



AI



Quantum circuit simulation



Combinatorial optimization

# Einsum is all you need

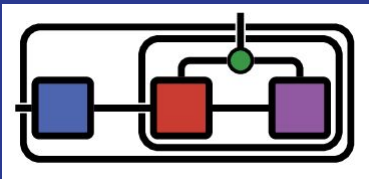
Jinguo Liu (  GiggleLiu)



OMEinsum.jl

Andreas Peter & GiggleLiu

Google summer of code (2019)



# You will know

- What is Einsum, by examples.
- Features in OMEinsum and OMEinsumContractionOrders.
- What is Einsum contraction order, and why it matters.

Required background knowledge: basic linear algebra



# Get your hands dirty!

## Quick Start (requires Julia REPL)

```
# press `]` to enter Pkg mode
```

```
pkg> add OMEinsum, OMEinsumContractionOrders
```

```
julia> using OMEinsum, OMEinsumContractionOrders
```



# Julia's tensor ecosystems

Note 1: TensorKit does not support CUDA yet, although TensorOperations supports it.

Note 2: ITensorsGPU is not registered yet.

Note 3: The contraction order optimizer in TensorOperations is similar to NCon, this is slow for large scale tensor networks.

Note 4: ITensors only supports Abelian quantum numbers.

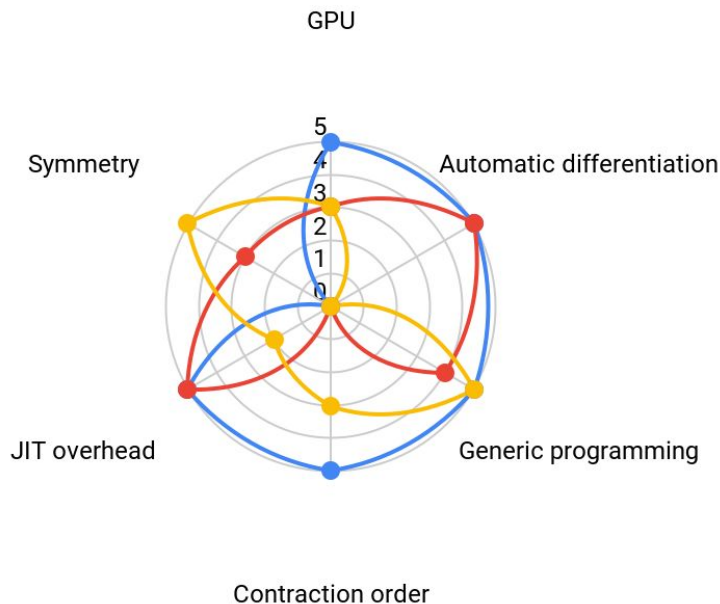
Note 5: The reason why ITensors has score 4 in generic programming is because some of its design pattern does not take different number types into consideration.

● OMEinsum +  
OMEinsumContractionOrders

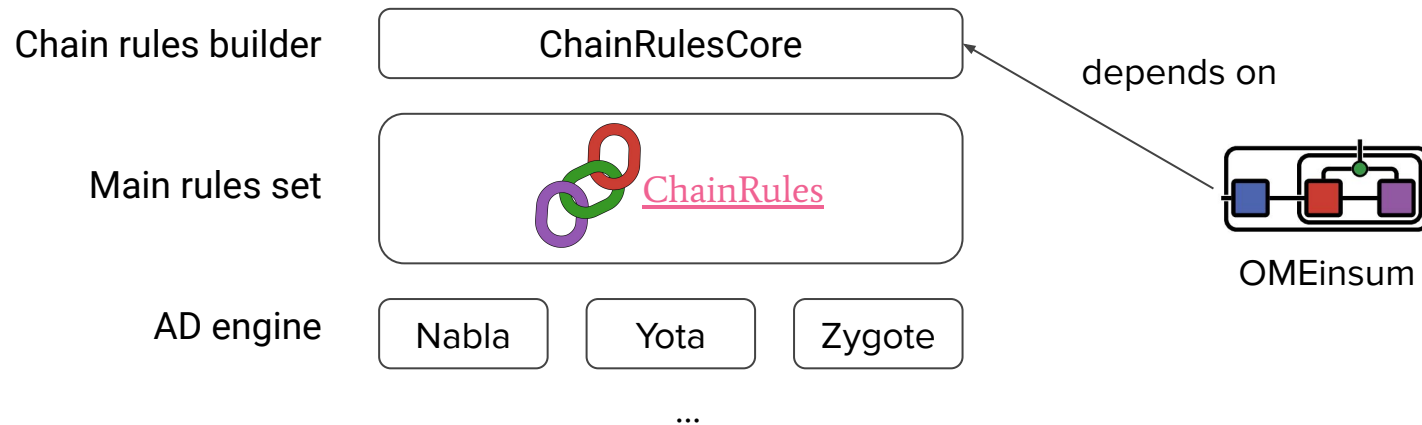
● ITensors + ITensorsGPU

● TensorOperations + TensorKit

Only tensor networks  
are supported.

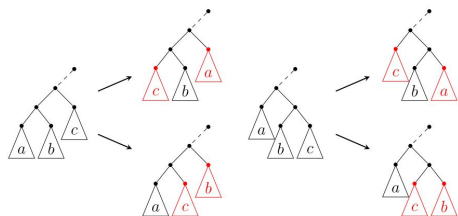


# Automatic differentiation



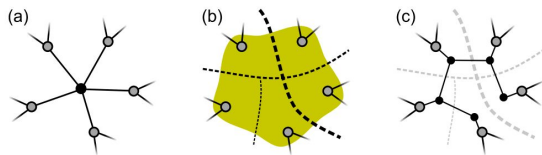
# Finding optimal einsum contraction orders

## TreeSA



Kalachev, G., Panteleev, P., & Yung, M.-H.  
*Recursive Multi-Tensor Contraction for XEB  
Verification of Quantum Circuits.* arXiv:  
2108.05665

## KaHyParBipartite



Gray, Johnnie, and Stefanos Kourtis.  
*Hyper-optimized tensor network contraction.*  
Quantum 5 (2021): 410.

GreedyMethod, fast but not optimal

SABipartite, a replacement of KaHyParBipartite when KaHyPar can not be installed

# Einsum is useful

All use GPU

Papers motivating  
OMEinsum

- Liao, Hai-Jun, et al. "Differentiable programming tensor networks." *Physical Review X* 9.3 (2019): 031041.
- Feng Pan, Pan Zhang. *Simulating the Sycamore quantum supremacy circuits*. arXiv: 2103.03074
- Feng Pan, Keyang Chen, Pan Zhan. *Solving the sampling problem of the Sycamore quantum supremacy circuits*. arXiv:2111.03011

Autodiff

Papers using  
OMEinsum

- Xun Gao, Marcin Kalinowski, Chi-Ning Chou, Mikhail D. Lukin, Boaz Barak, Soonwon Choi. *Limitations of Linear Cross-Entropy as a Measure for Quantum Advantage*. arXiv:2112.01657.
- Jin-Guo Liu, Lei Wang, Pan Zhang. *Tropical Tensor Network for Ground States of Spin Glasses*. arXiv:2008.06888
- Jinguo Liu, Shengtao Wang, et al and Xun Gao. *Computing Properties of Independent Sets by Generic Programming Tensor Networks*. not published yet

Contraction  
order

Generic  
programming

# Summary - We talked about OMEinsum.jl

- Einsum notation
  - Its representation power
  - Estimate time complexity
  - Contraction order matters
- Features
  - GPU
  - Automatic differentiation
  - **Contraction order optimization**
  - Generic programming

## Open source events



国内: 开源软件供应链点亮计划



Abroad: Google Summer of Code

## Discussion



Github issue



Julia slack (@GiggleLiu)

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