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F8

$$\begin{array}{c|ccc|c|c} \hline 5. & 0 & 3 & 4 & & x \\ \hline A & 1 & 0 & 5 & x= & y \\ & 2 & 1 & 0 & & z \\ \hline \end{array} \quad A_4 = \begin{array}{c|c} 134 \\ 115 \\ 48 \\ \hline \end{array}$$

$$\begin{cases} 3x + 4z = 134 \\ x + 5z = 115 \\ 2x + y = 48 \end{cases}$$

$$\left(\begin{array}{ccc|c} 0 & 3 & 4 & 134 \\ 1 & 0 & 5 & 115 \\ 2 & 1 & 0 & 48 \end{array} \right) \xrightarrow{R_1 \leftrightarrow R_2} \sim \left(\begin{array}{ccc|c} 1 & 0 & 5 & 115 \\ 0 & 3 & 4 & 134 \\ 0 & 1 & -10 & -182 \end{array} \right) \xrightarrow{R_2 \leftrightarrow R_3} \sim \left(\begin{array}{ccc|c} 1 & 0 & 5 & 115 \\ 0 & 1 & -10 & -182 \\ 0 & 3 & 4 & 134 \end{array} \right)$$

$$\left(\begin{array}{ccc|c} 1 & 0 & 5 & 115 \\ 0 & 1 & -10 & -182 \\ 0 & 3 & 4 & 134 \end{array} \right) \xrightarrow{R_3 - 3R_2} \left(\begin{array}{ccc|c} 1 & 0 & 5 & 115 \\ 0 & 1 & -10 & -182 \\ 0 & 0 & 34 & 680 \end{array} \right) \xrightarrow{R_3 \cdot \frac{1}{34}} \left(\begin{array}{ccc|c} 1 & 0 & 5 & 115 \\ 0 & 1 & -10 & -182 \\ 0 & 0 & 1 & 20 \end{array} \right)$$

$$z = 20$$

$$y = 10 \cdot 20 = 200$$

$$x = (-182) + 200$$

$$x = 18$$

$$x + 5 \cdot 20 = 115 \quad 20 + 18 + 5 = 58 \quad \text{Resposta: A}$$

$$x = 115 - 100$$

$$x = 15$$

Exercício II

$$1. \begin{cases} 2x - y - 3z = -5 \\ x + 3y - z = 11 \\ x - z = 3 \end{cases} \quad S = \begin{cases} x - z = 3 \\ x + 3y - z = 11 \\ 2x - y - 3z = -5 \end{cases}$$

$$\left[\begin{array}{ccc|ccc} 2 & -1 & 0 & -5 & 3 & 0 \\ 1 & 3 & -1 & 11 & 0 & 0 \\ 1 & 0 & -1 & 3 & 0 & 0 \end{array} \right] \sim \left[\begin{array}{ccc|ccc} 0 & 3 & 4 & 8 & 0 & 0 \\ 0 & -1 & 0 & -8 & 0 & 0 \\ 0 & 0 & 25 & -25 & 0 & 0 \end{array} \right]$$

$$x - z = 3$$

$$x - 5(-1) = 3$$

$$x = 3 - 5$$

$$x = -2$$

$$3y + 4z = 8$$

$$3y + 4(-1) = 8$$

$$3y = 8 + 4$$

$$y = \frac{12}{3}$$

$$y = 4$$

$$25z = -25$$

$$z = \frac{-25}{25}$$

$$z = -1$$

$$z = -1$$

$$V = \{ (-2, 4, -1) \}$$

$$2. \begin{cases} x = 2y \\ 2y = 3z \\ x + y + z = 11 \end{cases} \quad \begin{matrix} x = 2y & y = ? \\ z = 2y & \\ \end{matrix}$$

$$x + y + z = 11$$

$$2y + y + 2y = 11$$

$$6y + 3y + 2y = 35$$

$$11y = 33$$

$$y = \frac{33}{11} = 3$$

$$y = 3$$

$$x = 2y$$

$$y = 3$$

$$z = 2y$$

$$z = 6$$

$$x + 2y + 3z$$

$$x = 2 \cdot 3$$

$$3$$

$$6$$

$$6 + 2 \cdot 3 + 3 \cdot 2$$

$$x = 6$$

$$z = 2 \cdot 3$$

$$3$$

$$z = 2$$

$$6 + 6 + 6 = 18$$

Resposta: D

$$5. \begin{cases} 2x + y = 5 \\ 2y + z = 3 \\ 3x + 2y + z = 7 \end{cases} \quad D = \left[\begin{array}{ccc|c} 2 & 1 & 0 & 5 \\ 0 & 2 & 1 & 3 \\ 3 & 2 & 1 & 7 \end{array} \right] \rightarrow \begin{cases} 2x + y = 5 \\ 2y + z = 3 \\ 3x + 2y + z = 7 \end{cases}$$

$$0 + 4 + 0 = 4 \quad 4 + 5 + 0 = 9$$

$$Dx = \left[\begin{array}{cc|c} 5 & 1 & 0 \\ 3 & 2 & 1 \\ 7 & 2 & 1 \end{array} \right] \rightarrow \begin{cases} 5x + y = 9 \\ 3x + 2y + z = 4 \\ 7x + 2y + z = 7 \end{cases}$$

$$Dy = \left[\begin{array}{cc|c} 2 & 5 & 0 \\ 0 & 3 & 1 \\ 3 & 7 & 1 \end{array} \right] \rightarrow \begin{cases} 2y + 5z = 9 \\ 3y + z = 4 \\ 3y + z = 7 \end{cases}$$

$$0 + 6 + 3 = 9 \quad 9 + 7 + 0 = 16 \quad 0 + 14 + 0 = 14 \quad 6 + 15 + 0 = 21$$

$$Dz = \left[\begin{array}{cc|c} 2 & 1 & 5 \\ 0 & 2 & 3 \\ 3 & 2 & 7 \end{array} \right] \rightarrow \begin{cases} 2x + y + 5z = 9 \\ 2y + 3z = 4 \\ 3x + 2y + 7z = 16 \end{cases}$$

$$x = 4, y = 7, z = -5$$

Resposta: D

$$30 + 12 + 0 = 42 \quad 25 + 9 + 0 = 34$$

$$6. \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 2 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 7 \\ -1 \end{bmatrix} \rightarrow \begin{cases} x = 3 \\ 2x + y = 7 \\ -x + 2y + 2z = -1 \end{cases}$$

$$D = \left[\begin{array}{ccc|c} 1 & 0 & 0 & 3 \\ 2 & 1 & 0 & 7 \\ 1 & 2 & 2 & -1 \end{array} \right] \rightarrow \begin{cases} x = 3 \\ 2x + y = 7 \\ -x + 2y + 2z = -1 \end{cases}$$

$$Dz = \left[\begin{array}{ccc|c} 1 & 0 & 3 & 1 \\ 2 & 1 & 7 & 2 \\ -1 & 2 & -1 & -2 \end{array} \right] \rightarrow \begin{cases} x = 3 \\ y = 2 \\ -x + 2y + 2z = -1 \end{cases}$$

$$0 + 0 + 0 = 0 \quad 2 + 0 + 0 = 2 \quad -5 + 14 + 0 = 9 \quad -1 + 0 + 12 = 11$$

$$Dy = \left[\begin{array}{cc|c} 1 & 3 & 0 \\ 2 & 7 & 0 \\ -1 & -1 & 2 \end{array} \right] \rightarrow \begin{cases} x + 3y = 3 \\ 2x + 7y = 2 \\ -x - y + 2z = 11 \end{cases}$$

$$x = 3, y = 2, z = 0$$

Resposta: E

$$0 + 0 + 12 = 12 \quad 14 + 0 + 0 = 14$$

$$4. \begin{cases} x + 2y - 3z = 29 \\ x + 3y + 2z = 4 \\ x - y - 2z = 8 \end{cases} \quad D = \begin{vmatrix} 1 & 2 & -3 \\ 1 & 3 & 2 \\ 1 & -1 & -2 \end{vmatrix} \begin{vmatrix} 1 & 2 \\ 1 & 3 \\ 1 & -1 \end{vmatrix} \rightarrow 1 - (-15) = 16$$

$$D_x = \begin{vmatrix} 29 & 2 & -3 \\ 4 & 3 & 2 \\ 8 & -1 & -2 \end{vmatrix} \begin{vmatrix} 29 & 2 \\ 4 & 3 \\ 8 & -1 \end{vmatrix} \rightarrow -130 - (-146) = 16$$

$$-72 - 58 - 16 = -146 \quad -174 + 32 + 12 = -130$$

$$D_y = \begin{vmatrix} 1 & 29 & -3 \\ 1 & 4 & 2 \\ 1 & 8 & -2 \end{vmatrix} \begin{vmatrix} 1 & 29 \\ 1 & 4 \\ 1 & 8 \end{vmatrix} \rightarrow 26 - (-54) = 80$$

$$-12 + 16 - 58 = -54 \quad -8 + 58 - 24 = 26$$

$$D_z = \begin{vmatrix} 1 & 2 & 29 \\ 1 & 3 & 4 \\ 1 & -1 & 8 \end{vmatrix} \begin{vmatrix} 1 & 2 \\ 1 & 3 \\ 1 & -1 \end{vmatrix} \rightarrow 3 - 99 = -96$$

$$87 - 4 + 16 = 99 \quad 24 + 8 - 29 = 3$$

$$x = \frac{16}{16} = 1$$

$$y = \frac{80}{16} = 5$$

$$z = \frac{-96}{16} = -6$$

$$x + y + z = 1 + 5 - 6 = 0$$

Resposta: A

$$2. \begin{cases} 3x + 4y - z = 1 \\ 4x + 5y + 2z = 12 \\ x - 2y + 3z = 8 \end{cases} \quad D = \begin{vmatrix} 3 & 4 & -1 \\ 4 & 5 & 2 \\ 1 & -2 & 3 \end{vmatrix} \begin{vmatrix} 3 & 4 \\ 4 & 5 \end{vmatrix} + 61 - 31 = 30$$

$$-5 - 12 + 48 = 31 \quad 45 + 8 + 8 = 61$$

$$D_y = \begin{vmatrix} 3 & 1 & -1 \\ 4 & 12 & 2 \\ 1 & 8 & 5 \end{vmatrix} \begin{vmatrix} 3 & 1 \\ 4 & 12 \end{vmatrix} - 8 \cdot 78 - 48 = 30 \quad y = \frac{D_y}{D}$$

$$-12 + 48 + 12 = 48 \quad 108 + 2 - 52 = 78 \quad y = \frac{30}{30} = 1$$

Resposta: A

$$3. \begin{cases} x + 2y + z = 1 \\ 3x + y - 11z = -2 \\ 2x + 3y - z = 1 \end{cases} \quad D = \begin{vmatrix} 1 & 2 & 1 \\ 3 & 1 & -11 \\ 2 & 3 & -1 \end{vmatrix} \begin{vmatrix} 1 & 2 \\ 3 & 1 \end{vmatrix} - 36 - (-37) = 1$$

$$2 \cdot 53 - 6 = -37 \quad -1 \cdot 44 + 9 = -36$$

$$D_x = \begin{vmatrix} 1 & 2 & 1 \\ -2 & 1 & -11 \\ 1 & 3 & -1 \end{vmatrix} \begin{vmatrix} 1 & 2 \\ -2 & 1 \end{vmatrix} + 29 - (-28) = -1 \quad D_y = \begin{vmatrix} 1 & 1 & 1 \\ 3 & 2 & -11 \\ 2 & 1 & -1 \end{vmatrix} \begin{vmatrix} 3 & 2 \\ 2 & 1 \end{vmatrix}$$

$$1 \cdot 33 + 4 = 28 \quad -1 \cdot 22 - 6 = -28 \quad -4 - 11 \cdot 3 = -78 \quad 2 + 22 + 1 = -17$$

$$D_z = \begin{vmatrix} 1 & 2 & 1 \\ 3 & 1 & -2 \\ 2 & 3 & 1 \end{vmatrix} \begin{vmatrix} 3 & 1 \\ 2 & 3 \end{vmatrix} - 2 - 2 = 6 \quad -11 \cdot (-18) = 1$$

$$2 \cdot 6 + 6 = 2 \quad 1 \cdot 8 + 9 = 2 \quad x = -1 = -1 \quad y = 1 = 1 \quad z = 0 = 0$$

$$v = \frac{1}{2}(-1, 1, 0) \quad a + b + c = 0 \quad -1 + 1 + 0 = 0$$

Resposta: C

1. a. $\begin{cases} 2x - y = 2 \\ -x + 6y = -5 \end{cases}$

$D = \begin{vmatrix} 2 & -1 \\ -1 & 6 \end{vmatrix} = 12 - 1 = 11$

$D_x = \begin{vmatrix} 2 & -1 \\ -5 & 6 \end{vmatrix} = 12 - 5 = 7$

$D_y = \begin{vmatrix} 2 & 2 \\ -1 & 3 \end{vmatrix} = 6 - (-2) = 8$

$x = \frac{D_x}{D} = \frac{7}{11}$ $y = \frac{D_y}{D} = \frac{8}{11}$

Resposta: $x = \frac{7}{11}$ $y = \frac{8}{11}$

b. $\begin{cases} 3x - y + z = 1 \\ 2x + 3z = -1 \\ 4x + y - 2z = 7 \end{cases}$

$D = \begin{vmatrix} 3 & -1 & 1 \\ 2 & 0 & 3 \\ 4 & 1 & 2 \end{vmatrix} = 3(0-3) - 1(2-12) + 1(2-4) = -9 + 10 - 2 = -1$

$D_x = \begin{vmatrix} 1 & -1 & 1 \\ -1 & 0 & 3 \\ 7 & 1 & 2 \end{vmatrix} = 1(0-7) - 1(2-21) + 1(-1-7) = -7 + 19 - 8 = 4$

$D_z = \begin{vmatrix} 3 & 1 & 1 \\ 2 & -1 & 3 \\ 4 & 1 & 2 \end{vmatrix} = 3(2-4) - 1(2-12) + 1(2-4) = -6 + 10 - 2 = 2$

$D_y = \begin{vmatrix} 3 & 1 & 1 \\ 2 & 0 & 3 \\ 4 & 1 & 2 \end{vmatrix} = 3(0-3) - 1(2-12) + 1(2-4) = -9 + 10 - 2 = -1$

$x = \frac{D_x}{D} = \frac{4}{-1} = -4$ $y = \frac{D_y}{D} = \frac{-1}{-1} = 1$ $z = \frac{D_z}{D} = \frac{2}{-1} = -2$

$0 - 3 - 14 = -17$ $0 + 4 + 2 = 6$ $6 - (-17) = 23$

$z = \frac{D_z}{D} = \frac{2}{-1} = -2$

Resposta: $x = -4$ $y = 1$ $z = -2$