# Introduction to the Message Passing Interface (MPI)

#### F. Schornbaum

University Erlangen-Nuremberg - System Simulation

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Introduction to MPI 12.2014

### Outline

- MPI Overview
- Process model and language bindings
- Messages and point-to-point communication
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication

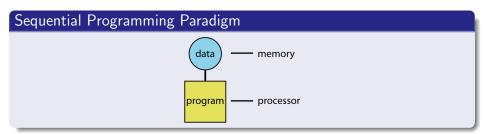


### Outline

- MPI Overview
  - one program on several processors
  - work and data distribution
  - the communication network
- Process model and language bindings
- Messages and point-to-point communication
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication

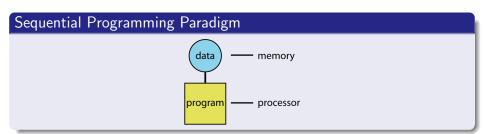


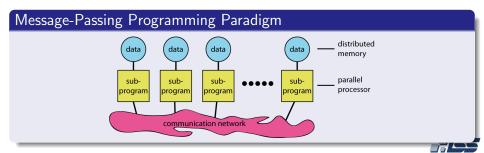
# The Message-Passing Programming Paradigm





# The Message-Passing Programming Paradigm

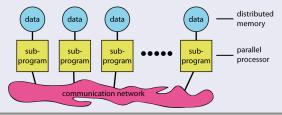




# The Message-Passing Programming Paradigm

#### Each processor in a message passing program runs a sub-program

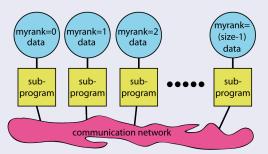
- ullet written in a conventional sequential language, e.g., C(++) or Fortran
- typically the same on each processor (SPMD)
- the variables of each sub-program have
  - the same name
  - but different locations (distributed memory) and different data!
  - i.e., all variables are private
- communicate via special send & receive routines (message passing)



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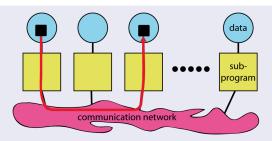
#### Data and Work Distribution

- the value of myrank is returned by special library function
- the system of size processes is started by special MPI initialization program (mpirun or mpiexec)
- all distribution decisions are based on myrank
- i.e., which process works on which data



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### Messages



- Messages are packets of data moving between sub-programs
- Necessary information for the message passing system:
  - sending process
  - source location
  - source data type
  - source data size

- receiving process
- destination location
- destination data type
- destination buffer size

#### Access

- A sub-program needs to be connected to a message passing system
- A message passing system is similar to:
  - mail box
  - phone line
  - fax machine
  - etc.
- MPI:
  - sub-program must be linked with an MPI library
  - the total program (i.e., all sub-programs of the program) must be started with the MPI startup tool



# Addressing

- Messages need to have addresses to be sent to
- Addresses are similar to:
  - mail addresses
  - phone number
  - fax number
  - etc.
- MPI: addresses are ranks of the MPI processes (sub-programs)



#### Point-to-Point communication

- Simplest from of message passing
- One process send a message to another
- Different types of point-to-point communication:
  - non-buffered = synchronous send
  - buffered = asynchronous send



# Synchronous/Asynchronous Sends

### Synchronous Sends

- The sender gets an information that the message is received
- Analog to the beep or okay-sheet of a fax



# Synchronous/Asynchronous Sends

### Synchronous Sends

- The sender gets an information that the message is received
- Analog to the beep or okay-sheet of a fax

### Buffered = Asynchronous Sends

• We only know when the message has left



#### Process 0

```
send ( &a, 1, 1 );
receive( &b, 1, 1 );
```

### Process 1

```
send ( &a, 1, 0 );
receive( &b, 1, 0 );
```



#### Process 0

```
send ( &a, 1, 1 );
receive( &b, 1, 1 );
```

### Process 1

```
send ( &a, 1, 0 );
receive( &b, 1, 0 );
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Depending on the implementation of send and receive this might lead to a **deadlock**!



#### Process 0

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```

Depending on the implementation of send and receive this might lead to a **deadlock**!

#### Process 0

```
receive( &b, 1, 1 );
send ( &a, 1, 1 );
```

#### Process 1

```
receive( &b, 1, 0 );
send ( &a, 1, 0 );
```



### Process 0

```
send ( &a, 1, 1 );
receive( &b, 1, 1 );
```

### Process 1

```
send (&a, 1, 0);
receive( &b, 1, 0 );
```

Depending on the implementation of send and receive this might lead to a deadlock!

#### Process 0

```
receive( &b, 1, 1 );
send ( &a, 1, 1 );
```

#### Process 1

```
receive( &b, 1, 0 );
send ( &a, 1, 0 );
```

Even with buffered send this code will lead to a **deadlock!** 

# **Blocking Operations**

- Operations are local activities, e.g.,
  - sending (a message)
  - receiving (a message)
- Some operations may **block** until another process acts:
  - synchronous send operation blocks until receive is posted
  - receive operation blocks until message is sent
- Relates to the completion of an operation
- Blocking subroutine returns only when the operation has completed



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# Non-Blocking Operations

- Non-blocking operation: returns immediately and allow the sub-program to perform other work.
- At some later time the sub-program must test or wait for the completion of the non-blocking operation.
- All non-blocking operations must have matching wait (or test) operations. (Some system or application resources can be freed only when the non-blocking operation is completed.)
- A non-blocking operation immediately followed by a matching wait is equivalent to a blocking operation
- Non-blocking operations are not the same as sequential subroutine calls: the operation may continue while the application executes the next statements!



#### Collective Communications

- Collective communication routines are higher level routines.
- Several processes are involved at a time
- May allow optimized internal implementations, e.g., tree based algorithms
- Can be built out of point-to-point communications



# Collective Communications (cont'd)

#### Broadcast

• A one-to-many communication



# Collective Communications (cont'd)

#### **Broadcast**

A one-to-many communication

#### **Reduction Operations**

• Combine data from several processes to produce a single result



# Collective Communications (cont'd)

#### **Broadcast**

A one-to-many communication

### Reduction Operations

Combine data from several processes to produce a single result

#### **Barriers**

Synchronize processes



# Goals and Scope of MPI

- MPI's prime goals
  - to provide a message-passing interface
  - to provide source-code portability
  - to allow efficient implementations
- it also offers:
  - a great deal of functionality
  - support for heterogeneous parallel architectures
- With MPI-2:
  - important additional functionality
  - no changes to MPI-1.
- With MPI-2.1, 2.2, 3.0:
  - important additional functionality to fit on new hardware principles
  - deprecated MPI routines moved to chapter "Deprecated Functions"



### Outline

- MPI Overview
- Process model and language bindings
  - starting several MPI processes
- Messages and point-to-point communication
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication



# Compilation/Header Files/Function Format

### Compilation



# Compilation/Header Files/Function Format

### Compilation

#### Header files

```
#include <mpi.h>
```



# Compilation/Header Files/Function Format

### Compilation

#### Header files

```
#include <mpi.h>
```

#### MPI Function Format

```
error = MPI_Xxxxx( parameter, ... );
MPI_Xxxxxx( parameter, ... );
```

### MPI Function Format Details

- MPI\_.... namespace is reserved for MPI constants and routines, i.e., application routines and variable names must not begin with MPI\_.
- Output arguments in C(++) are handled via passing-by-pointer:

#### Function definitions

```
MPI_Comm_rank( ..., int *rank );
MPI_Recv( ..., MPI_Status *status );
```

### Usage in your code

```
main( ... ) {
   int myrank;
   MPI_Status recv_status;
   MPI_Comm_rank( ..., &myrank );
   MPI_Recv( ..., &recv_status );
}
```

# Initializing MPI

- Should be the very first function call inside the main function
- Must be the very first MPI function call

#### Function definition

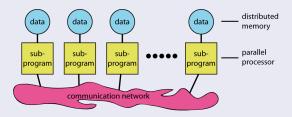
```
MPI_Init( int *argc, char ***argv );
```

### Usage in your code

```
#include <mpi.h>
int main( int argc, char** argv )
{
   MPI_Init( &argc, &argv );
   ...
}
```

### Starting the MPI Program

- Start mechanism is implementation dependent
- mpirun -np number\_of\_processes ./executable (most implementations)
- mpiexec -n number\_of\_processes ./executable (with MPI-2 standard)



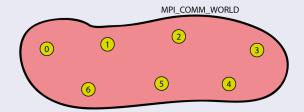
• The parallel MPI processes exist at least after MPI\_Init was called.



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### Communicator MPI\_COMM\_WORLD

- All processes (= sub-programs) of one MPI program are combined in the communicator MPI\_COMM\_WORLD
- MPI\_COMM\_WORLD is a predefined handle in mpi.h
- Each process has its own rank in a communicator:
  - starting with 0
  - ending with size-1





#### Handles

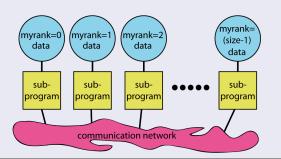
- Handles identify MPI objects
- For the programmer, handles are
  - predefined constants in mpi.h
    - example: MPI\_COMM\_WORLD
    - predefined values exist only after MPI\_Init was called
  - values returned by some MPI routines, to be stored in variables that are defined as special MPI typedefs
- Handles refer to internal MPI data structures



#### Rank

- The rank identifies different processes
- The rank is the basis for any work and data distribution

int MPI\_Comm\_rank( MPI\_Comm comm, int \*rank );





#### Size

• How many processes are contained within a communicator?

```
int MPI_Comm_size( MPI_Comm comm, int *size );
```



# Exiting MPI

```
int MPI_Finalize();
```

- MUST be called last by all processes
- After MPI\_Finalize:
  - Further MPI-calls are forbidden
  - Especially re-initialization with MPI\_Init is forbidden



# Example: MPI Hello World (I)

```
#include <mpi.h>
int main( int argc, char **argv )
   // Definition of the variables
   int size; //The total number of processes
   int rank; //The rank/number of this process
   // MPI initialization
   MPI_Init( &argc, &argv );
   // Determining the number of CPUs and the rank for each CPU
   MPI_Comm_size( MPI_COMM_WORLD, &size );
   MPI_Comm_rank( MPI_COMM_WORLD, &rank );
   . . .
```

# Example: MPI Hello World (II)

```
// 'Hello World' output for CPU 0
   if(rank == 0)
      cout << " Hello World" << endl;</pre>
   // Output of the own rank and size of each CPU
   cout << " I am CPU " << rank << " of " << size << " CPUs" << endl;
   // MPT finalizations
   MPI_Finalize();
   return 0;
}
```

# Example: MPI Hello World (III)

Possible output of the program:

```
I am CPU 2 of 4 CPUs
Hello World
I am CPU 0 of 4 CPUs
I am CPU 3 of 4 CPUs
I am CPU 1 of 4 CPUs
```

Note: The output of the program is non-deterministic!



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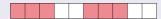
### Outline

- MPI Overview
- Process model and language bindings
- Messages and point-to-point communication
  - the MPI processes can communicate
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication



# Messages

- A message contains a number of elements of some particular datatype
- MPI datatypes:
  - Basic datatype
  - Derived datatypes



- Derived datatypes can be built up from basic or derived data types
- Data type handles are used to describe the type of the data in the memory.
- Example: message with 5 integers

2345	654	96574	-12	7676
------	-----	-------	-----	------



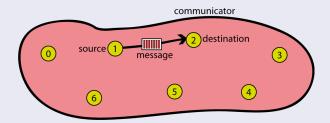
# MPI Basic Datatypes

MPI_CHAR	char	Treated as printable character
MPI_SHORT	signed short int	
MPI_INT	signed int	
MPI_LONG	signed long int	
MPI_LONG_LONG	signed long long	
MPI_SIGNED_CHAR	signed char	Treated as integral value
MPI_UNSIGNED_CHAR	unsigned char	Treated as integral value
MPI_UNSIGNED_SHORT	unsigned short int	
MPI_UNSIGNED	unsigned int	
MPI_UNSIGNED_LONG	unsigned long int	
MPI_UNSIGNED_LONG_LONG	unsigned long long	
MPI_FLOAT	float	
MPI_DOUBLE	double	
MPI_LONG_DOUBLE	long double	
MPI_BYTE		
MPI_PACKED		



### Point-to-Point Communication

- Communication between two processes
- Source process sends message to destination process
- Communication takes place within a communicator, e.g., MPI\_COMM\_WORLD
- Processes are identified by their ranks in the communicator



# Sending a Message

- buf is the starting point of the message with count elements
- dest is the rank of the destination process within the communicator comm
- tag is an additional nonnegative integer piggyback information, additionally transferred with the message
- The tag can be used by the program to distinguish different types of messages



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## Receiving a Message

- buf, count, datatype describe the receive buffer
- Receiving the message sent by process with rank source in comm
- Envelope information is returned in status
- Only messages with matching tag are received



### Requirements for Point-to-Point Communications

#### For a communication to succeed:

- Sender must specify a valid destination rank
- Receiver must specify a valid source rank
- The communicator must be the same
- Tags must match
- Message datatypes must match
- Receiver's buffer must be large enough



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### Wildcarding

- Receiver can wildcard
- To receive from any source ⇒ source = MPI\_ANY\_SOURCE
- To receive from any tag ⇒ tag = MPI\_ANY\_TAG
- Actual source and tag are returned in the receiver's status parameter



# Communication Envelope

Envelope information is returned from MPI\_Recv in status

```
status.MPI_SOURCE
status.MPI_TAG
status.MPI_ERROR
count via MPI_Get_count()
```

```
From: source rank
     tag
To: destination rank
 Item 1
 Item 2
            "count"
 Item 3
           elements
 Item 4
 Item n
```

#### Communication Modes

Send communication modes

- synchronous send

1 1

- buffered [asynchronous] send

- standard send

- ready send

 $\Rightarrow$   $\Rightarrow$  MPI\_Ssend

⇒ MPI\_Bsend

 $\Rightarrow$  MPI\_Send

 $\Rightarrow$  MPI\_Rsend

Receiving all modes

 $\Rightarrow$  MPI\_Recv



### Communication Modes – Definitions

Sender mode	Definition	Notes
Synchronous send MPI_Ssend	Only completes when the receive has started	
Buffered send MPI_Bsend	Always completes (unless an error occurs), irrespective of receiver	needs application- defined buffer to be declared with MPI_Buffer_attach
Standard send MPI_Send	Either synchronous or buffered	Uses an internal buffer
Ready send MPI_Rsend	May be started <b>only</b> if the matching receive is already posted!	Highly dangerous!
Receive MPI_Recv	Completes when a message has arrived	same routine for all communication modes



### Rules for the Communication Modes

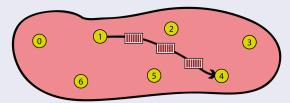
- Standard send (MPI\_Send)
  - minimal transfer time
  - may block due to synchronous mode
  - ullet ightarrow risks with synchronous send
- Synchronous send (MPI\_Ssend)
  - risk of deadlock
  - risk of serialization
  - ullet risk of waiting o idle time
- Ready send (MPI\_Rsend)
  - use never, except you have a 200% guarantee that Recv is already called in the current version and all future versions of your code



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## Message Order Preservation

- Rule for messages on the same connection, i.e., same communicator, source, and destination rank:
- Messages do not overtake each other
- This is true even for non-synchronous sends.



• If both receives match both messages, the order is preserved.



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### Outline

- MPI Overview
- Process model and language bindings
- Messages and point-to-point communication
- Non-blocking communication
  - - to avoid idle time and deadlocks
- Derived data types
- Virtual topologies
- Collective communication

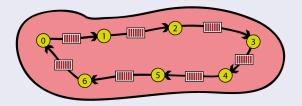


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### Deadlock

• Code in each MPI process:

```
// This will block and never return, because MPI_Recv
// cannot be called in the right-hand MPI process
MPI_Ssend( ..., right_rank, ... );
MPI_Recv( ..., left_rank, ... );
```



 Same problem with standard send mode (MPI\_Send) if MPI implementation chooses synchronous protocol

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### Non-Blocking Communications

### Separate communication into three phases:

- Initiate non-blocking communication
  - returns immediately
  - routine name starting with MPI\_I...
- Do some work (perhaps involving other communications?)
- Wait for non-blocking communication to complete



# Non-Blocking Examples

### Non-blocking send

MPI\_Isend(...)
doing some other work
MPI\_Wait(...)





# Non-Blocking Examples

### Non-blocking send

MPI\_Isend(...)
doing some other work
MPI\_Wait(...)

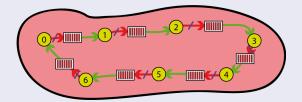


### Non-blocking receive

MPI\_Irecv(...)
doing some other work
MPI\_Wait(...)

### Non-Blocking Send

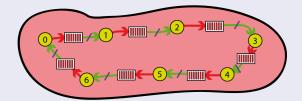
- Initiate non-blocking send
  - ightarrow In the ring example: initiate non-blocking send to the right neighbor
- Do some work:
  - → In the ring example: Receive the message from left neighbor
- Now, the message transfer can be completed
- Wait for non-blocking send to complete





### Non-Blocking Receive

- Initiate non-blocking receive
   In the ring example: Initiate non-blocking receive from left neighbor
- Do some work:
   in the ring example: Sending the message to the right neighbor
- Now, the message transfer can be completed
- Wait for non-blocking receive to complete





### Request Handles

#### Request handles

- are used for non-blocking communication
- must be stored in local variables (MPI\_Request)
- the value
  - is generated by a non-blocking communication routine
  - is used (and freed) in the MPI\_Wait routine



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# Non-Blocking Synchronous Send

- buf must not be accessed between Issend and Wait

  (In MPI-2.2, this restriction is relaxed to "must not be modified")
- "Issend + Wait directly after Issend" is equivalent to blocking call (Ssend)
- status is not used in Issend, but in Wait (with send: nothing returned)

## Non-Blocking Receive

```
int MPI_Irecv( void* buf, int count,
                 MPI_Datatype datatype, int source,
                 int tag, MPI_Comm comm,
                 MPI_Request *request);
 int MPI_Wait( MPI_Request *request, MPI_Status *status );

    buf must not be used between Irecv and Wait
```



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### Blocking and Non-Blocking

- Send and receive can be blocking or non-blocking
- A blocking send can be used with a non-blocking receive, and vice-versa.
- Non-blocking sends can use any mode standard – MPI Isend

synchronous – MPI\_Issend

buffered – MPI\_lbsend

ready – MPI\_Irsend

- Synchronous mode affects completion, i.e., MPI\_Wait/MPI\_Test, not initiation, i.e., MPI\_I...
- The non-blocking operation immediately followed by a matching wait is equivalent to the blocking operation



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### Completion

#### One must

- Wait or
- ullet loop with Test until request is completed, i.e., flag ==1



## Multiple Non-Blocking Communications

#### You have several request handles:

- Wait or test for completion of one message MPI\_Waitany / MPI\_Testany
- Wait or test for completion of all messages
   MPI\_Waitall / MPI\_Testall \*)
- Wait or test for completion of as many messages as possible MPI\_Waitsome / MPI\_Testsome \*)



\*) Each status contains an additional error field. This field is only used if MPI\_ERR\_IN\_STATUS is returned (also valid for send operations)

### Outline

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- Non-blocking communication
- Derived data types
  - transfer of any combination of typed data
- Virtual topologies
- Collective communication



# MPI Datatypes

- Description of the memory layout of the buffer
  - for sending
  - for receiving
- Basic types
- Derived types
  - vectors
  - structs
  - others



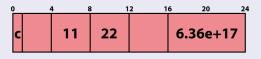
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## Data Layout and the Describing Datatype Handle

```
const int count
                      = 2
  const int blocklength = 2
  const int stride
                       =4
  MPI_Datatype columntype;
  MPI_Type_vector( count, blocklength, stride, MPI_INT,
                   &columntype);
  MPI_Type_commit( &columntype );
  MPI Send( &buffer, 1, columntype, ...);
 &buffer = the start address
                             the datatype handle
                             describes the data layout
            of the data
int
```

## Derived Data Types – Type Maps

- A derived datatype is logically a pointer to a list of entries
- A derived datatype describes the memory layout of, e.g., structures, common blocks, subarrays, some variables in the memory
- Example:

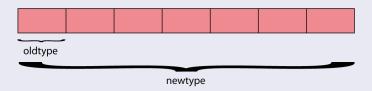


basic datatype	displacement	
MPI_CHAR	0	
MPI_INT	4	
MPI_INT	8	
MPI_DOUBLE	16	



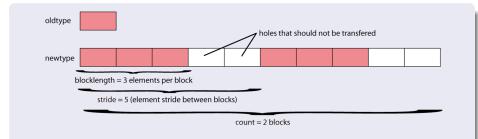
## Contiguous Data

- The simplest derived datatype
- Consists of a number of contiguous items of the same datatype





### Vector Datatype





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### Committing a Datatype

- Before a datatype handle is used in message passing communication,
   it needs to be committed with MPI\_Type\_commit
- This must be done only once (by each MPI process)

```
int MPI_Type_commit( MPI_Datatype *datatype );
```

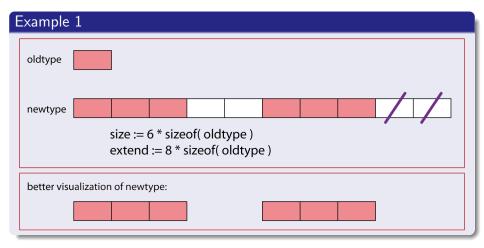


### Size and Extent of a Datatype

- Size := number of bytes that have to be transferred
- Extend := spans from first to last byte
- Basic datatypes: Size = Extend = number of bytes used by the compiler
- Derived datatypes:



# Size and Extent of a Datatype (cont'd)





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#### Outline

- MPI Overview
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- Derived data types
- Virtual topologies
  - - a multi-dimensional process naming scheme
- Collective communication



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### Virtual Topologies

- Convenient process naming
- Naming scheme to fit the communication pattern
- Simplifies writing of code
- Can allow MPI to optimize communications

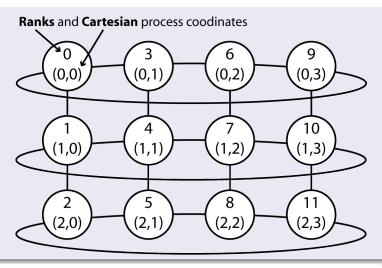


### How to use a Virtual Topology

- Creating a topology produces a new communicator
- MPI provides mapping functions
  - to compute process ranks, based on the topology naming scheme
  - and vice versa.



# Example – A 2-dimensional Cylinder



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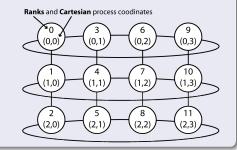
### Topology Types

- Cartesian Topologies
  - each process is connected to its neighbor in a virtual grid
  - boundaries can be cyclic, or not
  - processes are identified by Cartesian coordinates
  - of course, communication between any two processes is still allowed
- Graph Topologies
  - general graphs
  - not covered here



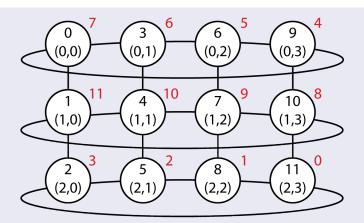
# Creating a Cartesian Virtual Topology

```
comm_old = MPI_COMM_WORLD
  ndims = 2
    dim = { 3, 4 }
periods = { 0, 1 }
reorder = see next slide
```





# Example – A 2-dimensional Cylinder

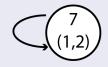


- Ranks in comm and comm\_cart may differ, if reorder == 1
- This reordering can allow MPI to optimize communications

F. Schornbaum (LSS) Introduction to MPI 12.2014

### Cartesian Mapping Functions

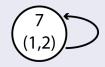
Mapping ranks to process grid coordinates





### Cartesian Mapping Functions

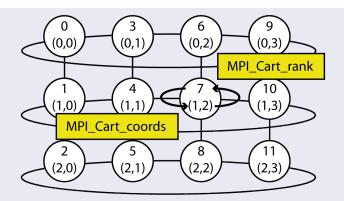
Mapping process grid coordinates to ranks



MPI\_Cart\_rank( MPI\_Comm comm, int \*coords, int \*rank );



#### Own Coordinates



Each process gets its own coordinates with

```
MPI_Comm_rank ( comm_cart, &my_rank );
MPI_Cart_coords( comm_cart, my_rank, maxdims, my_coords );
```

### Cartesian Mapping Functions

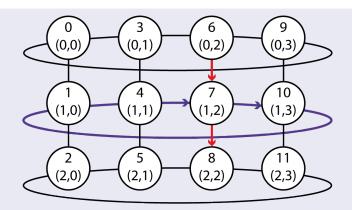
• Computing ranks of neighboring processes

- Returns MPI\_PROC\_NULL if there is no neighbor
- MPI\_PROC\_NULL can be used as source or destination rank in each communication → Then, this communication will be a noop!



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### MPI\_Cart\_shift - Example



MPI\_Cart\_shift( cart, direction, displace, rank\_source, rank\_dest ); example of 0 +1 6 8 process rank=7 1 +1 4 10



#### Outline

- MPI Overview
- Process model and language bindings
- Messages and point-to-point communication
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication
  - - e.g., broadcast



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#### Collective communication

- Communications involving a group of processes
- Called by all processes in a communicator
- Examples:
  - Barrier synchronization
  - Broadcast, scatter, gather
  - Global sum, global maximum, etc.



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#### Characteristics of Collective communication

- Collective action over a communicator
- All processes of the communicator must communicate, i.e., must call the collective routine
- Synchronization may or may not occur, therefore all processes must be able to start the collective routine
- All collective operations are blocking
- No tags
- Receive buffers must have exactly the same size as send buffers



### Barrier Synchronization

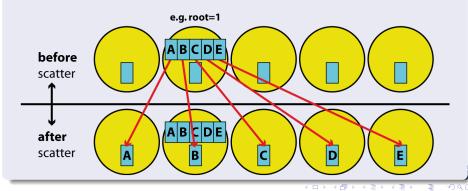
```
MPI_Barrier( MPI_Comm comm );
```

#### MPI\_Barrier is normally never needed:

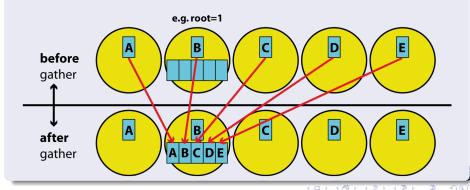
- all synchronization is done automatically by the data communication
  - a process cannot continue before it has the data that it needs
- if used for debugging
  - please guarantee, that it is removed in production
- for profiling: to separate time measurement of
  - Load imbalance of computation [MPI\_Wtime(); MPI\_Barrier(); MPI\_Wtime();]
  - communication epochs [MPI\_Wtime(); MPI\_Allreduce(); ...; MPI\_Wtime()]
- if used for synchronizing external communication (e.g., I/O)
  - exchanging tokens may be more efficient and scalable than a barrier on MPI\_COMM\_WORLD

#### **Broadcast**

```
int MPI_Bcast( void* buffer, int count,
                MPI_Datatype datatype,
                int root, MPI_Comm comm );
                                e.g.root=2
   before
   bcast
   after
   bcast
```



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### Global Reduction Operations

- To perform a global reduce operation across all members of a group
- $d_0 \circ d_1 \circ d_2 \circ \dots \circ d_{s-2} \circ d_{s-1}$ 
  - $d_i = \text{data in process rank i}$ 
    - single variable, or
    - vector
  - o = associative operation
  - Example:
    - global sum or product
    - global maximum or minimum
    - global user-defined operation
  - floating point rounding may depend on usage of associative law
    - $[(d_0 \circ d_1) \circ (d_2 \circ d_3)] \circ [... \circ (d_{s-2} \circ d_{s-1})]$
    - $((((((d_0 \circ d_1) \circ d_2) \circ d_3) \circ ...) \circ d_{s-2}) \circ d_{s-1})$



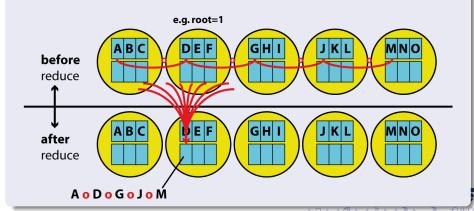
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# Predefined Reduction Operation Handles

Predefined operation handle	Function
MPI_MAX	Maximum
MPI_MIN	Minimum
MPI_SUM	Sum
MPI_PROD	Product
MPI_LAND	Logical AND
MPI_BAND	Bitwise AND
MPI_LOR	Logical OR
MPI_BOR	Bitwise OR
MPI_LXOR	Logical exclusive OR
MPI_BXOR	Bitwise exclusive OR
MPI_MAXLOC	Maximum and location of the maximum
MPI_MINLOC	Minimum and location of the minimum



#### MPI\_Reduce



### Example of Global Reduction

- Global integer sum
- Sum of all inbuf values should be returned in resultbuf
- root = 0; MPI\_reduce( &inbuf, &resultbuf, 1, MPI\_INT, MPI\_SUM, root, MPI\_COMM\_WORLD );
- The result is only placed in resultbuf at the root process

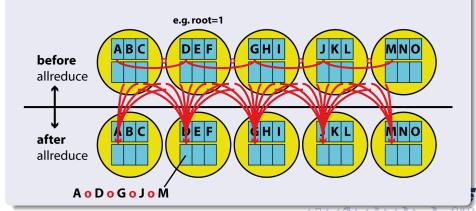


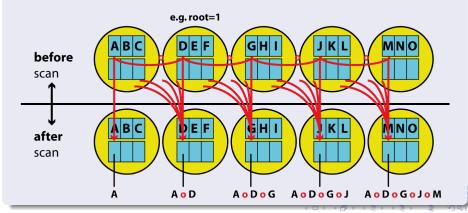
### Variants of Reduction Operations

- MPI\_Allreduce
  - no root
  - returns the result in all processes
- MPI\_Reduce\_scatter
  - result vector of the reduction operation is scattered to the processes into the real result buffers
- MPI Scan
  - prefix reduction
  - result at process with rank i := reduction of inbuf-values from rank 0 to rank i



#### MPI\_Allreduce





#### Outline

- MPI Overview
- Process model and language bindings
- Messages and point-to-point communication
- Non-blocking communication
- Derived data types
- Virtual topologies
- Collective communication
- Serialization
  - how to order the execution of MPI processes



#### Motivation

### Question

How can MPI processes be serialized?



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### Solution 1

```
if( rank == 0 ) /* ... */
MPI_Barrier( MPI_COMM_WORLD );
if( rank == 1 ) /* ... */
MPI_Barrier( MPI_COMM_WORLD );
// ...
```



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#### Solution 1

```
if( rank == 0 ) /* ... */
MPI_Barrier( MPI_COMM_WORLD );
if( rank == 1 ) /* ... */
MPI_Barrier( MPI_COMM_WORLD );
// ...
```

```
MPI_Comm_size( MPI_COMM_WORLD, &size );
MPI_Comm_rank( MPI_COMM_WORLD, &rank );

for( int i=0; i<size; ++i ) {
   if( i == rank ) /* ... */
   MPI_Barrier( MPI_COMM_WORLD );
}</pre>
```



### Solution 2

- Each process waits for a message from the processes with rank-1 (blocking receive)
- Do some work
- Send a message to the process with rank rank+1

