## Call:
## lm(formula = temperature_C ~ depth + year4 + daynum, data = July.Temps)
##
## Coefficients:
## (Intercept)      depth      year4      daynum
##   -8.57556    -1.94644     0.01134     0.03978

#10

TEMP.regression <- lm(data = July.Temps, temperature_C ~ depth + year4 +
daynum)
summary(TEMP.regression) #get summary of temperature by chosen variables
```

```
##
## Call:
## lm(formula = temperature_C ~ depth + year4 + daynum, data = July.Temps)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.6536 -3.0000  0.0902  2.9658 13.6123
##
## Coefficients:
##              Estimate Std. Error  t value Pr(>|t|)
## (Intercept) -8.575564   8.630715  -0.994  0.32044
## depth       -1.946437   0.011683 -166.611 < 2e-16 ***
## year4        0.011345   0.004299   2.639  0.00833 **
## daynum       0.039780   0.004317   9.215 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.817 on 9724 degrees of freedom
## Multiple R-squared:  0.7412, Adjusted R-squared:  0.7411
## F-statistic: 9283 on 3 and 9724 DF,  p-value: < 2.2e-16
```

11. What is the final set of explanatory variables that the AIC method suggests we use to predict temperature in our multiple regression? How much of the observed variance does this model explain? Is this an improvement over the model using only depth as the explanatory variable?

Answer: The final set of variables is depth, daynum, and year. The AIC suggests that using depth, year, and daynum provides a better correlation to temperature than just depth alone. When depth was used alone, only 73.87% of variance in lake temperature was accounted for, however when year and daynum are added, 74.11% of the variance in temperature is accounted for.

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## Analysis of Variance

12. Now we want to see whether the different lakes have, on average, different temperatures in the month of July. Run an ANOVA test to complete this analysis. (No need to test assumptions of normality or similar variances.) Create two sets of models: one expressed as an ANOVA models and another expressed as a linear model (as done in our lessons).

```
#12
july.temp.anova <- aov(data = July.Temps , temperature_C ~ lakename)
summary(july.temp.anova) #create anova of July temps by chosen variables
```

```
##              Df Sum Sq Mean Sq F value Pr(>F)
## lakename      8  21642   2705.2     50 <2e-16 ***
## Residuals    9719 525813     54.1
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
july.temp.linear <- lm(data = July.Temps, temperature_C ~ lakename)
summary(july.temp.linear)
```

```
##
## Call:
## lm(formula = temperature_C ~ lakename, data = July.Temps)
##
## Residuals:
```

```
##      Min      1Q  Median      3Q      Max
## -10.769  -6.614  -2.679   7.684  23.832
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      17.6664    0.6501  27.174 < 2e-16 ***
## lakenamCrampton Lake    -2.3145    0.7699  -3.006 0.002653 **
## lakenamEast Long Lake   -7.3987    0.6918 -10.695 < 2e-16 ***
## lakenamHummingbird Lake -6.8931    0.9429  -7.311 2.87e-13 ***
## lakenamPaul Lake        -3.8522    0.6656  -5.788 7.36e-09 ***
## lakenamPeter Lake       -4.3501    0.6645  -6.547 6.17e-11 ***
## lakenamTuesday Lake    -6.5972    0.6769  -9.746 < 2e-16 ***
## lakenamWard Lake        -3.2078    0.9429  -3.402 0.000672 ***
## lakenamWest Long Lake   -6.0878    0.6895  -8.829 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.355 on 9719 degrees of freedom
## Multiple R-squared:  0.03953,    Adjusted R-squared:  0.03874
## F-statistic:    50 on 8 and 9719 DF,  p-value: < 2.2e-16
```

```
#create linear regression of July temps by chosen variables
```

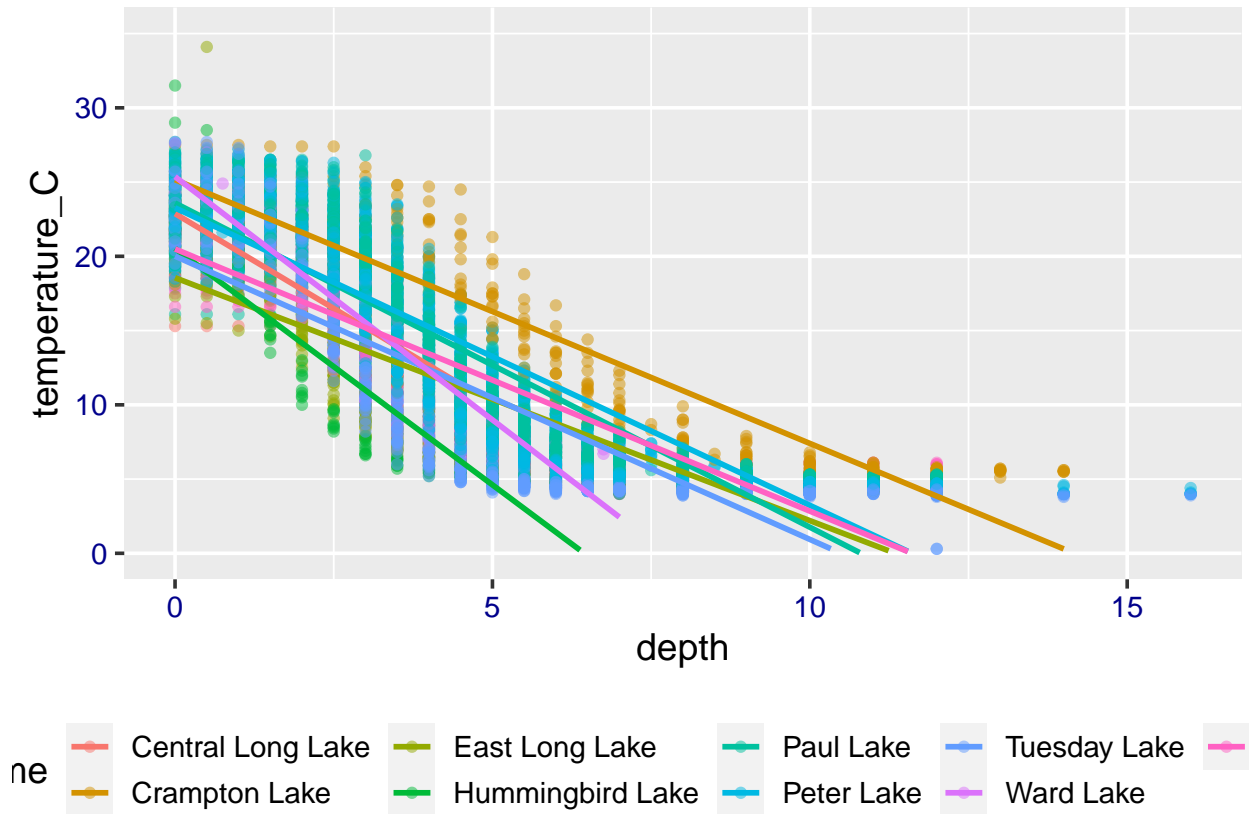
13. Is there a significant difference in mean temperature among the lakes? Report your findings.

Answer: Yes, there is a significant difference between all of the lakes as they all have p-values less than 0.05.

14. Create a graph that depicts temperature by depth, with a separate color for each lake. Add a `geom_smooth` (method = "lm", se = FALSE) for each lake. Make your points 50 % transparent. Adjust your y axis limits to go from 0 to 35 degrees. Clean up your graph to make it pretty.

```
#14.
plot.of.temp.by.depth <- ggplot(July.Temps, aes(x = depth, y = temperature_C, color = lakenam))+
  geom_point(alpha = 0.5)+ #set transparency to 50%
  ylim(0, 35)+ #limit data plotted
  geom_smooth(method = "lm", se = FALSE)+#add best fit line
my.theme #include by theme
print(plot.of.temp.by.depth) #print graph

## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 73 rows containing missing values (geom_smooth).
```



15. Use the Tukey's HSD test to determine which lakes have different means.

#15

```
TukeyHSD(july.temp.anova) #use Tukey's HSD test
```

```
## Tukey multiple comparisons of means
## 95% family-wise confidence level
##
## Fit: aov(formula = temperature_C ~ lakename, data = July.Temps)
##
## $lakename
##
```

	diff	lwr	upr	p adj
## Crampton Lake-Central Long Lake	-2.3145195	-4.7031913	0.0741524	0.0661566
## East Long Lake-Central Long Lake	-7.3987410	-9.5449411	-5.2525408	0.0000000
## Hummingbird Lake-Central Long Lake	-6.8931304	-9.8184178	-3.9678430	0.0000000
## Paul Lake-Central Long Lake	-3.8521506	-5.9170942	-1.7872070	0.0000003
## Peter Lake-Central Long Lake	-4.3501458	-6.4115874	-2.2887042	0.0000000
## Tuesday Lake-Central Long Lake	-6.5971805	-8.6971605	-4.4972005	0.0000000
## Ward Lake-Central Long Lake	-3.2077856	-6.1330730	-0.2824982	0.0193405
## West Long Lake-Central Long Lake	-6.0877513	-8.2268550	-3.9486475	0.0000000
## East Long Lake-Crampton Lake	-5.0842215	-6.5591700	-3.6092730	0.0000000
## Hummingbird Lake-Crampton Lake	-4.5786109	-7.0538088	-2.1034131	0.0000004
## Paul Lake-Crampton Lake	-1.5376312	-2.8916215	-0.1836408	0.0127491
## Peter Lake-Crampton Lake	-2.0356263	-3.3842699	-0.6869828	0.0000999
## Tuesday Lake-Crampton Lake	-4.2826611	-5.6895065	-2.8758157	0.0000000
## Ward Lake-Crampton Lake	-0.8932661	-3.3684639	1.5819317	0.9714459
## West Long Lake-Crampton Lake	-3.7732318	-5.2378351	-2.3086285	0.0000000
## Hummingbird Lake-East Long Lake	0.5056106	-1.7364925	2.7477137	0.9988050
## Paul Lake-East Long Lake	3.5465903	2.6900206	4.4031601	0.0000000

## Peter Lake-East Long Lake	3.0485952	2.2005025	3.8966879	0.0000000
## Tuesday Lake-East Long Lake	0.8015604	-0.1363286	1.7394495	0.1657485
## Ward Lake-East Long Lake	4.1909554	1.9488523	6.4330585	0.0000002
## West Long Lake-East Long Lake	1.3109897	0.2885003	2.3334791	0.0022805
## Paul Lake-Hummingbird Lake	3.0409798	0.8765299	5.2054296	0.0004495
## Peter Lake-Hummingbird Lake	2.5429846	0.3818755	4.7040937	0.0080666
## Tuesday Lake-Hummingbird Lake	0.2959499	-1.9019508	2.4938505	0.9999752
## Ward Lake-Hummingbird Lake	3.6853448	0.6889874	6.6817022	0.0043297
## West Long Lake-Hummingbird Lake	0.8053791	-1.4299320	3.0406903	0.9717297
## Peter Lake-Paul Lake	-0.4979952	-1.1120620	0.1160717	0.2241586
## Tuesday Lake-Paul Lake	-2.7450299	-3.4781416	-2.0119182	0.0000000
## Ward Lake-Paul Lake	0.6443651	-1.5200848	2.8088149	0.9916978
## West Long Lake-Paul Lake	-2.2356007	-3.0742314	-1.3969699	0.0000000
## Tuesday Lake-Peter Lake	-2.2470347	-2.9702236	-1.5238458	0.0000000
## Ward Lake-Peter Lake	1.1423602	-1.0187489	3.3034693	0.7827037
## West Long Lake-Peter Lake	-1.7376055	-2.5675759	-0.9076350	0.0000000
## Ward Lake-Tuesday Lake	3.3893950	1.1914943	5.5872956	0.0000609
## West Long Lake-Tuesday Lake	0.5094292	-0.4121051	1.4309636	0.7374387
## West Long Lake-Ward Lake	-2.8799657	-5.1152769	-0.6446546	0.0021080

16. From the findings above, which lakes have the same mean temperature, statistically speaking, as Peter Lake? Does any lake have a mean temperature that is statistically distinct from all the other lakes?

Answer: Paul lake is the only one with a similar temperature. Its difference in temperature mean is closest to Peter Lake at only -0.49, however it is not a statistically significant similarity as its p-value is greater than 0.05. Central Long Lake is most distinct from the other lakes as it has the greatest difference in mean temperature compared to the other lakes in the data set.

17. If we were just looking at Peter Lake and Paul Lake. What's another test we might explore to see whether they have distinct mean temperatures?

Answer: A HSD test would be good to use as it would group lakes that are similar to one another by letter categories.