N741 Homework 8

Julianne

April 11, 2017

Rcode available here: https://github.com/JulianneA/N741hmwk8

```
## Parsed with column specification:
## cols(
##
     X1 = col_integer(),
##
     X2 = col_integer(),
##
    X3 = col_integer(),
     X4 = col_integer(),
##
     X5 = col_integer(),
##
     X6 = col_integer(),
##
     X7 = col_integer(),
##
     X8 = col_integer(),
##
     X9 = col_integer(),
##
     X10 = col_integer(),
##
     X11 = col_integer()
## )
## Warning: 16 parsing failures.
## row col
             expected actual
  24 X7 an integer
## 41 X7 an integer
## 140
       X7 an integer
## 146 X7 an integer
## 159 X7 an integer
## See problems(...) for more details.
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
```

PCA with full dataset

1. Perform the PCA

```
## Importance of components:

## PC1 PC2 PC3 PC4 PC5 PC6

## Standard deviation 2.4289 0.88088 0.73434 0.67796 0.61667 0.54943

## Proportion of Variance 0.6555 0.08622 0.05992 0.05107 0.04225 0.03354

## Cumulative Proportion 0.6555 0.74172 0.80163 0.85270 0.89496 0.92850

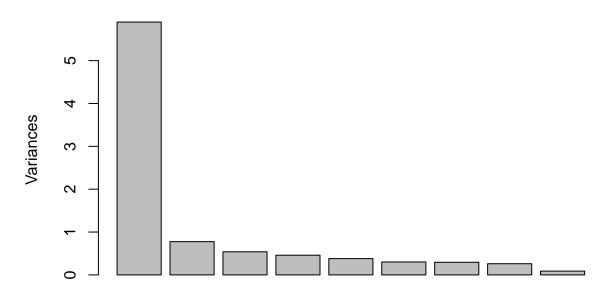
## PC7 PC8 PC9
```

```
## Standard deviation 0.54259 0.51062 0.29729 ## Proportion of Variance 0.03271 0.02897 0.00982 ## Cumulative Proportion 0.96121 0.99018 1.00000
```

2. Make plots of the variance and PVE

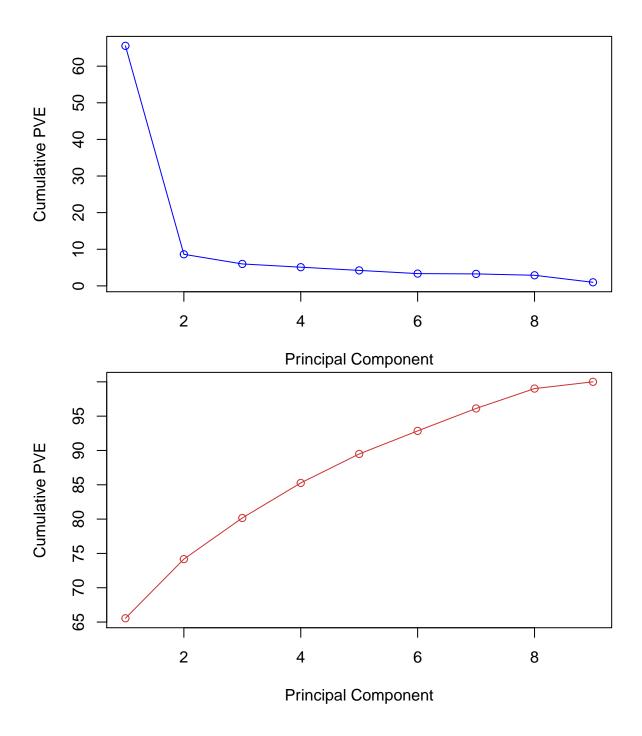
Plot of the Variances of Each PC

pr.out



Plot of the PVE and Cumulative PVE of each PC

```
## [1] 65.5499928 8.6216321 5.9916916 5.1069717 4.2252870 3.3541828
## [7] 3.2711413 2.8970651 0.9820358
```

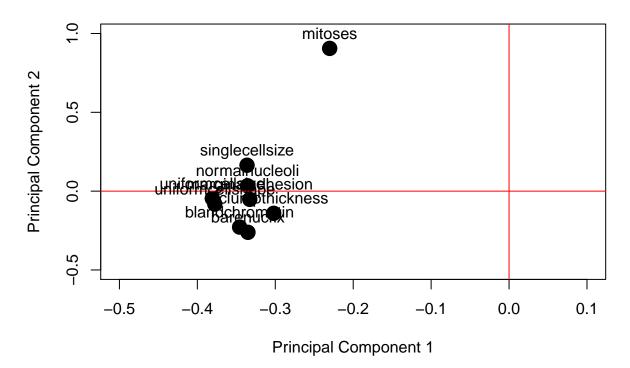


3. Make a "loadings plot" of the variables

```
PC1
                                                    PC3
##
                                       PC2
                                                                PC4
## clumpthickness
                    -0.3020626 -0.14080053
                                           0.866372452 -0.10782844
                    -0.3807930 -0.04664031 -0.019937801
## uniformcellsize
                                                         0.20425540
## uniformcellshape -0.3775825 -0.08242247
                                            0.033510871
                                                         0.17586560
## marginaladhesion -0.3327236 -0.05209438 -0.412647341 -0.49317257
## singlecellsize
                    -0.3362340 0.16440439 -0.087742529
                                                         0.42738358
                    -0.3350675 -0.26126062 0.000691478 -0.49861767
## barenucfix
## blandchromatin
                    -0.3457474 -0.22807676 -0.213071845 -0.01304734
```

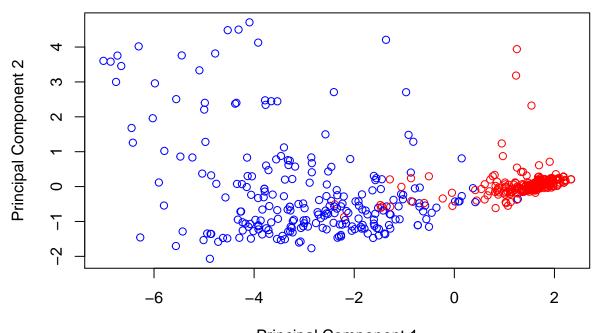
```
## normalnucleoli
                    -0.3355914 0.03396582 -0.134248356 0.41711347
## mitoses
                    -0.2302064
                                0.90555729
                                           0.080492170 -0.25898781
##
                            PC5
                                        PC6
                                                      PC7
## clumpthickness
                     0.08032124 -0.24251752 -0.008515668
                                                          0.24770729
## uniformcellsize
                    -0.14565287 -0.13903168 -0.205434260 -0.43629981
## uniformcellshape -0.10839155 -0.07452713 -0.127209198 -0.58272674
## marginaladhesion -0.01956898 -0.65462877
                                             0.123830400
## singlecellsize
                    -0.63669325
                                 0.06930891
                                             0.211018210
                                                           0.45866910
                                 0.60922054
  barenucfix
                    -0.12477294
                                             0.402790095 -0.12665288
## blandchromatin
                                 0.29889733 -0.700417365
                     0.22766572
                                                           0.38371888
  normalnucleoli
                     0.69021015
                                 0.02151820
                                            0.459782742
                                                           0.07401187
                                 0.14834515 -0.132116994 -0.05353693
##
  mitoses
                     0.10504168
##
                             PC9
  clumpthickness
                    -0.002747438
## uniformcellsize
                    -0.733210938
## uniformcellshape
                     0.667480798
## marginaladhesion
                     0.046019211
  singlecellsize
                     0.066890623
## barenucfix
                    -0.076510293
## blandchromatin
                     0.062241047
## normalnucleoli
                    -0.022078692
## mitoses
                     0.007496101
```

Loadings Plot for PC 1 and 2



4. Scores Plot on 1st 2 PCs

Scores Plot on PC 1 and 2



Principal Component 1
Blue=Benign (class=2) and Red=Malignant (class=4)

Homework 8 Tasks

PCA with Benign Cases only

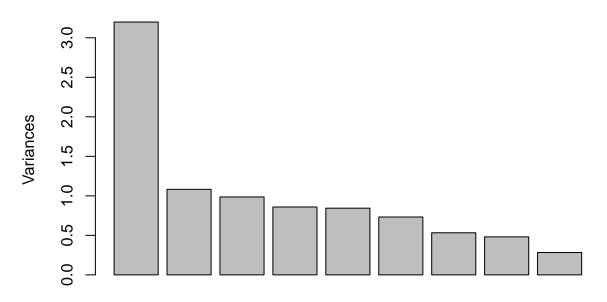
1. Perform the PCA

```
## Importance of components:
##
                                           PC3
                                                    PC4
                                                            PC5
                                                                    PC6
                             PC1
                                    PC2
## Standard deviation
                          1.7887 1.0405 0.9930 0.92684 0.91865 0.85577
## Proportion of Variance 0.3555 0.1203 0.1096 0.09545 0.09377 0.08137
## Cumulative Proportion 0.3555 0.4758 0.5854 0.68081 0.77458 0.85595
                              PC7
                                      PC8
                                              PC9
## Standard deviation
                          0.72971 0.69343 0.53208
## Proportion of Variance 0.05916 0.05343 0.03146
## Cumulative Proportion 0.91512 0.96854 1.00000
```

2. Make plots of the variance and PVE

Plot of the Variances of Each PC

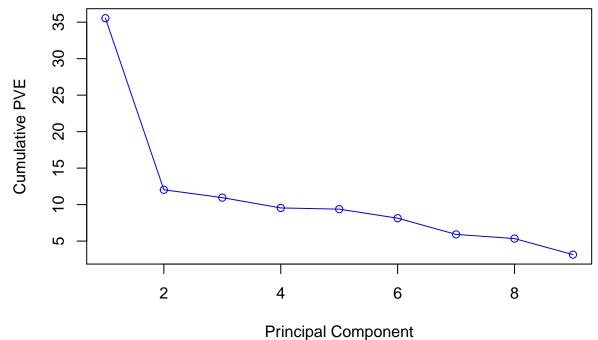


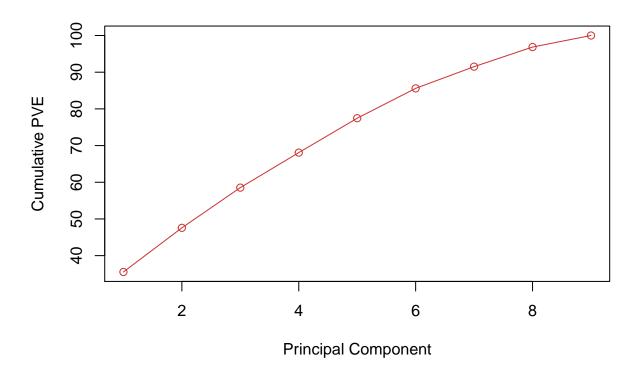


Plot of the PVE and Cumulative PVE of each PC

[1] 35.550174 12.029083 10.957095 9.544841 9.376951 8.137200 5.916378

[8] 5.342677 3.145601





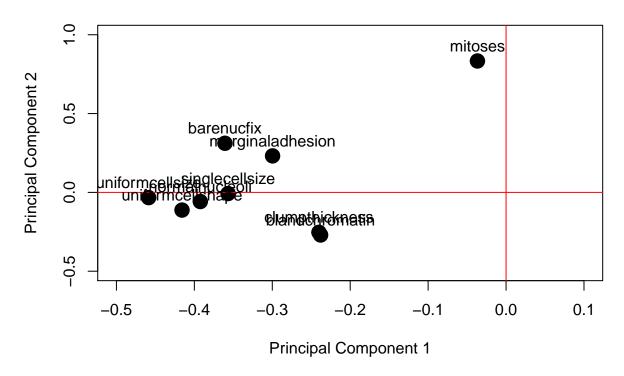
3. Make a "loadings plot" of the variables

```
##
                           PC1
                                        PC2
                                                    PC3
                                             0.62484649 -0.199323941
## clumpthickness
                   -0.24011520 -0.253256825
## uniformcellsize
                   -0.45864830 -0.033204671 -0.02085097 -0.330649289
## uniformcellshape -0.41582963 -0.112167262
                                             0.09869789 -0.447953433
  marginaladhesion -0.29961721 0.231565724
                                             0.37743125
                                                         0.606952624
  singlecellsize
                   -0.35673183 -0.007389172 -0.04352450
                                                         0.279971872
  barenucfix
                   0.250068883
  blandchromatin
                   -0.23796491 -0.270255849 -0.60100673
                                                         0.128887383
  normalnucleoli
                   -0.39235641 -0.058082399 -0.28511559 -0.009877498
##
  mitoses
                   -0.03672453
                                0.833641905 -0.09625297 -0.352503945
##
                           PC5
                                      PC6
                                                  PC7
## clumpthickness
                     0.51477010 -0.1751030
                                           0.38404427
                                                       0.06874853
  uniformcellsize
                                0.1864954 -0.13495407 -0.04930335
                   -0.18213500
## uniformcellshape -0.21954352
                                0.2370728 -0.26160782 -0.23353820
## marginaladhesion 0.19804701
                                0.1093704 -0.52767057 -0.12507351
## singlecellsize
                    -0.38970577 -0.5702306
                                           0.33220762 -0.45240165
## barenucfix
                                0.4982717
                                           0.55467287
                                                      0.34056137
                   -0.13507321
## blandchromatin
                                0.1690343
                                           0.06913716 -0.33732847
                     0.58710974
## normalnucleoli
                     0.07300474 -0.4678173 -0.25315695
                                                       0.67741729
## mitoses
                     0.30704026 -0.2133771 0.02302674 -0.17124652
##
                           PC9
## clumpthickness
                   -0.01329810
## uniformcellsize
                   -0.76823067
  uniformcellshape
                    0.61377445
## marginaladhesion -0.02229120
## singlecellsize
                     0.01861508
## barenucfix
                     0.12950293
## blandchromatin
                     0.02593358
## normalnucleoli
                     0.11886569
```

mitoses

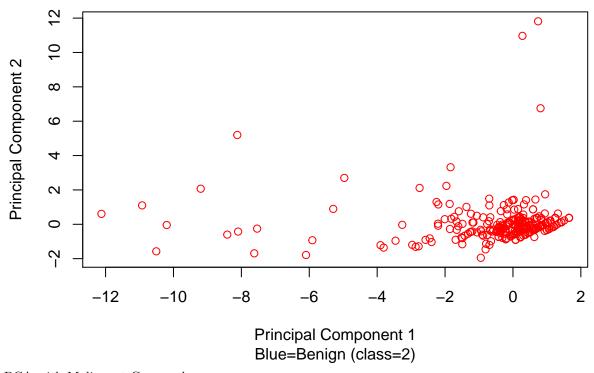
0.02257633

Loadings Plot for PC 1 and 2



4. Scores Plot on 1st 2 PCs

Scores Plot on PC 1 and 2



#

PCA with Malignant Cases only

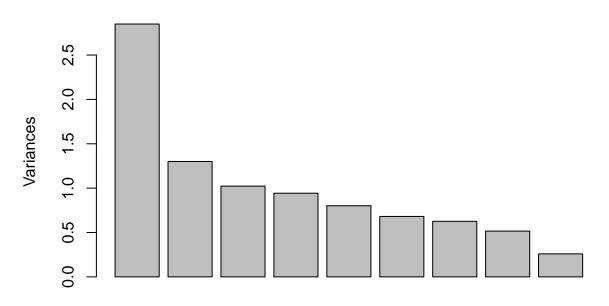
1. Perform the PCA

```
## Importance of components:
                                    PC2
                                           PC3
                                                   PC4
                                                          PC5
                                                                  PC6
                                                                          PC7
##
                             PC1
## Standard deviation
                          1.6881 1.1405 1.0114 0.9710 0.8955 0.82523 0.79132
## Proportion of Variance 0.3166 0.1445 0.1137 0.1048 0.0891 0.07567 0.06958
## Cumulative Proportion
                          0.3166 0.4611 0.5748 0.6795 0.7687 0.84432 0.91389
##
                             PC8
                                    PC9
## Standard deviation
                          0.7181 0.5092
## Proportion of Variance 0.0573 0.0288
## Cumulative Proportion 0.9712 1.0000
```

2. Make plots of the variance and PVE

Plot of the Variances of Each PC

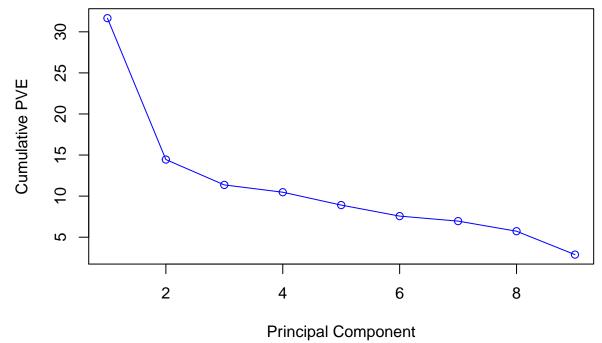


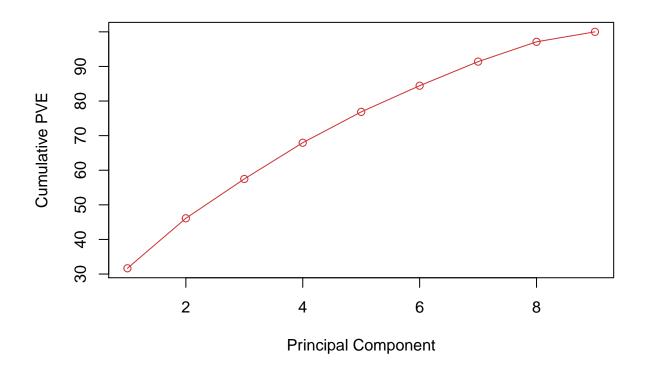


Plot of the PVE and Cumulative PVE of each PC

[1] 31.661845 14.452164 11.364996 10.475550 8.910443 7.566671 6.957691

[8] 5.730245 2.880396





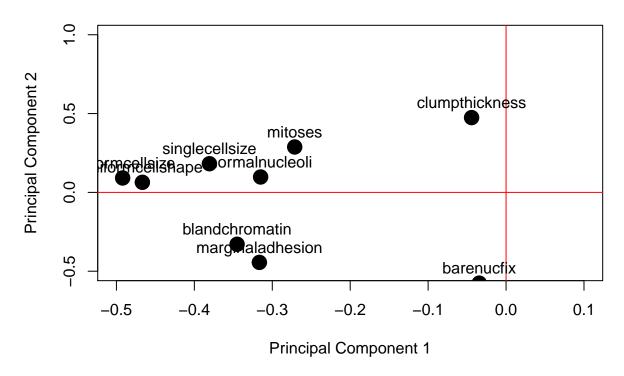
3. Make a "loadings plot" of the variables

```
##
                            PC1
                                        PC2
                                                    PC3
## clumpthickness
                    -0.04423311
                                0.47453175 -0.72050432
                                                         0.03375094
## uniformcellsize
                   -0.49200997
                                0.09144594 -0.10713144 -0.23385625
## uniformcellshape -0.46669310
                                0.06386848 -0.19774730 -0.24213467
## marginaladhesion -0.31654337 -0.44402770
                                                         0.25657447
                                            0.10728697
  singlecellsize
                    -0.38065450
                                0.18190583
                                            0.12106578
                                                         0.20864693
## barenucfix
                    -0.03443192 -0.57557062 -0.49808880
                                                         0.35266296
  blandchromatin
                    -0.34513808 -0.32908090 -0.09767689 -0.30475120
                                             0.36209294 -0.12934244
  normalnucleoli
                                0.09772667
                    -0.31497084
  mitoses
                    -0.27121420
                                 0.28809974
                                             0.12401793
                                                         0.73634571
##
##
                            PC5
                                        PC6
                                                    PC7
## clumpthickness
                    -0.33747692
                                0.19363953
                                            0.06219100
## uniformcellsize
                     0.25878373
                                0.05030229 -0.22115522 -0.11677498
## uniformcellshape
                     0.20325032 -0.13515456 -0.40047847 -0.22875166
## marginaladhesion -0.08457519
                                0.56327695 -0.28239595
                                                         0.46360581
## singlecellsize
                     0.44399919 -0.28036154
                                            0.49840771
                                                         0.47849939
## barenucfix
                    -0.04647075 -0.52478456 -0.04208568 -0.03054114
## blandchromatin
                    -0.26382710
                                0.24258816
                                            0.66277346 -0.31133678
## normalnucleoli
                    -0.69424240 -0.44416638 -0.13065490
                                                         0.20939361
## mitoses
                    -0.14072880
                                PC9
##
## clumpthickness
                     0.009006567
## uniformcellsize
                    -0.742531194
## uniformcellshape
                    0.638825011
## marginaladhesion
                     0.078657744
## singlecellsize
                     0.103499670
## barenucfix
                    -0.121683838
## blandchromatin
                     0.074285922
## normalnucleoli
                    -0.056828116
```

mitoses

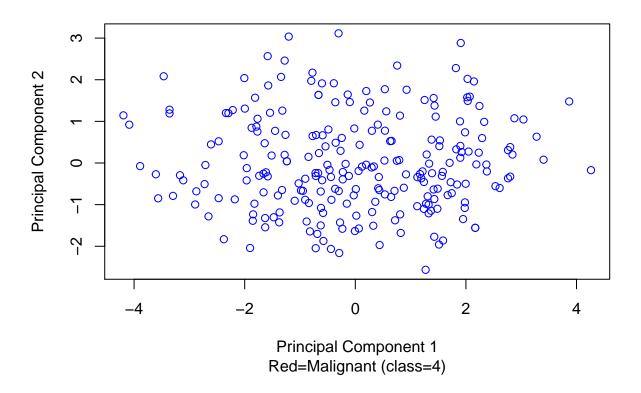
-0.003860273

Loadings Plot for PC 1 and 2



4. Scores Plot on 1st 2 PCs

Scores Plot on PC 1 and 2



Questions

2. In the overall dataset, when looking at the loadings plot, which variables cluster together? which variables do not lie with that cluster?

In the overall dataset, Mitoses is clearly the most profound outlier, with single cell size and clump thickness lying a bit to the outskirts of the cluster that contains all other variables: Uniformity of Cell Size, Uniformity of Cell Shape, Marginal Adhesion, Bare Nuclei, Bland Chromatin, Normal Nucleoli.

3. How do the variable clusters seen in the loading plots for the Benign data subset and Malignant subset differ? and how are they similar if at all?

The cluster pattern in the loading plot for the benign data subset looks similar to the clustering pattern from the combined dataset, with mitoses as the most profound outlier, although many of the remaining variables, while clustered, are in different locations in the benign plot compared to the whole dataset plot. The loading plot for the malignant subset appears most different from the other two, with the variables more distributed throughout the loading plot relative to the combined and benign plots. In the malignant plot, clump thickness and bare nuclei are the most distinct outliers, and are more strongly outliers on the x axis (Principal Component 1) compared to the y axis. Additionally, the malignant plot has certain variables, such as bare nuclei and clump thickness with completely flipped values (negative to positive or vice versa) compared to the benign plot.

4. Is using 2 principal components reasonable for summarizing the variability seen in this Breast Cancer dataset with 9 measurements? Explain your reasoning for (a) the overall dataset, (b) the Benign subset and (c) the Malignant subset

The Overall dataset would require the least number of principal components to explain the most variability in the data, as indicated by the scree plots. These plots indicate that using just two PCs would explain approximately 75% of the variability in the data, whereas just two PCs would explain just under 50% of the variability in both the Benign and Malignant subsets. Therefore, based on scree plots, 2 principal components would likely be reasonable for summarizing variability in just the overall dataset. The Benign subset has a 2nd large decrease in cumulative PCE between the 6th-7th variables and the malignant subset has a 2nd (relatively) large decrease between the 4th-5th variables and a 3rd between the 8th-9th variables. These "elbows" should be considered when trying to explain variability in the dataset, but they seem to indicate that more variables are required to adequately explain variability in the subsets compared to the full dataset.

5. While PCA is an unsupervised data analysis method (i.e. no "target" class information is used in the analysis), do you think the 2 PCs extracted do a good job of helping to distinguish Benign cases from Malignant cases (i.e. look back at the overall dataset Scores Plot). Explain your rationale.

The 2 PCs extracted seem to do an adequate job of distinguishing between benign and malignant, but would likely be more useful to rule-in malignancy rather than rule it out. The rationale for this is because the malignancy seems to cluster together much more than benign, and while the PCs identified do an adequate job of isolating malignancies, they seem to be more effective at ruling out benign tumors. This means that using the PCs, individuals can fall into "malignant", "likely not malignant", and "definitely not malignant" categories, and additional testing could be conducted on the "likely not malignant" group to continue to rule in/out malignancy.