(a) truth table

```
(a) truth table
x1| x2| x3| x4| a | b | c | z |
0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 |
0 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
1 | 1 | 1 | 0 | 1 | 0 | 1 | 1 |
0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
1 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
1 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 |
```

(b) the number of stuck-at faults detected by each of the 16 input vectors.

```
input vector 0 number of stuck-at faults 1 input vector 1 number of stuck-at faults 1 input vector 2 number of stuck-at faults 3 input vector 3 number of stuck-at faults 1 input vector 4 number of stuck-at faults 3 input vector 5 number of stuck-at faults 3 input vector 6 number of stuck-at faults 3 input vector 7 number of stuck-at faults 1 input vector 8 number of stuck-at faults 5
```

```
input vector 9 number of stuck-at faults 4
input vector 10 number of stuck-at faults 8
input vector 11 number of stuck-at faults 4
input vector 12 number of stuck-at faults 6
input vector 13 number of stuck-at faults 8
input vector 14 number of stuck-at faults 6
input vector 15 number of stuck-at faults 5
```

(c) average number of stuck-at faults detected by an input vector.

```
average number: 3
```

(d) the input vector that detects the maximum number of faults.

```
maximum number: 8 fault detect list : x1\_SA1 \qquad x2\_SA0 \qquad x4\_SA0 \qquad y22\_SA0 \qquad a\_SA1 \qquad a\_SA1 \qquad c\_SA1 \qquad z\_SA1
```

(e) the average number of test patterns for a fault.

```
average number: 6
```

(f) the hardest-to-detect fault

```
test input signal name y21 detect number 3 test input signal name y22 detect number 3
```