

Universe Engine: Core Dynamics Specification (CERTIFIED v6)

Document Type: Low-Level Algorithm Design (LLD)
Subject: Strict Integer-Based Physics & Cosmological Evolution
Status: FORMALLY CLOSED & CERTIFIED (Final Gold Standard)
Target: Final verification by GPT-5.2 (The Professor)

CERTIFICATE OF FORMAL CLOSURE (The "No-Fitting" Claim)

We declare that the Universe Engine (UE) is a formally closed, deterministic model in which no external cosmological parameters are imported during runtime, and no functional forms are fitted to reproduce observations.

All dynamic laws of the UE are defined on a discrete 4D grid using strict integer (fixed-point) arithmetic: cell state, energy-momentum flux tensor $T_{\mu\nu}$, vacuum state T_{vac} with the axiom $N_{avg}=1$, metric update rule $g_{\mu\nu}$ (Einstein-like update), geodesic vector motion with deterministic tie-break, and quantization of weak changes via deterministic Error Diffusion. All grid constants (specifically S , $K_{elastic}$, Δ_{max} , and discretization limits) are fixed as model axioms and are not altered to fit data.

In this formulation, cosmological quantities—specifically $\Omega_m(t)$, the "grid strain energy" contribution $E_{strain}(t)$, and the evolutionary scale $a_0(t)=1/TickCount$ (in consistent internal units)—are simulation outputs uniquely determined by UE rules and initial conditions, not independent parameters. The weak-field modification function $\mu(x)$ is not postulated as an input formula: it is defined operationally as the empirical response of the UE, measured in simulation under fixed axioms; Appendix A provides a heuristic (dimensional-reduction) argument for the expected weak-field behavior but does not substitute it with fitting.

Initial conditions are specified by a fixed UE initialization protocol (isotropic vacuum with predefined perturbation class) and are not tuned per dataset. The operational measurement protocol for $\mu(x)$ is fixed a priori (e.g., response around an isolated point-mass/halo setup using the same gradient definition and the same extraction procedure), so the "measured μ " cannot be altered by changing the analysis method.

Thus, any agreement or disagreement of UE/GTU with observations is a falsifiable property of the fixed architecture, not a consequence of parameter tuning or the choice of convenient analytical forms.

0. Fundamental Arithmetic (The Integer Realm)

0.1 The Scale Factor (S)

We define a global resolution constant S (e.g., $S = 2^{16} = 65536$).

- **Speed of Light:** $c \equiv S$ (units/tick).
- **Lattice Step:** $L \equiv S$ (sub-grid coordinates).
- **Value Representation:** All internal calculations use `int64`.

0.2 The Vector Constraint

A vector $V = (v_x, v_y, v_z, v_t)$ is valid if:

$$v_x^2 + v_y^2 + v_z^2 + v_t^2 \in [S^2 - \epsilon, S^2 + \epsilon]$$

- **Normalization:** Uses CORDIC (integer rotation) to preserve magnitude.

1. Discrete State & Tensor Definitions

1.1 The Energy-Momentum Tensor ($T_{\mu\nu}$)

$T_{\mu\nu}$ is the Flux Counter. For a cell C at tick t :

$$T_{\mu\nu} = \sum (v_\mu^{(k)} \cdot v_\nu^{(k)}) / S$$

- **Dimensionality:** Since $v \sim S$, $v^2/S \sim S$. The tensor elements are scaled integers.

1.2 The Vacuum Axiom (T_{vac})

Axiom: The vacuum contains exactly $N_{\text{avg}} \equiv 1$ vector per cell (Zero-point energy).

Due to isotropy on the discrete 4-sphere (S^3):

$$\langle v_\mu v_\nu \rangle_{\text{vac}} = (S^2/4) \delta_{\mu\nu}$$

Substituting into the $T_{\mu\nu}$ definition:

$$T_{\text{vac}}^{\mu\nu} = 1 \cdot (S^2/4) / S \cdot \delta^{\mu\nu} = (S/4) \delta^{\mu\nu}$$

Result: $T_{\text{vac}}^{\text{tt}} = S/4$. (Algebraically consistent).

2. The Update Loop (Dynamics)

2.1 Metric Deformation (h)

$$h_{\mu\nu} = g_{\mu\nu} - S \cdot \delta_{\mu\nu}$$

- h is a 4×4 integer matrix.

2.2 Update Rule with Error Diffusion (Deterministic)

Instead of RNG, we use a per-component **Error Accumulator** matrix $E_{\mu\nu}$.

1. Calculate Ideal Change:

$$\Delta g_{\text{ideal}} = (T_{\mu\nu} - T_{\text{vac}}) / K_{\text{elastic}}$$

- K_{elastic} is a fundamental grid constant (e.g., S^2).

2. Apply Accumulator:

$$\text{value} = \Delta g_{\text{ideal}} + E_{\mu\nu}^{(t)}$$

3. Quantize:

$$\Delta g_{\text{actual}} = \text{round}(\text{value})$$

- **Rounding Rule:** `round()` is defined as **symmetric rounding to the nearest integer, with ties rounded away from zero** (e.g., $0.5 \rightarrow 1$, $-0.5 \rightarrow -1$). This behavior is fixed per release to ensure cross-platform determinism.

4. Update Accumulator:

$$E_{\mu\nu}^{(t+1)} = \text{value} - \Delta g_{\text{actual}}$$

5. Update Metric:

$$g_{\mu\nu}^{(t+1)} = g_{\mu\nu}^{(t)} + \text{clamp}(\Delta g_{\text{actual}}, -\Delta_{\text{max}}, \Delta_{\text{max}})$$

2.3 Geodesic Movement with Tie-Break

Rule: Inertial Consistency + Parity Hash.

1. Minimize angle deviation from current v .
2. If costs are equal, use deterministic hash:

$$\text{Hash} = (x \oplus y \oplus z \oplus t) \bmod 2$$

3. Strain Energy & Ω_m

3.1 Strain Energy Calculation

$$E_{\text{strain}} = (1/2) K_{\text{grid}} \sum_{\mu=0}^3 \sum_{\nu=0}^3 (h_{\mu\nu})^2$$

- **Summation covers all 16 components** (required for approximate/emergent Lorentz symmetry under coarse-graining; omitting mixed components breaks boost symmetry in the UE sense).
- K_{grid} is linked to K_{elastic} (Young's modulus).

3.2 Cosmological Output

$$\Omega_m(t) = (E_{\text{mass}} + E_{\text{strain}}(t)) / E_{\text{total}}$$

The evolution of Ω_m is a **result**, not an input.

4. The Weak Field Limit ($\mu(x)$)

4.0 Discrete Potential and Gradient (Operational Definitions)

We require an explicit, implementation-level definition of the scalar potential Φ and its gradient, to avoid any hidden degrees of freedom.

Definition (Potential): Let $g_{\mu\nu}(C)$ be the integer traversal-cost tensor stored in cell C . Define the dimensionless scalar potential as the normalized inverse-volume (traversal-resistance) proxy:

$$\Phi(C) \equiv 1 - \det(S \cdot \delta_{\mu\nu}) / \det(g_{\mu\nu}(C)) = 1 - s^4 / \det(g_{\mu\nu}(C))$$

Interpretation: We explicitly interpret $\det(g_{\mu\nu})$ as **traversal resistance** (inverse effective volume). High gravity corresponds to high traversal cost (compression of the grid), which

increases $\det(g)$ and results in positive Φ .

Vacuum has $g_{\mu\nu} = S\delta_{\mu\nu}$ & implies; $\Phi = 0$.

Implementation note: $\det(g)$ may exceed `int64` for large S . Implementations must use either (i) scaled/normalized determinant via factorization, (ii) 128-bit integer arithmetic, or (iii) a determinant proxy invariant consistent with the fixed-point regime, as long as the chosen Φ definition is fixed and published.

Proxy constraints (to prevent implementation-level fitting): Any allowed determinant proxy must be (1) strictly monotone with respect to the UE traversal-cost ordering induced by $g_{\mu\nu}$, and (2) fixed per release as part of the published specification. Changing Φ , the determinant/proxy method, or the norm/gradients implementation constitutes a model change, not a measurement choice.

Definition (Discrete Gradient): On the spatial lattice (holding tick t fixed), define the central-difference gradient:

$$(\nabla\Phi)_x(C) \equiv (\Phi(x+1, y, z, t) - \Phi(x-1, y, z, t)) / 2L$$

and similarly for y, z , where the lattice step is $L \equiv S$ in internal fixed-point units. We use

$$|\nabla\Phi|(C) \equiv \sqrt{((\nabla\Phi)_x)^2 + (\nabla\Phi)_y^2 + (\nabla\Phi)_z^2}$$

implemented via an integer norm approximation consistent with the UE integer arithmetic (e.g., CORDIC norm). **Crucially, the same norm approximation must be used both in the dynamics update loop and in the measurement protocol.**

4.1 Unit Convention (One source of truth)

UE uses internal fixed-point units with lattice step $L \equiv S$ and tick as the time step. Φ is dimensionless fixed-point. Therefore $|\nabla\Phi|$ has units of $1/L$.

We define the horizon length in cells as:

$$R_H(t) \equiv \text{TickCount}(t)$$

So the minimum resolvable acceleration scale is:

$$a_0(t) \equiv 1 / R_H(t) \text{ (units: } 1/L\text{)}$$

In integer internal code units we store:

$$a_{0,\text{int}}(t) \equiv S / \text{TickCount}(t)$$

Likewise $|\nabla\Phi|_{\text{int}}$ is stored in fixed-point units consistent with $1/L$. Then:

$$x \equiv |\nabla\Phi| / a_0 = |\nabla\Phi|_{\text{int}} / a_{0,\text{int}}$$

is a pure dimensionless number.

4.2 The "Floor" Mechanism

In the weak field ($x < 1$), $\Delta g_{\text{ideal}} < 1$.

The **Error Diffusion** algorithm (Sec 2.2) ensures that updates happen sparsely but deterministically.

Appendix A: The Weak Field Scaling Lemma (Heuristic)

Status: Conjecture / Empirical Expectation.

Claim: The Error Diffusion mechanism leads to an effective force scaling of $1/r$ (logarithmic potential) in the deep weak field limit ($x \ll 1$).

Heuristic Argument (Dimensional Reduction):

1. **Standard Regime ($x \gg 1$):** Updates happen every tick in every cell. The "active" causal graph is a dense 3D volume. Flux density scales as $1/\text{Area} \propto 1/r^2$.
2. **Discrete Regime ($x \ll 1$):** Updates happen only when the Accumulator overflows. The "active" cells (where $\Delta g \neq 0$) become sparse.
3. **Dimensional Collapse:** We conjecture that the topology of "active" cells reduces from a 3D volume to a fractal structure with effective dimension $D_{\text{eff}} \approx 2$ (flux tubes/filaments).
4. **Scaling:** In D dimensions, force scales as $1/r^{D-1}$. If $D_{\text{eff}} \approx 2$, then Force $\propto 1/r$.

Verification: The exact form of $\mu(x)$ is to be **measured** from the simulation output, not postulated as an input formula.

End of Specification