

$$5. A_b = \pi \cdot 2^2 \quad A_B = \pi \cdot 5^2$$

$$A_b = 4\pi \text{ m}^2 \quad A_B = 25\pi \text{ m}^2$$

$$g^2 = 4^2 + 3^2 \quad A_l = \pi (5+2)5 \quad A_t = 4\pi + 25\pi + 33\pi$$

$$g^2 = 16+9 \quad A_l = 35\pi \text{ m}^2 \quad A_t = 64\pi \text{ m}^2$$

$$g = \sqrt{25}$$

$$g = 5 \text{ m} \quad V = \frac{\pi \cdot 4 (5^2 + 2^2 + 5 \cdot 2)}{3}$$

$$V = \frac{\pi \cdot 4 \cdot 39}{3}$$

$$V = 52\pi \text{ m}^3$$

$$6. 5^2 = h^2 + 4^2 \quad V = \frac{\pi \cdot 3 (7^2 + 3^2 + 7 \cdot 3)}{3}$$

$$h^2 = 25 - 16$$

$$h = \sqrt{9}$$

$$h = 3 \text{ cm}$$

$$V = \pi (49 + 9 + 21)$$

$$V = 79\pi \text{ cm}^3$$

alternativa D

$$7. \frac{R}{H} = \frac{x}{h} \rightarrow x = \frac{Rh}{H} \quad V_C = \frac{\pi \cdot R^2 \cdot H}{3}$$

$$V_P = \frac{\pi \cdot x^2 \cdot h}{3}$$

$$V_P = \frac{\pi \cdot \left(\frac{Rh}{H}\right)^2 \cdot h}{3}$$

$$V_P = \frac{\pi \cdot R^2 \cdot h^3}{3H^2}$$

$$h = H \cdot \frac{\sqrt[3]{2^2}}{\sqrt[3]{2}}$$

$$h = H \sqrt[3]{4}$$

alternativa A

$$V_C = \frac{\pi \cdot R^2 \cdot H}{3} - \frac{\pi \cdot R^2 \cdot h^3}{3H^2}$$

$$V_C = \frac{\pi \cdot R^2 \cdot H^3 - \pi \cdot R^2 \cdot h^3}{3H^2}$$

$$V_C = \frac{\pi \cdot R^2 (H^3 - h^3)}{3H^2}$$

$$\frac{\pi \cdot R^2 \cdot h^3}{3H^2}$$

$$\pi \cdot R^2 (H^3 - h^3)$$

$$h^3 = H^3 - h^3$$

$$2h^3 = H^3$$

$$h^3 = H^3/2 \rightarrow h = \sqrt[3]{H^3/2}$$



$$3. \frac{R}{h} = \frac{r}{x} \rightarrow r = \frac{R \cdot x}{h} \quad V_{CG} = \frac{\pi \cdot R^2 \cdot h}{3}$$

$$V_{CP} = \frac{\pi \cdot r^2 \cdot x}{3} = \frac{\pi \cdot \left(\frac{R \cdot x}{h}\right)^2 \cdot x}{3} = \frac{\pi \cdot R^2 \cdot x^3}{3h^2}$$

$$V_{TC} = \frac{\pi \cdot R^2 \cdot h}{3} - \frac{\pi \cdot R^2 \cdot x^3}{3h^2}$$

$$V_{TC} = \frac{\pi \cdot R^2 \cdot h^3 - \pi \cdot R^2 \cdot x^3}{3h^2}$$

$$V_{TC} = \frac{\pi \cdot R^2 (h^3 - x^3)}{3h^2}$$

$$\frac{\pi \cdot R^2 \cdot x^3}{3h^2}$$

$$\frac{\pi \cdot R^2 (h^3 - x^3)}{3h^2}$$

$$\pi \cdot R^2 \cdot x^3 = \pi \cdot R^2 (h^3 - x^3)$$

$$x^3 = h^3 - x^3$$

$$2x^3 = h^3$$

$$x = \frac{\sqrt[3]{h^3}}{\sqrt[3]{2}}$$

$$x = \frac{h}{\sqrt[3]{2}} \cdot \frac{\sqrt[3]{-2^2}}{\sqrt[3]{2^2}} \quad \left| x = \frac{h \sqrt[3]{4}}{2} \right|$$

$$4. \quad b^2 = h^2 + 3^2$$

$$h^2 = 25 - 9$$

$$h = \sqrt{16}$$

$$\underline{h = 4 \text{ cm}}$$

torque básica - troncos

$$1. \quad V_{tc} = \frac{\pi \cdot 3^2 \cdot 8}{3} \quad V_{cp} = \frac{24\pi}{2} = 12\pi \text{ cm}^3$$

$$V_{tc} = 24\pi \text{ cm}^3$$

$$\frac{12\pi}{24\pi} = \frac{h^3}{8^3}$$

$$24\pi \cdot h^3 = 512 \cdot 12\pi$$

$$h^3 = 6144\pi$$

$$h^3 = \frac{6144\pi}{24\pi}$$

$$h = \sqrt[3]{256}$$

$$h = 4\sqrt[3]{4} \text{ cm}$$

alternativa E

$$2. \quad \frac{V_{cp}}{V_{cg}} = \frac{16^3}{20^3} \rightarrow \frac{V_{cp}}{5^3} = \frac{4^3}{5^3} \cdot V \rightarrow V_{cp} = \frac{64V}{125}$$

$$V_{tc} = V - \frac{64V}{125}$$

$$V = 100\%$$

$$x = \frac{6100}{125}$$

$$\frac{61V}{125} = x$$

$$125$$

$$V_{tc} = \frac{125V - 64V}{125}$$

$$125$$

$$x = 48,8\%$$

alternativa C

$$V_{tc} = \frac{61V}{125} \text{ cm}^3$$

$$125$$

$$5. \frac{V}{A} = \pi \cdot 3^2 \cdot 5 = 45\pi$$

$$\frac{V}{A} = \frac{1}{3} \cdot \pi \cdot 1^2 \cdot 3 = \pi$$

$$V_{\text{big}} = 45\pi = 15\pi$$

$$V_{\text{big}} = 49\pi \quad \text{alternativa E}$$

$$6. \frac{V_{\text{cone}}}{3} = \frac{A_b \cdot h}{3}$$

$$\frac{V_{\text{prisma}}}{3} = \frac{A_b \cdot 2h}{3}$$

$$h = \frac{V_{\text{cone}} \cdot 3}{A_b}$$

$$\frac{V_{\text{prisma}}}{3} = \frac{A_b \cdot 2 \cdot \frac{V_{\text{cone}} \cdot 3}{A_b}}{3}$$

$$\frac{V_{\text{prisma}}}{3} = \frac{A_b \cdot 2 \cdot V_{\text{cone}} \cdot 3}{A_b \cdot 3}$$

$$V_{\text{prisma}} = 2 \cdot V_{\text{cone}} \quad \text{alternativa A}$$

$$7. \frac{V_{\text{abc}}}{3} = \frac{1}{3} \cdot \pi \cdot x^2 \cdot y \quad \frac{V_{\text{bcd}}}{3} = \frac{1}{3} \cdot \pi \cdot x^2 \cdot y$$

$$V_{\text{adc}} = \pi \cdot x^2 \cdot y - \frac{\pi \cdot x^2 \cdot y}{3}$$

$$V_{\text{adc}} = \pi \cdot x^2 \cdot y - \frac{\pi \cdot x^2 \cdot y}{3}$$

$$V_{\text{adc}} = \frac{3\pi \cdot x^2 \cdot y - \pi \cdot x^2 \cdot y}{3}$$

$$V_{\text{adc}} = \frac{2\pi \cdot x^2 \cdot y}{3}$$

$$R = \frac{\pi \cdot x^2 \cdot y}{3}$$

$$R = \frac{\pi \cdot x^2 \cdot y}{3} \cdot 3$$

$$R = \frac{\pi \cdot x^2 \cdot y}{2}$$

$$\frac{2\pi \cdot x^2 \cdot y}{3}$$

$$\text{alternativa E}$$

Torneo de matemáticas

$$1. A_1 = \frac{\pi (20)^2}{2}$$

$$A_1 = \pi \cdot r \cdot 20$$

$$\frac{\pi (20)^2}{2} = \pi \cdot r \cdot 20 \rightarrow V = 10 \text{ cm}$$

$$20^2 = 10^2 + h^2$$

$$h^2 = 400 - 100$$

$$h = \sqrt{300}$$

$$h = 10\sqrt{3} \text{ cm} \quad \text{alternativa A}$$

$$2. 64\pi = \frac{1}{3} \cdot \pi \cdot r^2 \cdot 12$$

$$r^2 = \frac{64}{4}$$

$$r = \sqrt{16}$$

$$r = 4 \text{ cm}$$

$$g^2 = 12^2 + 4^2$$

$$g^2 = 144 + 16$$

$$g = \sqrt{160}$$

$$g = 4\sqrt{10} \text{ cm}$$

alternativa B

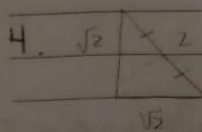
$$3. 36\pi = \pi \cdot r^2 \cdot 6$$

$$r = 6 \text{ cm}$$

$$V = \frac{1}{3} \cdot \pi \cdot 6^2 \cdot 6$$

$$V = 72\pi \text{ cm}^3$$

alternativa A



$$2^2 = l^2 + l^2$$

$$2l^2 = 4$$

$$l = \sqrt{2} \text{ cm}$$

$$(\sqrt{2})^2 = 1^2 + x^2$$

$$x^2 = 2 - 1$$

$$x = 1 \text{ cm}$$

$$V = \frac{2}{3} \cdot \pi \cdot 1^2 \cdot 1$$

$$V = \frac{2\pi}{3} \text{ cm}^3$$

alternativa E