FLORIDA STATE UNIVERSITY COLLEGE OF ARTS & SCIENCES

THIS IS MY TITLE:

AND THIS IS ITS SECOND LINE

By

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TABLE OF CONTENTS

Li	st of	Figures	· · · · · · · · · · · · · · · · · · ·	/ii		
Li	st of	Abbrev	iations	iii		
A	bstrac	et		ix		
1	Introduction					
	1.1	Mathe	ematics of Fluid Flow	2		
		1.1.1	Continuum Description of Fluids	4		
		1.1.2	Equation of State	6		
	1.2	Turbu	lence	7		
		1.2.1	Historical Perspective	8		
		1.2.2	Round Jet Theory	8		
		1.2.3	Numerical Approaches	8		
	1.3	Super	critical Carbon Dioxide	8		
		1.3.1	Applications of Interest	10		
		1.3.2	Overview of Current Numerical Landscape	11		
2	Mo	del Ov	rerview 1	14		
	2.1	Introd	luction	14		
	2.2	Gover	ning Equations	14		
		2.2.1	High Pressure Corrections for Transport Models	15		
	2.3	Nume	rical Methods	15		
		2.3.1	Subgrid-Scale Modeling for Large Eddy Simulation	15		
		2.3.2	Piecewise Parabolic Method Overview	16		
		2.3.3	Approximate Riemann Solver Details	16		
		2.3.4	Time Stepping with RK2	16		
3	Sim	nulation	ns 1	17		
	3.1	Comp	utational Domain	17		
		3.1.1	AMReX and Discretization	17		
		3.1.2	Initial and Boundary Conditions	17		
	3.2	Case I	Descriptions	19		

		3.2.1 Parameter Choices	19
	3.3	Compute Time and Hardware Specifications	19
	3.4	Post-Processing Procedures	19
4	Res	sults	20
	4.1	Ideal Gas Comparison	20
		4.1.1 Mean Turbulence Statistics	20
	4.2	Cross-Case Comparisons	20
		4.2.1 Axial Visuals	20
5	Con	nclusion	21
	5.1	Summary	21
	5.2	Future Work	21
Bi	bliogr	raphy	22
Bi	ograp	phical Sketch	29

LIST OF FIGURES

1.1	Characteristic length scale of problem, L , compared to mean free path of particles, ℓ , for a flow with large Knudsen number (left) vs. small Knudsen number (right)	3
1.2	A fluid of arbitrary volume V bounded by surface S with velocity $\vec{v}(\vec{x},t)$. A differential volume and surface area is given by dv and ds , respectively. \vec{n} is the outward-pointing unit normal vector to the surface S	4
1.3	Example of streamlines in laminar (left) vs. turbulent (right) flow	7
1.4	LES resolves large scale eddies (black) and models fine scale eddies (red) that are unresolved due to mesh size	9
1.5	Phase diagram for Carbon Dioxide (CO2). Critical pressure, p_c , and temperature, T_c , are 73.773 bar and 304.128 K, respectively	9
1.6	Size comparison for steam vs. supercritical Carbon Dioxide (sCO2) turbine via Echogen Power Systems LLC [41]	10
3.1	Two dimensional slice schematic of jet setup. Four levels of refinement are enforced within the green box based on proximity to jet inlet. Refinement based on vorticity criterion then occurs within the blue region. Outside the blue region, adaptive mesh refinement (AMR) is explicitly turned off to allow flow structures to be dissipated numerically and allowed to leave the domain without incurring spurious reflections.	18

LIST OF ABBREVIATIONS

The following short list of abbreviations are used throughout this document.

AMR Adaptive Mesh Refinement CFD Computational Fluid Dynamics CO2Carbon Dioxide DNS Direct Numerical Simulation Department of Energy DOE Exascale Computing Project ECP EoSequation of state HPC high-performance computing LES Large Eddy Simulation **NIST** National Institute of Standards and Technology NREL National Renewable Energy Laboratory PPM piecewise parabolic method Peng-Robinson equation of state PR EoS RANS Reynolds-Averaged Navier-Stokes

rms root mean square

sCO2 Supercritical Carbon Dioxide

SGS Subgrid Scale

SMD dynamic Smagorinsky

SRK EoS Soave-Redlich-Kwong equation of state

ABSTRACT

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CHAPTER 1

INTRODUCTION

Fluids are a vital part of everyday life - two of the most common ones being the air we breath and the water we drink. Less obvious are all the ways even these common fluids function behind the scenes in our day to day activities. Water, for example, serves an important role in various industrial settings, proving useful in areas ranging from thermal management to energy production; steam turbines alone accounted for 45% of electricity generation in the United States in 2021 [54]. Improvements to these types of systems impact technologies across a variety of fields and are thus an important area of research. One strategy toward this end, and the primary motivator of the work presented here, is the use of supercritical fluids as the working fluid of these systems.

In order to discuss supercritical fluids further, we must first go into more detail about general fluids. A *fluid* is a large collection of mutually interacting particles (e.g. molecules, atoms, etc.) in a state of constant and chaotic motion. This results in the continuous deformation of the substance under the effects of a shearing stress. The two categories of fluids that most people are familiar with are gases and liquids. *Liquids* are (mostly) incompressible and have definite volume for a set temperature and pressure. *Gases* are compressible and do not have definite volume. A simplified distinction between the two is that both gases and liquids will conform to the shape of whatever container they are in, but gases will further spread to fill all available space present.

A supercritical fluid is a fluid that is held above a critical temperature and pressure, at which point the distinction between a gas and liquid phase no longer exists [17, 55]. Supercritical fluids have qualities associated with both gases and liquids yet simultaneously have features that exclude them from fully being categorized as one or the other. For example, while they have viscosities akin to gases, they have solvent capabilities associated with liquids []. Similarly, while they have densities in line with liquids, they lack surface tension []. One benefit of this duality is that supercritical fluids can be fine tuned to be more gas-like or more liquid-like depending on the application at hand. This also results in ambiguity on how to actually classify them, with some sources considering them highly compressed gases [21], expanded liquids [1], or even as their own distinctly separate phase [6]. The distinction usually lies on the specifics of the regime and the application at hand.

This work is concerned with sCO2 in particular. sCO2 has many beneficial features to a wide variety of industrial applications, as we will detail further in section []. Many of the applications of interest to this work involve injection technologies that require a round turbulent jet configuration within the system. While much research has gone into sCO2 flows, the current landscape is lacking in turbulence of this type with the context of understanding the underlying physics relating to the flow itself. For research that does involve other supercritical turbulent jets, the regimes explored in those works typically involve transcritical fluid injection within the regime of interest or explore regions outside the scope of this work.

The goal of this work is to explore the pseudo-boiling region of the pseudo-critical zone and analyze the influence of extreme thermodynamic fluctuations on turbulence statistics within the flow field. To that end, the rest of this chapter continues as follows: first, the mathematical framework for modeling compressible Newtonian fluids is provided to form the basis of the modeling done in this dissertation. Further consideration is then given to turbulence modeling and the numerical methods developed for studying turbulence to provide insight into the quantities of interest analyzed within this dissertation and the choices of numerical methods used herein. Important applications of supercritical carbon dioxide in particular are provided to motivate the problem presented in this dissertation. Existing numerical studies on supercritical fluids are reviewed to demonstrate how this dissertation fits into the current landscape of research and to emphasize the contribution the results of this work make to the field. This chapter concludes with an outline of the dissertation, the goals of the dissertation, and the main contributions made through this work.

1.1 Mathematics of Fluid Flow

Scale is one of the key factors to consider when developing a mathematical description of a fluid system. For example, consider modeling flow past a satellite in the exosphere vs. the flow past a turtle in the ocean; these two mediums have vastly different characteristics and would thus require different modeling techniques. Scale is also an important concept when it comes to turbulence in particular so we will begin that discussion here with our choice in perspective for the mathematical framework of our system of interest.

From a kinetic perspective, particle motion within a fluid can be broken up into two phases: particle interaction and free flight. Average time spent in free flight, $\langle t_f \rangle$, is typically much greater than collision time for a given interaction, t_c . The average length traveled between collisions is known as the mean free path, ℓ . Since free flight time dominates particle interaction time, this phase determines the length scale of the kinetic description of motion. In addition to this inherent physical scale, there is also a scale associated with the resolution of the problem itself, L. These two scales are important, as the mathematical description of your model depends on how these two scales compare to one another. This comparison is related through the non-dimensional Knudsen number:

$$Kn = \frac{\ell}{L} \tag{1.1}$$

Flows with large Knudsen number $(Kn \gg 10)$ require modeling from the kinetic or microscopic perspective as particle interactions become sparse enough compared to the scope of the problem to require a statistical mechanics framework. On the other hand, small Knudsen number flows $(Kn \ll 0.01)$ have a problem scale that far exceeds the particle-level interactions present, giving way to an average overall motion within the fluid. This scale dichotomy is demonstrated with the graphic in Figure 1.1. For small Knudsen flows, a continuum description of the fluid is appropriate for capturing this macroscopic behavior.

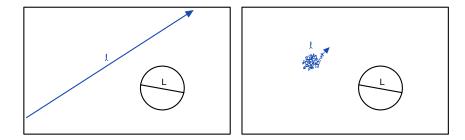


Figure 1.1: Characteristic length scale of problem, L, compared to mean free path of particles, ℓ , for a flow with large Knudsen number (left) vs. small Knudsen number (right)

This work falls within the small Knudsen regime, so we will be working with the continuum description of fluids. In this section we will discuss the Navier-Stokes Equations that arise from this modeling technique and how we account for the supercritical nature of the flow through our choice of equation of state.

1.1.1 Continuum Description of Fluids

The continuum hypothesis assumes that the fluid has no fine structures and that it is perfectly continuous, i.e. the properties of a small subdivision are the same as other subdivisions. This allows for the approximation of physical quantities at the infinitesimal limit [24].

For example, consider a fluid with arbitrary volume V as depicted in Figure 1.2.

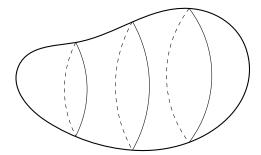


Figure 1.2: A fluid of arbitrary volume V bounded by surface S with velocity $\vec{v}(\vec{x},t)$. A differential volume and surface area is given by dv and ds, respectively. \vec{n} is the outward-pointing unit normal vector to the surface S.

For a fluid with density $\rho(\vec{x},t)$, mass within a small representative volume can be described with

$$\rho dv$$

Total mass in the arbitrary volume is then given by

$$\iiint_V \rho \, dv$$

The rate of change of mass through the volume is now

$$\frac{d}{dt} \iiint_{V} \rho \, dv$$

$$= \iiint_{V} \frac{\partial \rho}{\partial t} \, dv \tag{1.2}$$

Simultaneously, overall change in mass throughout the volume can be described by the net mass flux through the surface S. Volumetric flow through a small portion of the bounding surface is given by

$$\vec{v} \cdot \vec{n} \, ds$$

Total mass flux through the entire surface is then

$$\iint_{S} \rho \, \vec{v} \cdot \vec{n} \, ds \tag{1.3}$$

Applying the divergence theorem to Eq. 1.3 yields the following volume integral

$$\iiint_{V} \nabla \cdot (\rho \, \vec{v}) \, dv \tag{1.4}$$

Assuming there is no additional source generating or leaking mass within the control volume, we can relate Eqs. 1.2 to 1.4:

$$\iiint_{V} \frac{\partial \rho}{\partial t} dv = -\iiint_{V} \nabla \cdot (\rho \, \vec{v}) \, dv$$

$$\iiint_{V} \frac{\partial \rho}{\partial t} dv + \iiint_{V} \nabla \cdot (\rho \, \vec{v}) \, dv = 0$$

$$\iiint_{V} \left(\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \, \vec{v}) \right) dv = 0$$
(1.5)

Note the inclusion of the negative sign for the right side of the initial equality; in the surface integral formulation, the outward facing normal describes flux out of the volume, thus yielding a decrease in mass within the volume. Since Eq. 1.5 holds for any arbitrary volume V, the integrand must be identically equal to zero:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \, \vec{v}) = 0 \tag{1.6}$$

Through the continuum hypothesis and conservation of mass, we have now arrived at the continuity equation in Eq. 1.6. This specific process demonstrates an even more fundamental relationship known as a conservation law. More generally, for some integrated property ϕ , the rate of change of ϕ within a control volume must be equal to the amount of ϕ lost or gained through the boundaries of the control volume plus what is created or consumed by any sinks or sources, s, within the volume (sinks having positive orientation to match the positive orientation of the outward-facing normal \vec{n}) \parallel .

$$\frac{\partial \phi}{\partial t} + \nabla \cdot (\phi \, \vec{v}) + s = 0 \tag{1.7}$$

In addition to this concept applying to conservation of mass, as was seen in this section, the idea outlined by Eq. 1.7 applies to conservation of momentum and energy within the fluid. Together, these expressions combine to form the basis of the Navier-Stokes Equations, as will be seen in more detail in chapter 2. The important takeaway from this section is that with the continuum hypothesis and fundamental laws of physics, one can adequately capture macroscopic flow behavior for the types of flows we are interested in within this work.

1.1.2 Equation of State

Conservation of mass, momentum, and energy gives us five equations to describe our fluid system. For compressible flows, this is not enough information to solve for all the unknowns within the system of coupled partial differential equations. A sixth equation, known as the Equation of State (EoS), must be chosen in order to close the system. The EoS relates three of the six unknowns: pressure, temperature, and density. Here we will briefly discuss some EoS options and their distinguishing characteristics in order to motivate the choice made for this work.

The simplest option available is the ideal gas EoS, which comes from the ideal gas law. This EoS relates density, pressure, and temperature in the following manner:

$$p = \frac{RT}{V_m} \tag{1.8}$$

where p is pressure, R is the universal gas constant, T is temperature, and $V_m = \frac{V}{n}$ is the molar volume of the fluid (it is common to express density in terms of molar volume for sake of simplicity in writing the EoS with V being volume and n being the number of moles). The ideal gas EoS is fairly accurate for liquids and gases at moderate temperatures and low pressures. It fails at low temperatures and high pressures, especially near the transition region from gas to liquid. The inaccuracy noted in this region means this EoS would not be suitable for the area of interest within this study.

Cubic EoS generally provide more accuracy than the ideal gas EoS. The first cubic EoS was developed by van der Waal in 1873, modifying the ideal gas EoS to take into consideration the finite size of molecules and interactions between molecules (the ideal gas EoS only accounts for interactions with the container and treats molecules as point particles). Other cubic EoS can be thought of as modifications from this base form:

$$p = \frac{RT}{V_m - b} - \frac{a}{V_m^2} \tag{1.9}$$

where a and b are constants related to the pressure and temperature at the critical point, p_c and T_c respectively:

$$a = \frac{27(RT_c)^2}{64p_c}, \quad b = \frac{RT_c}{8p_c}$$

One of the main benefits of using a cubic EoS is that they can have comparable and sometimes even better accuracy compared to their higher order counterparts, thus reducing computational costs. However, it is important to take into consideration the regime of interest in addition to the fluid of interest when choosing an EoS, as each one has its own pros and cons. For example, molecule polarity and density are two factors that can have a high impact in selection between the Soave-Redlich-Kwong Equation of State (SRK EoS) and Peng-Robinson Equation of State (PR EoS) alone [20].

This work uses the SRK EoS as will be more thoroughly introduced in chapter 2. It has been shown that this equation of state is fairly accurate for the parameter regime under careful consideration in this work []. This accuracy is detailed further in chapter 3 through comparisons with data from National Institute of Standards and Technology (NIST). Overall, when adequately considered, the EoS is the key avenue to incorporating specific fluid properties into the mathematical model.

1.2 Turbulence

In addition to the categorizing of fluid type, fluid flow can be distinguished into different types based on certain defining flow characteristics. The main two classifications of note are laminar flow and turbulent flow.

Laminar flow is denoted by fluid particles having well-defined parallel trajectories of motion, or streamlines. Streamlines do not cross, meaning adjacent layers within the fluid flow by one another with little to no mixing. From a more generalized perspective, the flow appears to be smooth. In contrast to this, turbulent flow is characterized by its unpredictable and chaotic trajectories. Streamlines do cross resulting in swirls and eddies of varying length scales which induce mixing. Turbulent flow can be qualitatively described as being rough due to this high degree of fluctuation within the velocity and pressure fields present. This generalized description is depicted in Figure 1.3.

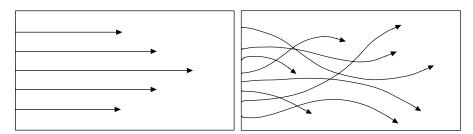


Figure 1.3: Example of streamlines in laminar (left) vs. turbulent (right) flow.

The Reynolds number is a dimensionless value that can be used to distinguish laminar flow from turbulent flow. It is defined as follows:

$$Re = \frac{\rho u L}{\mu} \tag{1.10}$$

where ρ and μ are the density and dynamic viscosity of the fluid, respectively, u is the flow velocity, and L is a characteristic length scale associated with the given flow scenario (e.g. pipe diameter). As is demonstrated by the ratio in Equation 1.10, the Reynolds number measures the relative effects of inertial forces compared to viscous forces within a given flow scenario. A small Reynolds number signifies the dominance of viscous forces; fluid parcels moving in tandem want to "stick together," resulting in the sheared flow and parallel trajectories seen in laminar flow. Turbulence is then characterized by a large Reynolds number, where inertial forces take precedence. Here, deviations within the laminar flow field result in lateral mixing between shear layers. This creates eddies and random trajectories that result in the chaotic motion of turbulent flow.

This work focuses on the turbulent round jet and its associated dynamics in the context of supercritical fluids. The remainder of this section details a brief historical overview of turbulence modeling and numerical methods developed for studying turbulence in order to motivate the modeling and numerical choices made within this work.

1.2.1 Historical Perspective

This is a brief history of turbulence study from a mathematics perspective.

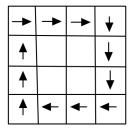
1.2.2 Round Jet Theory

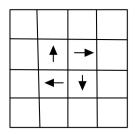
1.2.3 Numerical Approaches

These are some of the numerical approaches in use, including what we use and why we use it.

1.3 Supercritical Carbon Dioxide

As mentioned earlier, supercritical fluids have many qualities that make them desirable as working fluids in a variety of systems. We now shift our focus to one particular fluid of interest: Carbon Dioxide (CO2). As seen in the phase diagram of Figure 1.5, the critical temperature, T_c , and critical pressure, p_c , of CO2 are 304.128 K and 73.773 bar. The critical temperature and pressure of CO2 is fairly easy to attain, making it a strong candidate for systems with hight thermal outputs. Additionally, sCO2 has a relatively low toxicity and environmental impact [], and





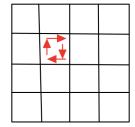


Figure 1.4: LES resolves large scale eddies (black) and models fine scale eddies (red) that are unresolved due to mesh size.

is chemically stable, non-flammable, and readily available []. For these reasons, sCO2 is a highly coveted alternative working fluid in many different applications, and is one of the most widely used supercritical fluids along with water [17].

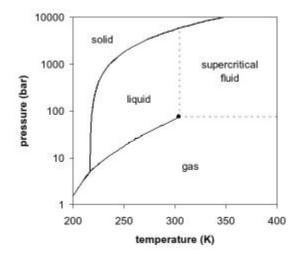


Figure 1.5: Phase diagram for Carbon Dioxide (CO2). Critical pressure, p_c , and temperature, T_c , are 73.773 bar and 304.128 K, respectively.

In the next part of this section, we will explore some applications of sCO2 in which the turbulent round jet configuration is used. Then we will go through a brief review of recent studies involving sCO2, and more generally supercritical turbulent jets, in order to demonstrate where this work fits in among current research. Finally, we outline the structure of the remainder of the dissertation.

1.3.1 Applications of Interest

One of the key applications of interest that motivates this work is the use of sCO2 as the working fluid in advanced cycles for power generation. sCO2 has shown promise as a working fluid for both indirect cycle and direct-firing cycles [60, 61]. One example of indirect cycle improvement uses sCO2 in place of water for the conventional steam-Rankine cycle. An example of where these types of configurations may prove useful is in managing thermal runoff from existing coal and natural gas combustion processes [60]. Compared to steam, sCO2 is less corrosive, more thermally stable, and has increased power density. The critical point of CO2 is easily accessible, and once achieved, allows for the use of a single phase fluid design, leading to a simplified and more compact turbine (see Figure 1.6). Ultimately, this also allows for lower operation and maintenance costs [13]. The benefits of using sCO2 turbines over the traditional steam design has been highly researched and has only seen an increase in momentum for implementation [12, 15, 13, 41].

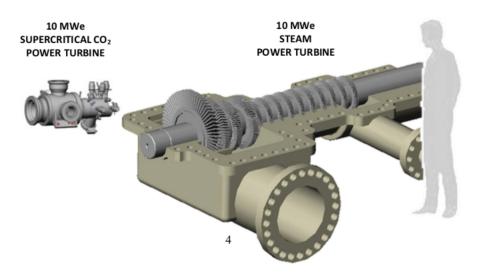


Figure 1.6: Size comparison for steam vs. sCO2 turbine via Echogen Power Systems LLC [41].

An example of direct-firing cycles that use sCO2 include the Allam cycle [4]. When compared to the conventional Brayton cycle, studies show that the Allam cycle has much higher efficiency [14, 5]. Additionally, the carbon footprint for the Allam cycle is virtually zero, allowing for CO2 produced from the system to be stored underground or used elsewhere, aiding in carbon sequestration efforts [18]. This two-for-one benefit of using sCO2-based cycles such as the Allam cycle has spurned much research [58, 8] and development [47] into related technologies.

Of particular importance to these applications is the round turbulent jet, as this is a major component of many injection technologies. The high densities associated with the liquid-like aspect of supercritical fluids coupled with the relatively low gas-like viscosity associated with them typically results in a high Reynolds flow, often resulting in a turbulent system. The turbulence physics of these jets is crucial in developing machinery for these systems. Current experimental research is mainly application oriented. Research into the sCO2 jet's rock breaking ability has been of primary importance to Enhanced Geothermal Systems (EGS) applications [43, 44, 31, 52, 29], with additional focus being given to pipeline leakage and flow dynamics upon wall impact [57, 56], which unfortunately does not explore the underlying turbulence statistics of the flow. Enhanced recovery of unconventional reservoirs for oil and gas development is an additional area where rock breaking research is often applied [23, 22]. Chemical engineering design aspects of sCO2 injection are more focused on solubility dynamics as opposed to turbulence [25, 27]. Other experiments focus on similar application specific quantities of interest, such as heat transfer and mixing, which is related in part to the turbulence dynamics [63, 32], but they also note the difficulty in experimental design for investigating these aspects of the flow under the conditions needed to replicate those in real applications [25]. Thus, numerical simulations are necessary to further explore the turbulence statistics of these flows.

1.3.2 Overview of Current Numerical Landscape

Numerical simulations are a necessary tool for investigating many aspects of supercritical flow fields due to the often challenging nature of experiment design for the extreme conditions inherent to these systems. Studies using direct numerical simulation (DNS) have been implemented to help establish benchmark test cases for other types of numerical schemes [39, 51]. Ruiz et al. use 2D DNS to simulate a mixing layer created by two streams of supercritical Oxygen and gaseous Nitrogen, using two different computational fluid dynamics (CFD) solvers to add confidence to their results [48]. A 3D DNS is used by Ries at al. to simulate a round Nitrogen jet for comparison with experimental data produced by Mayer et al. [46]. However, this study requires a reduction in Reynolds number from 1.62×10^5 , based on the injection diameter, to 5300 in order to feasibly execute the computations. Li also utilizes a low Reynolds number of 1750 to study a round turbulent sCO2 jet with a preconditioning scheme [28]. The Reynolds-averaged Navier-Stokes (RANS) approach has also been implemented utilizing theory from the ideal gas case [34], but with the goal

of ascertaining a more general understanding of why specifically sCO2's rock-breaking ability is better than that of water.

Much research has gone into the development of appropriate numerical methods for investigations regarding turbulence in supercritical fluids. In order to maintain a high Reynolds flow and better capture the effects of the supercritical nature of the fluid on the turbulence dynamics, the use of large eddy simulation (LES) has been explored. The impact of subgrid scale (SGS) models in capturing transcritical and supercritical dynamics of cryogenic Nitrogen have been analyzed through comparison with the Mayer et al. experiment and highly accurate NIST data [42, 66, 67, 38, 59]. Schmitt et al. does a similar investigation using LES, then extending their investigation to include sCO2 after validation with the Mayer et al. data [50]. However, this investigation uses low-pressure jets and does note the SGS models might need additional contributions to handle non-linearities and the pressure regime. While many of these investigations note that SGS models may need modification to deal with supercritical flows [50, 42, 38, 66], it is noted by Muller et al. that given a sufficiently fine grid, the influence of SGS modeling and numerical flux discretization is essentially limited to second-order moments [38]. Thus, we will be using the compressible version of the dynamic Smagorinksy SGS closures for our investigation, with further consideration of any influence of SGS model on our quantities of interest being noted later on.

Many of the numerical investigations sited thus far consider cryogenic nitrogen in order to compare with the Mayer et al. experiment on supercritical jet turbulence [36]. A wide variety of numerical investigations into jet turbulence using sCO2 exist but typically explore either other parameter regimes of interest or application-specific quantities of interest. Examples of turbulent adjacent quantities of interest include fluctuation characteristics based on inlet conditions [65], effects of nozzle and aperture differences on pressure and velocity decay [7] and wave features [33], mixing between sCO2 and other fluid phases [45], and energy dissipation [30]. These studies all involve high pressure jets and are commonly found in applications involving rock fracturing. Related configurations are also studied, such as the swirling-round sCO2 jet [62], turbulent jet-in-crossflows [64], slot jet impingement [3], and channel flow [2].

While much of the literature thus far has explored the impact of different numerical methods on modeling supercritical fluid flows and has aimed to strengthen the validity of these simulations in spite of the lack of experimental data available in the current landscape, a general consensus has still not been reached on how the supercritical nature of these fluids impacts the turbulence physics of these models. Thus, there remain open questions for understanding the fundamental flow

behavior of turbulent jets in a supercritical environment, especially near the supercritical point, where both experimental and numerical investigations are still a challenge.

Our objective is to use LES to investigate the turbulence physics of sCO2 near the critical point in order to capture the effects of widely varying thermal properties of supercritical fluids. Using the compressible Navier-Stokes equation solver, PeleC [40], closed with the SRK EoS, we consider three cases in order to examine various quantities of interest associated with classical turbulence mechanics. These three cases are chosen to capture different areas around a peak in specific heat that is associated with the pseudo-critical region. The rest of this dissertation is outlined as follows. Chapter 2 details the model used for this study and gives an overview of the numerical methods implemented through PeleC. Chapter 3 outlines the simulation setup with parameter choices and validation. Results for cross-case comparisons and comparisons with external work are then presented in Chapter 4, with a summary and future work detailed in Chapter 5.

CHAPTER 2

MODEL OVERVIEW

2.1 Introduction

Chapter 1 introduced the general mathematical framework needed for modeling fluid flow.

2.2 Governing Equations

We consider the three-dimensional compressible Navier-Stokes equations:

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_j} (\rho u_j) = 0,$$

$$\frac{\partial}{\partial t} (\rho u_i) + \frac{\partial}{\partial x_j} (\rho u_i u_j + p \delta_{ij} - \sigma_{ij}) = 0,$$

$$\frac{\partial}{\partial t} (\rho E) + \frac{\partial}{\partial x_j} ((\rho E + p) u_j + q_j - \sigma_{ij} u_i) = 0$$
(2.1)

where ρ is the density, u_j is the velocity for the x_j direction, p is the pressure, $E = e + \frac{u_i u_i}{2}$ is the total energy, $e = c_v T$ is the internal energy, T is the temperature, and c_v is the heat capacity at constant volume. Additionally, the diffusive fluxes are

$$\sigma_{ij} = 2\mu S_{ij} - \frac{2}{3}\mu \delta_{ij} S_{kk} q_j = -k \frac{\partial T}{\partial x_j}$$
(2.2)

where $S_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$ is the strain-rate tensor, μ is the dynamic viscosity, and k is the thermal conductivity. External forces such as gravity are not included in this study. Chung's high pressure correction for viscosity and thermal conductivity are included for the transport variables μ and k [9]. The system is closed using the SRK EoS [53] to relate pressure, density, and temperature as follows:

$$p = \frac{RT}{V_m - b} - \frac{a\alpha}{V_m(V_m + b)} \tag{2.3}$$

$$a = \frac{0.42747R^2T_c^2}{P_c} \tag{2.4}$$

$$b = \frac{0.08664RT_c}{P_c} \tag{2.5}$$

$$\alpha = \left(1 + \left(0.48508 + 1.55171\omega - 0.15613\omega^2\right) \left(1 - T_r^{0.5}\right)\right)^2 \tag{2.6}$$

$$T_r = \frac{T}{T_c} \tag{2.7}$$

where R is the ideal gas constant, T is the absolute temperature, V_m is the molar volume of the species, T_c and P_c are the critical temperature and pressure of the species, respectively, and ω is the acentric factor of the species. Additionally, a, b, and α are all species-specific parameters calculated via equations 2.4, 2.5, and 2.6. All cases are run with a single species, that being CO2.

2.2.1 High Pressure Corrections for Transport Models

2.3 Numerical Methods

To discretize and evolve the system of partial differential equations given in 2.1, including the LES SGS terms, we use PeleC, a compressible hydrodynamics code for reacting flows that leverages AMReX for AMR []. PeleC is a highly scalable code for heterogeneous architectures that is being developed as part of the Exascale Computing Project (ECP) through the Department of Energy (DOE). It leverages the PelePhysics library for complex physics, including chemical reactions, non-ideal EoS, and high fidelity transport models. For spatial discretization, PeleC contains a few variations of the general piecewise parabolic method (PPM) originally derived by Colella and Woodward [10]. We utilize a variation that allows for extrema preservation in the presence of steep gradients [37, 11]. For time discretization, a second order Runge-Kutta scheme is used, and the time step is dynamically limited using a Courant number of 0.9.

2.3.1 Subgrid-Scale Modeling for Large Eddy Simulation

We use the dynamic Smagorinsky (SMD) LES model for compressible flow as described by Martín, Piomelli, and Graham [35]. In this context, the compressible Navier-Stokes equations 2.1 should be interpreted in their Favre-filtered form, where, in this work, the grid provides the implicit filtering of the equations. The SGS stress tensor, τ_{ij} , is included in the diffusive fluxes and is calculated as follows:

$$\tau_{ij} - \frac{\delta_{ij}}{3} \tau_{kk} = -C_s^2 2 \overline{\Delta}^2 \overline{\rho} |\widetilde{S}| \left(\widetilde{S}_{ij} - \frac{\delta_{ij}}{3} \widetilde{S}_{kk} \right) = C_s^2 \alpha_{ij},$$

$$\tau_{kk} = C_I 2 \overline{\rho} \overline{\Delta}^2 |\widetilde{S}|^2 = C_I \alpha$$
(2.8)

where $\bar{\cdot}$ denotes the filtered variables, $\tilde{\cdot} = \overline{\rho \cdot}/\overline{\rho}$ is the Favre-filter operation, with $\overline{\Delta}$ being the filter width associated with the smallest scale retained by the filtering operation ($\overline{\Delta}$ is the grid spacing for our cases). Additionally, $|\tilde{S}| = (2\tilde{S}_{ij}\tilde{S}_{ij})^{1/2}$. The two model coefficients are calculated as follows:

$$C = C_s^2 = \frac{\langle \mathcal{L}_{ij} M_{ij} \rangle}{\langle M_{kl} M_{kl} \rangle}, \qquad C_I = \frac{\langle \mathcal{L}_{kk} \rangle}{\langle \beta - \widehat{\alpha} \rangle}$$
 (2.9)

$$Pr_{\rm T} = \frac{C\langle T_k T_k \rangle}{\langle \mathcal{K}_j T_j \rangle} \tag{2.10}$$

where

$$T_{j} = -\widehat{\Delta}^{2}\widehat{\overline{\rho}}|\widetilde{\widetilde{S}}|\frac{\partial \widecheck{T}}{\partial x_{j}} + \overline{\Delta}^{2}\overline{\rho}|\widehat{\widetilde{S}}|\frac{\widehat{\partial T}}{\partial x_{j}}, \qquad \qquad \mathcal{K}_{j} = \left(\frac{\widehat{\rho u_{j}}\widehat{\rho T}}{\overline{\rho}}\right) - \frac{\widehat{\rho u_{j}}\widehat{\rho T}}{\widehat{\overline{\rho}}}.$$
 (2.11)

For our simulations, we implement the three point box filter as described in [49] with a filter-grid, ratio of 2, i.e. $\hat{\Delta} = 2\overline{\Delta}$.

As noted previously, the choice of SGS modeling is important in accurately capturing the turbulence statistics of the system. Müller et al. found that while the choice in thermodynamic modeling is crucial in capturing first-order moments, the effects SGS modeling is limited to second-order moments [38]. Therefore, our conclusions relating to the turbulence dynamics will be unaffected. That being said, [38] also notes that the choice in SGS model and numerical flux discretization had a larger than expected effect on resolved Reynolds stress profiles. Specifically, the constant Smagorinsky model yielded decaying fluctuation magnitudes during early evolution, resulting in the transition to a fully turbulent mixing zone to start from lower turbulence levels. However, this did agree with the jet break-up location inferred from mean density profiles, which were shifted slightly downstream by comparison to other SGS models. These relationships will be taken into consideration for this study as well and noted in the discussion of Reynolds stress profiles.

- 2.3.2 Piecewise Parabolic Method Overview
- 2.3.3 Approximate Riemann Solver Details
- 2.3.4 Time Stepping with RK2

CHAPTER 3

SIMULATIONS

3.1 Computational Domain

3.1.1 AMReX and Discretization

Our target simulation is a 3D LES with a grid size that is 100 times the smallest scale of the turbulent flow. In our setup, the domain length in each direction is: x = 25d, y = 62.5d, and z = 25d, where the jet diameter d = 0.01 cm and the y-axis is the axial direction of the jet. This smallest scale of these turbulent flows, known as the Kolmogorov scale [26], can be approximated:

$$\eta = \left(\frac{\nu^3}{\varepsilon}\right) \tag{3.1}$$

where $\nu = \mu/\rho$ is the kinematic viscosity and $\varepsilon = v_J^3/d$ is used to approximate the average rate of dissipation of turbulence kinetic energy per unit mass. For these turbulent jets, $\eta = 5.37 \times 10^{-6}$ cm. Therefore, to keep the calculation tractable and achieve an adequate LES grid size, we implement four levels of refinement, with a refinement ratio of 2, leading to 80, 200, and 80 cells on the coarsest level in the x, y, and z directions, respectively. This results in an initial mesh size of $\Delta x_0 = \Delta y_0 = \Delta z_0 = 0.3125$, leading to $\Delta x_3 = \Delta y_3 = \Delta z_3 = 3.9062 \times 10^{-4}$, where the subscript denotes the AMR level. These four levels of refinement occur in the region outward from the jet inlet up to a distance of 20d in the x and z direction and 60d in the y direction, as can be seen in Figure 3.1. The refinement criterion is given by the vorticity, specifically with $\omega \geq 5000^{2l}$, where ω is the magnitude of the vorticity and l is the AMR level. For the first ten flow throughs of the simulation, mesh refinement only occurs up to one level within the refinement region to establish the flow pattern. Thereafter, the simulation proceeds with the four levels of mesh refinement until reaching steady state, whereupon statistics are collected for analysis.

3.1.2 Initial and Boundary Conditions

Our inlet consists of an opening centered in the xz-plane with diameter $d=0.01\,\mathrm{cm}$ through which the sCO2 jet is initialized. The pressure in the jet at the inlet is the same as that of the quiescent background fluid and it is given by $p_j=p_0=10.1325\,\mathrm{MPa}$. The ambient fluid remains at rest while the jet is initialized with an inflow velocity of $v_j=1800\,\mathrm{cm\,s^{-1}}$, leading to a Reynolds

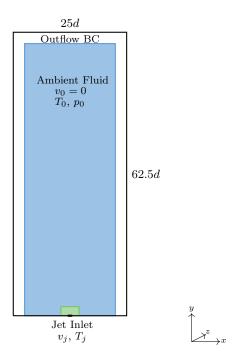


Figure 3.1: Two dimensional slice schematic of jet setup. Four levels of refinement are enforced within the green box based on proximity to jet inlet. Refinement based on vorticity criterion then occurs within the blue region. Outside the blue region, AMR is explicitly turned off to allow flow structures to be dissipated numerically and allowed to leave the domain without incurring spurious reflections.

number of the initialized jet of $Re_j = 22910$, with v_j and d being the reference velocity and length scale respectively. For the jet temperature and pressure conditions given, the reference density is $\rho_j = 3.019 \times 10^{-1} \,\mathrm{g\,cm^{-3}}$, as calculated via the SRK EoS in PeleC. To implement a turbulent inflow, we add noise to this input velocity using the mean velocity and root mean square (rms) values from a predetermined DNS velocity profile [16]. We begin by scaling the DNS values with our given jet velocity and radius. After determining which scaled DNS values we are near for the radius determined by our mesh, a linear interpolant is created to compute the mean velocity at our given radius. Noise is then added to each cylindrical component of the velocity as follows:

$$v = \langle v_{\text{DNS}} \rangle + \left(v'_{\text{DNS}} + \beta v'_{\text{DNS}} r_1 \sin \theta_1 \right) \cdot r_2 \sin \theta_2$$
 (3.2a)

$$u = u'_{\text{DNS}} + \beta u'_{\text{DNS}} r_3 \sin \theta_3 \tag{3.2b}$$

$$w = w'_{\text{DNS}} + \beta w'_{\text{DNS}} r_4 \sin \theta_4 \tag{3.2c}$$

where $\langle u_y \rangle$ is the mean velocity in the axial direction, $u' = \langle u^2 \rangle^{\frac{1}{2}}$ is the rms for each velocity component, and $\beta = 0.1$. Each r_i and θ_k value is randomly generated as follows:

$$r_i = \sqrt{-2.0\log\left(X_i\right)} \tag{3.3a}$$

$$\theta_k = 2\pi X_k \tag{3.3b}$$

where X_n are random numbers between 0 and 1. The inflow parameters are finalized after being converted into Cartesian coordinates.

We implement zero gradient boundary conditions for all boundaries not involving the jet inflow. Additionally, AMR is halted at a distance of 2.5d from the boundary in the x and z directions, and that of 5d in the axial direction in order to ensure that all waves are dissipated, thus avoiding spurious reflections from the boundaries.

3.2 Case Descriptions

3.2.1 Parameter Choices

3.3 Compute Time and Hardware Specifications

3.4 Post-Processing Procedures

CHAPTER 4

RESULTS

- 4.1 Ideal Gas Comparison
- 4.1.1 Mean Turbulence Statistics
 - 4.2 Cross-Case Comparisons
- 4.2.1 Axial Visuals

CHAPTER 5

CONCLUSION

- 5.1 Summary
- 5.2 Future Work

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BIOGRAPHICAL SKETCH

This is my biography.