

$$\int \frac{2x+3}{(x-2)(x+5)} = \int \left(\frac{A}{x-2} + \frac{B}{x+5} \right) = \int \frac{Ax+5A+Bx-2B}{(x-2)(x+5)}$$

$$\begin{cases} A+B=2 \\ 5A-2B=3 \end{cases} \quad \begin{matrix} A=1 \\ B=1 \end{matrix}$$

$$\int \left(\frac{1}{x-2} + \frac{1}{x+5} \right) = \ln|x-2| + \ln|x+5|$$

$$\int e^{2x} \cos 3x \, dx$$

$$u = e^{2x} \quad du = 2e^{2x} \, dx$$

$$dv = \cos 3x \, dx \quad v = \frac{1}{3} \sin 3x$$

$$e^{2x} \cdot \frac{1}{3} \sin 3x - \frac{2}{3} \int \sin 3x \cdot e^{2x} \, dx =$$

$$u = e^{2x} \quad du = 2e^{2x} \, dx$$

$$dv = \sin 3x \quad v = -\frac{1}{3} \cos 3x$$

$$= \frac{e^{2x} \sin 3x}{3} - \frac{e^{2x} \cos 3x}{3} + \frac{2}{3} \int \cos 3x e^{2x} \, dx$$

$$\frac{1}{3} \int e^{2x} \cos 3x \, dx = \frac{e^{2x} (\sin 3x - \cos 3x)}{3}$$

$$\ln 2$$

$$\int_0^{\ln 2} x e^{-x} \, dx$$

$$u = x \quad du = dx$$

$$dv = e^{-x} \, dx \quad v = -e^{-x}$$

$$e^{-x} \cdot x - \int -e^{-x} \, dx = -e^{-x} \cdot x - e^{-x} = -e^{-x} (x+1) \Big|_0^{\ln 2}$$

$$-e^{-\ln 2} (\ln 2 + 1) + e^0 \cdot \frac{1}{(0+1)} = -\frac{\ln 2 + 3}{2}$$

$$f(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} x^n$$

$$y = e^x$$

$$\frac{e^0 x^0}{0!} + \frac{e^0 x^1}{1!} + \frac{e^0 x^2}{2!} + \dots = \sum \frac{x^n}{n!}$$