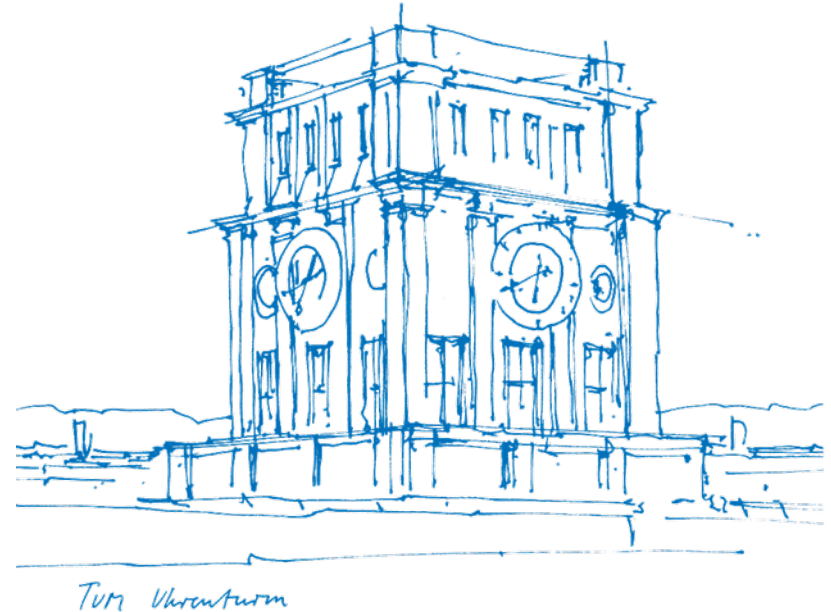


# Deep Learning Methods for Reynolds-Averaged Navier-Stokes Simulations of Airfoil Flows

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Chair of Computer Graphics and Visualization  
Munich, 11. May 2020



# Introduction

TODO

# Background – RANS

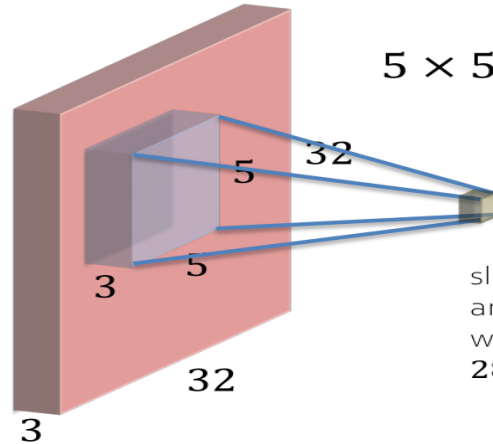
TODO

# Background – RANS

TODO

# Background – Convolutions

$32 \times 32 \times 3$  image

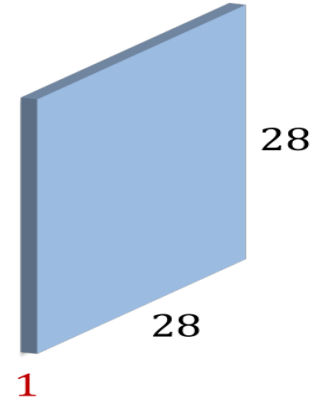


$5 \times 5 \times 3$  filter



slide over all spatial locations  $x_i$   
and compute all output  $z_i$   
w/o padding, there are  
 $28 \times 28$  locations

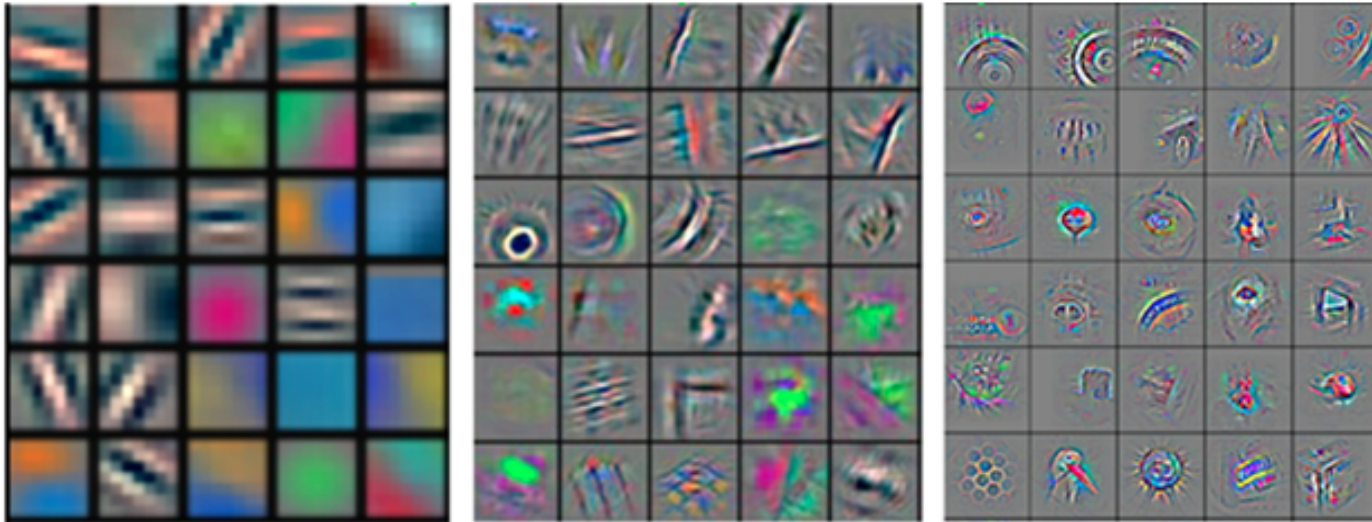
activation map  
(also feature map)



Taken from I2DL WS19/20 (TUM)

# Background – Convolutions

Low-Level Features, Mid-Level Features, High-Level Features: each filter captures different characteristics



Taken from <https://arxiv.org/pdf/1311.2901.pdf>

# Data Generation

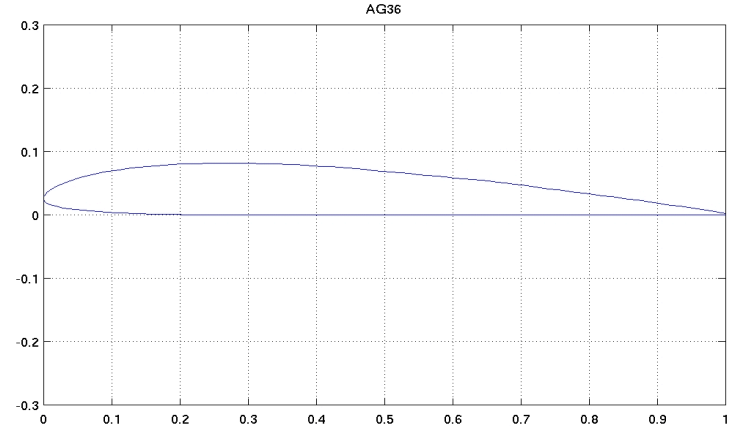
Airfoil shapes are provided by the UIUC database

Reynolds number:  $[0.5, 5] \cdot 10^6$  (highly turbulent)

Angle of attack:  $[-22.5, 22.5]$

Ground truth generated with OpenFOAM  
(pressure, x velocity, y velocity)

Training data resolution:  $3 \times 128 \times 128$



# Pre-processing – Data

## Input channels

1. Bit mask representing airfoil shape
2. x velocity component
3. y velocity component

Reynolds number encoded as differently scaled  
freestream velocity vectors wrt. their magnitude

## Target channels

1. Pressure field
2. x velocity field
3. y velocity field

Data from the RANS solution



# Pre-processing – Normalization

Motivation: Flatten space of solutions, accelerate learning by simplifying the learning task for the NN

Normalization of target channels by division with freestream magnitude (vector norm, default: L2):

This makes pressure and velocity dimensionless

$$\tilde{v}_o = \frac{v_o}{\|v_i\|}, \quad \tilde{p}_o = \frac{p_o}{\|v_i\|^2} - \text{important to remove quadratic scaling of pressure}$$

For a better understanding:

$$\text{Pressure: } [p]_{SI} = 1 \text{ Pa} = 1 \frac{\text{kg}}{\text{m} \cdot \text{s}^2}$$

$$\text{Density: } [\rho]_{SI} = 1 \frac{\text{kg}}{\text{m}^3} - \text{constant in incompressible flow}$$

$$\text{Velocity: } [v]_{SI} = \frac{\text{m}}{\text{s}}$$

# Pre-processing – Offset removal & value clamping

Motivation: eliminate ill-posed learning goal & improve numerical precision

Spatially move pressure distribution into the origin

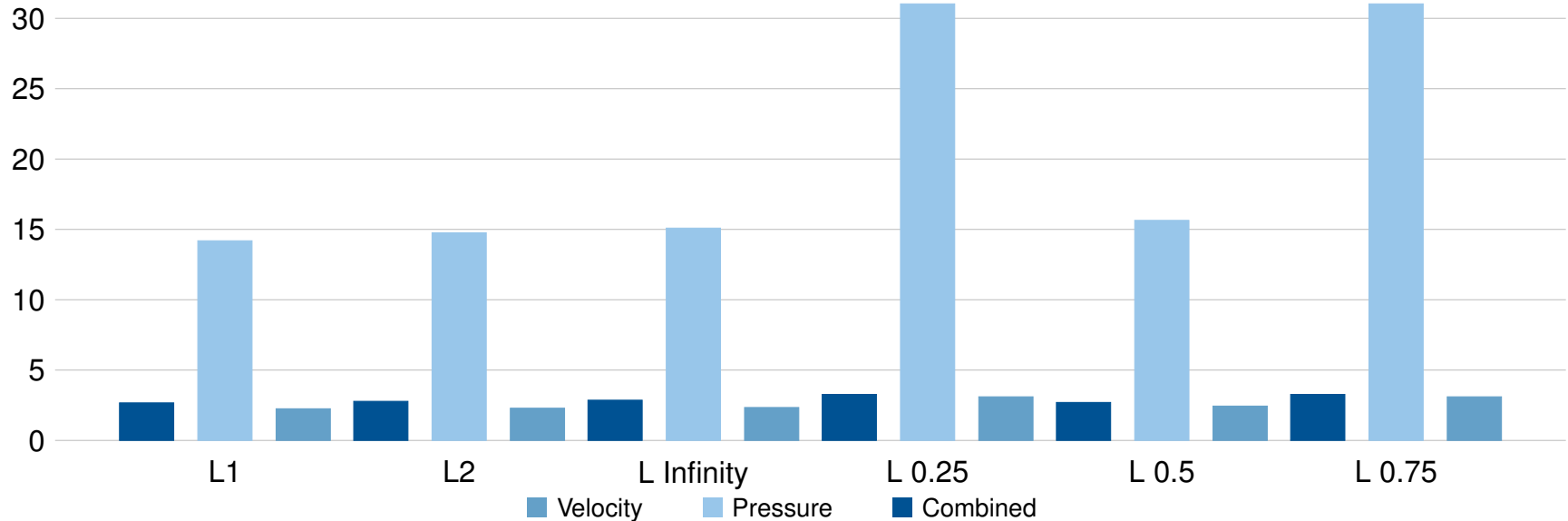
$$\hat{p}_o = \tilde{p}_o - p_{mean}$$

Clamp both input and target channels into  $[-1, 1]$  range by dividing by the maximum absolute value

# Pre-processing – Evaluation

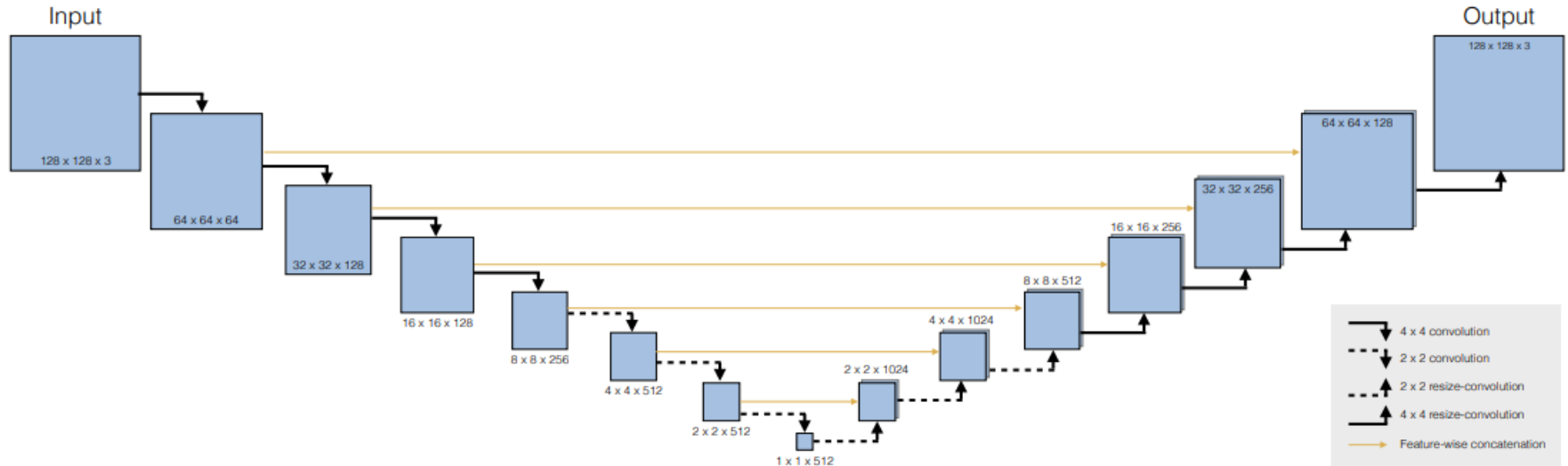
Vector norms used in pre-processing comparison wrt. error, default: L2 (in %)

L1 normalization achieves the best error rates (p, vel, combined: **14.19%**, **2.251%**, **2.646%** – L2: 14.76%, 2.291%, 2.780%)



# Architecture

U-Net derivative proposed in the paper:



Taken from <https://arxiv.org/pdf/1810.08217.pdf>

# Architecture – Convolutional blocks

## Encoder

1. Activation – Leaky ReLu (0.2)
2. Convolution – Width down, Depth up
3. Batch normalization
4. Dropout (1%)

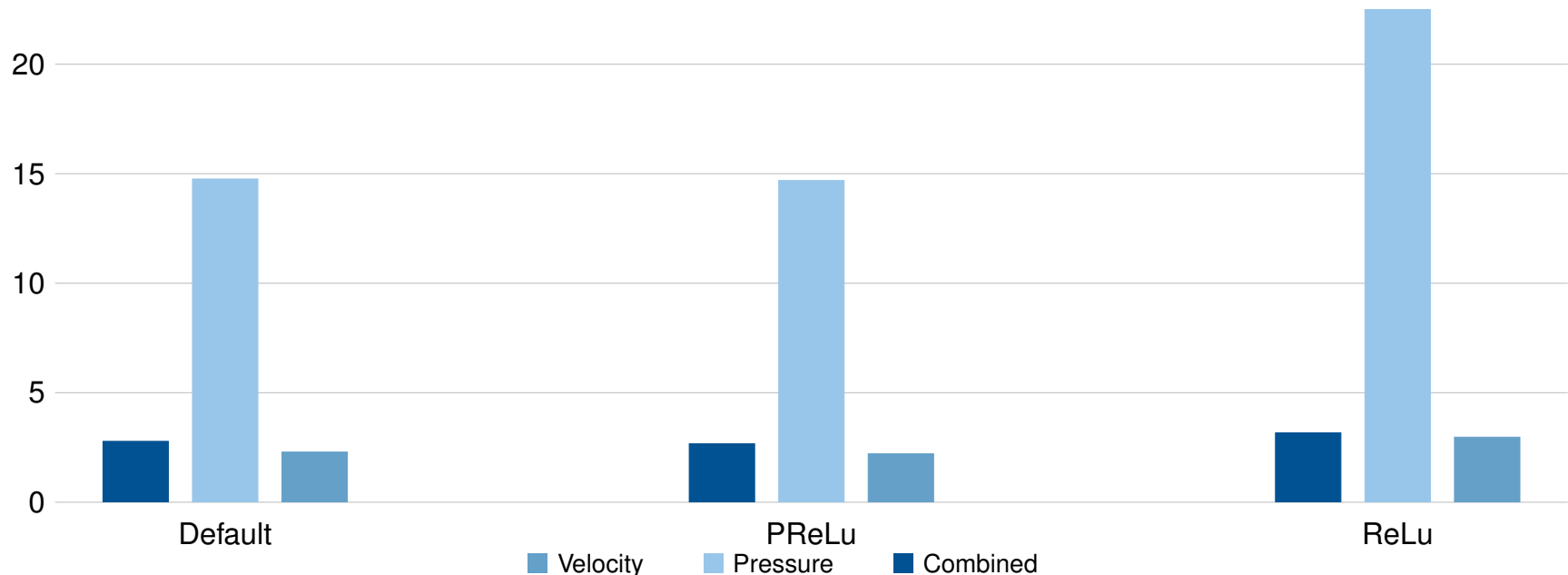
## Decoder

1. Activation – ReLu
2. Upsampling – linear (2.0)
3. Convolution – Width up, Depth down
4. Batch normalization
5. Dropout (1%)

# Architecture – Evaluation

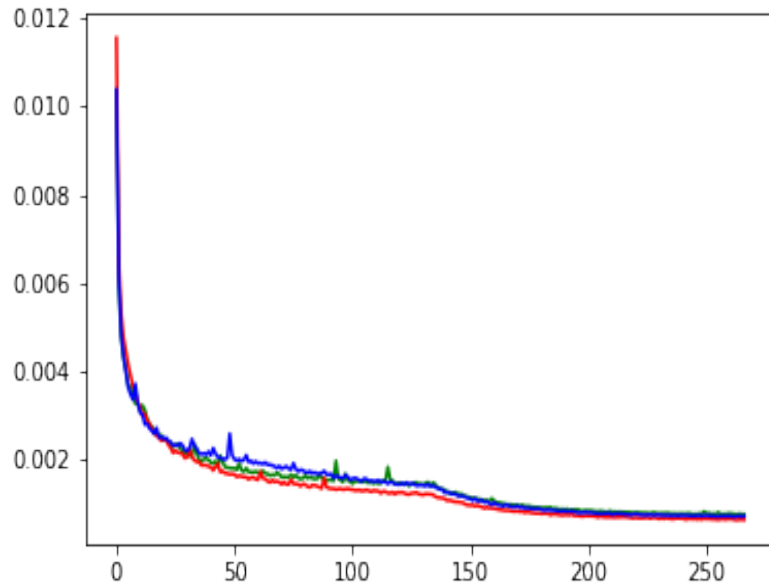
Error percentage of different activation functions after 160k iterations (266 epochs).

PReLU achieves the best error rates (p, vel, combined: **14.69%**, **2.216%**, **2.676%** – Default: 14.76%, 2.296%, 2.787%)

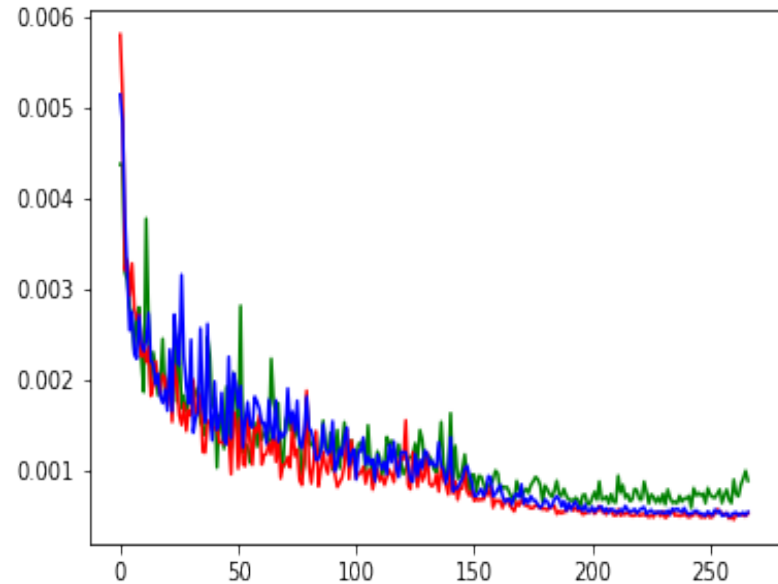


# Architecture – Evaluation

Training loss



Validation loss



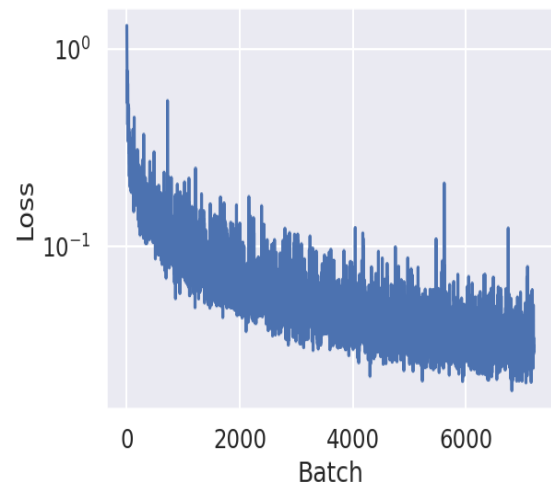
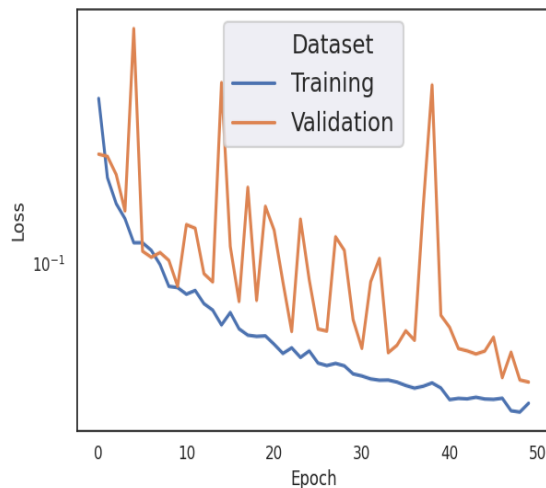
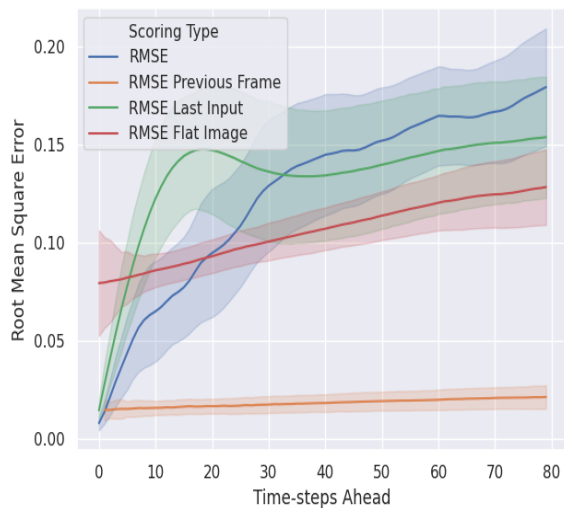
# Transfer

TODO



# Transfer

RMSE with variance, validation loss and batch loss on Bigger Tub environment:

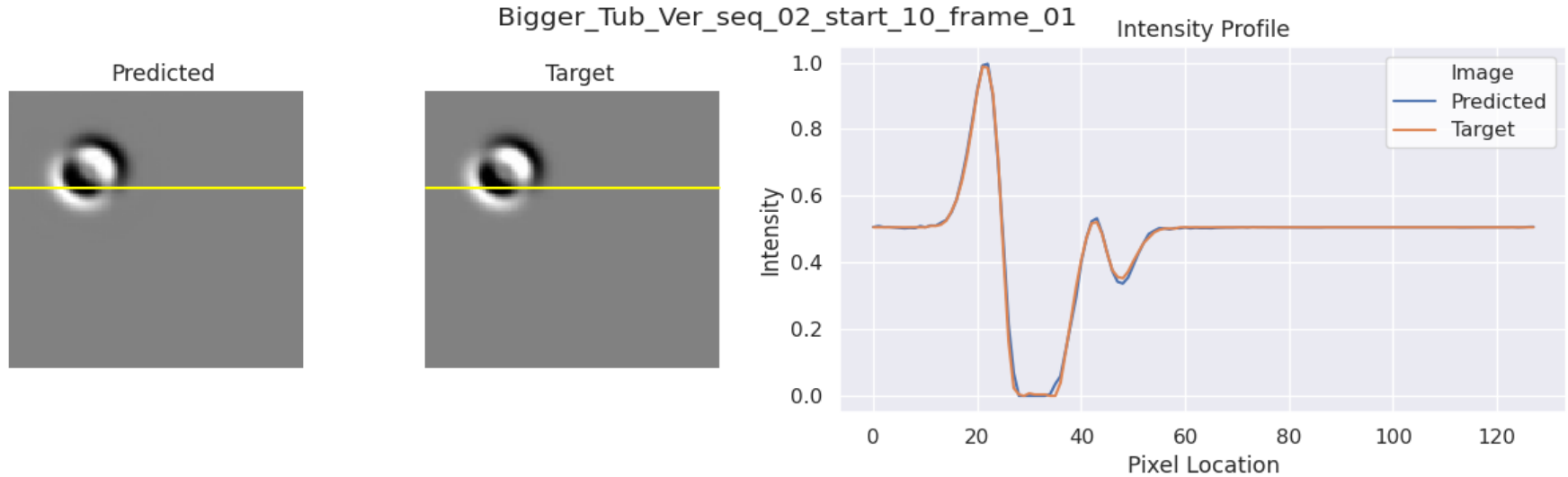


All plots in Transfer were made with [https://github.com/stathius/wave\\_propagation](https://github.com/stathius/wave_propagation)

# Transfer

Wave propagation prediction

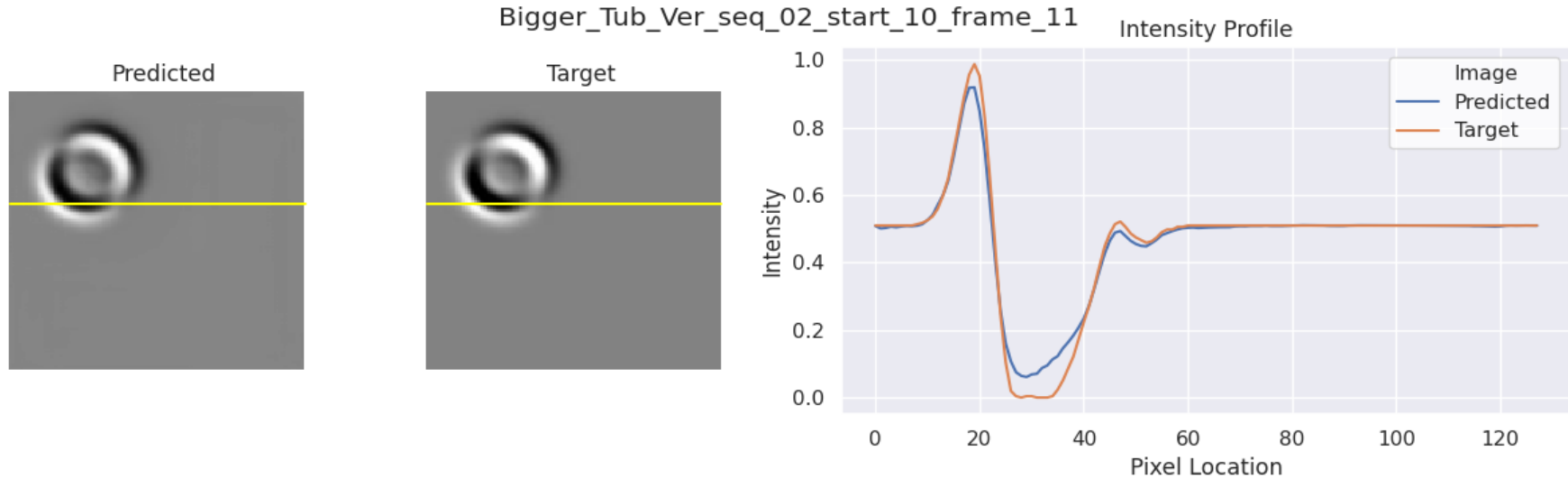
Intensity profile on scanline – Frame 1



# Transfer

Wave propagation prediction

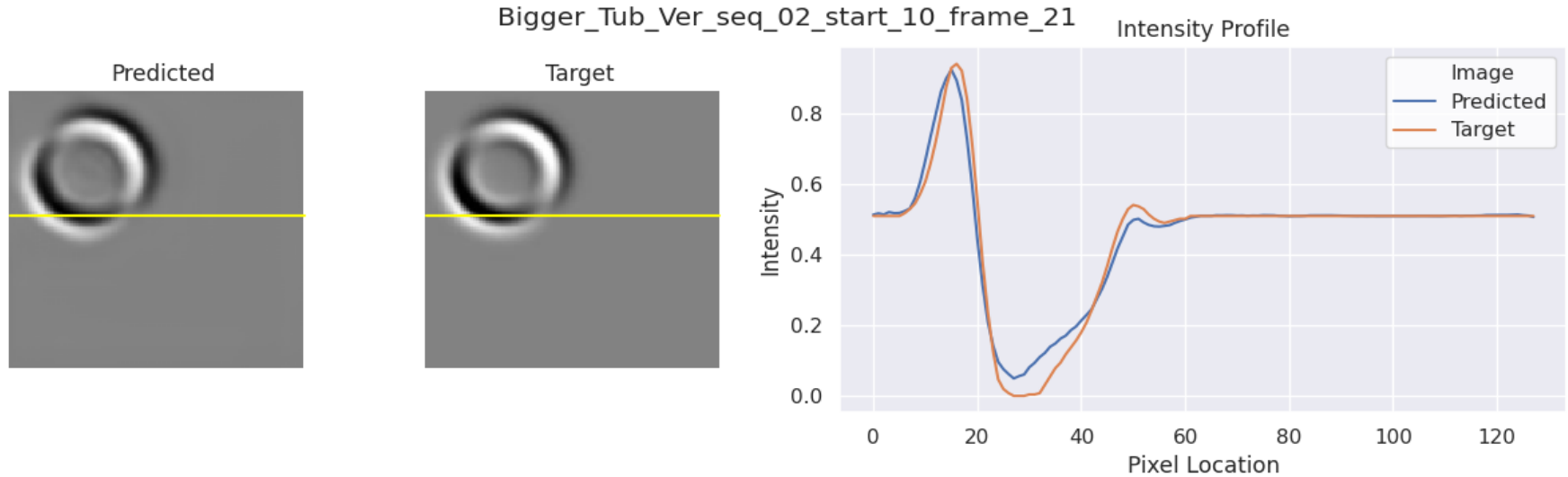
Intensity profile on scanline – Frame 11



# Transfer

Wave propagation prediction

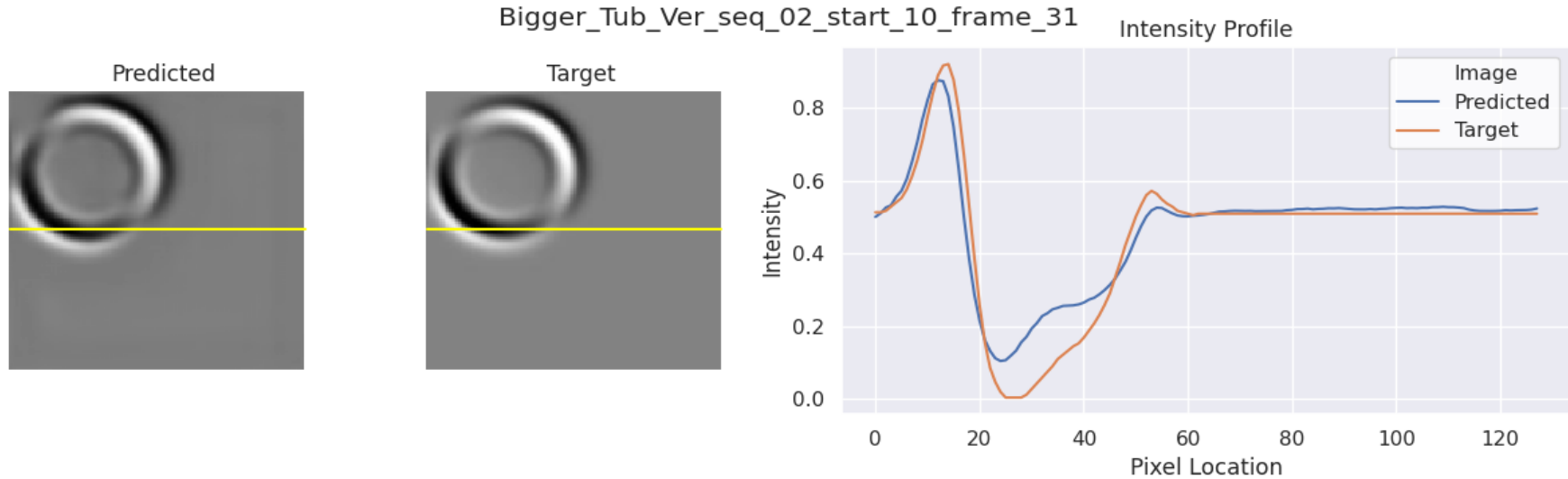
Intensity profile on scanline – Frame 21



# Transfer

Wave propagation prediction

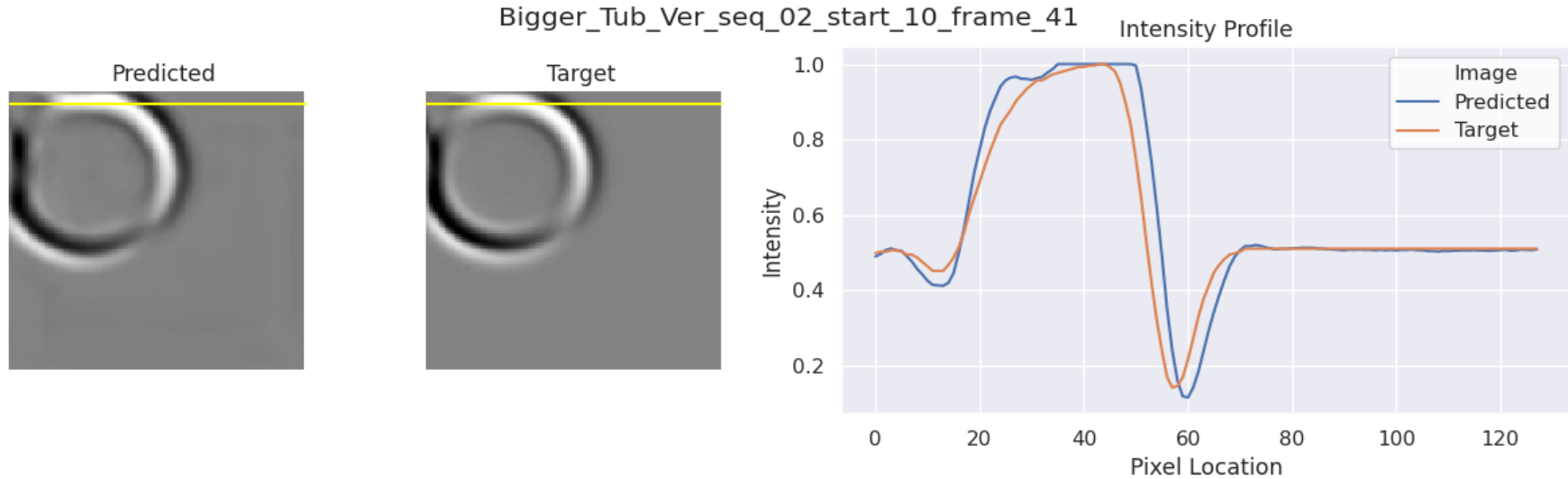
Intensity profile on scanline – Frame 31



# Transfer

Wave propagation prediction

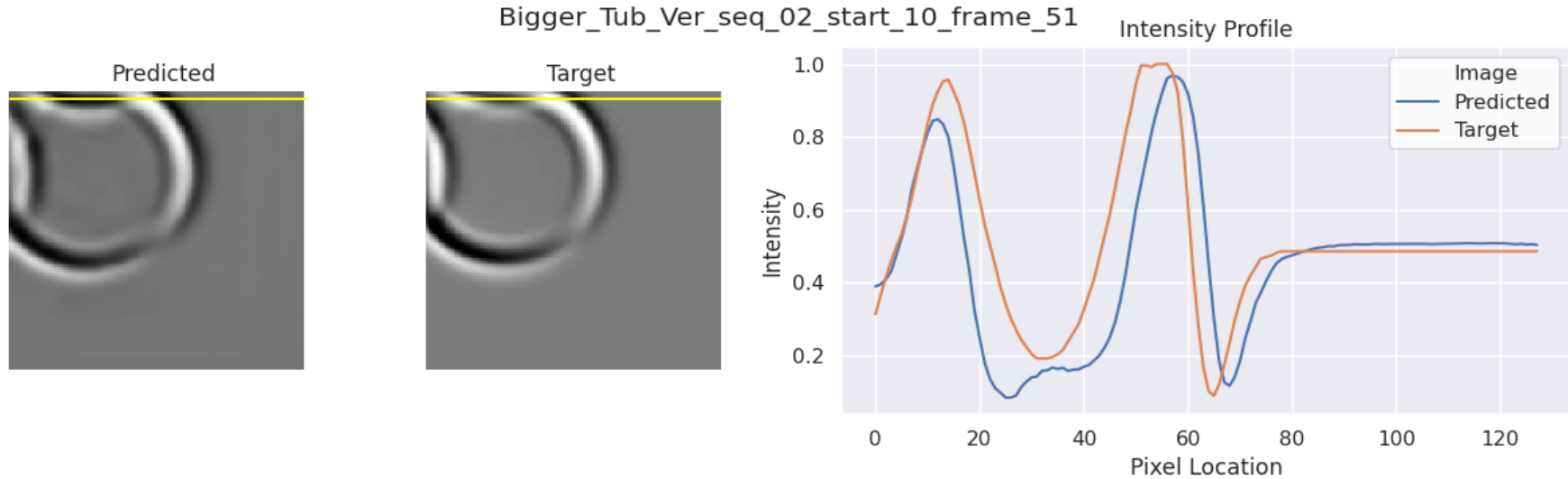
Intensity profile on scanline – Frame 41



# Transfer

Wave propagation prediction

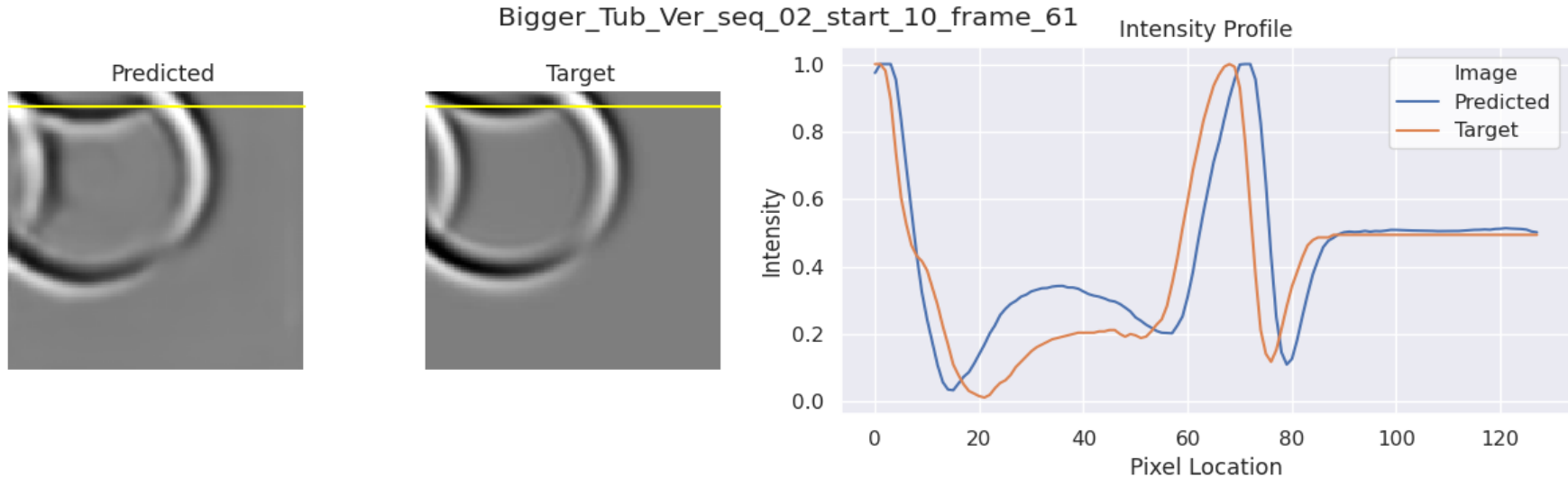
Intensity profile on scanline – Frame 51



# Transfer

Wave propagation prediction

Intensity profile on scanline – Frame 61

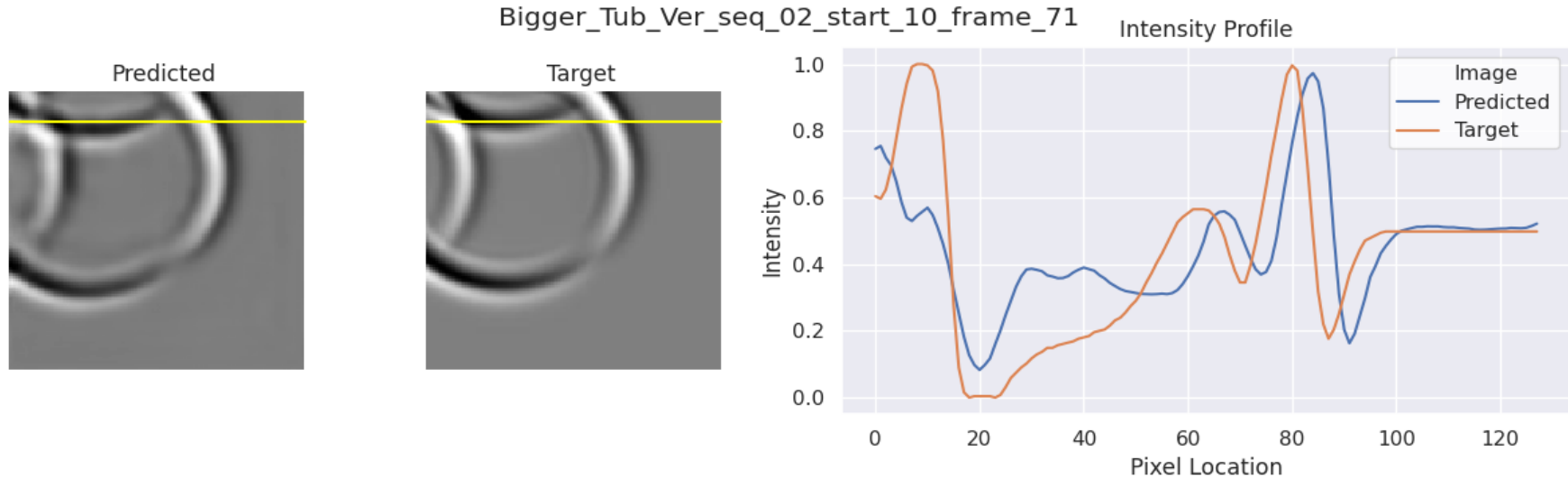




# Transfer

Wave propagation prediction

Intensity profile on scanline – Frame 71

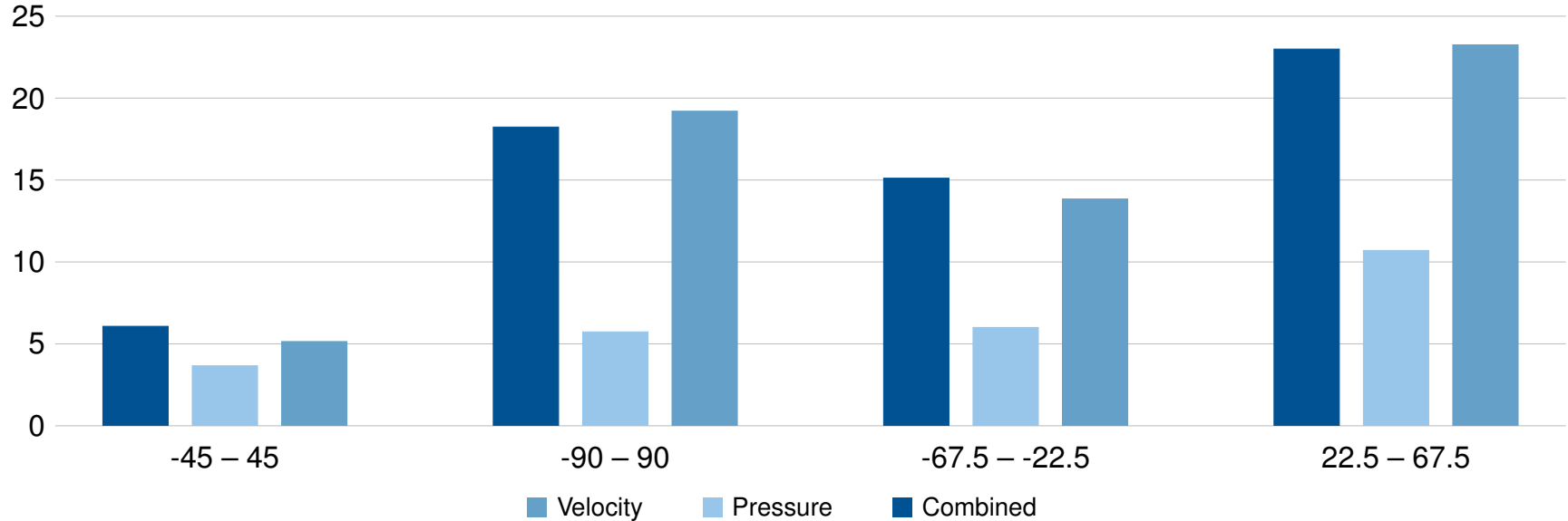


# Generalization

TODO

# Generalization

Error percentage of different angle of attack intervals wrt. ground truth  $[-22.5, 22.5]$



# Discussion

TODO

# Discussion

## Positiv

Punkt 1

Punkt 2

Punkt 3

Punkt 4

## Negativ

Punkt 1

Punkt 2

Punkt 3

Punkt 4

# Summary

TODO

# Backup slides

TODO