

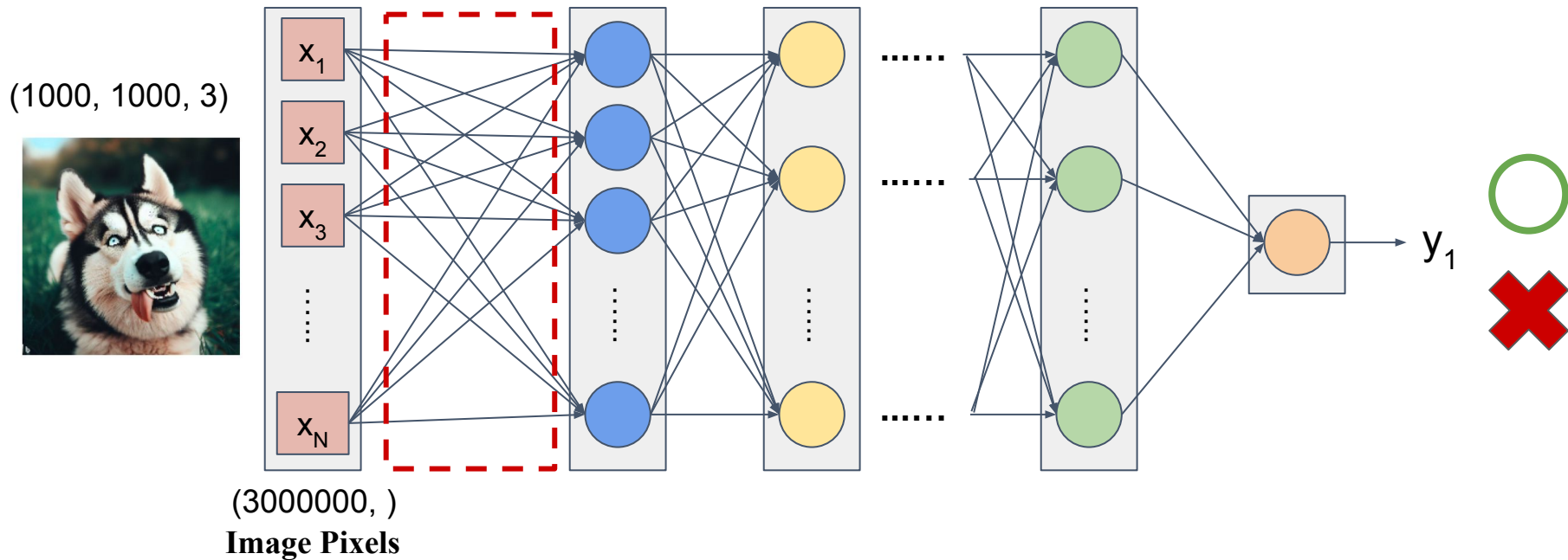
# Convolution

# Convolutional Neural Network (CNN)

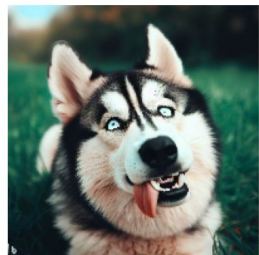
卷積神經網路

# Fully Connected Neural Network

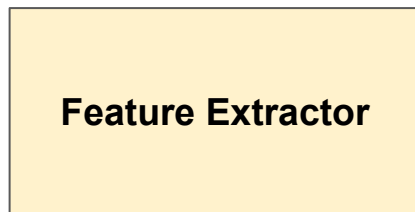
$n = 1000 \times 1000 \times 3$  (height, weight, channels(RGB))



# Image Recognition



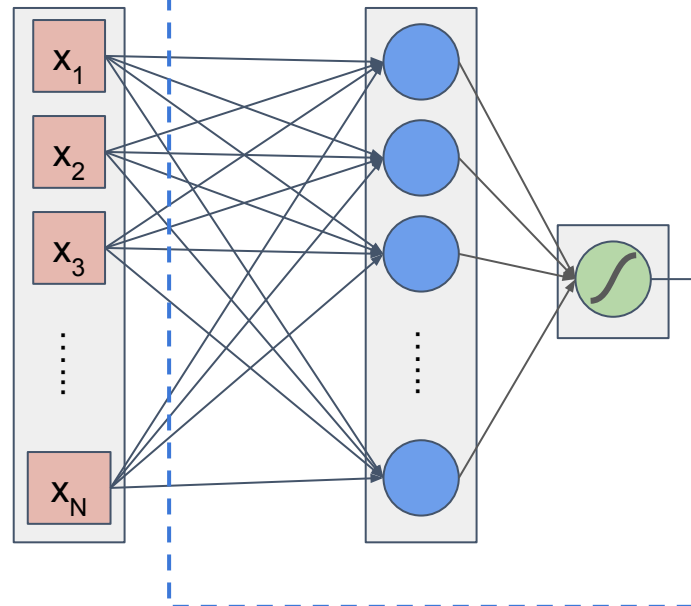
Domain knowledge



e.g.

1. Color
2. Line
3. Texture
4. GLCM
5. HoG
6. Radiomics

feature vector  
(特徴向量)

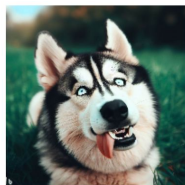


Trainable Classifier

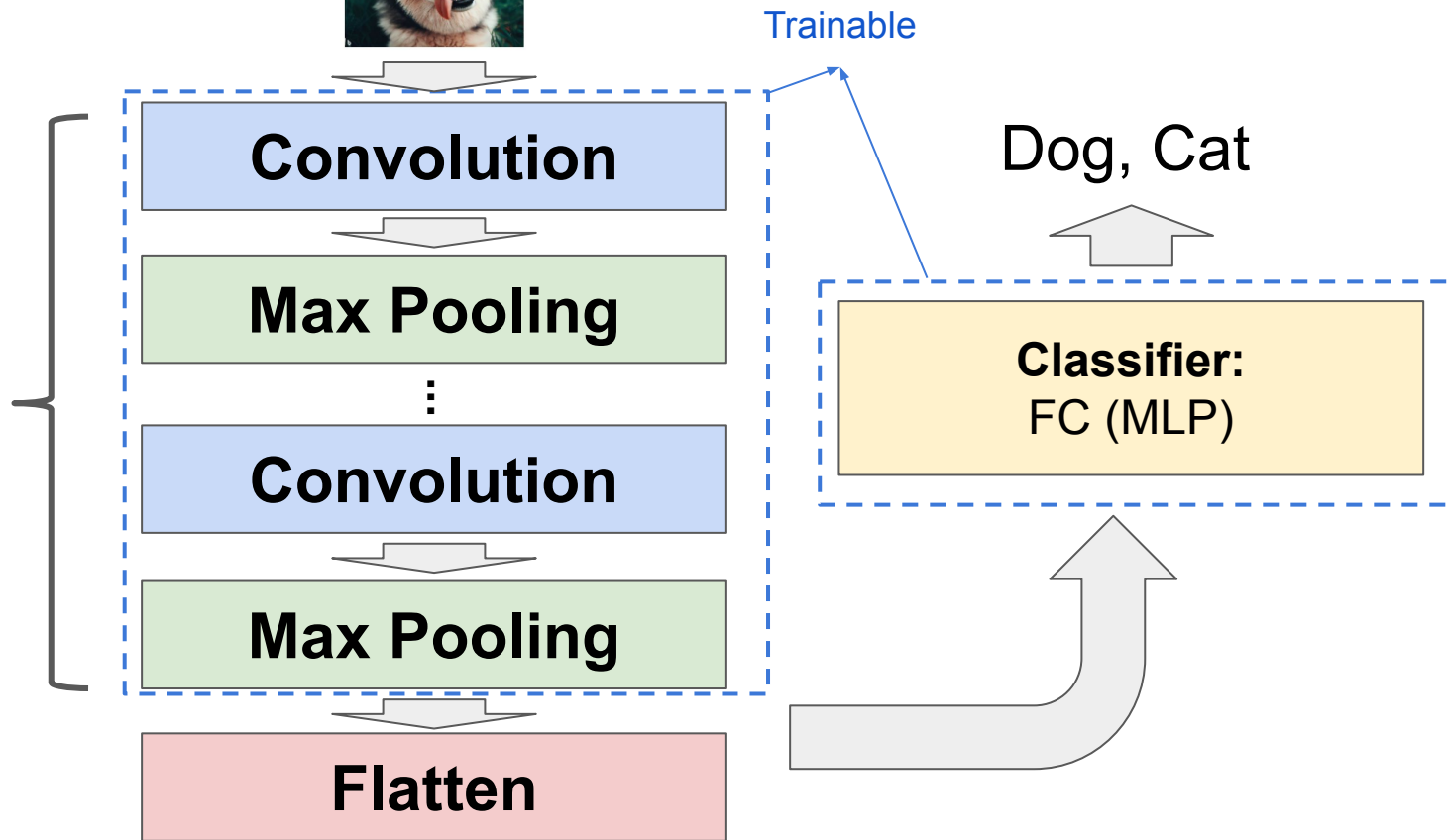
$y_1$



# CNN model



Feature  
Extractor  
(Encoder)

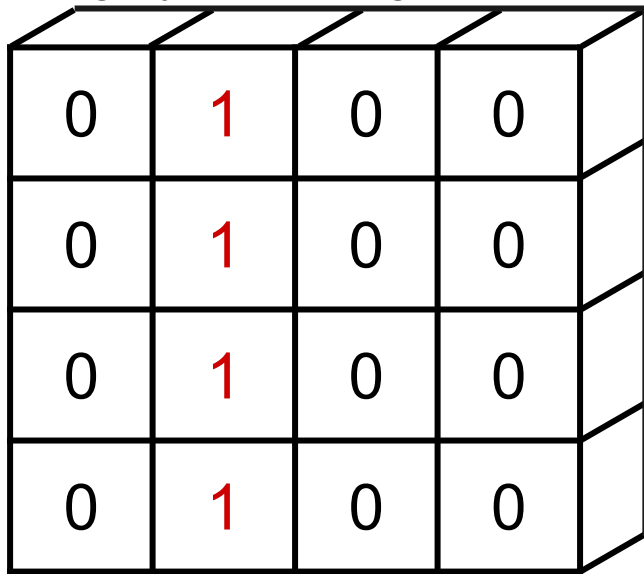


# CNN - Convolution

NOTE:

- 卷積層輸入必定有通道數
- PyTorch 將通道數放在前 (channel first)

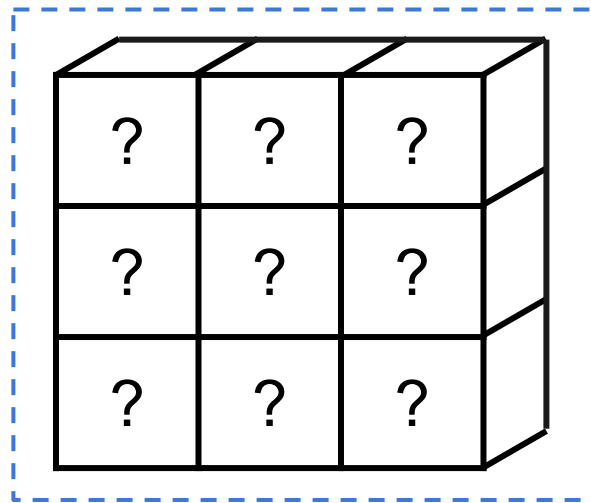
- For grayscale image (channels = 1)



4 x 4 image

(1, 4, 4) = (Channels, Height, Width)

Trainable

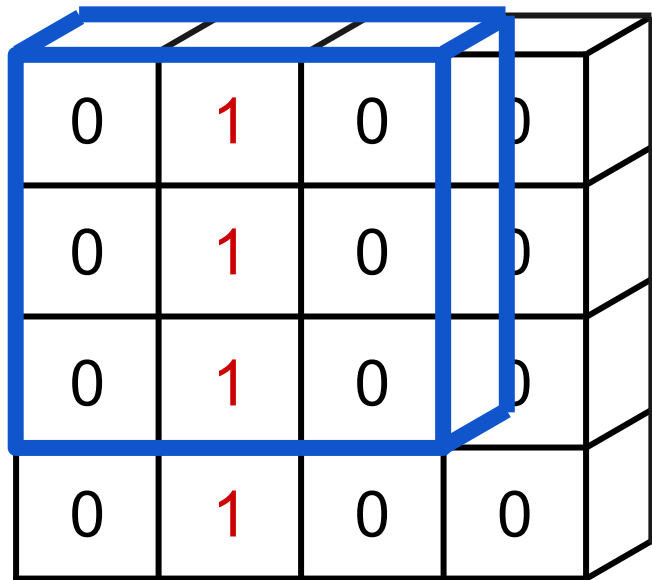


3 x 3 filter (kernel)

(1, 3, 3)

# CNN - Convolution

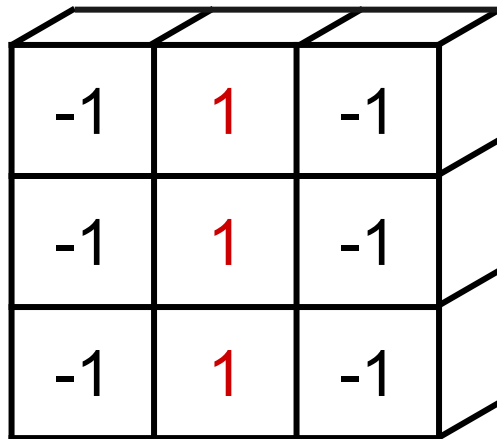
- For grayscale image (channels = 1)



0	1	0	0
0	1	0	0
0	1	0	0
0	1	0	0

4 x 4 image

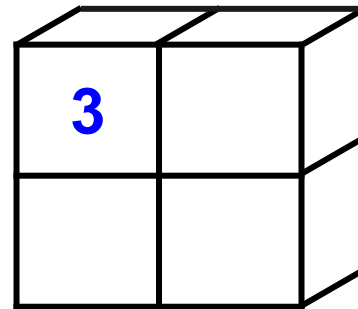
(1, 4, 4) = (C, H, W)



-1	1	-1
-1	1	-1
-1	1	-1

3 x 3 filter (kernel)

(1, 3, 3)

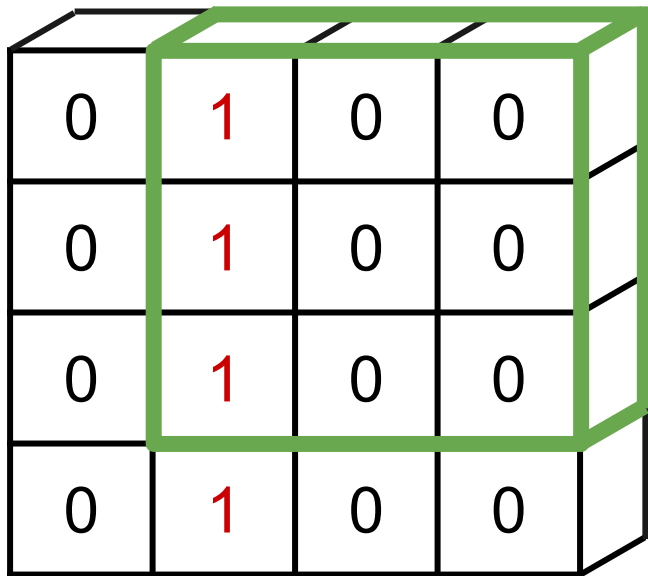


3	

$$\begin{aligned} & -1*0 + 1*1 + -1*0 + \\ & -1*0 + 1*1 + -1*0 + \\ & -1*0 + 1*1 + -1*0 \\ & = 3 \end{aligned}$$

# CNN - Convolution

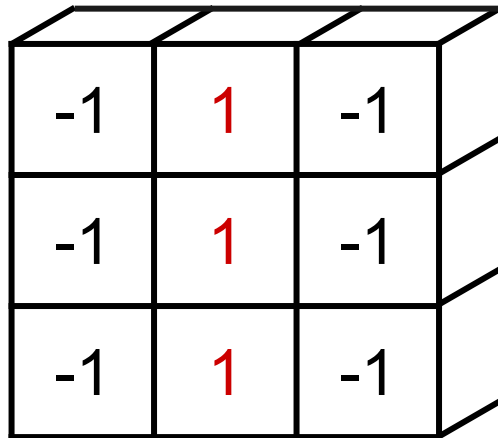
- For grayscale image (channels = 1)



0	1	0	0
0	1	0	0
0	1	0	0
0	1	0	0

4 x 4 image

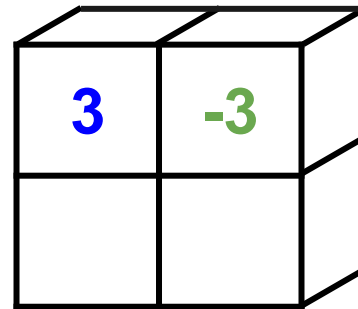
(1, 4, 4) = (C, H, W)



-1	1	-1
-1	1	-1
-1	1	-1

3 x 3 filter (kernel)

(1, 3, 3)



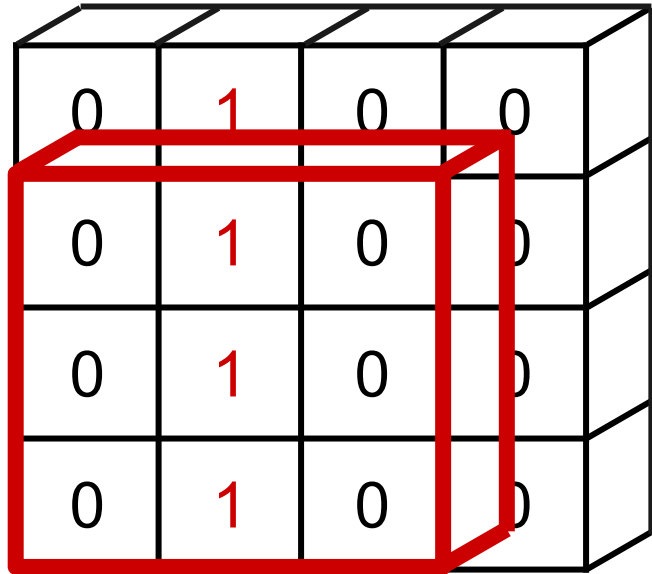
3	-3

$$\begin{aligned} & -1*1 + 1*0 + -1*0 + \\ & -1*1 + 1*0 + -1*0 + \\ & -1*1 + 1*0 + -1*0 \\ & = -3 \end{aligned}$$



# CNN - Convolution

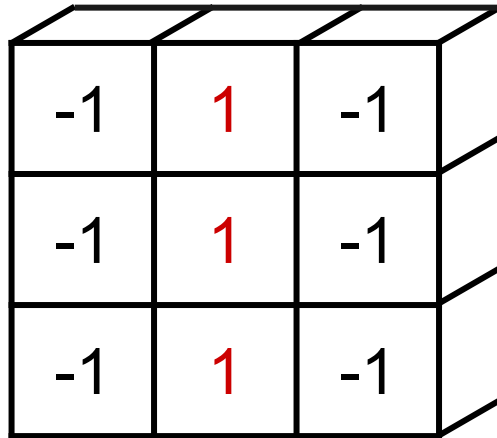
- For grayscale image (channels = 1)



0	1	0	0
0	1	0	0
0	1	0	0
0	1	0	0

4 x 4 image

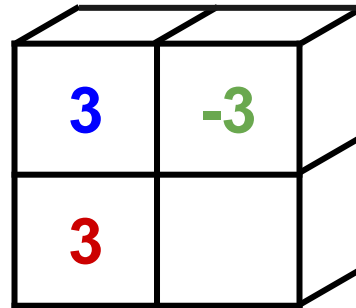
(1, 4, 4) = (C, H, W)



-1	1	-1
-1	1	-1
-1	1	-1

3 x 3 filter (kernel)

(1, 3, 3)

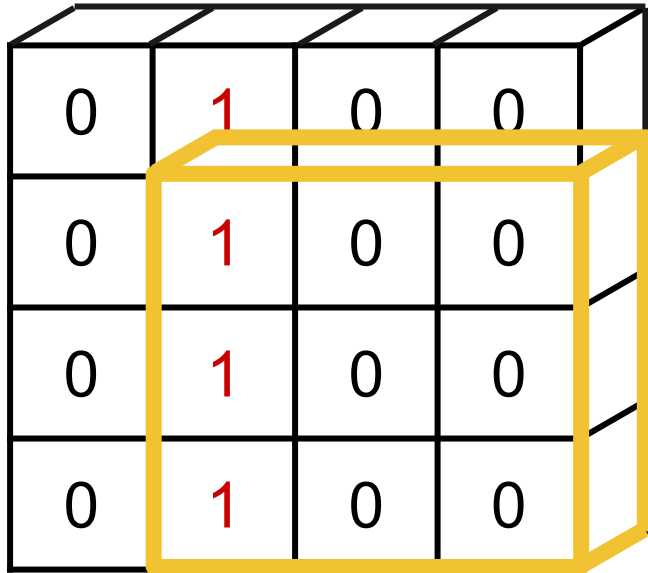


3	-3
3	

$$\begin{aligned} & -1*0 + 1*1 + -1*0 + \\ & -1*0 + 1*1 + -1*0 + \\ & -1*0 + 1*1 + -1*0 \\ & = 3 \end{aligned}$$

# CNN - Convolution

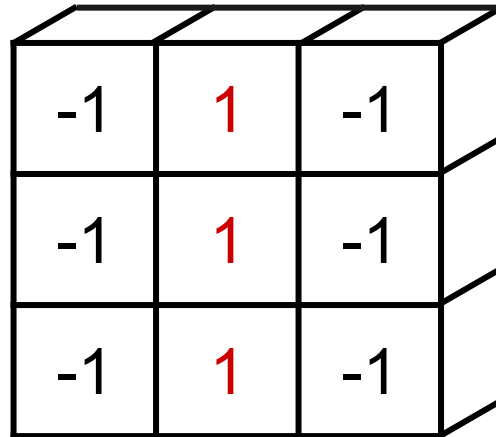
- For grayscale image (channels = 1)



0	1	0	0
0	1	0	0
0	1	0	0
0	1	0	0

4 x 4 image

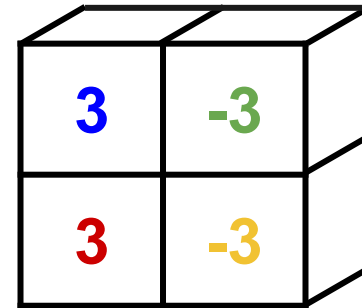
(1, 4, 4) = (C, H, W)



-1	1	-1
-1	1	-1
-1	1	-1

3 x 3 filter (kernel)

(1, 3, 3)



3	-3
3	-3

$$\begin{aligned} & -1*1 + 1*0 + -1*0 + \\ & -1*1 + 1*0 + -1*0 + \\ & -1*1 + 1*0 + -1*0 \\ & = -3 \end{aligned}$$

# CNN - Convolution

- For grayscale image (channels = 1)

0	1	0	0
0	1	0	0
0	1	0	0
0	1	0	0

4 x 4 image

(1, 4, 4) = (C, H, W)

-1	1	-1
-1	1	-1
-1	1	-1

Trainable

3 x 3 filter (kernel)

(1, 3, 3)

3	-3
3	-3

feature map

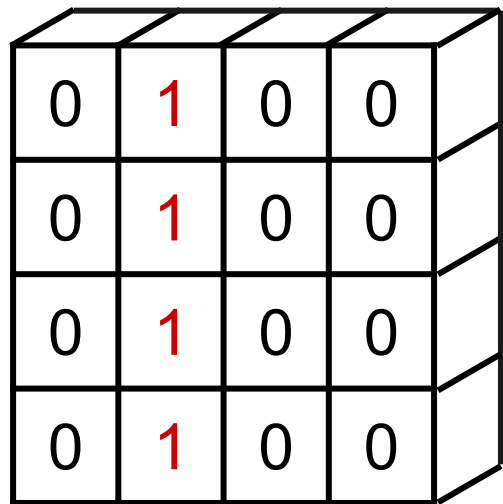
(1, 2, 2)



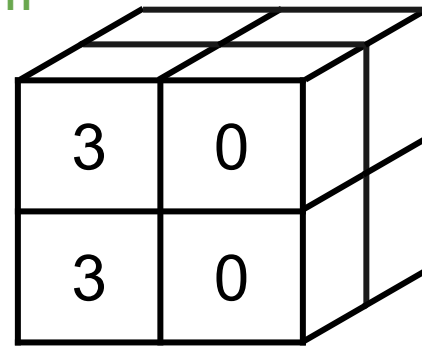
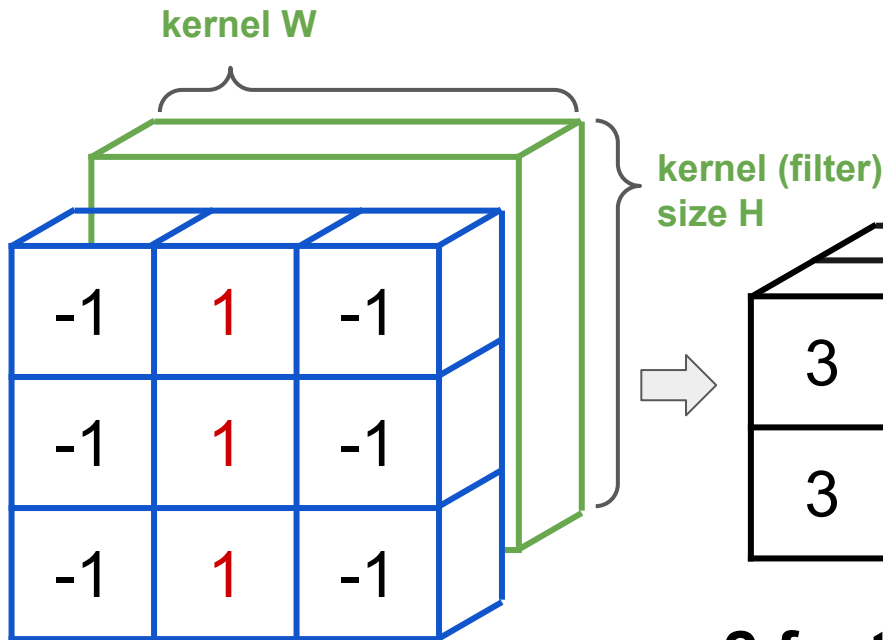
Information (feature)

left side with **vertical line**

# CNN - Convolution



(1, 4, 4)  
(C, H, W)



**2 feature maps**

(2, 2, 2,)  
(C', H', W')

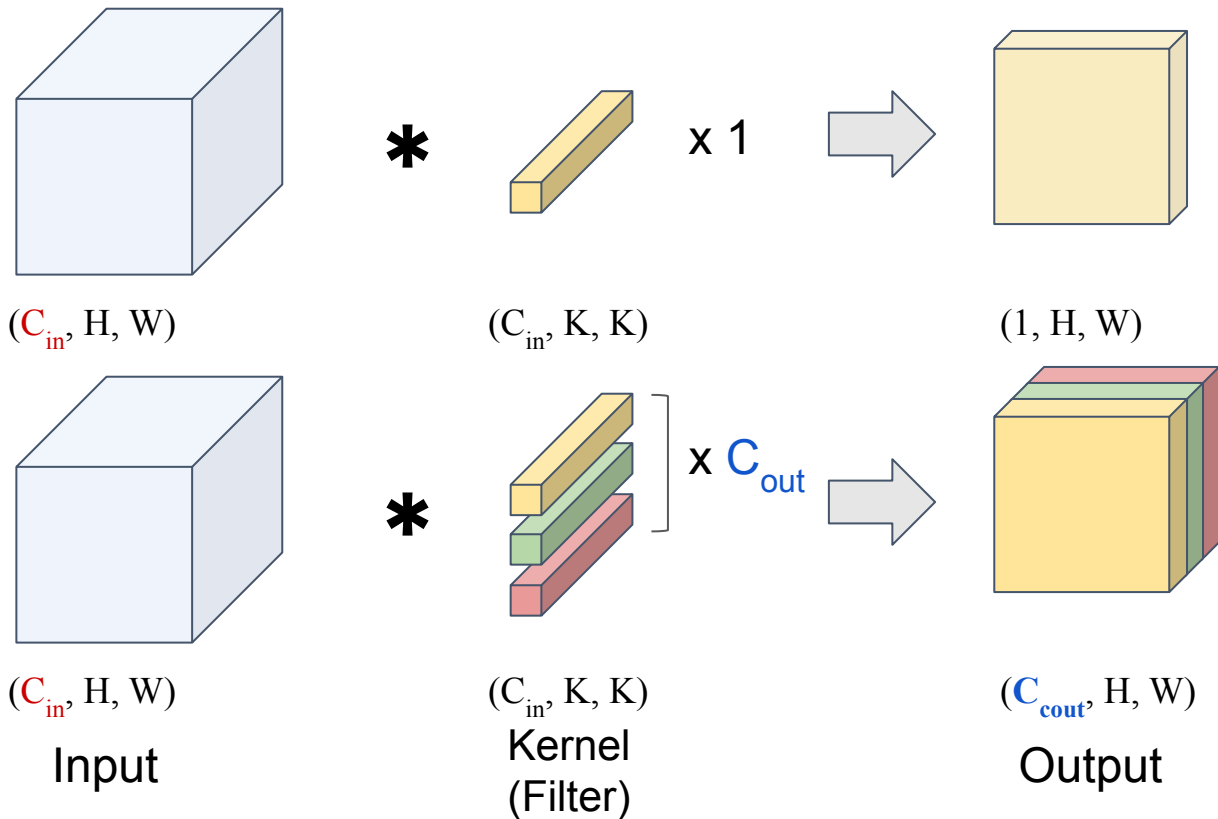


```
torch.nn.Conv2d(in_channels=1,  
                 out_channels=2,  
                 kernel_size=3)
```

# Convolution



```
torch.nn.Conv2d( $C_{in}$ ,  $C_{out}$ , kernel_size=K)
```



# Convolution

- Filter (kernel) **channels** is based on input **channels**

- e.g.

- 1 filter, kernel size=3x3
- kernel shape
  - (Channels, kernel\_H, kernel\_W)
  - (3, 3, 3)

- Channels

- 1

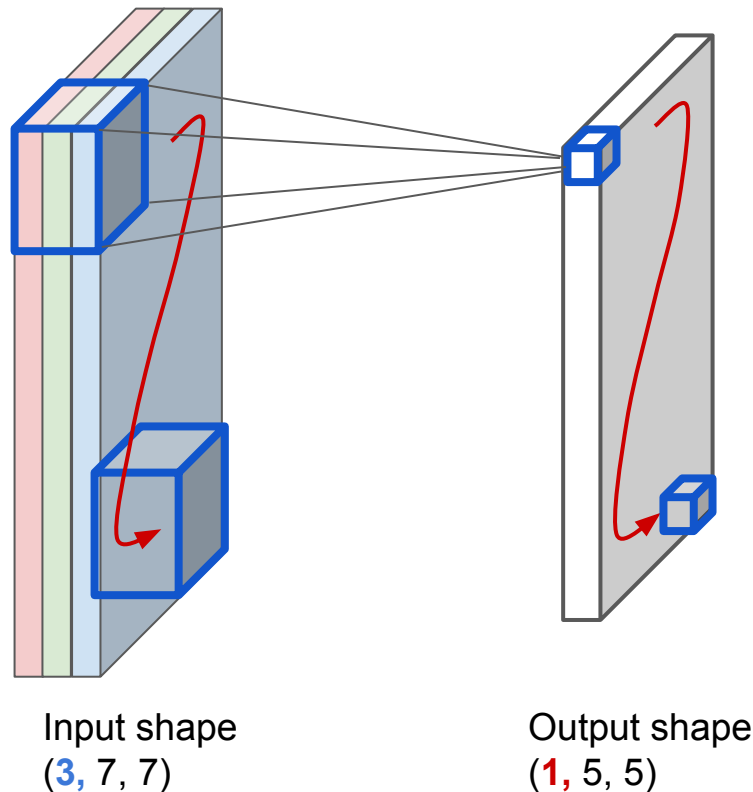
- Grayscale
- CT, X-ray
- Ultrasound

- 3

- Color RGB

- N: whatever you want

- 2: PET + CT
- 4: RGB + Infrared
- 4: RGB + Edge detection

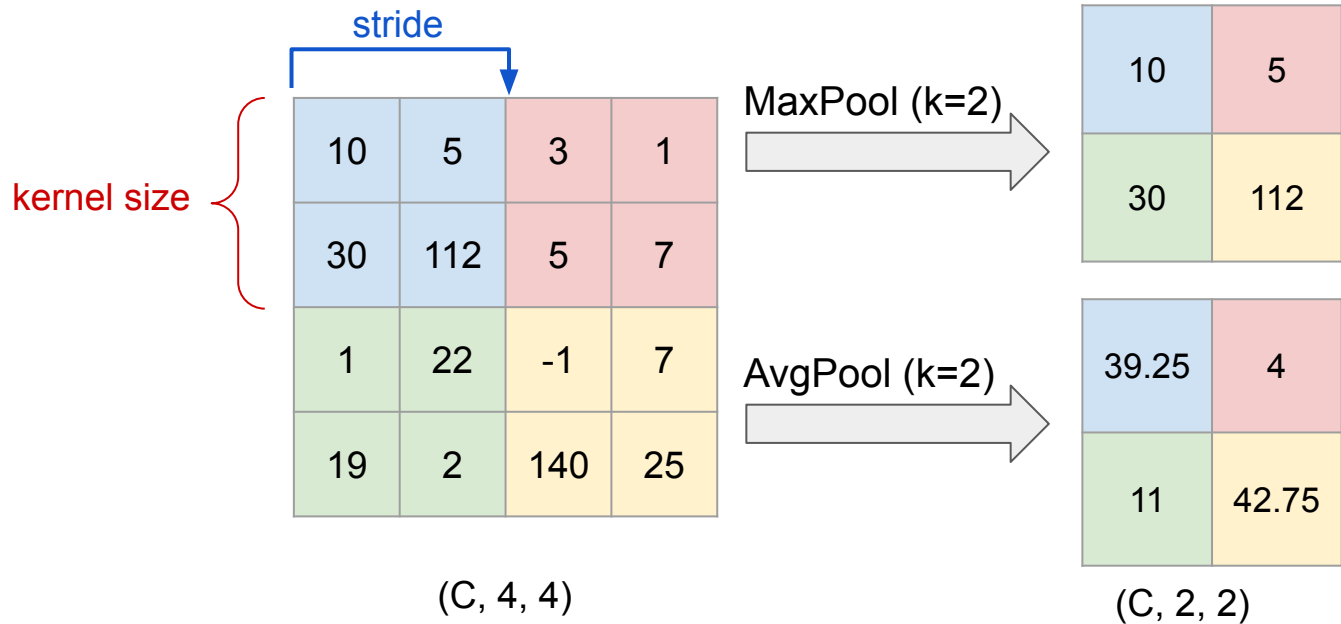


# Pooling Layer (池化層)

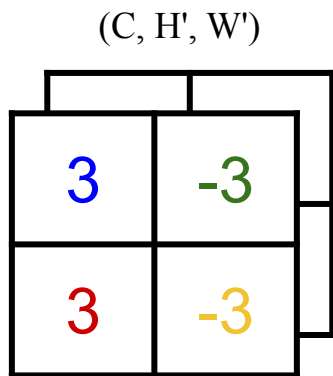


```
torch.nn.MaxPool1d(2)
torch.nn.MaxPool1d(
    kernel_size=2,
    stride=None)
torch.nn.MaxPool1d(
    kernel_size=2,
    stride=2)
torch.nn.AvgPool1d()
```

- e.g.
  - **Max** pooling
  - **Average** pooling
- Reduce size, computing complexity



## After Convolution + max pooling



feature map 做下一層的輸入"image"



$(3, H, W)$

**Convolution**

**Max Pooling**

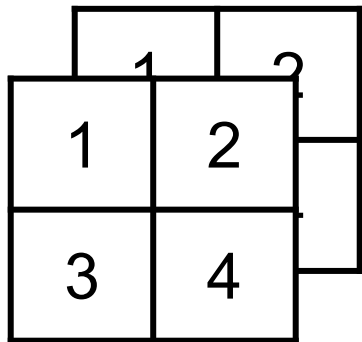
**Convolution**

**Max Pooling**



# CNN - Flatten

- Flatten input tensor
- Reshape



feature maps

(2, 2, 2)  
(C, H, W)

PyTorch `torch.nn.Flatten()`

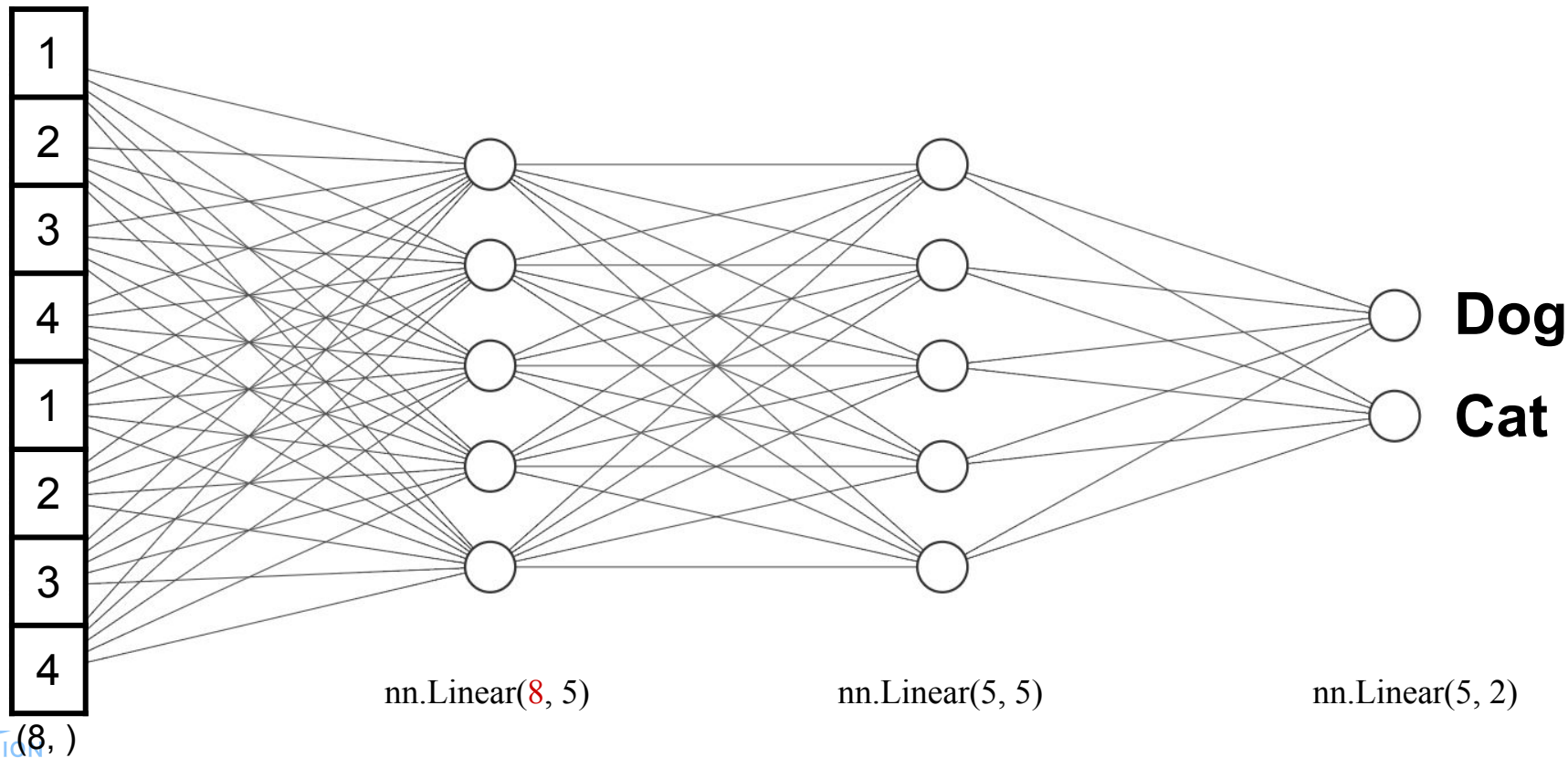
Flatten

feature vector ( 特徴向量 )

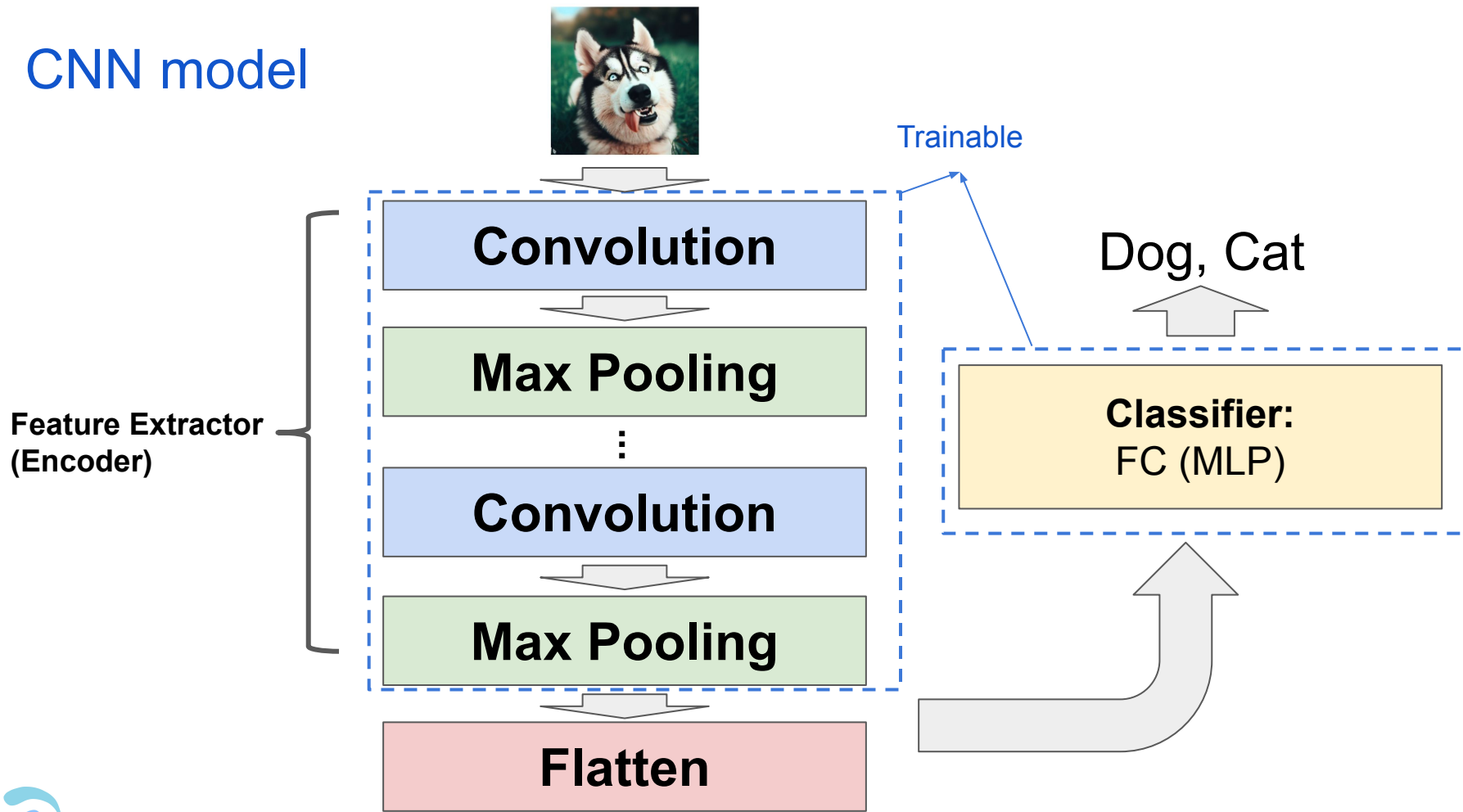


(8, )  
(CxHxW)

# CNN - FC



# CNN model



# Convolution Layer Parameters

0	1	0
0	1	0
0	1	0

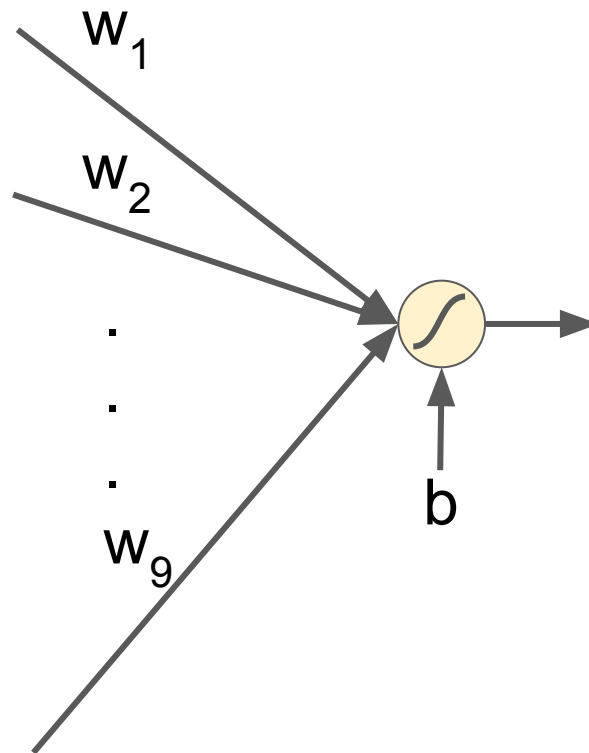
kernel



$w_1$	$w_2$	$w_3$
$w_4$	$w_5$	$w_6$
$w_7$	$w_8$	$w_9$

$b$
-----

Trainable parameters

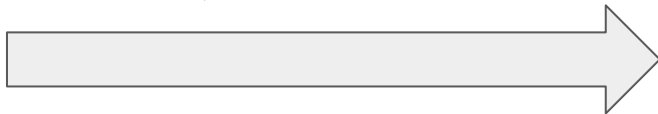


# Convolution v.s. Fully Connected (# of parameters)



(3, 100, 100)

Conv: 1, 3x3 filters



$$\underbrace{(3 \times 3 \times 3)}_{\substack{\text{filter} \\ w \times h \times c}} + 1) \times \underbrace{1}_{\text{bias}} = 28$$

input channels

filter(kernel) count

FC: 1 neurons

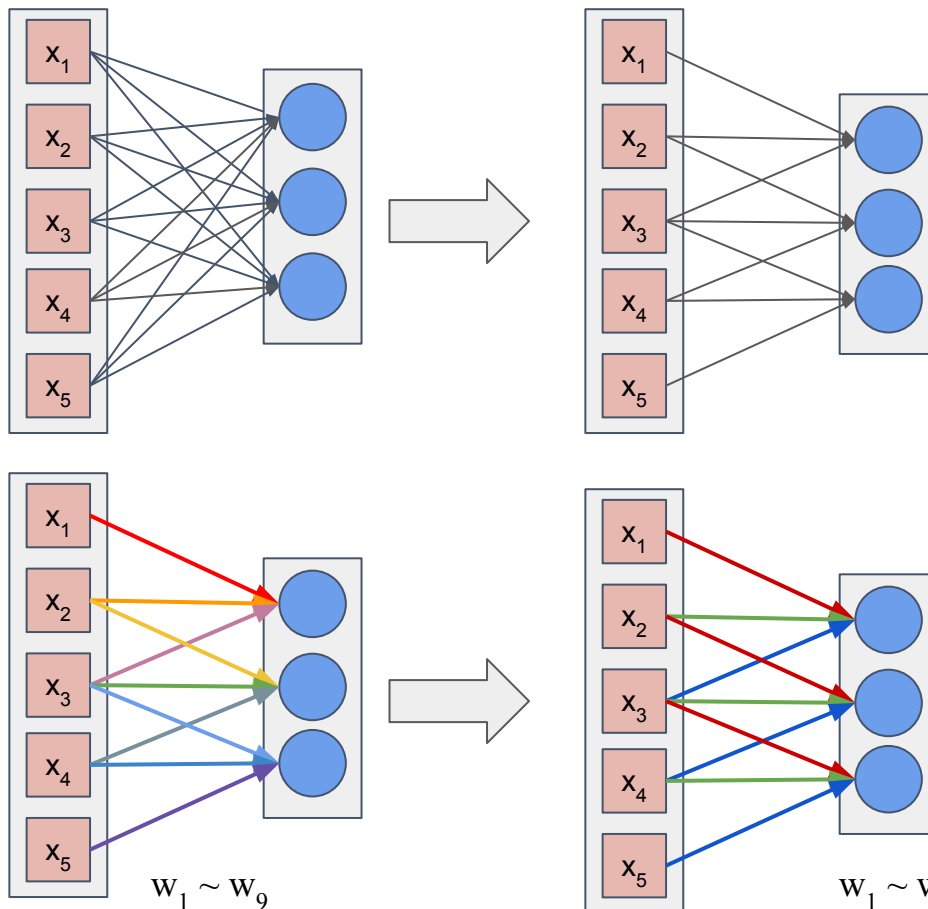


$$\underbrace{(100 \times 100 \times 3)}_{\text{\# of pixels}} + 1) \times \underbrace{1}_{\text{bias}} = 30001$$

neuron count

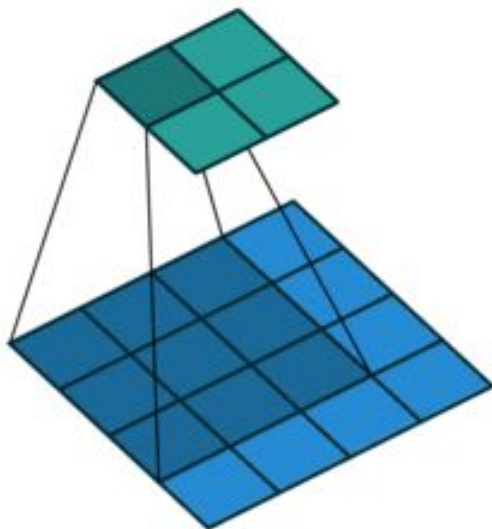
# Convolution

- Local connectivity
  - Neuron connect to **local features**
- Sharing parameters
  - filter use **same parameters** to convolve different region

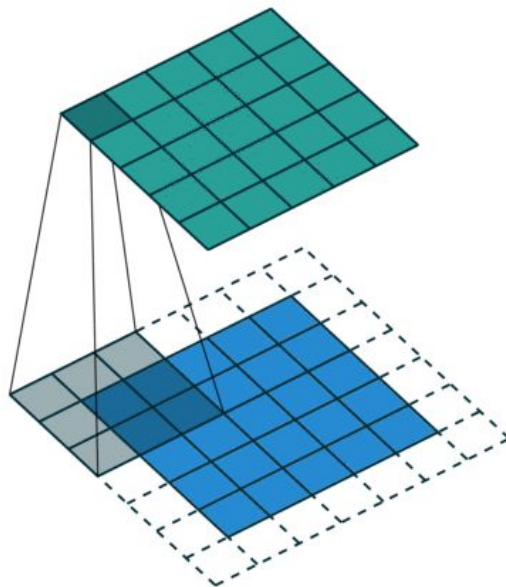


# Convolution: Padding(填充)

- `torch.nn.Conv2d(padding=0)`
- Default: 0, no padding



- `torch.nn.Conv2d(padding='same')`
- `torch.nn.Conv2d(padding=1)`
- $\text{padding} \approx (\text{kernel\_size} - 1) / 2$
- same: input size = output size



[source](#)

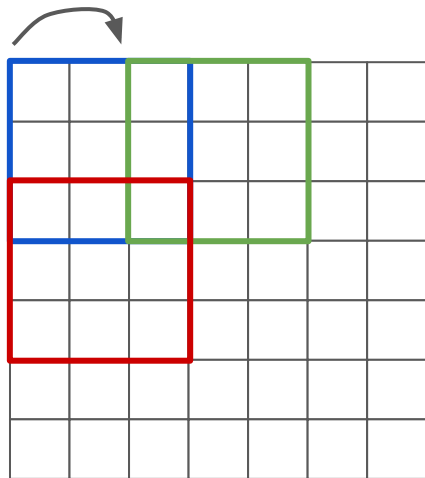
# Stride (歩長)

- Trainable **Pooling** layer
- Default: 1

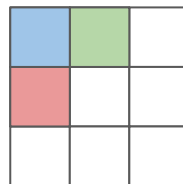


```
torch.nn.Conv2d(C1, C2, strides=2)
```

strides = 2



$(C_1, 7, 7)$

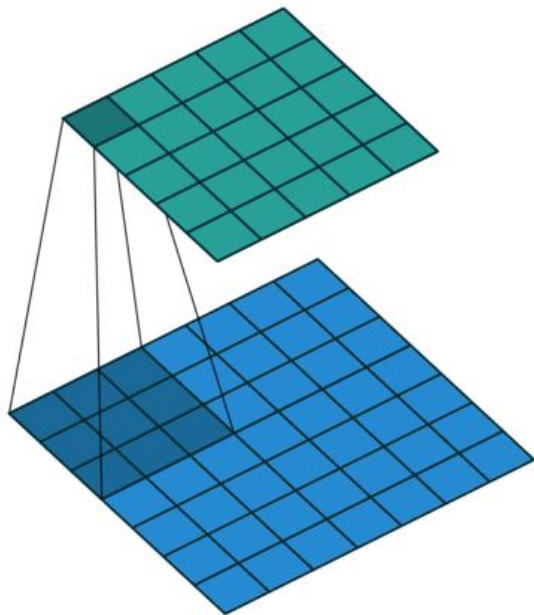


$(C_2, 3, 3)$   
 $\approx (C_2, H/2, W/2)$

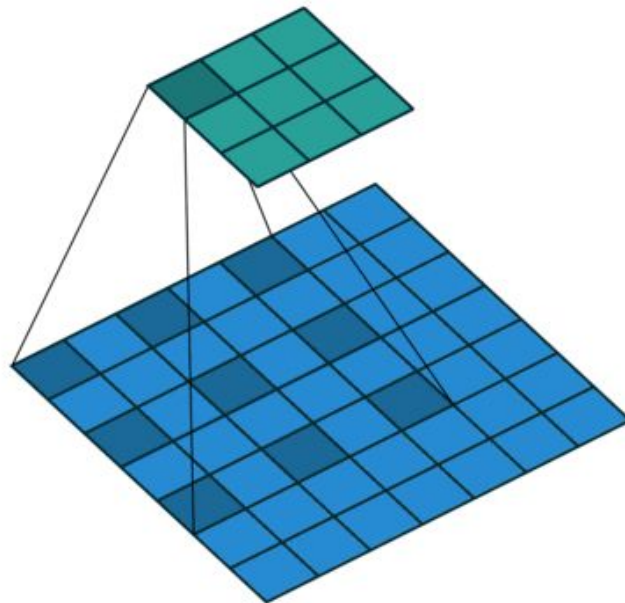


# Convolution: Dilation

- Increase the **receptive field**

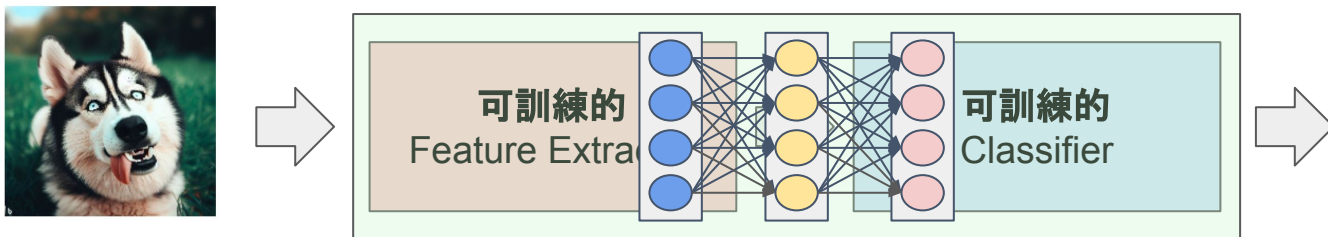
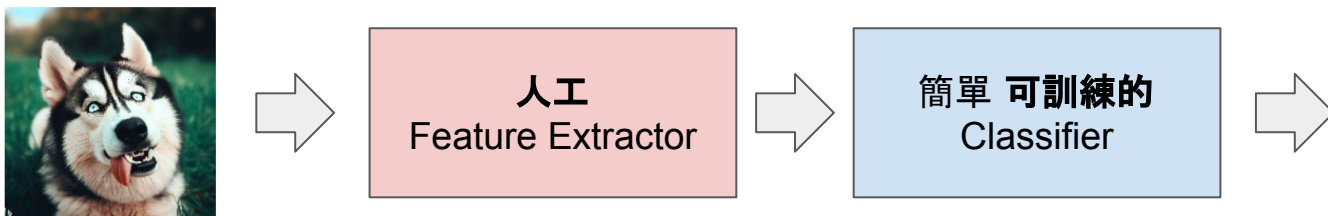
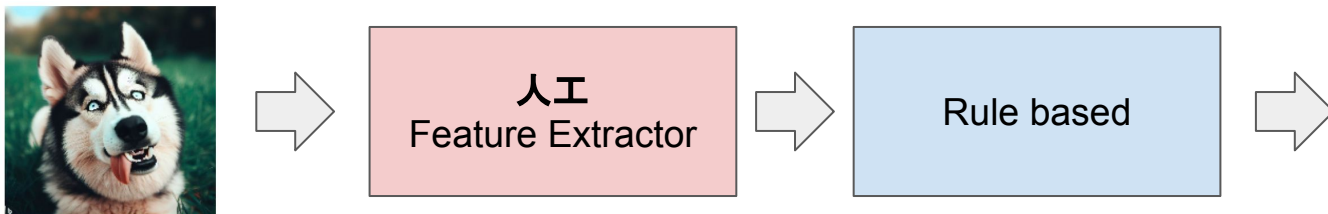


`torch.nn.Conv2d(dilation=1)`

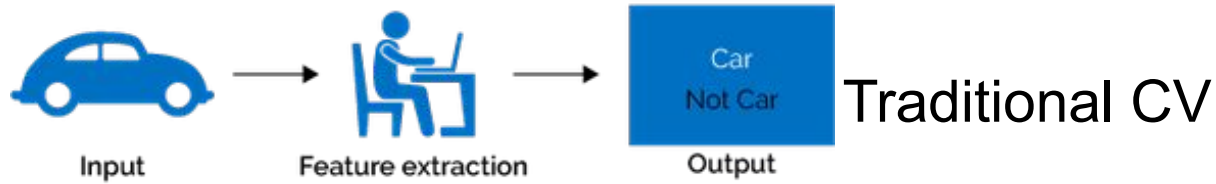


`torch.nn.Conv2d(dilation=2)`

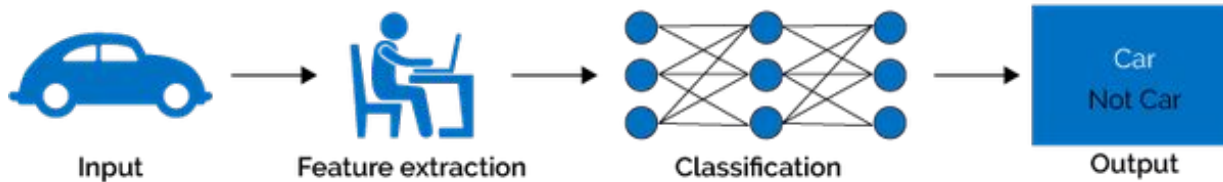
# Traditional v.s ML v.s DL



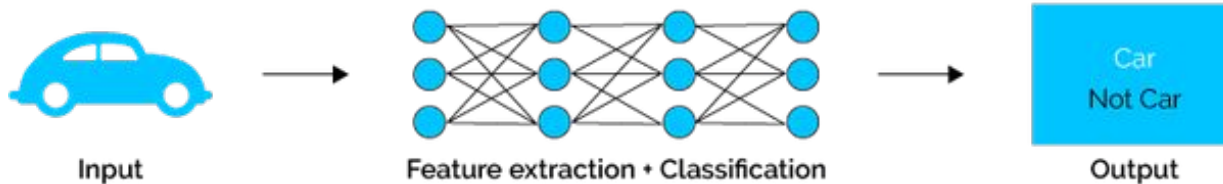
# End-to-end Training



## Machine Learning

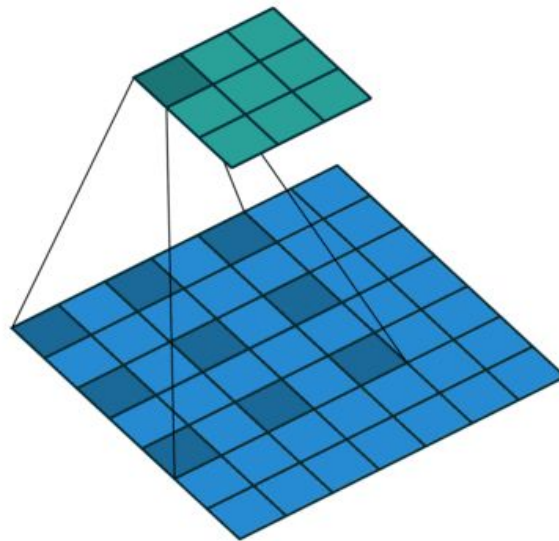
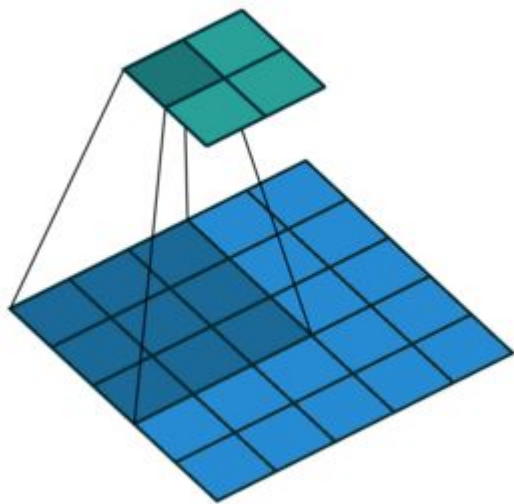


## Deep Learning



# Materials

- Convolution Animation
- [https://github.com/vdumoulin/conv\\_arithmetic](https://github.com/vdumoulin/conv_arithmetic)

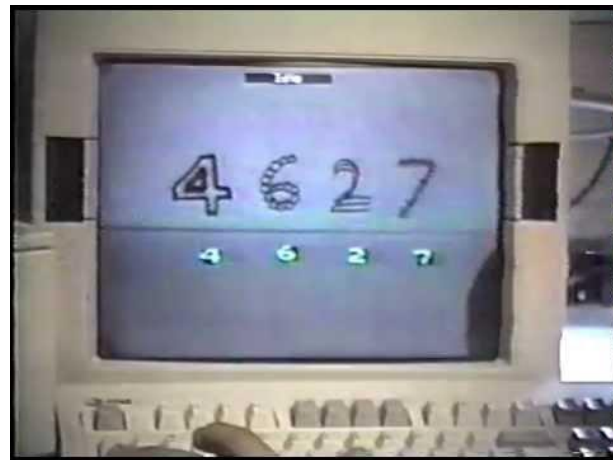


# Summary

- 什麼是卷積層？
- 卷積神經網路架構
  - Conv.
  - Maxpooling
  - Flatten
  - Classifier
- 卷積神經網路參數

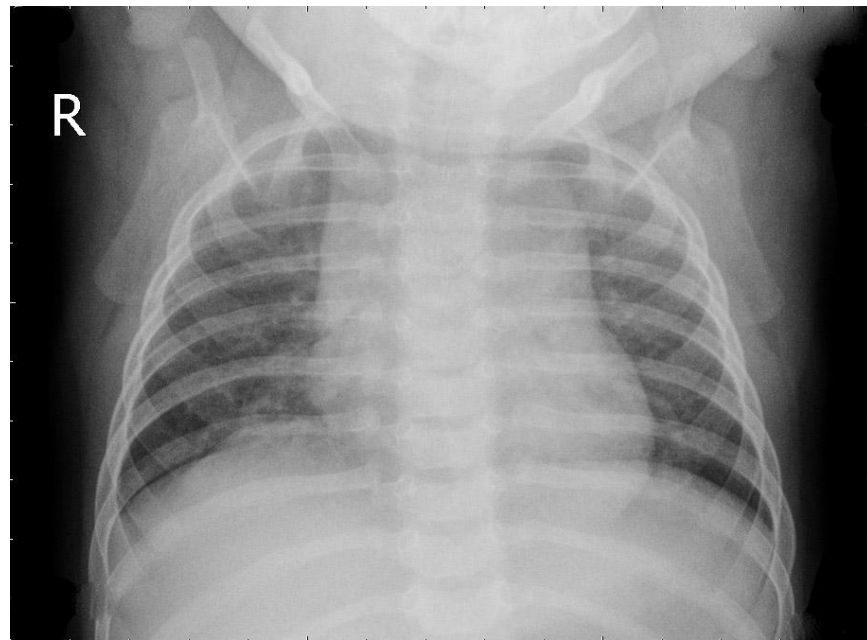


Yann LeCun

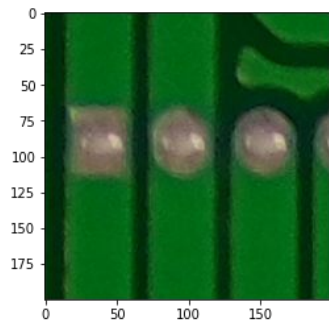
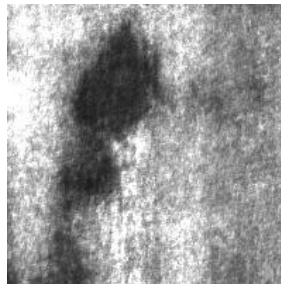
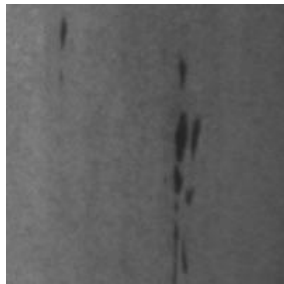
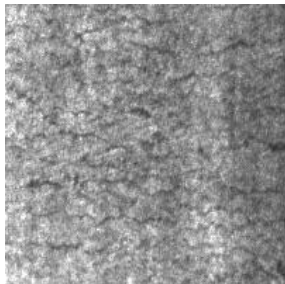


Convolutional Network Demo from 1993  
[https://youtu.be/FwFduRA\\_L6Q](https://youtu.be/FwFduRA_L6Q)

# Exercise: Pneumonia Classification

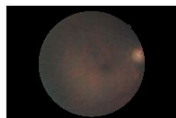


# Exercise: Defect Classification

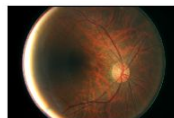


# HW Retinopathy Classification

- Kaggle link:
- <https://www.kaggle.com/c/diabetic-retinopathy-classification-3>
- 5 classes classification: 0~4



0 (0)



0 (0)



1 (1)



0 (0)



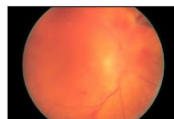
3 (3)



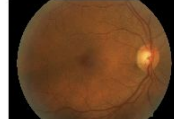
0 (0)



0 (0)



4 (4)

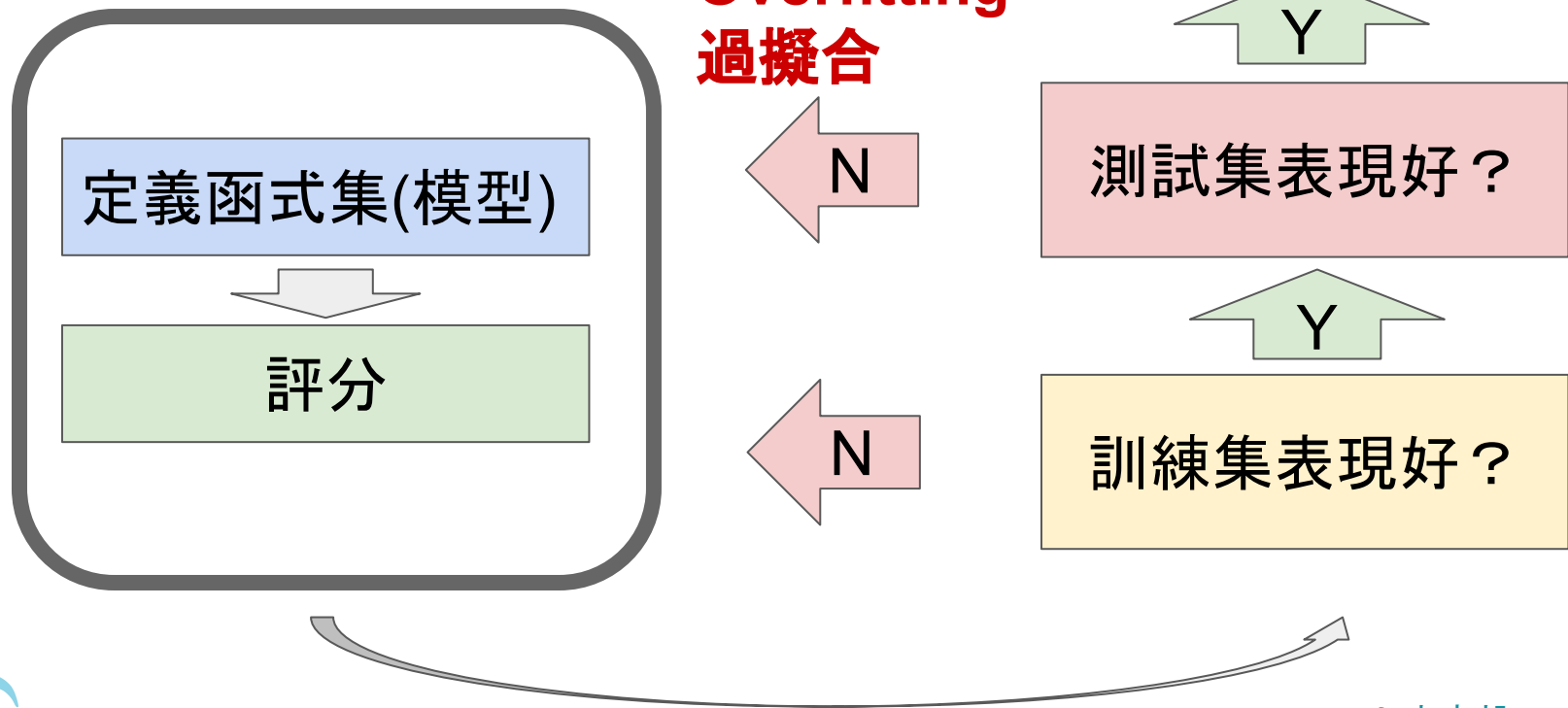


0 (0)

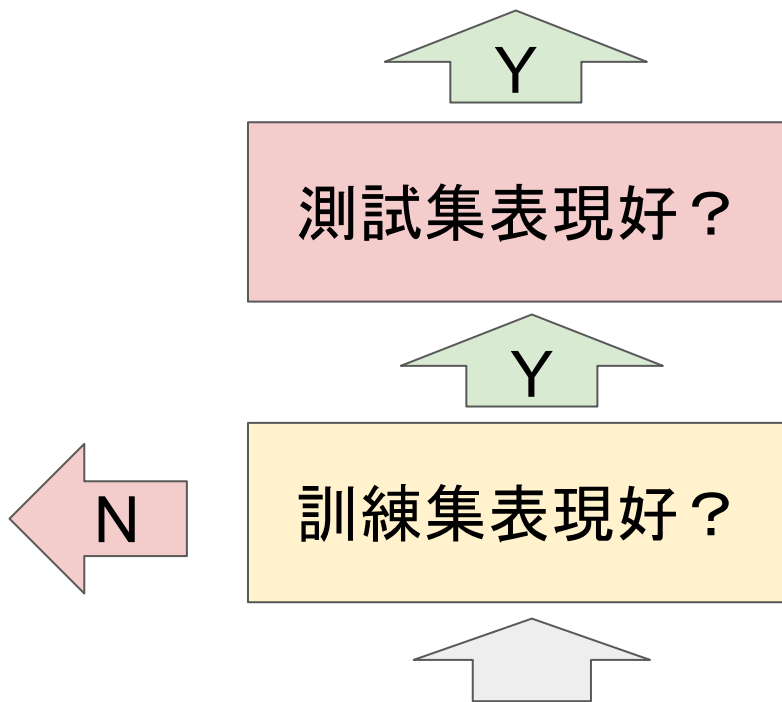
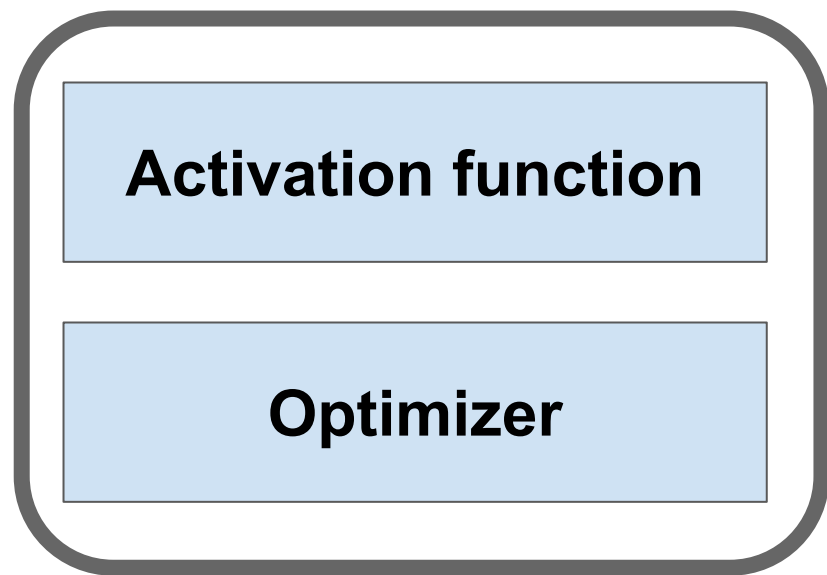


# Deep Learning Training Tips

# Training Process



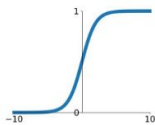
# Training Process



# Activation Function

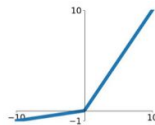
## Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



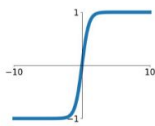
## Leaky ReLU

$$\max(0.1x, x)$$



## tanh

$$\tanh(x)$$

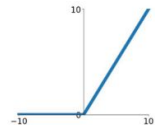


## Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

## ReLU

$$\max(0, x)$$



## ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

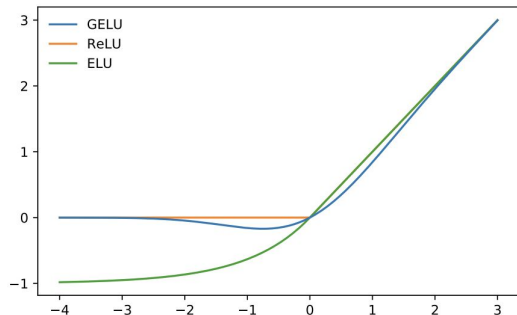
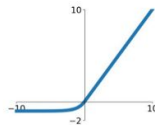


Figure 1: The GELU ( $\mu = 0, \sigma = 1$ ), ReLU, and ELU ( $\alpha = 1$ ).



Sigmoid (0~1)

tanh (-1 ~ 1)

ReLU

LeakyReLU


ELU

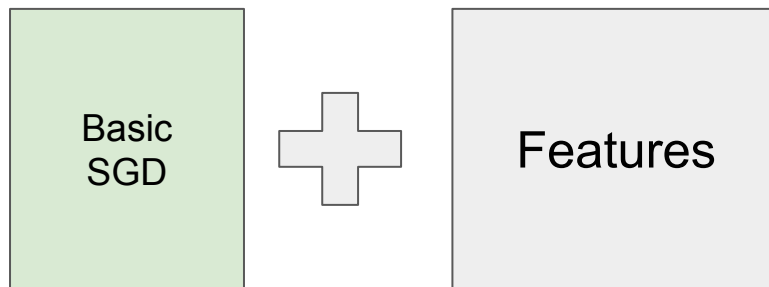
GELU

Mish

...

# Optimizer - Learning rate

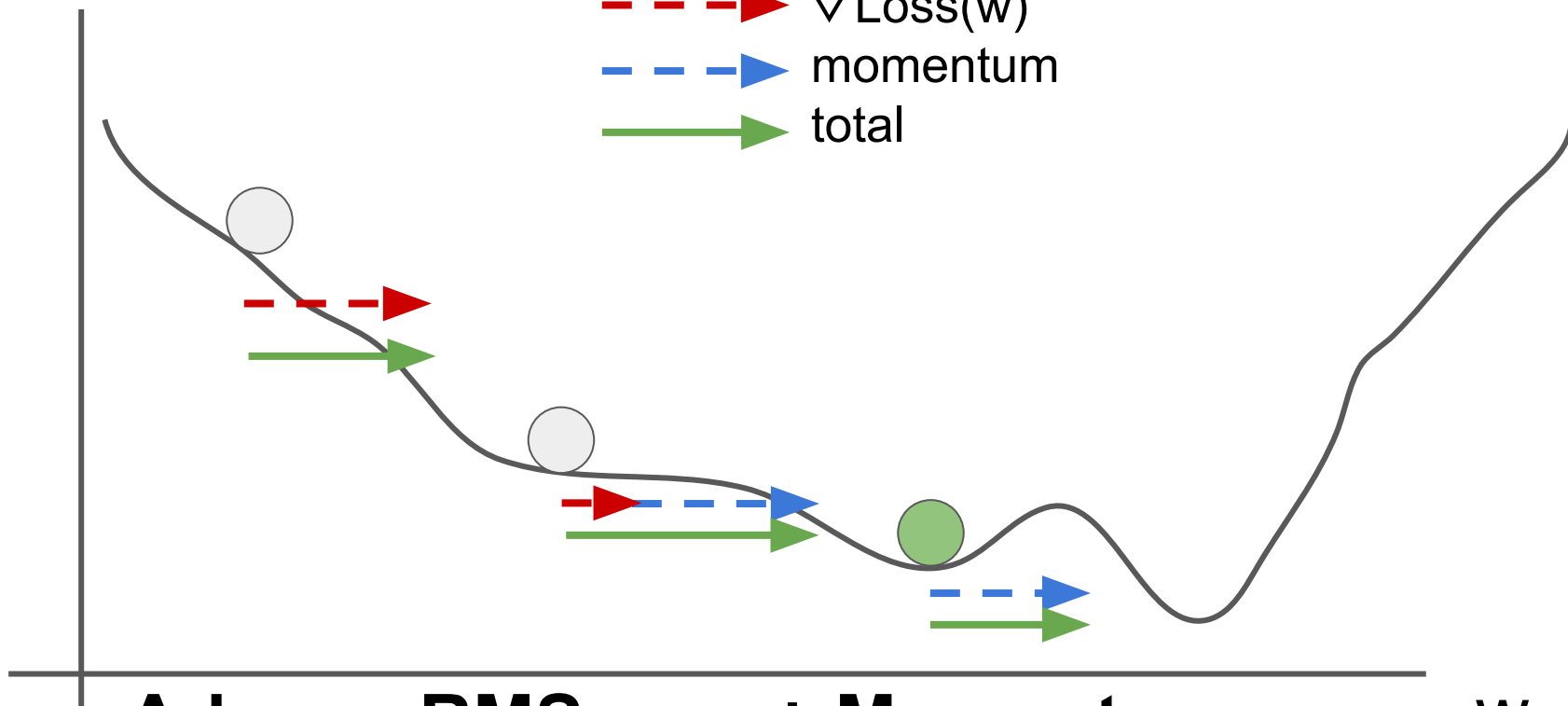
- [torch.optim](#)  PyTorch
- SGD (Stochastic Gradient Descent)
- **Adam, AdamW**
- Adagrad (Adaptive Learning Rate)
- RMSprop
- **Ranger, [Ranger21](#)**



# Momentum

Loss

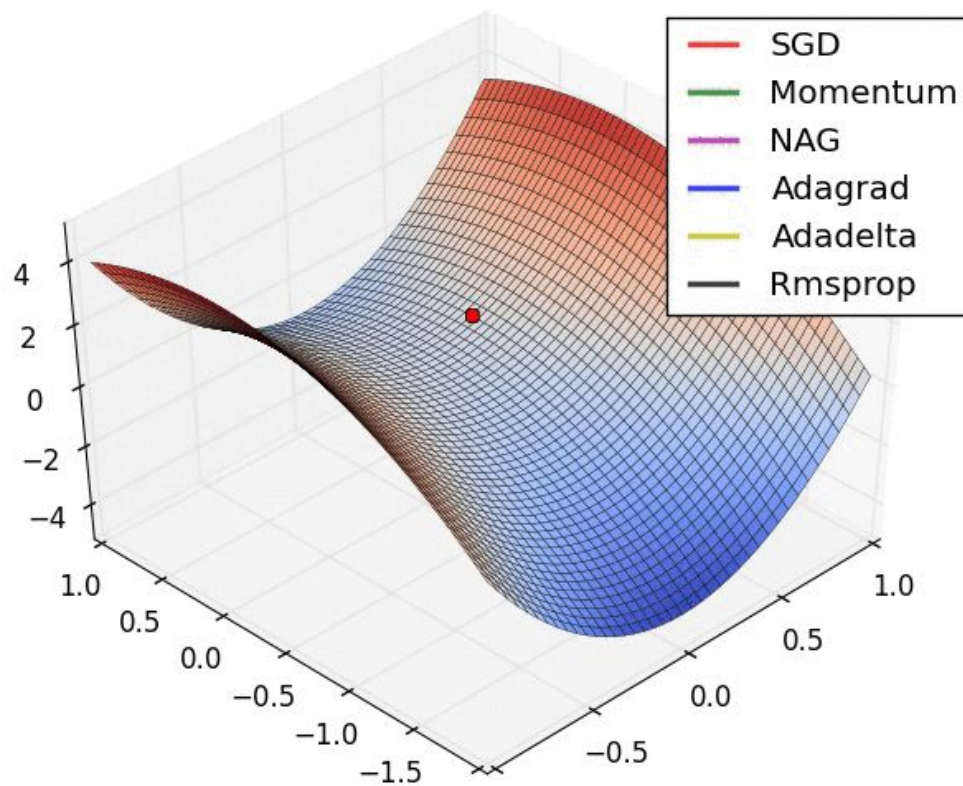
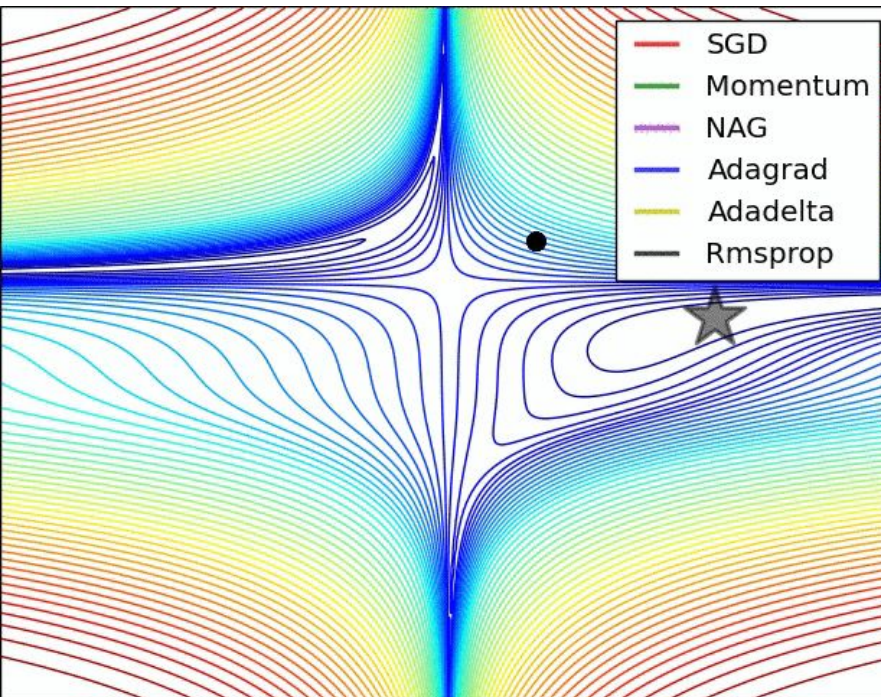
-   $\nabla \text{Loss}(w)$
-  momentum
-  total



**Adam = RMSprop + Momentum**

**w**

# Optimizer



# Training Process

Early stop

Regularization

Dropout

Overfitting  
過擬合

N

測試集表現好？

Y

Y

訓練集表現好？

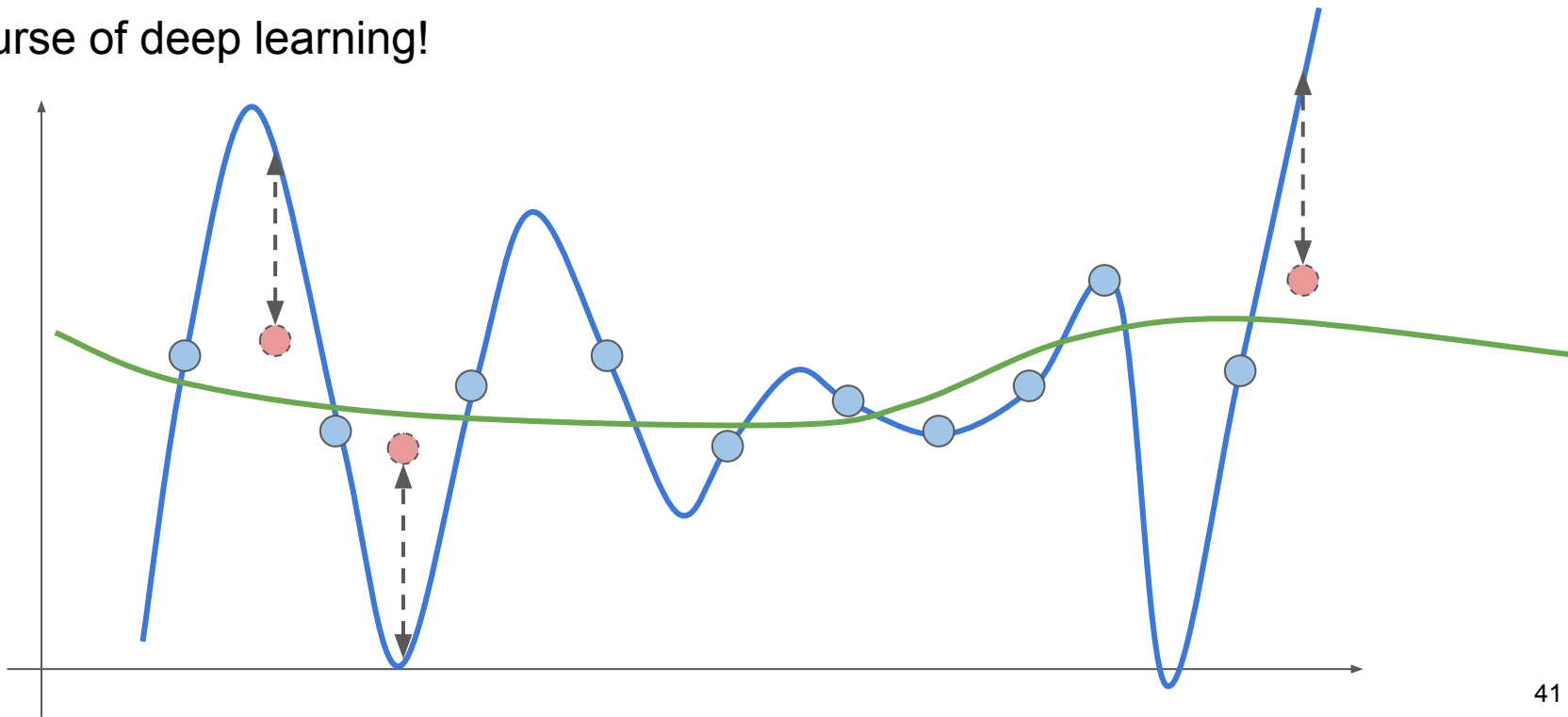


# Overfitting (過擬合): Regression

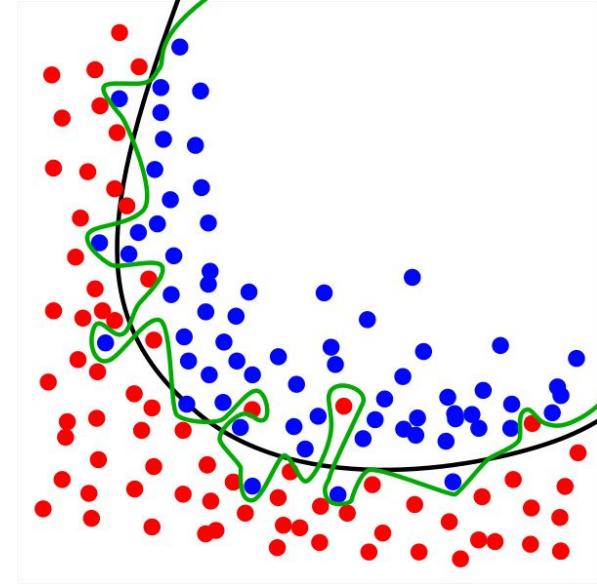
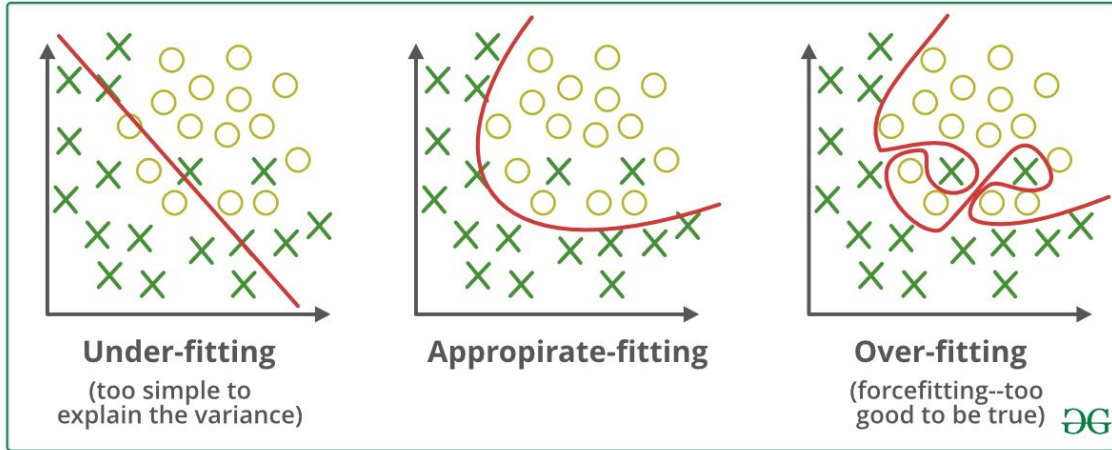
Training loss  $\downarrow$ , Test/Validation loss  $\uparrow$

The curse of deep learning!

- Training data
- Validation / Test data
- Simple model
- Deep learning model



# Overfitting : Classification



# Early stop

IF improved:

keep training

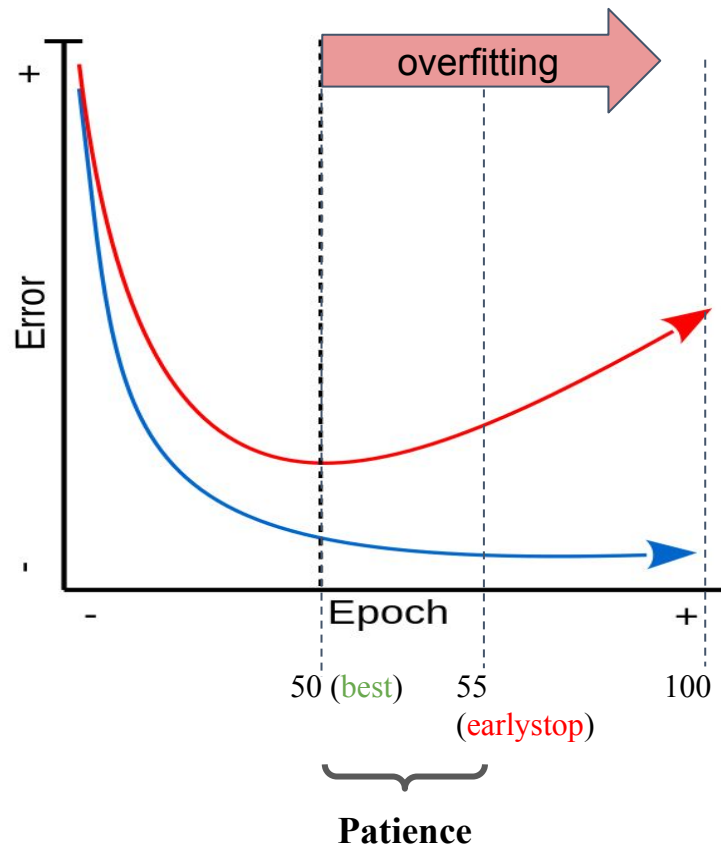
ELSE:

IF no improvement after **patience** epochs

**stop** training

ELSE

keep training

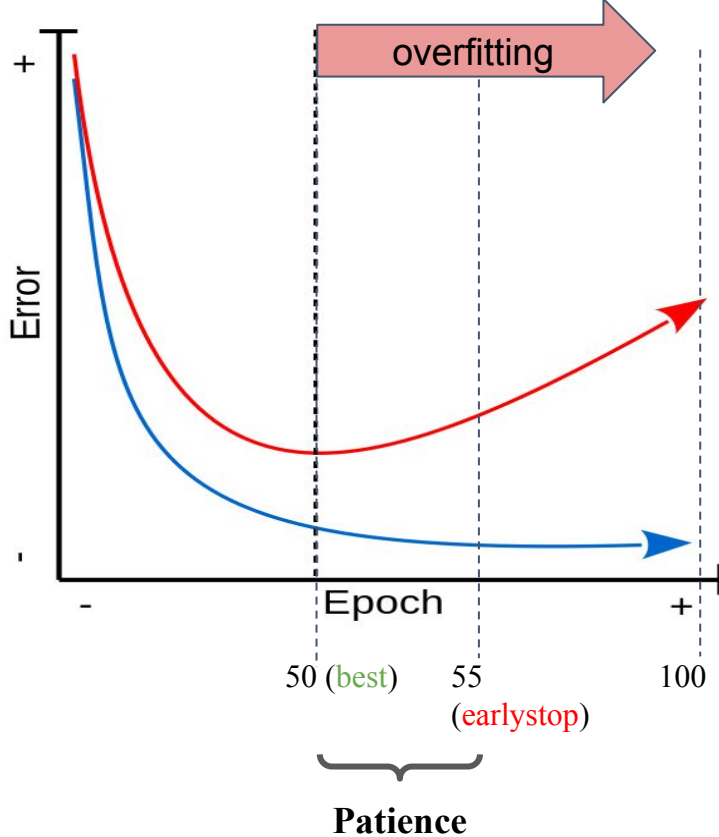


# Early stop



Error

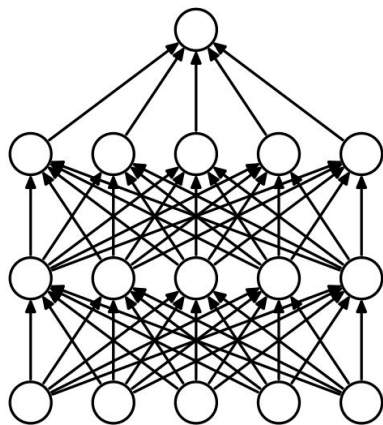
```
1 EPOCHS = 50
2 # Earlystopping
3 patience = 5
4 earlystop_counter = 0
5 best_loss = np.inf
6
7 for epoch in tqdm(range(EPOCHS)):
8     train_loss, train_acc = train(dataloader_train, model, optimizer)
9     val_loss, val_acc = test(dataloader_val, model)
10
11     # Earlystopping
12     if val_loss < best_loss:
13         earlystop_counter = 0
14         best_loss = val_loss
15     else:
16         earlystop_counter += 1
17     if earlystop_counter >= patience:
18         print('Early stop!')
19         break
```



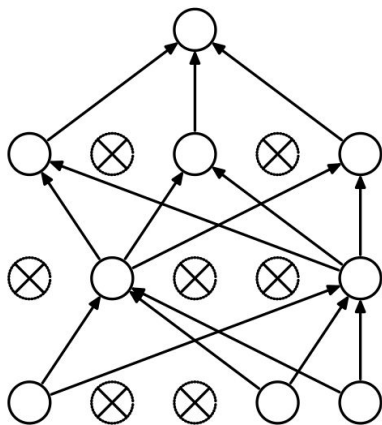
also save best model

# Dropout

- Sub-network with less parameters
- Reduce over fitting
- [torch.nn.Dropout](#)
- $p$ : probability of an element to be zeroed. Default: 0.5



(a) Standard Neural Net

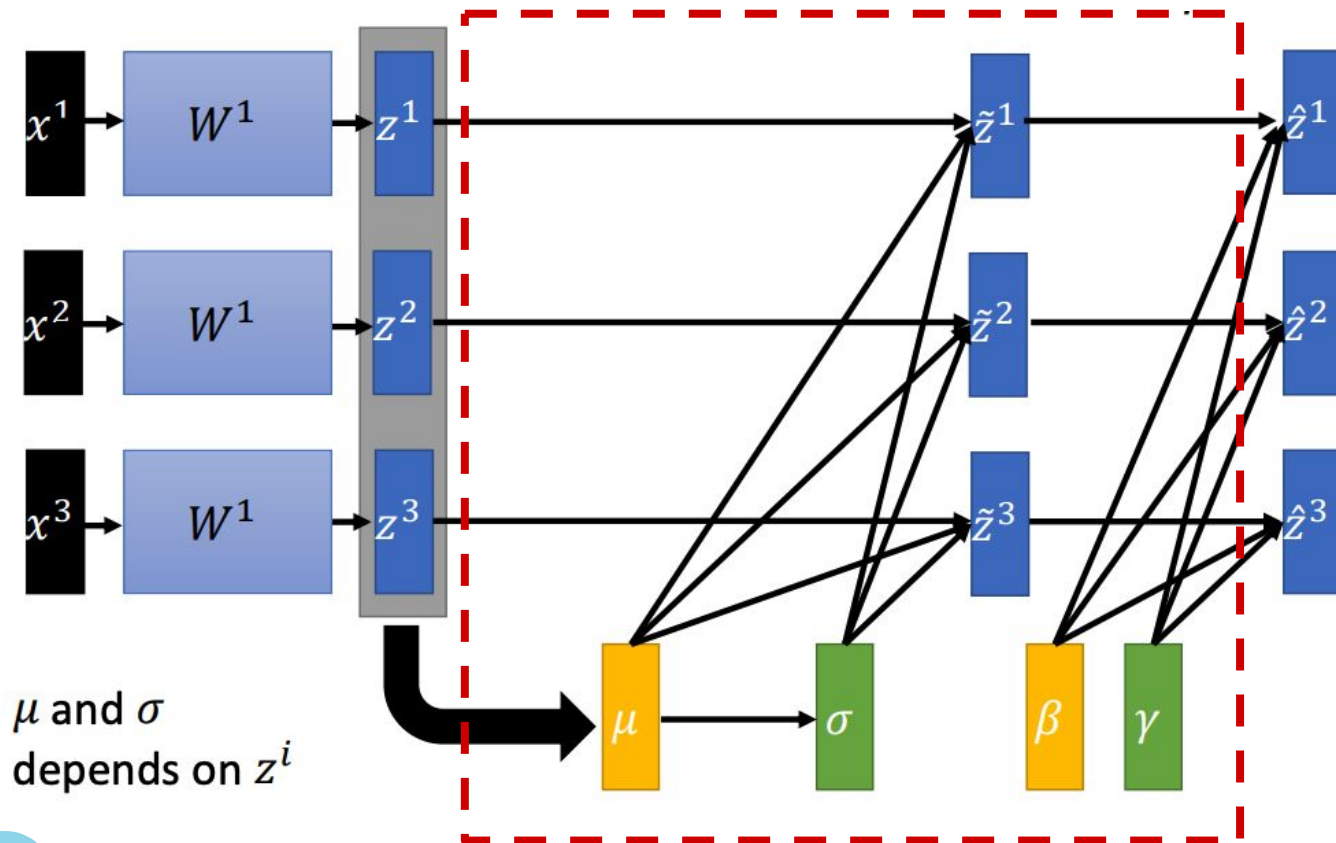


(b) After applying dropout.

 PyTorch

```
classifier = nn.Sequential(  
    nn.Linear(100, 64),  
    nn.ReLU(),  
    nn.Dropout(p=0.3),  
    nn.Linear(64, 3)  
)
```

# Batch Normalization



$$\tilde{z}^i = \frac{z^i - \mu}{\sigma}$$

$$\hat{z}^i = \gamma \odot \tilde{z}^i + \beta$$

$\mu$ : mean

$\sigma$ : std

$\gamma, \beta$ : learnable params

# Normalizations Layers



- Batch Normalization
- Layer Normalization
- Instance Norm
- Group Norm

```
nn.Conv2d(1, 16, 3),  
nn.BatchNorm2d(num_features=16),  
nn.ReLU(),  
nn.Conv2d(16, 16, 3),  
nn.BatchNorm2d(16),  
nn.ReLU(),
```

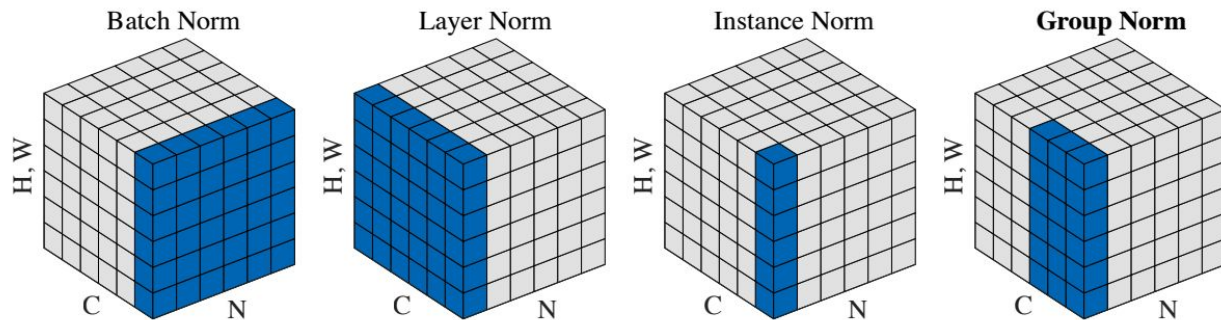





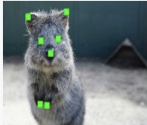
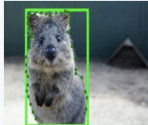








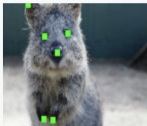
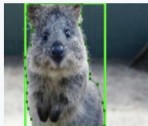



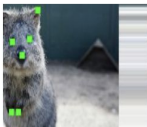
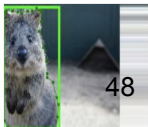
Figure 2. **Normalization methods.** Each subplot shows a feature map tensor, with  $N$  as the batch axis,  $C$  as the channel axis, and  $(H, W)$  as the spatial axes. The pixels in blue are normalized by the same mean and variance, computed by aggregating the values of these pixels.



# Data Augmentation

1. Generate more data by some techniques
2. Make model more robust
3. Frameworks

- a. [torchvision.transforms](https://pytorch.org/docs/stable/torchvision/transforms.html)
- b. imgaug: <https://github.com/aleju/imgaug>
  - i. Segmentation maps
  - ii. bounding boxes
  - iii. ...
- c. [albumentations](https://github.com/albumentations-team/albumentations)
- d. Others

	Image	Heatmaps	Seg. Maps	Keypoints	Bounding Boxes, Polygons
Original Input					
Gauss. Noise + Contrast + Sharpen					
Affine					
Crop + Pad					



# imgaug

```
1 # augmentation
2 seq = iaa.Sequential([
3     iaa.Fliplr(0.5), # 50% horizontal flip
4     iaa.Flipud(0.5), # 50% vertical flip
5     iaa.Affine(
6         rotate=(-10, 10), # random rotate -45 ~ +45 degree
7         shear=(-16, 16), # random shear -16 ~ +16 degree
8         scale={"x": (0.8, 1.2), "y": (0.8, 1.2)} # scale x, y: 80%~120%
9     ),
10 ])
```

```
# Augment 1 image
```

```
img_aug = seq.augment_image(img)
```

```
# Augment images (batch size = 4)
```

```
img_batch = np.stack([img]*4) # (4, 60, 184, 3)
```

```
img_aug_batch = seq.augment_images(img_batch)
```

# torchvision.transforms

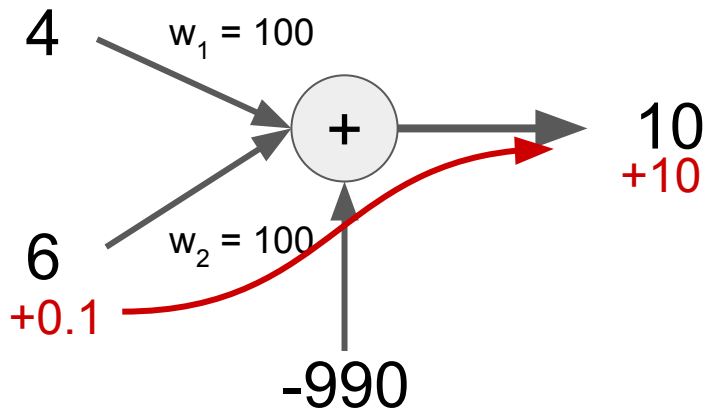
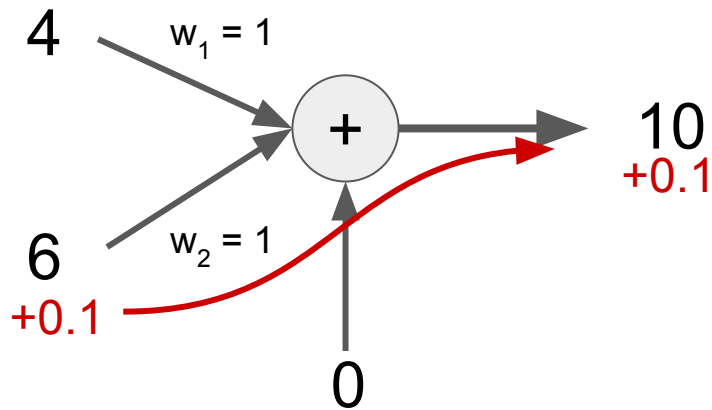
- [Illustration of transforms](#)
- [Tensor transforms and JIT](#)

Original image



# Regularization (正則化)

- Reduce overfitting
- Reduce influence of **noise**



 PyTorch [How to use L1, L2 and Elastic Net regularization with PyTorch?](#)