

Deep Learning Methods for Reynolds-Averaged Navier-Stokes Simulations of Airfoil Flows

Julian Hohenadel Technical University of Munich Chair of Computer Graphics and Visualization Munich, 11. May 2020





What this paper is about

Deep learning approach to infer Reynolds Averaged Navier-Stokes solutions for airfoil shapes

Fully convolutional U-Net architecture derivative in a fully supervised training environment

Classification of performance on inferring pressure and velocity fields

Generalization ability to parameter changes in the training data

Evaluation of different NN models regarding:

- network capacity
- training data size



Motivation

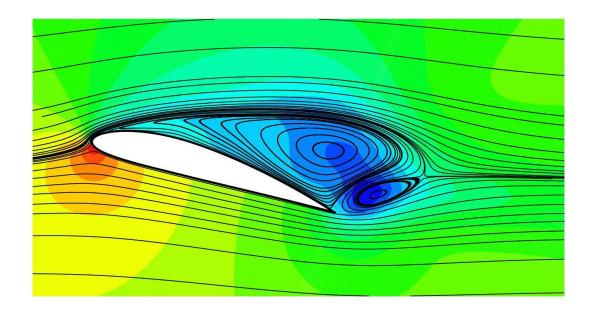
Why use deep learning for RANS systems:

- Similar highly nonlinear behaviour
- PDE systems are complex and hard to calculate
- RANS averages over the time component
 - \implies 1 frame as output
- Training data generatable
- CNN's yield good image feature extraction
- Success in computer vision
- Success in physics simulation





Background – RANS



Taken from https://www.pinterest.ch/pin/615163630322034457/



Background – RANS

Nonlinear partial differential equation (PDE) system based on Navier-Stokes equations

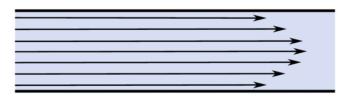
Used for the modeling of turbulent incompressible flows

Averages over time component

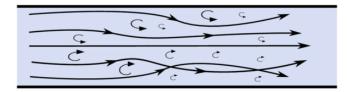
Reynolds number *Re*:

- dimensionless constant
- needed for calculation of turbulence models
- magnitude decides flow (laminar, turbulent)
- affects lift and drag coeffcients

laminar flow



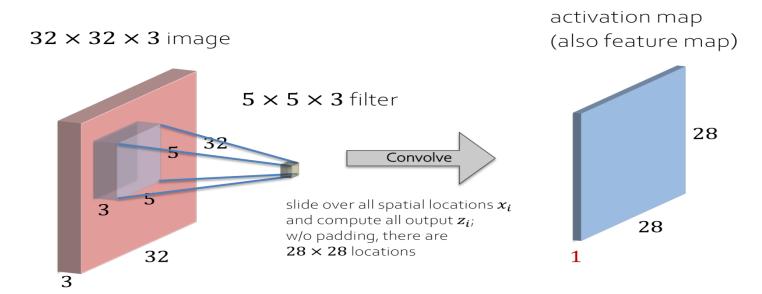
turbulent flow



Taken from https://diffzi.com/laminar-flow-vs-turbulent-flow/



Background – Convolutions

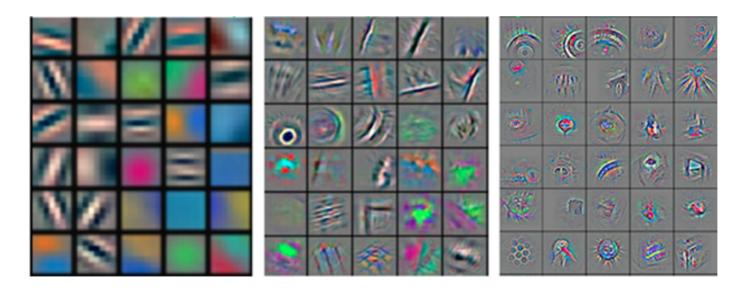


Taken from I2DL WS19/20 (TUM)



Background – Convolutions

Low-Level Features, Mid-Level Features, High-Level Features: each filter captures different characteristics



Taken from https://arxiv.org/pdf/1311.2901.pdf





Data Generation

Airfoil shapes are provided by the UIUC database

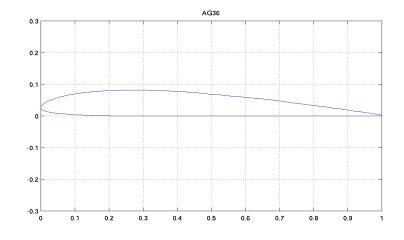
Reynolds number: [0.5,5] · 10⁶ (highly turbulent)

Angle of attack: [-22.5, 22.5]

Ground truth generated with OpenFOAM (pressure, x velocity, y velocity)

Training data resolution: $3 \times 128 \times 128$

(Inference region $128 \times 128 < \text{full simulation domain}$)



Taken from https://m-selig.ae.illinois.edu/ads/afplots/ag35.gif



Pre-processing – Data

Input channels	Target channels
Bit mask representing airfoil shape	Pressure field
2. x velocity component	2. x velocity field
3. y velocity component	3. y velocity field
Reynolds number encoded as differently scaled freestream velocity vectors wrt. their magnitude	Data from the RANS solution



Pre-processing – Normalization

Motivation: Flatten space of solutions, accelerate learning by simplifing the learning task for the NN

Normalization of target channels by division with freestream magnitude (vector norm, default: L2): This makes pressure and velocity dimensionless

$$ilde{v_o} = rac{v_o}{\|v_i\|}, \quad ilde{p_o} = rac{p_o}{\|v_i\|^2}$$
 – important to remove quadratic scaling of pressure

For a better understanding:

Pressure: $[p]_{Sl} = 1Pa = 1\frac{kg}{m \cdot s^2}$

Density: $[\rho]_{SI} = 1 \frac{kg}{m^3}$ – constant in incompressible flow

Velocity: $[v]_{SI} = \frac{m}{s}$



Pre-processing – Offset removal & value clamping

Motivation: eliminate ill-posed learning goal & improve numerical precision

Spatially move pressure distribution into the origin – RANS typically only needs ∇_{p} for computation

$$\hat{p_o} = \tilde{p_o} - p_{mean}$$

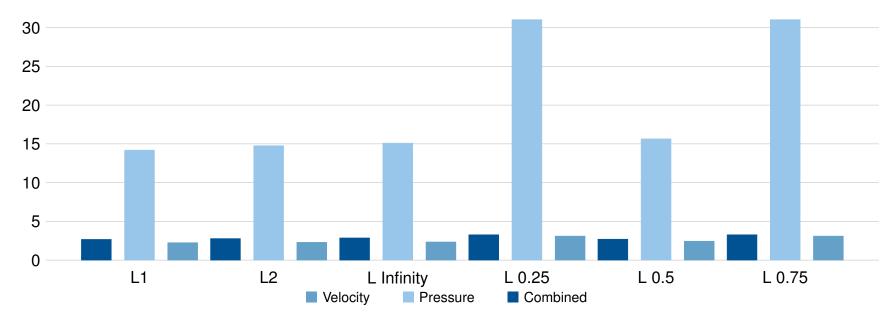
Clamp both input and target channels into [-1,1] range by diving by the maximum absolute value



Pre-processing – Evaluation

Vector norms used in pre-processing comparision wrt. error, default: L2 (in %)

L1 normalization achieves the best error rates (p, vel, combined: **14.19**%, **2.251**%, **2.646**% – L2: 14.76%, 2.291%, 2.780%)

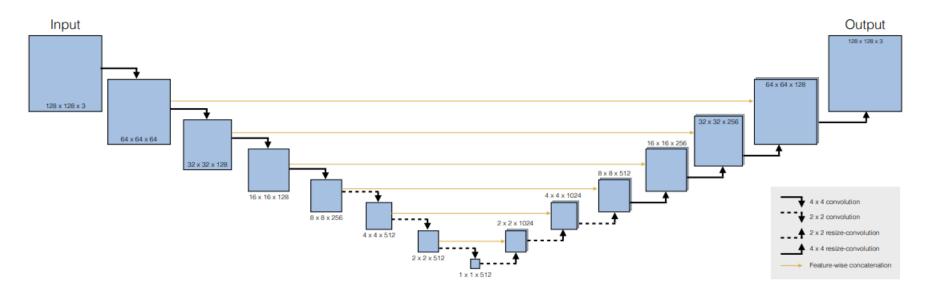






Architecture

U-Net derivative proposed in the paper:



Taken from https://arxiv.org/pdf/1810.08217.pdf



Architecture – Convolutional blocks

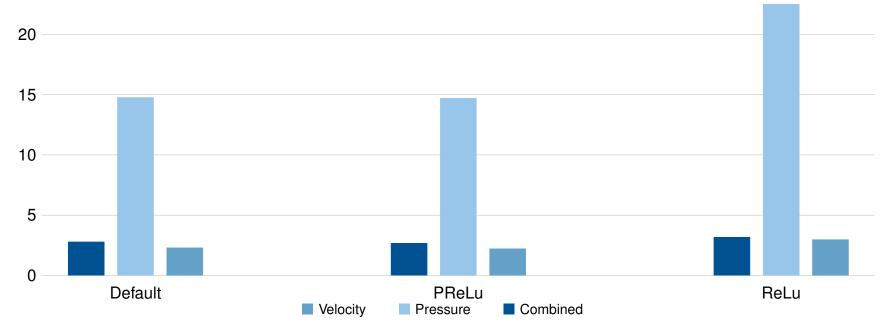
Encoder	Decoder
1. Activation – Leaky ReLu (0.2)	1. Activation – ReLu
2. Convolution – Width down, Depth up	2. Upsampling – linear (2.0)
3. Batch normalization	3. Convolution – Width up, Depth down
4. Dropout (1%)	4. Batch normalization
	5. Dropout (1%)



Architecture – Evaluation

Error percentage of different activation functions after 160k iterations (266 epochs).

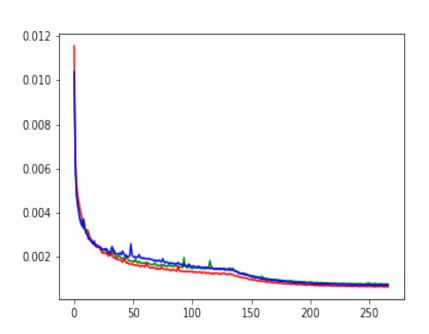
PReLu achieves the best error rates (p, vel, combined: **14.69**%, **2.216**%, **2.676**% – Default: 14.76%, 2.296%, 2.787%)



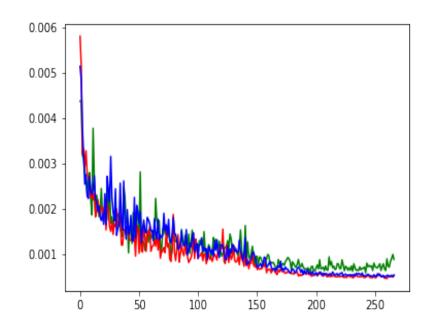


Architecture – Evaluation

Training loss



Validation loss





Transfer

Motivation: Can the network architecture adapt to other PDE systems and how well will it perform?

Another use case for PDE systems like RANS is predicting wave propagation on shallow water

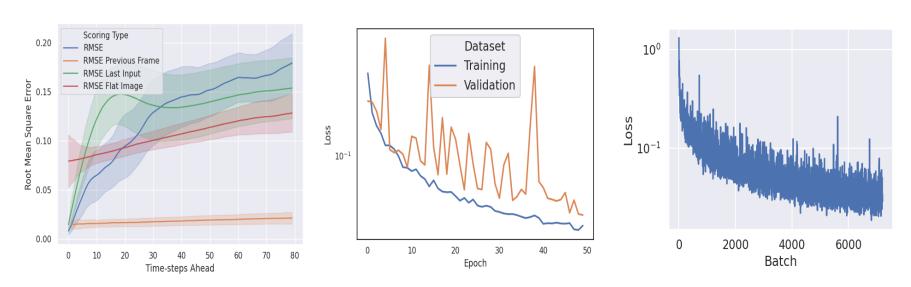
Wave propagation, in this case, is governed by the Saint-Venant equations (related with Navier-Stokes equations)

U-Net architecture changes:

- Input channels contain the last *n* time steps
- Output channels predict the next *m* time steps
- Output is refeeded as input to predict time series

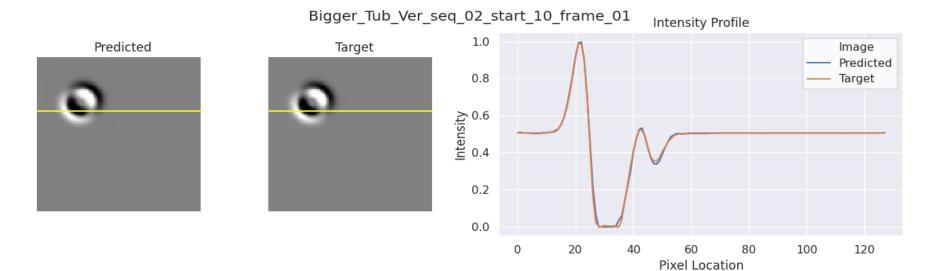


RMSE with variance, validation loss and batch loss on Bigger Tub environment:

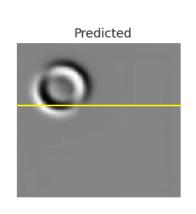


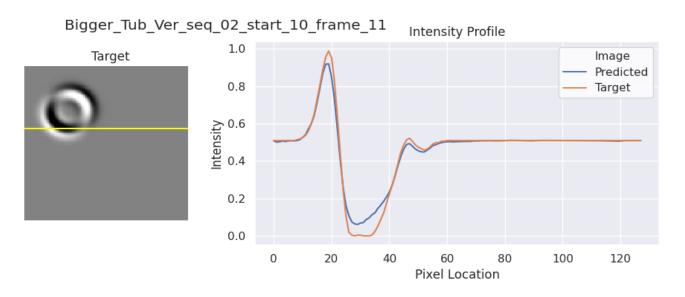
All plots and training in Transfer were made with https://github.com/stathius/wave_propagation



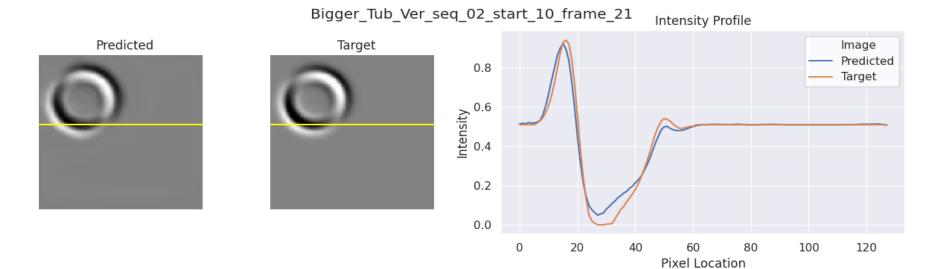




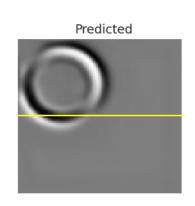


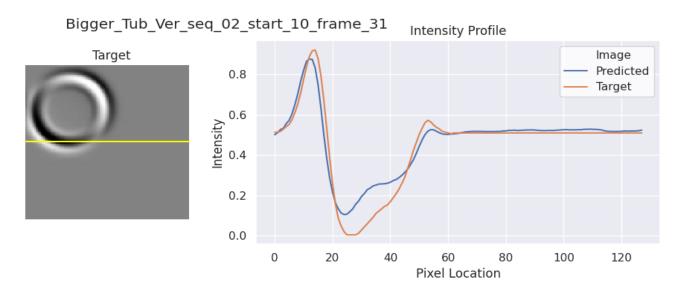




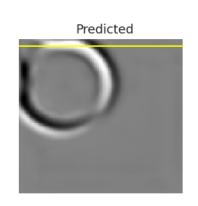


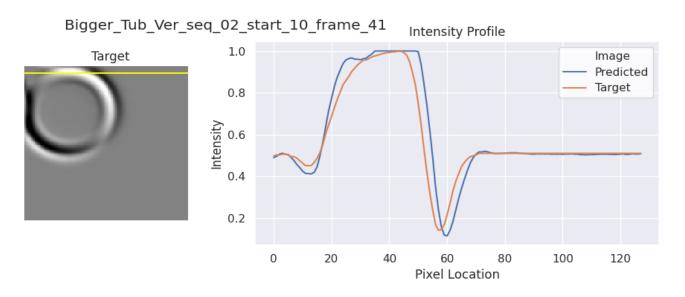




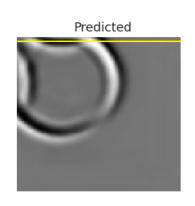


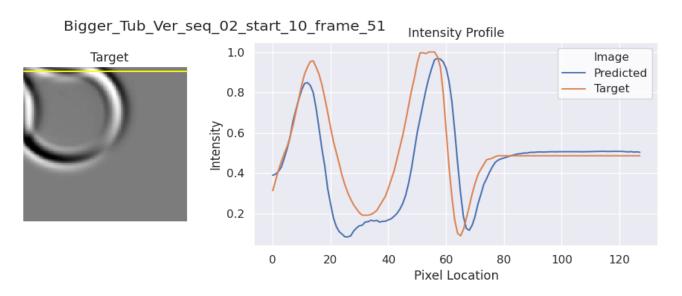




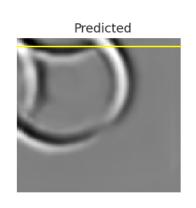


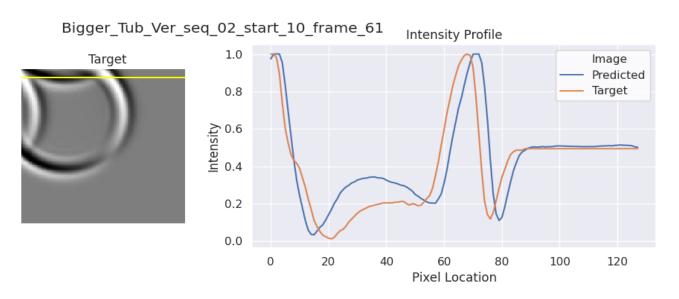




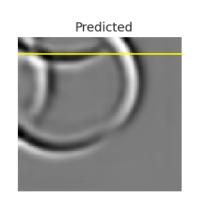


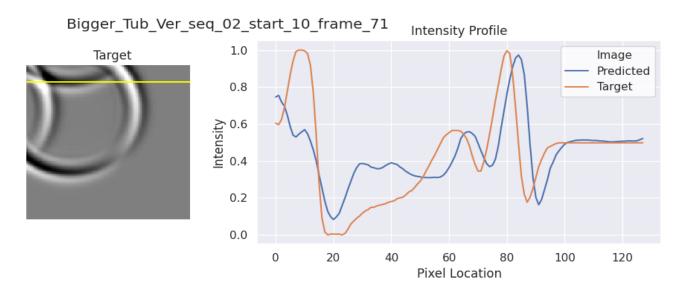








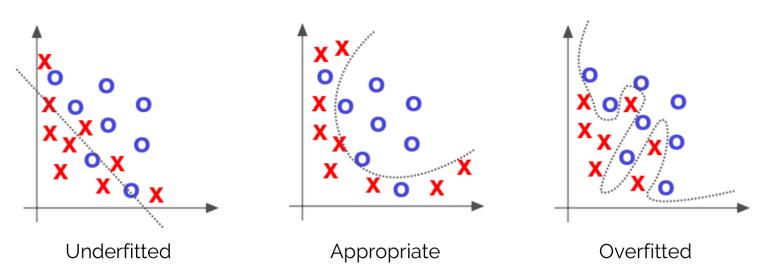






Generalization

Motivation: Key question in deep learning: How well does my NN perform on unseen data?



Taken from Deep Learning by Adam Gibson, Josh Patterson, O'Reily Media Inc., 2017



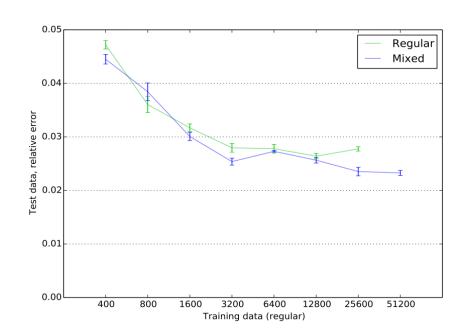
Generalization

Splitted up training data:

- Regular
- Mixed (50% regular, 50% sheared (±15 degrees))

The plot shows training with a 30.9 · 10⁶ parameter model

The high capacity supports training with the mixed dataset, achieving a even lower error



Taken from https://arxiv.org/pdf/1810.08217.pdf



Generalization – Evaluation

To test generalization new datasets need to be created

Generation of 1 training sample: \approx 70 seconds (using Google Colab)

Generation of 12.8*k* training samples: > 10 days – not feasible

⇒ Generate only new test sets containing 90 samples: < 2 hours – feasible

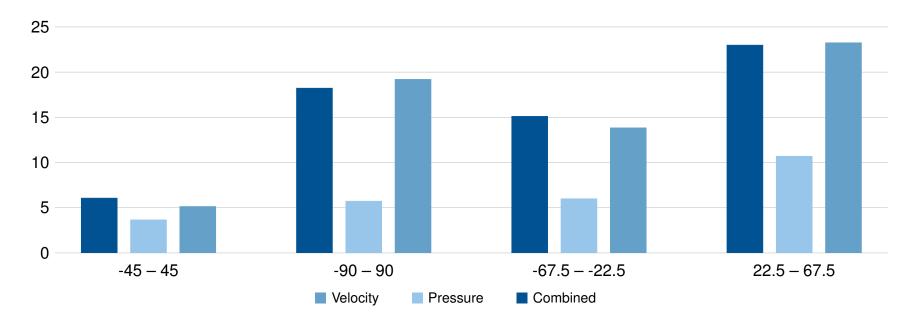
Extrapolation with different angle of attack intervals, default: [-22.5,22.5]:

- **•** [−45,45]
- **•** [−90,90]
- [-67.5, -22.5]
- [22.5,67.5]



Generalization – Evaluation

Error increase of different angle of attack intervals wrt. ground truth [-22.5, 22.5]





Discussion

Positiv

- Relative error < 3%
- Convolutions paired with an encoder decoder structure seem to catch regions of interest fast and reliable
- U-Nets can outperform LSTM's in accuracy as well as in speed with a fraction of capacity (in time-series problems)
- accuracy does not suffer too much from models with a lot less capacity mostly affects sharpness of solutions
- Inference speed is $1000 \times$ when compared with OpenFOAM solver
- Accuracy improvements still possible (bigger models, more training data)



Discussion

Negativ

- Proir knowledge needed for proper pre-processing
- Solvers needed for dataset generation
- Extrapolation yields mediocre results
- Fresh Training needed for other shapes (e.g. cars in wind tunnel)
 - transfer learning unlikely
- Trade off: training speed grid resolution
- Possible data loss from transformation:
 adaptive grid (solver) => cartesian grid (NN)
- no guarantee for correctness
- Accuracy improvements computationally expensive likely requires tailored architectures and loss functions



Summary

Investigate the accuracy of U-Net models for the inference of Reynolds-Averaged Navier-Stokes solutions

Data Generation $6 \times 128 \times 128$

- Input (encodes Reynolds number): Bit Mask, x & y velocity
- Target (RANS solution): Pressure, x & y velocity

Pre-Processing

- Make data dimensionless, flatten space of solutions
- Pressure offset removal, numerical precision

Architecture

- U-Net Encoder Bottleneck Decoder structure
- Activations highly depend on current task

Transfer

- U-Net as time-series prediction NN for wave propagation
- Input: last *n* frames, Output: next *m* frames, refeed

Generalization

- NN performance on unseen data: Different angels of attack
- mediocre performance on wider intervals (velocity)

Discussion

- low error (improvable), speed up, even with low capacity
- prior knowledge and solvers needed, poor extrapolation



Backup slides



Backup slides – Training Setup

Adam optimizer ($\beta_1 = 0.5, \beta_2 = 0.999$)

Learning rate: 0.0004

Learning rate decay: On

Batch size: 10

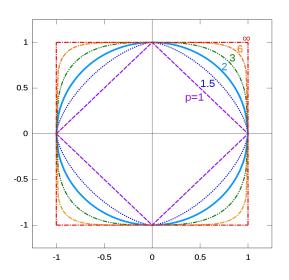
Iterations: 80000

Model parameters:

122.979, 487.107, 1.938.819, 7.736.067, 30.905.859



Backup slides – Norms on unit circle



Taken from: https://de.wikipedia.org/wiki/Norm_(Mathematik)#/media/Datei:Vector-p-Norms_qtl1.svg