

Deep Learning Methods for Reynolds-Averaged Navier-Stokes Simulations of Airfoil Flows

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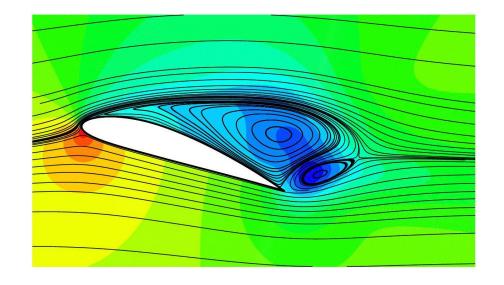






What this paper is about

- Inference of Reynolds-Averaged Navier-Stokes (RANS) solutions
- Pressure and velocity distributions
- Airfoil shapes
- Deep learning U-Net architecture derivative
- Generalization

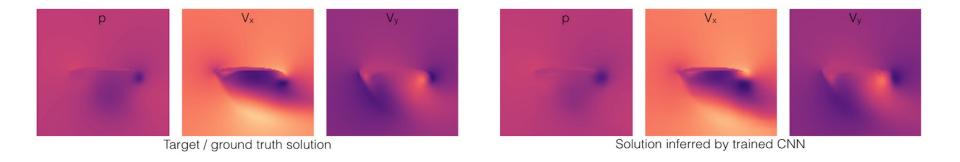


Taken from https://www.pinterest.ch/pin/615163630322034457/





Teaser



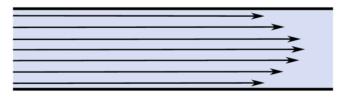
Taken from https://github.com/thunil/Deep-Flow-Prediction



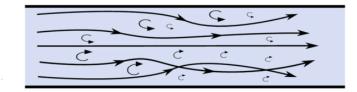
Background – RANS

- Nonlinear partial differential equation (PDE) system
- Based on Navier-Stokes equations
- Used for the modeling of turbulent incompressible flows
- Averages over time component





turbulent flow



Taken from https://diffzi.com/laminar-flow-vs-turbulent-flow/





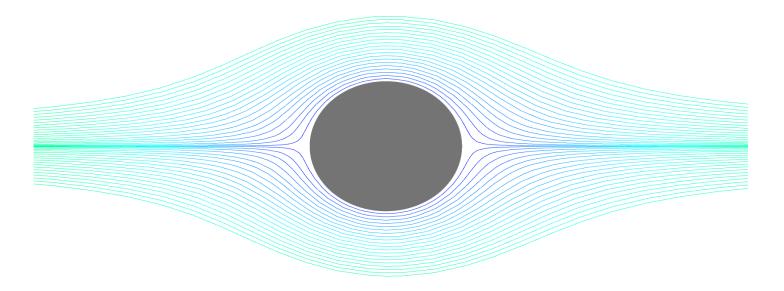
Background – RANS

Reynolds number Re:

- dimensionless constant
- needed for calculation of turbulence models
- magnitude decides flow (laminar, turbulent)
- affects lift and drag coeffcients



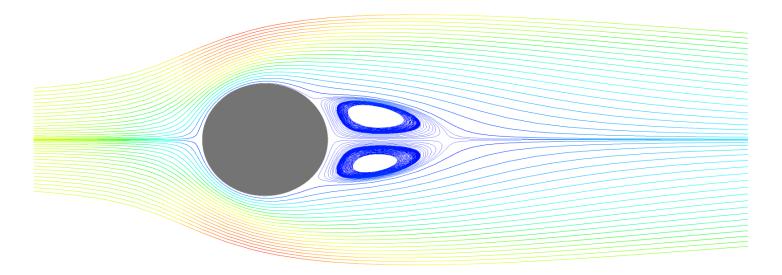
Background – Reynolds number: < 1



Taken from https://www.computationalfluiddynamics.com.au/reynolds-number-cfd/



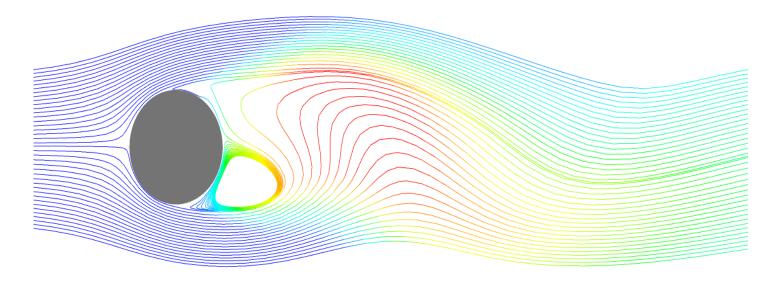
Background – Reynolds number: ≈ 10



Taken from https://www.computationalfluiddynamics.com.au/reynolds-number-cfd/



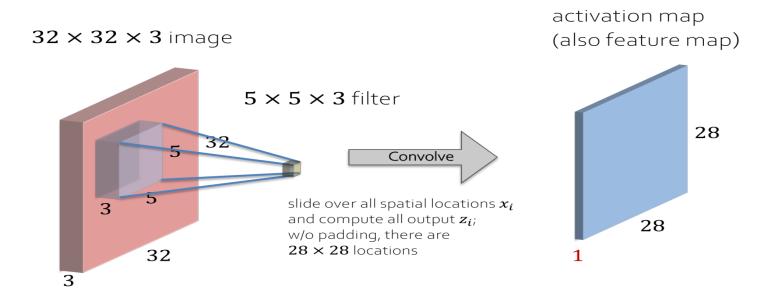
Background – Reynolds number: $\approx 1 \cdot 10^5$



Taken from https://www.computationalfluiddynamics.com.au/reynolds-number-cfd/



Background – Convolutions

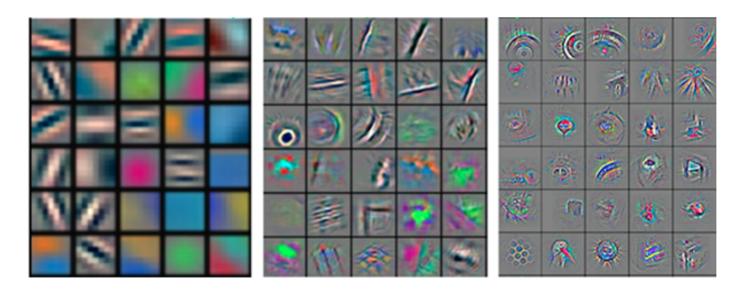


Taken from I2DL WS19/20 (TUM)



Background – Convolutions

Low-Level Features, Mid-Level Features, High-Level Features: each filter captures different characteristics



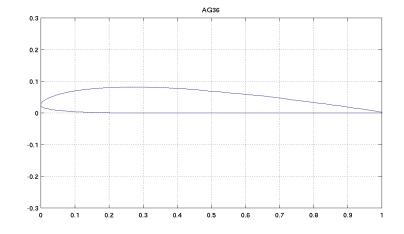
Taken from https://arxiv.org/pdf/1311.2901.pdf





Data – Generation

- Airfoil shapes from UIUC database
- Reynolds number: [0.5,5] · 10⁶ (highly turbulent)
- Angle of attack: [-22.5,22.5]
- Ground truth generated with OpenFOAM (pressure, x velocity, y velocity)
- Training data resolution: 3 × 128 × 128
 (Inference region < full simulation domain)

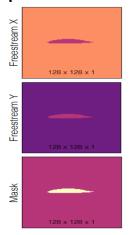


Taken from https://m-selig.ae.illinois.edu/ads/afplots/ag35.gif



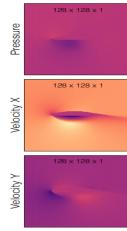
Data - Structure

Input channels



Reynolds number encoded as differently scaled freestream velocity vectors wrt. their magnitude

Target channels



Data from the RANS solution



Pre-processing – Normalization

Motivation: Flatten space of solutions, accelerate learning by simplifing the learning task for the NN

Bernoulli equation for incompressible (laminar) flow:

$$rac{{f v}^2}{2}+gz+rac{{f p}}{
ho}=constant$$

- v: velocity
- g: acceleration (constant)
- z: elevation (constant)
- *p*: pressure
- *ρ*: density (constant)

 $\implies v^2 \sim p$ – e.g. double the speed quadruples the pressure



Pre-processing – Normalization

Normalization of target channels by division with freestream magnitude:

$$ilde{v_o} = rac{v_o}{\|v_i\|}, \quad ilde{
ho_o} = rac{p_o}{\|v_i\|^2}$$
 – important to remove quadratic scaling of pressure





Pre-processing – Normalization

All units dissapear \implies really dimensionless:

- Pressure: $[p]_{Sl} = 1Pa = 1\frac{kg}{m \cdot s^2}$
- Density: $[\rho]_{SI} = 1 \frac{kg}{m^3}$ constant in incompressible flow
- Velocity: $[v]_{SI} = \frac{m}{s}$



Pre-processing – Offset removal & value clamping

Motivation: eliminate ill-posed learning goal & improve numerical precision

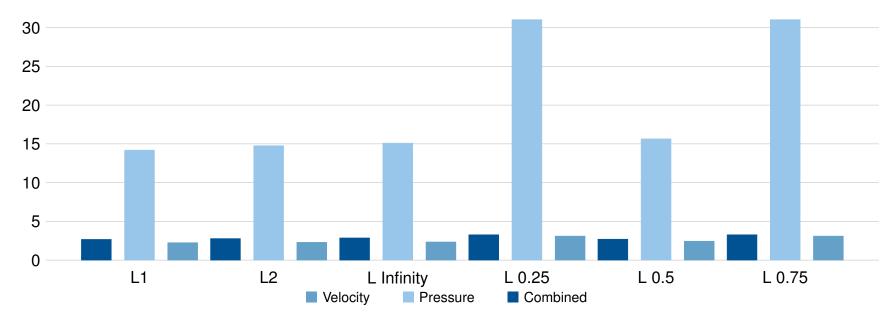
- RANS typically only needs ∇_p for computation
- Spatially move pressure distribution into the origin
- $\hat{p_o} = \tilde{p_o} p_{mean}$
- Clamp both input and target channels into [-1,1] range



Pre-processing – Evaluation

Vector norms used in pre-processing comparision wrt. error, default: L2 (in %)

L1 normalization achieves the best error rates (p, vel, combined: **14.19**%, **2.251**%, **2.646**% – L2: 14.76%, 2.291%, 2.780%)

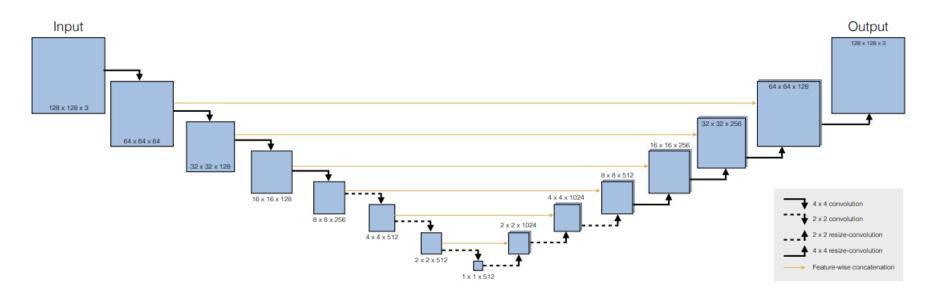






Architecture

U-Net derivative proposed in the paper:



Taken from https://arxiv.org/pdf/1810.08217.pdf



Architecture – Convolutional blocks

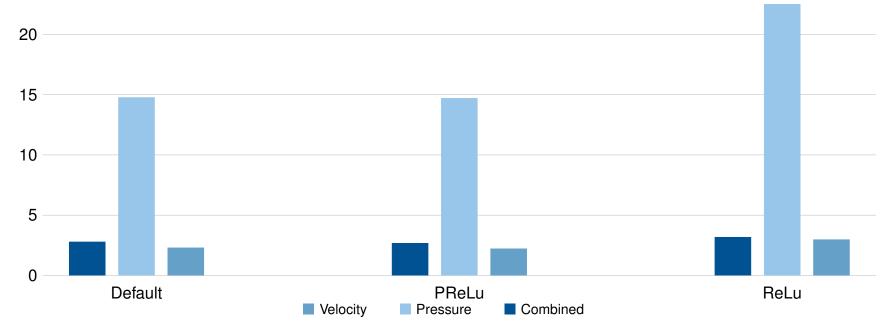
Encoder	Decoder
1. Activation – Leaky ReLu (0.2)	1. Activation – ReLu
2. Convolution – Width down, Depth up	2. Upsampling – linear (2.0)
3. Batch normalization	3. Convolution – Width up, Depth down
4. Dropout (1%)	4. Batch normalization
	5. Dropout (1%)



Architecture – Evaluation

Error percentage of different activation functions after 160k iterations (266 epochs).

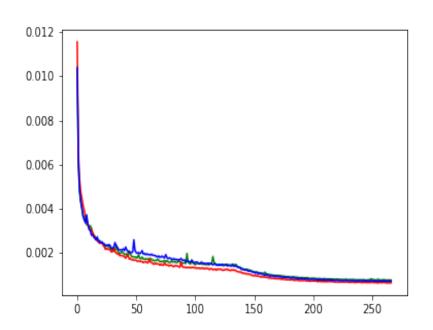
PReLu achieves the best error rates (p, vel, combined: **14.69**%, **2.216**%, **2.676**% – Default: 14.76%, 2.296%, 2.787%)



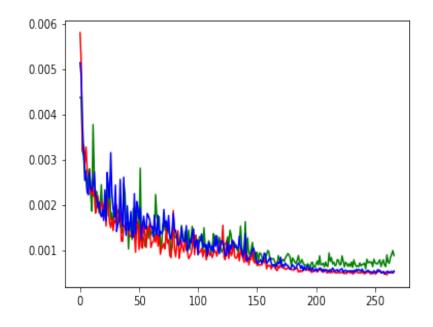


Architecture - Evaluation

Training loss (Default: b, PReLu: r, ReLu: g)



Validation loss (Default: b, PReLu: r, ReLu: g)





Transfer

Motivation: Can the network architecture adapt to other PDE systems & how will it perform?

Another use case for PDE systems: predicting wave propagation on shallow water

Governed by Saint-Venant equations (related with Navier-Stokes equations)



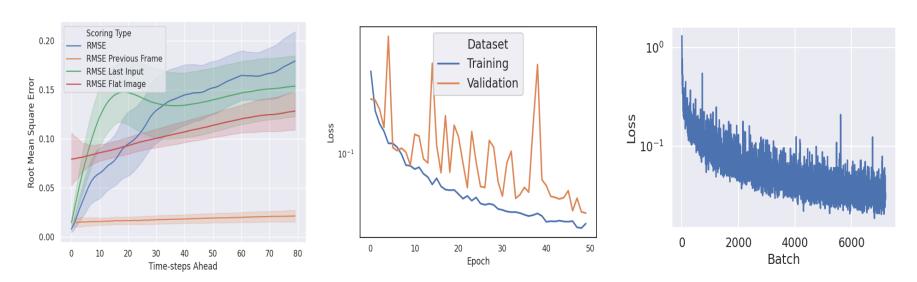
Transfer

U-Net architecture changes:

- Input channels contain the last *n* time steps
- Output channels predict the next *m* time steps
- Output is refeeded as input to predict time series

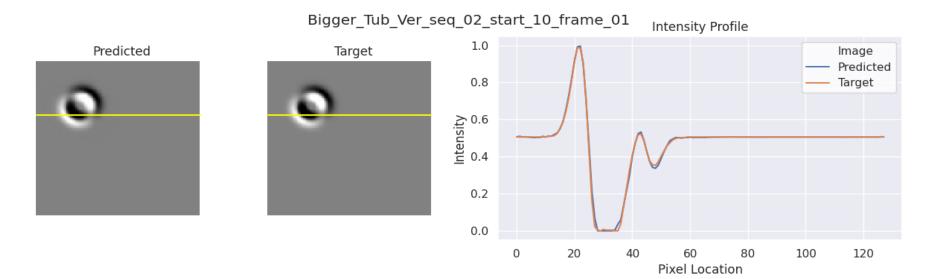


RMSE with variance, validation loss and batch loss on Bigger Tub environment:

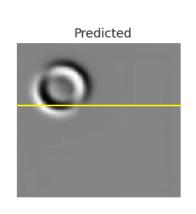


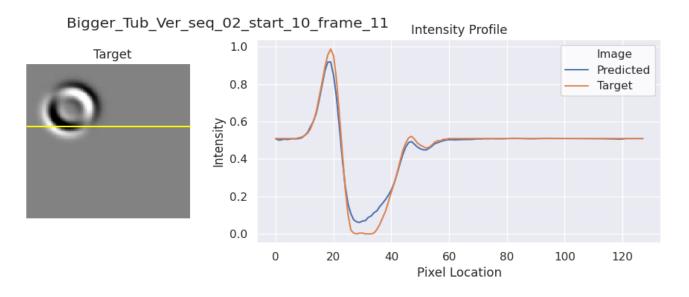
All plots and training in Transfer were made with https://github.com/stathius/wave_propagation



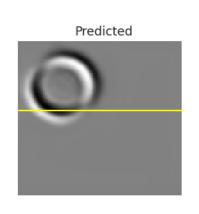


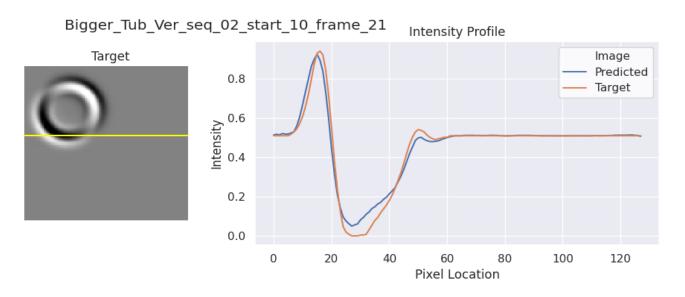




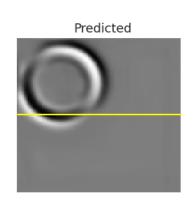


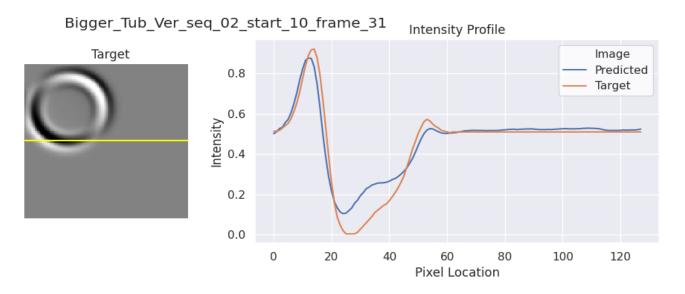




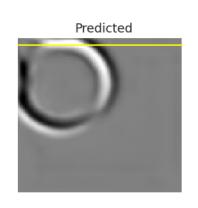


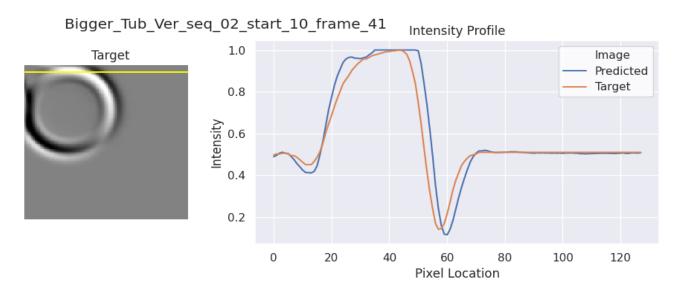




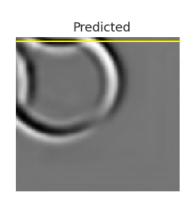


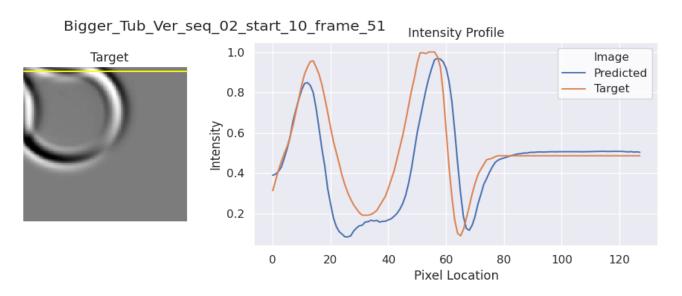




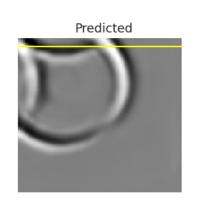


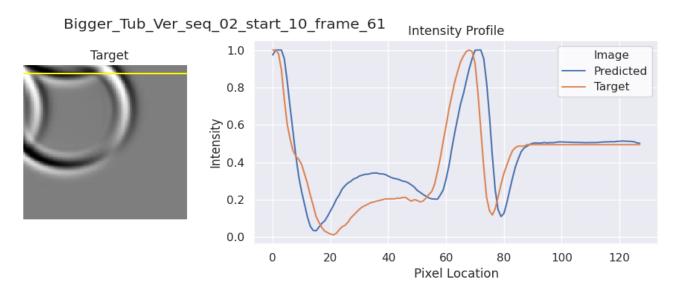




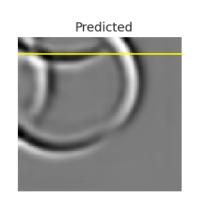


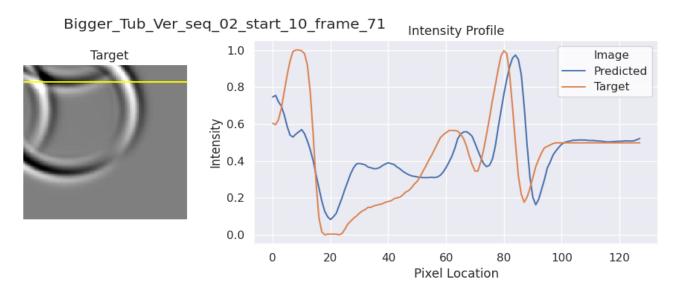




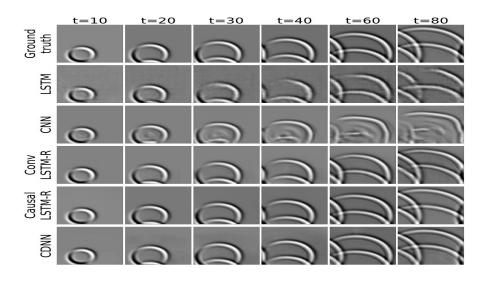










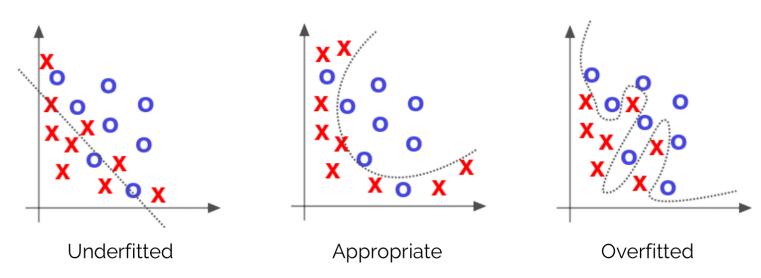


Taken from https://github.com/stathius/wave_propagation



Generalization

Motivation: Key question in deep learning: How well does my NN perform on unseen data?



Taken from Deep Learning by Adam Gibson, Josh Patterson, O'Reily Media Inc., 2017



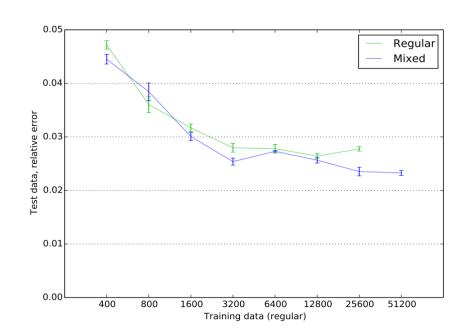
Generalization

Splitted up training data:

- Regular
- Mixed (50% regular, 50% sheared (±15 degrees))

The plot shows training with a 30.9 · 10⁶ parameter model

The high capacity supports training with the mixed dataset, achieving a even lower error

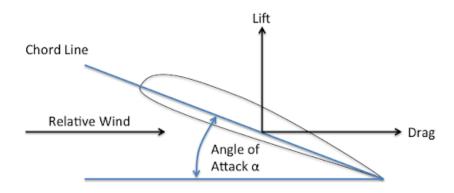


Taken from https://arxiv.org/pdf/1810.08217.pdf



Generalization – Evaluation

Generalization with different angels of attack:

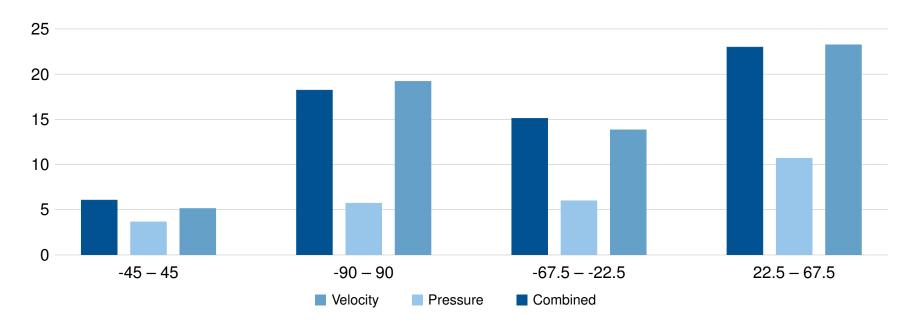


Taken from http://www.aviationchief.com/angle-of-attack.html



Generalization – Evaluation

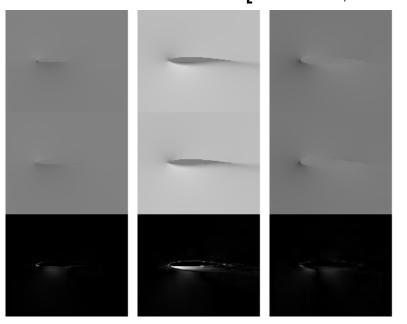
Error increase of different angle of attack intervals as test set wrt. ground truth [-22.5, 22.5]

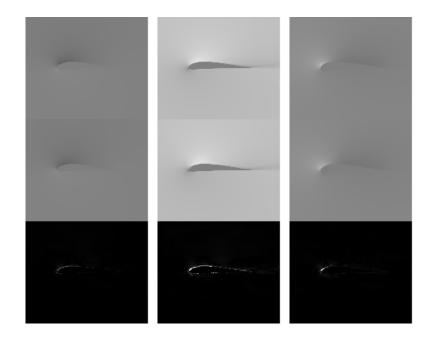






Generalization -[-22.5, 22.5]

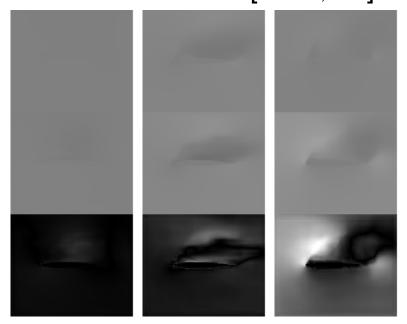


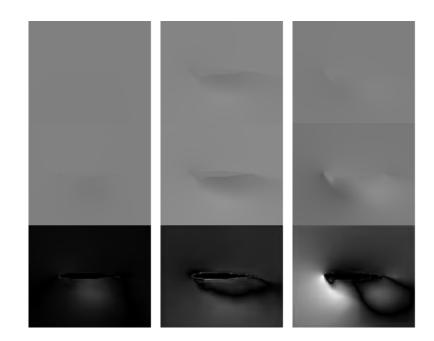






Generalization -[-45, 45]

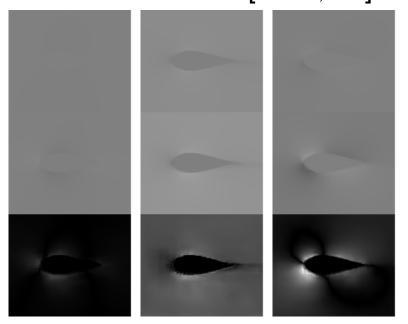


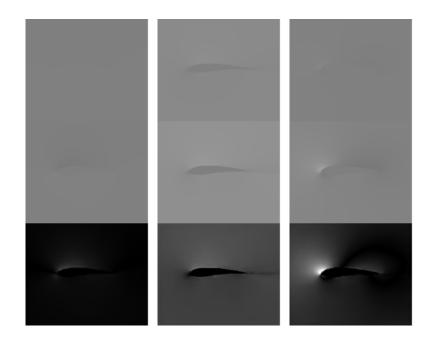






Generalization -[-90, 90]

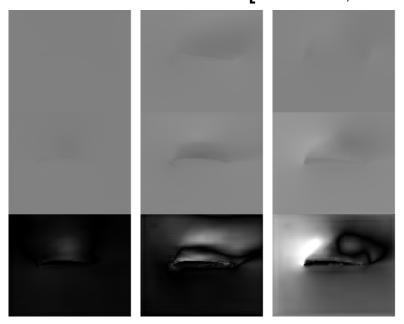


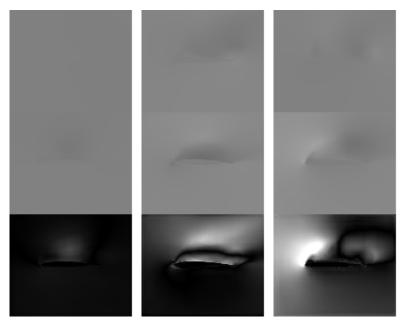






Generalization -[-67.5, -22.5]

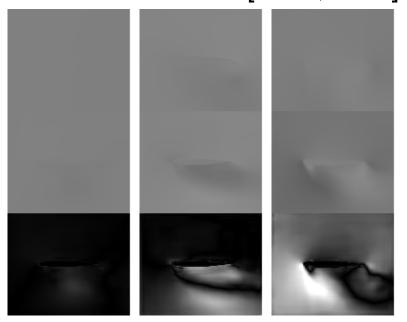


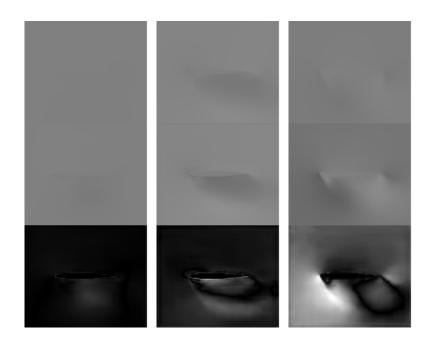






Generalization – [22.5, 67.5]

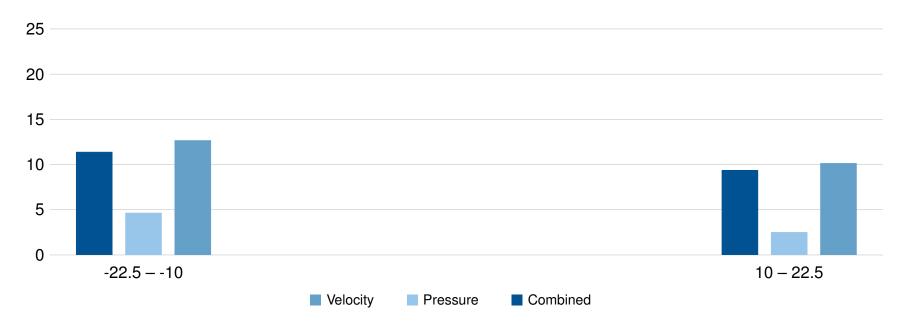






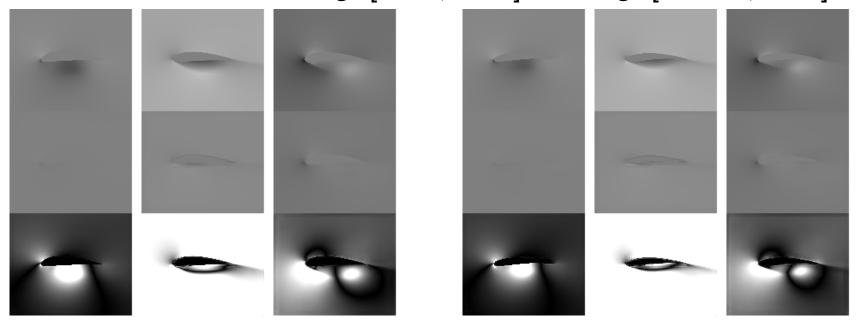
Generalization – Evaluation

Error increase of different angle of attack interpolations (test set) wrt. ground truth [-22.5, 22.5]



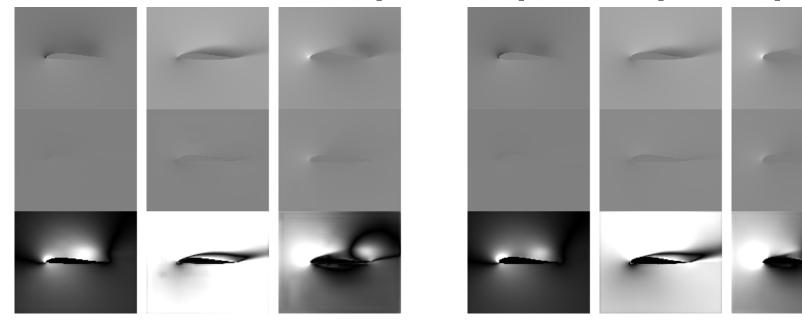


Generalization – training: [-10,22.5], testing: [-22.5,-10]





Generalization – training: [-22.5, 10], testing: [10, 22.5]





Discussion

Positive

- Relative error < 3%
- U-Net's catch regions of interest fast and reliable
- U-Net's can outperform LSTM's
- Capacity
- Inference speed (1000×)
- Accuracy improvements possible

Negative

- Prior knowledge
- Solvers needed (data generation)
- Generalization
- Trade off: training speed grid resolution
- Possible data loss from transformation
- no guarantee for correctness



Summary

Investigate the accuracy of U-Net models for the inference of Reynolds-Averaged Navier-Stokes solutions

Data

- Input (encodes Reynolds number): Bit Mask, x & y velocity
- Target (RANS solution): Pressure, x & y velocity

Pre-Processing

- Make data dimensionless, flatten space of solutions
- Pressure offset removal, numerical precision

Architecture

- U-Net Encoder Bottleneck Decoder structure
- Activations highly depend on task

Transfer

- U-Net as time-series prediction NN for wave propagation
- Input: last *n* frames, Output: next *m* frames, refeed

Generalization

- NN performance on unseen data: Different angels of attack
- underwhelming performance (velocity)

Discussion

- low error (improvable), speed up, even with low capacity
- prior knowledge and solvers needed, poor generalization



Backup slides





Backup slides – Training Setup

Adam optimizer ($\beta_1 = 0.5, \beta_2 = 0.999$)

Learning rate: 0.0004

Learning rate decay: On

Batch size: 10

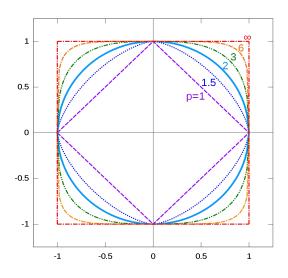
Iterations: 80000

Model parameters:

122.979, 487.107, 1.938.819, 7.736.067, 30.905.859



Backup slides – Norms on unit circle



Taken from: https://de.wikipedia.org/wiki/Norm_(Mathematik)#/media/Datei:Vector-p-Norms_qtl1.svg



Backup slides – Navier-Stokes

Navier-Stokes equation for incompressible flow:

$$\frac{\partial u}{\partial t} + (u \cdot \nabla)u - v\nabla^2 u = -\nabla(\frac{\rho}{\rho_0}) + g$$

- *u*: velocity
- *p*: pressure
- v: kinematic viscosity
- ρ_0 : uniform density
- *g*: gravitational acceleration



Backup slides – Saint-Venant

Saint-Venant equations for incompressible flow (1D):

$$\frac{\partial A}{\partial t} + \frac{\partial (Au)}{\partial x} = 0$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + g \frac{\partial \zeta}{\partial x} = -\frac{P}{A} \frac{\tau}{\rho}$$

- x: coordinate
- *t*: time
- A(x,t): cross-sectional area of the flow at x
- u(x,t): flow velocity
- $\zeta(x,t)$: free surface elevation
- $\tau(x,t)$: wall shear stress along the wetted perimeter P(x,t) of the cross section at x
- ρ: (constant) fluid density
- g: gravitational acceleration



Backup slides – Previous work

Previous work done in the area of physics simulations with deep learning:

- Accelerating Eulerian Fluid Simulation With Convolutional Networks
 - https://arxiv.org/pdf/1607.03597.pdf
- tempoGAN: A Temporally Coherent, Volumetric GAN for Super-resolution Fluid Flow
 - https://arxiv.org/pdf/1801.09710.pdf
- Deep Neural Networks for Data-Driven Turbulence Models
 - https://arxiv.org/pdf/1806.04482.pdf
- Data-driven discretization: a method for systematic coarse graining of partial differential equations
 - https://arxiv.org/pdf/1808.04930v1.pdf
- Hidden Fluid Mechanics: A Navier-Stokes Informed Deep Learning Framework for Assimilating Flow Visualization Data
 - https://arxiv.org/pdf/1808.04327.pdf