# R Notebook

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### 1 Paramétrage de la session

```
setwd('/home/julien1/Documents/BenoitBankMondial')
```

Option de mise en cache des chunks

#### 1.1 Chargement des librairies

```
library(foreach)
library()

## Warning in library(): library '/usr/lib/R/site-library' contains no packages

library(openxlsx) #pour la lecture des fichiers excels

library(foreach)
library(leaps) # pour la sélection de modèles

library(magrittr)

#install.packages('kableExtra')
#library(kableExtra)
```

#### 1.2 Chargement des données

```
X <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=2)
X.all <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=1)
X.eur <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=6)
X.noneur <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=7)
X.grandes <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=10)
X.petites <- read.xlsx("BDD_DEF_10mars2021++_2.xlsx", colNames=TRUE, rowNames = F, sheet=11)
#list.files()</pre>
```

#### 1.3 Fonctions

#### 1.3.1 de bootstrap

Définition d'une fonction de bootstrap qui affiche les valeurs de coefficients, les intervalles de confiance bilatéraux à 95% des coefficients de la régression dans Estim\_2.5 et Estim\_97.5 , la pval de la reg unique, le pval\_90 maximum avec son quantile à 90%. Affiche aussi le r2 ajusté minimum quantile à 5% et le r2 ajusté médian.

```
bootstrap <- function(f, data, boot=500){
cat('-----\n')
cat('Regression : ');print(f)
   sss <- summary(lm(formula = f, data=data))
   reg.coeff <- sss$coefficients[,c(1,4)]
   nvars <- length(attr(terms(f),"term.labels"))+1 # nb de variables dans le modèle, avec intercept
   foreach(i=1:boot,.combine=cbind)%do%{
   ind.boot <- sample(1:nrow(X), replace=T)
   reg <- lm(formula = f, data=X[ind.boot,])
   ss <- summary(reg)
   c( ss$coefficients[,1], # récupère la valeur des coeffs</pre>
```

```
r2.adj = ss$adj.r.squared, # récupère le r carré ajusté
        ss$coefficients[,c(4)] # récupère la p.value de chaque coef
}-> pvals.full # tableau des 500 coef, pvaleurs et r2 adj de tous les coeffs et de chaque modèle
pvals_0.9 <- apply(</pre>
  pvals.full[(nrow(pvals.full)-nvars+1):nrow(pvals.full),],
  1,
  quantile, probs=c(0.9)
  ) # pvals de chaque coef de chaque variable
Estim_2.5 <- apply(</pre>
  pvals.full[1:nvars, ],
  1,
  quantile, probs=c(0.025)
Estim_{97.5} \leftarrow apply(
  pvals.full[1:nvars, ],
  quantile, probs=c(0.975)
print(data.frame(
      Estim= round(reg.coeff[,1],2),
      pval = round(reg.coeff[,2],4),
      stars = star(reg.coeff[,2]),
      Estim_2.5 = round(Estim_2.5,2),
      Estim_97.5 = round(Estim_97.5, 2),
      pval_90 = round(pvals_0.9,4),
      stars_90 = star(pvals_0.9)
  )
 #print(req.coeff)
  r2.adj.boot <- quantile(pvals.full[nvars+1, ], probs=c(0.05,0.5))
  cat(" r2 ajusté :\t",
      sss$adj.r.squared ,
      "\t quantile 5% =",
      r2.adj.boot[1],
      " \t quantile 50% =",
      r2.adj.boot[2],"\n")
}
```

#### 1.3.2 de sélection de modèles

Fonction de sélection de variables dans les modèles

```
select.lm <- function(formula, data, nvmax=7 ){
  verbose=FALSE
  cat('-----\n')
  cat('Regression : '); print(formula)

selection <- regsubsets(x=formula, data=data, nvmax=nvmax, method='forward') # dans leaps
  if(verbose)print(selection)
  summary(selection) -> selection.summary
# selection.summary # pour afficher
```

```
for(crit in c('bic', 'adjr2', 'cp')){
    cat('Selected by ',crit,'\t -
    num.var <- which.min(selection.summary[[crit]]) # min bic et cp</pre>
    # mais max pour le r2 ajusté
        if(crit=='adjr2')num.var <- which.max(selection.summary[[crit]])</pre>
    #coef(selection, num.var) # print names of selected vars and their coef
    xvars <- paste(names(coef(selection,num.var))[-1],collapse='+')</pre>
    if(verbose)print(xvars)
    reg.formula <- formula(paste(y,'~',xvars))</pre>
    if(verbose)print(reg.formula)
    # Re-adjust the linear model
    reg.leaps <- lm(reg.formula, data=data)</pre>
    # and print the informations
    if(verbose)print(summary(reg.leaps))
    print(cbind(
        summary(reg.leaps)$coefficients[,c(1,4)]%>%round(4) ,
        star=star(summary(reg.leaps)$coefficients[,c(4)])
        ), quote=FALSE
    )
    cat('adj.r.squared = ',broom::glance(reg.leaps)[['adj.r.squared']],' p.value = ',broom::glance()
  }
}
# A VERIFIER
#select.lm(CDP ~ CEF + EPI + Taille + Croiss + Année+EUR, data=X.eur, nvmax=7)
```

## 2 Stats descriptives (+ outils Antoine)

#### 2.1 Paramètres statistiques

```
library(foreach)
#summary(X[,-(1:6)])
foreach(k=7:ncol(X), .combine=rbind)%do%{
  c(colnames(X)[k],
     as.vector(round(summary(X[,k]),2))[1:6],
     round(sd(X[,k], na.rm=T),2) )
} -> stat.summary
ncol(stat.summary)
## [1] 8
colnames(stat.summary) <- c('Variable','Min','1st Q', 'Median', 'Mean', '3rd Q','Max','SD')</pre>
rownames(stat.summary) <- NULL</pre>
as.data.frame(stat.summary)
##
      Variable Min 1st Q Median Mean 3rd Q
                                              Max
## 1
          FEF 9.03 9.94 10.24 10.16 10.42 10.85 0.37
                             9.77 9.67
## 2
          CEF 8.51 9.41
                                           10 10.5 0.43
## 3
          CDP
                  0
                               6 5.24
                                           7
                                                 8 2.45
## 4
          GRI
                         1
                                2 4.65
                                                 18 4.69
                  0
                                           9
```

```
## 5
            ΙV
                         8
                               13 11.54
                                           15
                                                 22 5.1
## 6
         ERSE
                   0
                         0
                                1 1.08
                                            2
                                                 5 1.21
## 7
         ERSEc
                   0
                         0
                                2 2.59
                                                 11 2.35
                                0 0.63
## 8
          ECL
                   0
                         0
                                                  8 1.23
                                            1
## 9
          ECLc
                   0
                      0.75
                              1.5 2.96
                                            4
                                                 16 3.37
## 10
           COT
                   0
                                2 1.97
                                            3
                                                  4 0.97
                         1
## 11
                         0
                                0 0.49
                   0
                                            1
           EPI 50.74 72.18 80.59 78.54 85.06 88.91 9.54
## 12
## 13
        Taille 11.64 11.91 12.16 12.13 12.35 12.57 0.25
                              0.5
## 14 Taille.1
                   0
                         0
                                    0.5
                                            1
                                                  1 0.5
## 15
        Croiss -0.36 -0.02
                             0.03 0.02 0.06 0.32 0.07
         Renta -1.32 0.27
## 16
                             0.48 0.53 0.87 1.31 0.42
```

#### 3 Tests Wilcoxon

#### 3.1 Loading package of the article on github

```
library(devtools)
#devtools::install_github('Julien-Bousquet/Benoit-Jamet-BankInvestmentOnCarbon-2022', force=TRUE) # ins
library(monpackage) #load package of the github
```

#### 3.2 Bootstraped Wilcoxon tests

```
set.seed(1)
names(X)
  [1] "X1"
##
                   "Année"
                              "2016"
                                          "2017"
                                                     "2018"
                                                                 "2019"
                   "CEF"
                              "CDP"
  [7] "FEF"
                                          "GRI"
                                                     "IV"
                                                                 "ERSE"
## [13] "ERSEc"
                   "ECL"
                              "ECLc"
                                          "COT"
                                                     "EUR"
                                                                 "EPI"
## [19] "Taille"
                   "Taille.1" "Croiss"
                                          "Renta"
VARS <- c( 'FEF', 'CEF', 'CDP', 'GRI', 'ECLc', 'EPI', 'Taille', 'Croiss', 'Renta', 'ERSEc')
b <- 500 # Nombre de ré-échantillonnages dans le bootstrap (0=pas de bootstrap)
p <- 0
GROUPS <- c('FEF','CEF','CDP','ECLc','GRI','ERSEc','Taille','EUR','EPI')</pre>
library(foreach)
foreach(g = GROUPS, .combine=rbind, packages='foreach')%do%{
  wilcoxon.cut.test(x=VARS, group=g, bootstrap=b, prop=p, data=X)
}-> AnalyseWilcoxonComplete
## Warning: executing %dopar% sequentially: no parallel backend registered
## p-value is in [ -2.136141e-24 ; -1.784627e-24 ]
## with quantile 50%= 1.800924e-24
## and quantile 95\% = 1.877389e-24
## p-value is in [ -1.099004e-17 ; -3.402509e-24 ]
## with quantile 50%= 8.605133e-22
## and quantile 95%= 1.085108e-19
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.7824077 ; 0 ]
```

```
## with quantile 50\% = 0.001587892
## and quantile 95%= 0.1652361
## p-value is in [ -0.9748608 ; 0.9761986 ]
## with quantile 50%= 0.03397214
## and quantile 95%= 0.7115634
## p-value is in [ -0.9865354 ; 1 ]
## with quantile 50%= 0.04761028
## and quantile 95%= 0.7578511
## p-value is in [ -0.8889091 ; 0.603664 ]
## with quantile 50%= 0.003435192
## and quantile 95%= 0.2105444
## p-value is in [ -0.9468213 ;
                                0.4126687 ]
## with quantile 50%= 0.004659604
## and quantile 95%= 0.2703426
## p-value is in [ -0.988165 ; 0.9898765 ]
## with quantile 50%= 0.01107189
## and quantile 95%= 0.7982568
AnalyseWilcoxonComplete
##
        tested group.by
                         p.value.50 p.value.95
                                                       p.value star
## 50%
                   FEF 1.800924e-24 1.877389e-24 -1.877389e-24 ***
          FEF
## 50%1
          CEF
                   FEF 8.605133e-22 1.085108e-19 -1.084887e-19
                   FEF 1.587892e-03 1.652361e-01 -1.651161e-01
## 50%2
          CDP
## 50%3
          GRI
                   FEF 3.397214e-02 7.115634e-01 -7.114578e-01
                   FEF 4.761028e-02 7.578511e-01 7.574885e-01
## 50%4
        ECLc
                   FEF 6.163585e-02 7.748011e-01 7.747231e-01
## 50%5
          EPI
                   FEF 3.435192e-03 2.105444e-01 -2.103916e-01
## 50%6 Taille
## 50%7 Croiss
                   FEF 4.217319e-01 9.290105e-01 -9.285967e-01
## 50%8 Renta
                   FEF 4.659604e-03 2.703426e-01 -2.701605e-01
## 50%9 ERSEc
                   FEF 1.107189e-02 7.982568e-01 -7.977455e-01
write.csv(AnalyseWilcoxonComplete,
         file='AnalyseWilcoxonComplete.csv',
         row.names = FALSE)
foreach(g = GROUPS, .combine=rbind)%do%{
  wilcoxon.cut.test(x=VARS, group=g, bootstrap=b, prop=0.2, data=X)
}-> AnalyseWilcoxonComplete
## p-value is in [ -1.569721e-19 ; -1.537554e-19 ]
## with quantile 50%= 1.561255e-19
## and quantile 95%= 1.567381e-19
## p-value is in [ -3.333634e-18 ; -1.543591e-19 ]
## with quantile 50%= 2.052587e-19
## and quantile 95%= 6.075783e-19
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -1; 0.6684035 ]
## with quantile 50%= 0.01985137
## and quantile 95%= 0.6099723
## p-value is in [ -0.5744595 ; 0.9757241 ]
## with quantile 50%= 0.002648983
## and quantile 95%= 0.5235668
```

```
## p-value is in [ -1; 0.661164]
## with quantile 50%= 0.01569452
## and quantile 95%= 0.589419
## p-value is in [ -0.2738877 ; 0.1617838 ]
## with quantile 50%= 0.0002361018
## and quantile 95%= 0.04221555
## p-value is in [ -0.6408882 ; 0.2673025 ]
## with quantile 50% = 0.0003543759
## and quantile 95%= 0.06384111
## p-value is in [ -0.9951592 ; 0.9636759 ]
## with quantile 50%= 0
## and quantile 95%= 0.7936062
## p-value is in [ -6.264688e-18 ; -1.540138e-19 ]
## with quantile 50%= 2.417176e-19
## and quantile 95%= 9.312642e-19
## p-value is in [ -1.569428e-19 ; -1.540426e-19 ]
## with quantile 50%= 1.561546e-19
## and quantile 95%= 1.567089e-19
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.7851391 ; 0.9877866 ]
## with quantile 50%= 0.001366678
## and quantile 95%= 0.8003257
## p-value is in [ -0.9832623 ; 0.4722232 ]
## with quantile 50%= 0.01121141
## and quantile 95\% = 0.4747668
## p-value is in [ -0.1824184 ; -2.159677e-10 ]
## with quantile 50%= 5.653717e-05
## and quantile 95%= 0.01878219
## p-value is in [ -0.08284694 ; -4.94739e-12 ]
## with quantile 50%= 3.540096e-05
## and quantile 95%= 0.01067034
## p-value is in [ -0.9975775 ; 0.9782415 ]
## with quantile 50% = 0.005656867
## and quantile 95%= 0.6184863
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -7.528216e-19 ; -1.780815e-20 ]
## with quantile 50%= 1.184985e-19
## and quantile 95%= 2.477816e-19
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
```

```
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.5571468 ; 0.667068 ]
## with quantile 50%= 0.001983048
## and quantile 95%= 0.1846208
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.7980848 ; 1 ]
## with quantile 50%= 0.005195436
## and quantile 95%= 0.2369678
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.9973353 ; 0.9973071 ]
## with quantile 50%= 0
## and quantile 95%= 0.7779006
## p-value is in [ -4.618e-20 ; -2.455991e-21 ]
## with quantile 50%= 2.69911e-20
## and quantile 95%= 3.619981e-20
## p-value is in [ -0.99043; 0.8856296]
## with quantile 50%= 0.01368067
## and quantile 95\% = 0.5080554
## p-value is in [ -0.3009727 ; -1.719622e-12 ]
## with quantile 50%= 7.372723e-05
## and quantile 95%= 0.01425586
## p-value is in [ -0.03185676 ; 0 ]
## with quantile 50%= 8.713685e-07
## and quantile 95%= 0.0005240306
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.932819 ; 0.9602202 ]
## with quantile 50\% = 0
## and quantile 95%= 0.7657781
## p-value is in [ -7.767132e-20 ; -4.453921e-21 ]
## with quantile 50%= 3.230889e-20
## and quantile 95%= 5.771433e-20
## p-value is in [ -1; 0.7399242 ]
## with quantile 50%= 0
## and quantile 95\% = 0.869293
## p-value is in [ -0.9732935 ; 0.8724447 ]
## with quantile 50%= 0.009490918
## and quantile 95\% = 0.3533363
```

```
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.3329054 ; 0.992002 ]
## with quantile 50%= 0.0006535427
## and quantile 95%= 0.0986979
## p-value is in [ -0.1107581 ; -2.313438e-13 ]
## with quantile 50%= 6.237316e-07
## and quantile 95%= 0.0004812098
## p-value is in [ -0.9641457 ; 0.9976076 ]
## with quantile 50%= 0.02480425
## and quantile 95\% = 0.5046973
## p-value is in [ -6.033783e-20 ; -2.29793e-22 ]
## with quantile 50%= 2.212472e-20
## and quantile 95%= 4.660801e-20
## p-value is in [ -0.02002517 ; 0.009792845 ]
## with quantile 50%= 1.943216e-06
## and quantile 95%= 0.0005170075
## p-value is in [ -0.006880268 ; 0.02417127 ]
## with quantile 50%= 9.02919e-08
## and quantile 95%= 0.000121242
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.9678188 ; 0.5155916 ]
## with quantile 50% = 0.003232032
## and quantile 95\% = 0.4455284
## p-value is in [ -0.01871987 ; 0 ]
## with quantile 50%= 3.378314e-06
## and quantile 95%= 0.0008165776
## p-value is in [ -0.9092269 ; 0.3996968 ]
## with quantile 50% = 0.0001371507
## and quantile 95%= 0.05797209
## p-value is in [ -1.571477e-19 ; -1.542439e-19 ]
## with quantile 50%= 1.561546e-19
## and quantile 95%= 1.567089e-19
## p-value is in [ -0.625953 ; 0.9618429 ]
## with quantile 50%= 0.002405528
## and quantile 95\%=0.272461
## p-value is in [ -0.9782398 ; 0.9584765 ]
## with quantile 50% = 0.01063757
## and quantile 95%= 0.7384844
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ 4.963394e-19 ; 6.611539e-07 ]
## with quantile 50%= 1.909668e-13
## and quantile 95%= 5.354863e-10
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ 2.17298e-20 ; 1.370151e-05 ]
## with quantile 50%= 5.657827e-14
## and quantile 95%= 1.385812e-10
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
```

```
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ -0.4358008 ; 0.9567297 ]
## with quantile 50\% = 0
## and quantile 95%= 0.2843814
##
## Please convert groups in reals. Or use bootstrap=0.
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ -0.7311738 ; 0 ]
## with quantile 50%= 0.006781334
## and quantile 95%= 0.3062536
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ -9.745805e-05; 0.0002194797]
## with quantile 50% = 1.844917e-09
## and quantile 95%= 1.641189e-06
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ -0.1527391 ; 0.1356284 ]
## with quantile 50%= 0.0002479528
## and quantile 95%= 0.04274986
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ 2.564105e-09 ; 0.6914656 ]
## with quantile 50%= 0.0002333051
## and quantile 95\% = 0.0265197
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ 5.380267e-23 ; 1.203552e-09 ]
## with quantile 50%= 1.330245e-17
## and quantile 95%= 3.210861e-14
##
## Please convert groups in reals. Or use bootstrap=0.
## p-value is in [ -0.04270856; 0]
## with quantile 50%= 3.062293e-05
## and quantile 95%= 0.004463312
## Warning in wilcoxon.cut.test(x = i, group = group, data = data, prop = prop, :
## Missing data removed.
## p-value is in [ -0.4069763 ; 0 ]
## with quantile 50% = 0.0005479639
## and quantile 95%= 0.05802174
## p-value is in [ -0.9878503 ; 0.8123853 ]
## with quantile 50%= 0.00133547
## and quantile 95\% = 0.2330653
## p-value is in [ -1.342385e-19 ; -7.944237e-20 ]
## with quantile 50%= 1.160588e-19
## and quantile 95%= 1.2642e-19
## p-value is in [ -0.9142935 ; 0.7332504 ]
## with quantile 50%= 0.0006834687
## and quantile 95%= 0.1292318
## p-value is in [ -0.9952295 ; 0.957084 ]
## with quantile 50% = 0.03328887
```

```
## and quantile 95%= 0.6931178
## p-value is in [ 1.645663e-15 ; 0.2080863 ]
## with quantile 50%= 3.782261e-07
## and quantile 95%= 0.0009076896
## p-value is in [ -0.6313064 ; 0.7591189 ]
## with quantile 50%= 0.0005183863
## and quantile 95%= 0.1238266
```

#### AnalyseWilcoxonComplete

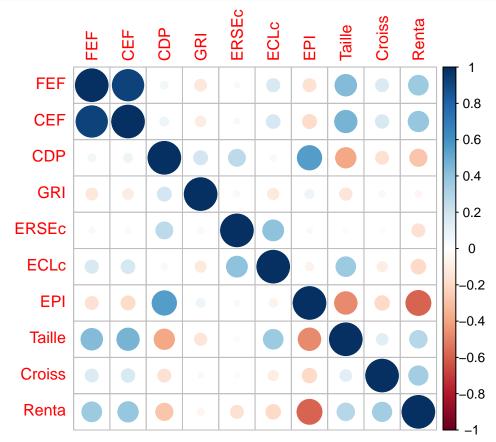
```
##
          tested group.by
                            p.value.50
                                          p.value.95
                                                           p.value star
                      FEF 1.561255e-19 1.567381e-19 -1.567381e-19
## 50%
## 50%1
             CEF
                      FEF 2.052587e-19 6.075783e-19 -6.058060e-19
## 50%2
             CDP
                      FEF 1.985137e-02 6.099723e-01 -6.096492e-01
## 50%3
                      FEF 8.736139e-02 7.899421e-01 -7.895529e-01
             GRI
## 50%4
            ECLc
                      FEF 2.648983e-03 5.235668e-01 5.228658e-01
## 50%5
             EPI
                      FEF 1.569452e-02 5.894190e-01 -5.892139e-01
## 50%6
          Taille
                      FEF 2.361018e-04 4.221555e-02 -4.205946e-02
## 50%7
          Croiss
                      FEF 2.364581e-01 9.240263e-01 9.237889e-01
## 50%8
                      FEF 3.543759e-04 6.384111e-02 -6.377771e-02
           Renta
## 50%9
           ERSEc
                      FEF 0.000000e+00 7.936062e-01 -7.935525e-01
## 50%10
                      CEF 2.417176e-19 9.312642e-19 -9.312227e-19
             FEF
## 50%11
             CEF
                      CEF 1.561546e-19 1.567089e-19 -1.567089e-19
                      CEF 8.655603e-02 8.134423e-01 -8.130886e-01
## 50%21
             CDP
## 50%31
             GRI
                      CEF 1.343553e-01 8.590319e-01 -8.586983e-01
## 50%41
            ECLc
                      CEF 1.366678e-03 8.003257e-01 8.002241e-01
## 50%51
             EPI
                      CEF 1.121141e-02 4.747668e-01 -4.739397e-01
## 50%61
          Taille
                      CEF 5.653717e-05 1.878219e-02 -1.878201e-02
## 50%71
          Croiss
                      CEF 2.017602e-01 8.534232e-01 -8.529535e-01
## 50%81
                      CEF 3.540096e-05 1.067034e-02 -1.066543e-02
           Renta
## 50%91
                      CEF 5.656867e-03 6.184863e-01 6.168073e-01
           ERSEc
## 50%12
             FEF
                      CDP 9.141345e-02 7.877933e-01 -7.872926e-01
## 50%13
             CEF
                      CDP 6.433334e-02 7.184436e-01 7.182011e-01
## 50%22
             CDP
                      CDP 1.184985e-19 2.477816e-19 -2.474958e-19
## 50%32
             GR.I
                      CDP 1.854165e-01 9.110454e-01 9.106257e-01
## 50%42
            ECLc
                      CDP 2.466506e-01 9.394127e-01 -9.394082e-01
## 50%52
             EPI
                      CDP 1.983048e-03 1.846208e-01 -1.845155e-01
## 50%62
          Taille
                      CDP 5.802212e-02 7.574319e-01 7.574319e-01
          Croiss
## 50%72
                      CDP 1.033472e-01 8.580861e-01 8.580859e-01
## 50%82
           Renta
                      CDP 2.398009e-01 8.991983e-01 -8.990693e-01
## 50%92
           ERSEc
                      CDP 5.195436e-03 2.369678e-01 -2.367900e-01
## 50%14
             FEF
                     ECLc 1.635855e-01 8.955892e-01 -8.953531e-01
## 50%15
                     ECLc 1.110716e-01 8.393781e-01 -8.389102e-01
             CEF
## 50%23
             CDP
                     ECLc 0.000000e+00 7.779006e-01 7.778293e-01
## 50%33
             GRI
                     ECLc 2.825270e-01 9.376802e-01 9.374348e-01
## 50%43
            ECLc
                     ECLc 2.699110e-20 3.619981e-20 -3.619583e-20
## 50%53
             EPI
                     ECLc 1.368067e-02 5.080554e-01 5.079705e-01
## 50%63
          Taille
                     ECLc 7.372723e-05 1.425586e-02 -1.423176e-02
## 50%73
                     ECLc 8.453268e-02 8.017255e-01 -8.017253e-01
          Croiss
## 50%83
           Renta
                     ECLc 1.302718e-01 8.295344e-01 8.295341e-01
## 50%93
                     ECLc 8.713685e-07 5.240306e-04 -5.226379e-04
           ERSEc
## 50%16
             FEF
                      GRI 2.473073e-01 9.475581e-01 -9.475580e-01
## 50%17
                      GRI 4.584726e-01 9.428025e-01 9.428025e-01
             CEF
## 50%24
             CDP
                      GRI 0.000000e+00 7.657781e-01 7.654398e-01
## 50%34
                      GRI 3.230889e-20 5.771433e-20 -5.770982e-20
             GRI
```

```
## 50%44
            ECLc
                      GRI 0.000000e+00 8.692930e-01 -8.685286e-01
## 50%54
             EPI
                      GRI 4.242536e-01 9.191158e-01 -9.188801e-01
                                                     9.428023e-01
## 50%64
          Taille
                      GRI 4.265019e-01 9.428023e-01
## 50%74
                      GRI 4.247538e-01 9.382821e-01
                                                      9.380442e-01
          Croiss
## 50%84
           Renta
                      GRI 3.193686e-01 9.287628e-01
                                                      9.285252e-01
## 50%94
           ERSEc
                      GRI 9.490918e-03 3.533363e-01
                                                      3.532759e-01
## 50%18
             FEF
                    ERSEc 5.030836e-01 9.428022e-01
                                                      9.428021e-01
## 50%19
             CEF
                    ERSEc 5.320973e-01 9.523240e-01
                                                      9.523240e-01
## 50%25
             CDP
                    ERSEc 6.535427e-04 9.869790e-02 -9.853659e-02
## 50%35
             GRI
                    ERSEc 1.693205e-01 8.852610e-01 8.849051e-01
## 50%45
            ECLc
                    ERSEc 6.237316e-07 4.812098e-04 -4.810229e-04
## 50%55
             EPI
                    ERSEc 2.480425e-02 5.046973e-01 5.040227e-01
## 50%65
                    ERSEc 4.992600e-01 9.332902e-01 -9.332901e-01
          Taille
## 50%75
          Croiss
                    ERSEc 5.030759e-01 9.332894e-01 9.332894e-01
## 50%85
                    ERSEc 5.016092e-02 6.909609e-01 6.908507e-01
           Renta
## 50%95
           ERSEc
                    ERSEc 2.212472e-20 4.660801e-20 -4.659232e-20
## 50%20
                   Taille 1.943216e-06 5.170075e-04 -5.133615e-04
             FEF
                                                                     ***
## 50%110
             CEF
                   Taille 9.029190e-08 1.212420e-04 -1.207847e-04
## 50%26
                   Taille 3.232032e-03 4.455284e-01 -4.432219e-01
             CDP
## 50%36
             GRI
                   Taille 3.530816e-01 9.373910e-01 -9.373856e-01
## 50%46
            ECLc
                   Taille 3.378314e-06 8.165776e-04 -8.063044e-04
## 50%56
                   Taille 1.371507e-04 5.797209e-02 5.785087e-02
             EPI
## 50%66
                   Taille 1.561546e-19 1.567089e-19 -1.567089e-19
          Taille
## 50%76
                   Taille 5.494907e-02 7.832825e-01
          Croiss
                                                      7.832822e-01
## 50%86
           Renta
                   Taille 2.405528e-03 2.724610e-01
                                                      2.724589e-01
## 50%96
           ERSEc
                   Taille 1.063757e-02 7.384844e-01 -7.382356e-01
## 50%27
             FEF
                      EUR 1.909668e-13 5.354863e-10
                                                      5.320457e-10
## 50%111
             CEF
                      EUR 5.657827e-14 1.385812e-10
                                                      1.369735e-10
## 50%28
                      EUR 0.000000e+00 2.843814e-01
             CDP
                                                      2.828360e-01
## 50%37
             GRI
                      EUR 2.094999e-01 9.381757e-01
                                                     9.381627e-01
## 50%47
            ECLc
                      EUR 6.781334e-03 3.062536e-01 -3.055345e-01
## 50%57
             EPI
                      EUR 1.844917e-09 1.641189e-06 -1.638368e-06
                                                                     ***
## 50%67
          Taille
                      EUR 2.479528e-04 4.274986e-02
                                                      4.251343e-02
## 50%77
                      EUR 2.333051e-04 2.651970e-02
                                                      2.647992e-02
          Croiss
## 50%87
                      EUR 1.330245e-17 3.210861e-14
           Renta
                                                      3.125045e-14
## 50%97
                      EUR 3.062293e-05 4.463312e-03 -4.440874e-03
           ERSEc
## 50%29
             FEF
                      EPI 2.225615e-01 9.287773e-01 -9.285399e-01
## 50%112
                      EPI 1.644993e-01 8.627981e-01 8.623270e-01
             CEF
## 50%210
             CDP
                      EPI 5.479639e-04 5.802174e-02 -5.800791e-02
## 50%38
                      EPI 2.742039e-01 9.112919e-01 9.111731e-01
             GRI
## 50%48
                      EPI 1.335470e-03 2.330653e-01
            ECLc
                                                     2.328466e-01
## 50%58
             EPI
                      EPI 1.160588e-19 1.264200e-19 -1.264200e-19
## 50%68
          Taille
                      EPI 6.834687e-04 1.292318e-01 1.288461e-01
## 50%78
                      EPI 3.328887e-02 6.931178e-01 -6.931176e-01
          Croiss
## 50%88
           Renta
                      EPI 3.782261e-07 9.076896e-04 9.019749e-04
## 50%98
           ERSEc
                      EPI 5.183863e-04 1.238266e-01 1.236165e-01
write.csv(AnalyseWilcoxonComplete,
          file='AnalyseWilcoxonComplete20pc.csv',
          row.names = FALSE)
```

#### 4 Corrélations

FEF; CEF; CDP; GRI; ERSEc; ECLc; EPI; Taille; Croiss; Renta

# library(corrplot) ## corrplot 0.84 loaded #X[,c('FEF','CEF','CDP','GRI','ERSEc','ECLc','EPI','Taille','Croiss','Renta')] M <- cor(X[,c('FEF','CEF','CDP','GRI','ERSEc','ECLc','EPI','Taille','Croiss','Renta')], use='pairwise.cc corrplot(M, )</pre>



```
devtools::install_github("Antoine-Masse/KefiR") # pour corrigraph
```

```
## Skipping install of 'KefiR' from a github remote, the SHA1 (2c49343e) has not changed since last ins
## Use `force = TRUE` to force installation
library(KefiR)
# Fonction en cours de développement pour Rstudio :
# fonctionne dans Rqui uniquement
```

# 5 Leaps : écremage de modèle

Ecrémage automatique pour toutes les variables, et ajustement du modèle le plus pertinent avec affichage résumé. Le mode de sélection du modèle n'impacte pas.

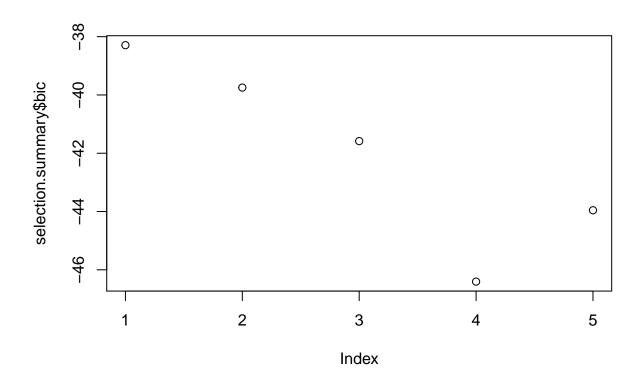
# corrigraph(X[,c('FEF','CEF','CDP','GRI','ERSEc','ECLc','EPI','Taille','Croiss','Renta')])

```
for(y in c('CDP','ECLc','GRI','ERSEc')){
  f <- formula(paste(y,'~FEF*CEF+EPI+COT+Taille+Croiss+Renta+EUR+Année'))</pre>
```

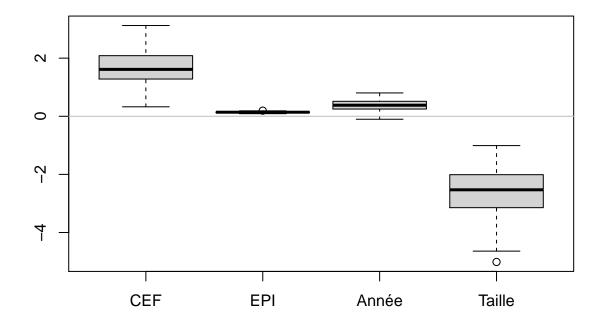
```
select.lm(f, data=X, nvmax=7)
}
## Regression : CDP ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR +
     Année
## Selected by bic
                   -----
            Estimate Pr(>|t|) star
## (Intercept) 358.7099 0
## FEF -37.0264 0
                            ***
## CEF
            -34.3773 1e-04
                            ***
## EPI
           0.1363 0
                            ***
## Taille
           -2.3632 0.0029
## Croiss
           -2.5158 0.2693
## Année 0.4077 0.03
## FEF:CEF 3.7194 0
            0.4077 0.011
                            ***
## adj.r.squared = 0.4794321
                            p.value = 1.630567e-16
## Selected by adjr2 -----
            Estimate Pr(>|t|) star
## (Intercept) 358.7099 0
## FEF
            -37.0264 0
                            ***
## CEF
            -34.3773 1e-04
                            ***
## EPI
          0.1363 0
                            ***
## Taille
           -2.3632 0.0029
            -2.5158 0.2693
## Croiss
## Année
            0.4077 0.011
## FEF:CEF 3.7194 0
                            ***
## adj.r.squared = 0.4794321 p.value = 1.630567e-16
## Selected by cp -----
           Estimate Pr(>|t|) star
## (Intercept) 358.7099 0
## FEF
            -37.0264 0
## CEF
            -34.3773 1e-04
                            ***
## EPI
           0.1363 0
            -2.3632 0.0029
## Taille
## Croiss
            -2.5158 0.2693
## Année
            0.4077 0.011
## FEF:CEF
            3.7194 0
                           ***
## adj.r.squared = 0.4794321
                            p.value = 1.630567e-16
## -----
## Regression : ECLc ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR +
##
     Année
## Selected by bic
                    _____
           Estimate Pr(>|t|) star
## (Intercept) -44.0417 0.0026
## EPI
            -0.1163 0.001
## Taille
           2.4212 0.05
## EUR
           5.63
                    0
## FEF:CEF 0.2442 0
                           ***
## adj.r.squared = 0.3794102 p.value = 4.005267e-14
##
```

```
## Selected by adjr2 -----
## Estimate Pr(>|t|) star
## (Intercept) -39.7523 0.0057 **
## EPI -0.1427 1e-04
## COT -0.4617 0.0478
## Taille 2.2533 0.0632 .
## Renta -1.4056 0.07 .
## EUR 5.204 0 **
## FEF:CEF 0.2614 0
                         ***
## adj.r.squared = 0.4039998 p.value = 2.672721e-14
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -39.7523 0.0057 **
       -0.1427 1e-04
## EPI
                          ***
           -0.4617 0.0478
## COT
         2.2533 0.0632 .
## Taille
## Renta
          -1.4056 0.07
         5.204 0
## FEF:CEF 0.2614 0
                         ***
## adj.r.squared = 0.4039998 p.value = 2.672721e-14
## -----
## Regression : GRI ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR +
## Année
## Selected by bic
                   -----
## Estimate Pr(>|t|) star
## (Intercept) 36.5672 0.0598 .
## Taille -2.6318 0.0998 .
## adj.r.squared = 0.01240338 p.value = 0.09978681
## Selected by adjr2
                  -----
## Estimate Pr(>|t|) star
## (Intercept) 36.5672 0.0598
## Taille -2.6318 0.0998
## adj.r.squared = 0.01240338 p.value = 0.09978681
## Selected by cp -----
           Estimate Pr(>|t|) star
## (Intercept) 36.5672 0.0598 .
## Taille -2.6318 0.0998
## adj.r.squared = 0.01240338 p.value = 0.09978681
## -----
## Regression : ERSEc ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR +
## Année
## Selected by bic
           Estimate Pr(>|t|) star
## (Intercept) -35.3474 0 ***
## CEF
           1.5441 2e-04
           2.5427
                   0
## EUR
                          ***
## Année 1.2439 0
                         ***
## adj.r.squared = 0.5371633 p.value = 2.801938e-23
##
```

```
## Selected by adjr2
##
              Estimate Pr(>|t|) star
## (Intercept) 114.0535 0.098
              -14.9821 0.0318
## FEF
## CEF
              -14.0962 0.0518
## COT
              -0.0998 0.482
## Renta
              0.1788 0.6942
              2.7685 0
## EUR
                                ***
             1.2235
## Année
                      0
                                ***
## FEF:CEF
            1.5693 0.0298
                                p.value = 3.866869e-21
## adj.r.squared = 0.5419516
## Selected by cp -----
              Estimate Pr(>|t|) star
## (Intercept) -35.3474 0
## CEF
              1.5441
                       2e-04
## EUR
              2.5427
                       0
                                ***
## Année
              1.2439
                       0
                                 p.value = 2.801938e-23
## adj.r.squared = 0.5371633
selection <- regsubsets(CDP~FEF+CEF+EPI+Taille+Croiss+Renta+Année+EUR,</pre>
                       data=X, nvmax=5, method='forward')
summary(selection) -> selection.summary
selection.summary
## Subset selection object
## Call: regsubsets.formula(CDP ~ FEF + CEF + EPI + Taille + Croiss +
      Renta + Année + EUR, data = X, nvmax = 5, method = "forward")
## 8 Variables (and intercept)
         Forced in Forced out
                       FALSE
## FEF
             FALSE
## CEF
             FALSE
                       FALSE
## EPI
             FALSE
                      FALSE
## Taille
             FALSE
                       FALSE
## Croiss
             FALSE
                      FALSE
## Renta
             FALSE
                      FALSE
## Année
             FALSE
                      FALSE
## EUR
             FALSE
                       FALSE
## 1 subsets of each size up to 5
## Selection Algorithm: forward
           FEF CEF EPI Taille Croiss Renta Année EUR
## 1 (1) " " " " " " " "
                             11 11
                                    ... ... ...
## 2 (1)""""*""
                              11 11
                                    11 11
                                          "*"
## 3 (1)""*""*""
                              11 11
                                    11 11
## 4 ( 1 ) " " "*" "*" "*"
                              11 11
                                    11 11
                                          "*"
## 5 (1) " " * " * " * " * "
                              "*"
plot(selection.summary$bic)
```



```
coef(selection,4)
## (Intercept)
                       CEF
                                   EPI
                                             Taille
                                                          Année
     3.3427957
                 1.6288761
                              0.1401063
                                        -2.6002996
                                                      0.3791030
reg1 <- lm(CDP~CEF+EPI+Année+Taille, data=X)</pre>
summary(reg1)
##
## lm(formula = CDP ~ CEF + EPI + Année + Taille, data = X)
##
## Residuals:
##
      Min
              1Q Median
                            3Q
## -5.898 -1.181 0.377 1.294 3.631
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.34280
                          11.26028
                                      0.297 0.767054
## CEF
                1.62888
                           0.43817
                                      3.717 0.000301 ***
## EPI
                0.14011
                           0.02192
                                      6.393 2.84e-09 ***
## Année
                0.37910
                           0.16787
                                      2.258 0.025632 *
## Taille
               -2.60030
                           0.83534
                                    -3.113 0.002290 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.9 on 127 degrees of freedom
```



```
reg$coefficients
## (Intercept)
                       CEF
                                    EPI
                                              Année
                                                         Taille
     9.5187351
                 2.4654584
                             0.1238625
                                          0.2393435 -3.4922123
names(summary(reg))
  [1] "call"
                         "terms"
                                         "residuals"
                                                         "coefficients"
##
  [5] "aliased"
                                         "df"
##
                        "sigma"
                                                         "r.squared"
## [9] "adj.r.squared" "fstatistic"
                                         "cov.unscaled"
                                                         "na.action"
```

#### summary(reg)

```
##
## Call:
## lm(formula = CDP ~ CEF + EPI + Année + Taille, data = X[ind,
##
      1)
##
## Residuals:
     Min
              1Q Median
                            3Q
                                  Max
## -5.006 -1.010 0.343 1.426
                                3.740
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 9.51874
                          13.10313
                                     0.726 0.468923
                           0.44835
## CEF
                2.46546
                                     5.499 2.06e-07 ***
## EPI
                0.12386
                           0.02391
                                     5.181 8.60e-07 ***
## Année
               0.23934
                           0.18772
                                     1.275 0.204677
               -3.49221
                           0.91311 -3.825 0.000206 ***
## Taille
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.995 on 125 degrees of freedom
     (10 observations deleted due to missingness)
## Multiple R-squared: 0.4238, Adjusted R-squared: 0.4054
## F-statistic: 22.99 on 4 and 125 DF, p-value: 2.974e-14
```

#### summary(X)

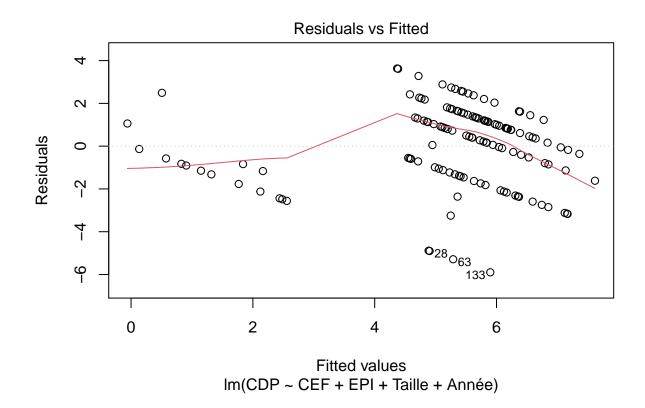
```
##
        X 1
                           Année
                                            2016
                                                           2017
   Length: 140
                      Min.
                             :16.00
                                       Min.
                                              :0.00
                                                      Min.
                                                             :0.00
   Class : character
                       1st Qu.:16.75
                                       1st Qu.:0.00
                                                      1st Qu.:0.00
   Mode :character
                       Median :17.50
                                       Median:0.00
                                                      Median:0.00
##
                              :17.50
                                              :0.25
                       Mean
                                       Mean
                                                      Mean
                                                            :0.25
##
                                       3rd Qu.:0.25
                       3rd Qu.:18.25
                                                      3rd Qu.:0.25
##
                       Max.
                              :19.00
                                              :1.00
                                       Max.
                                                      Max.
                                                             :1.00
##
##
         2018
                        2019
                                       FEF
                                                        CEF
##
   Min.
           :0.00
                  Min. :0.00
                                  Min. : 9.032
                                                   Min.
                                                         : 8.506
                                                   1st Qu.: 9.412
##
   1st Qu.:0.00
                   1st Qu.:0.00
                                  1st Qu.: 9.942
##
   Median:0.00
                  Median:0.00
                                  Median :10.245
                                                   Median : 9.766
##
   Mean
         :0.25
                  Mean :0.25
                                  Mean :10.160
                                                   Mean : 9.673
##
   3rd Qu.:0.25
                   3rd Qu.:0.25
                                  3rd Qu.:10.416
                                                   3rd Qu.: 9.996
##
   Max.
           :1.00
                   Max.
                          :1.00
                                  Max.
                                         :10.849
                                                   Max.
                                                          :10.500
##
##
        CDP
                         GRI
                                          ΙV
                                                         ERSE
##
                   Min. : 0.00
                                    Min. : 2.00
   Min.
           :0.000
                                                    Min.
                                                           :0.000
   1st Qu.:4.000
                   1st Qu.: 1.00
                                    1st Qu.: 8.00
##
                                                    1st Qu.:0.000
  Median :6.000
                   Median: 2.00
##
                                    Median :13.00
                                                    Median :1.000
   Mean
         :5.242
                   Mean : 4.65
                                    Mean :11.54
                                                    Mean :1.079
##
   3rd Qu.:7.000
                    3rd Qu.: 9.00
                                    3rd Qu.:15.00
                                                    3rd Qu.:2.000
##
   Max.
           :8.000
                    Max.
                          :18.00
                                    Max.
                                           :22.00
                                                    Max.
                                                           :5.000
           :8
##
   NA's
##
       ERSEc
                          ECL
                                           ECLc
                                                            COT
##
   Min.
          : 0.000
                     Min.
                            :0.0000
                                      Min. : 0.000
                                                       Min.
                                                              :0.000
```

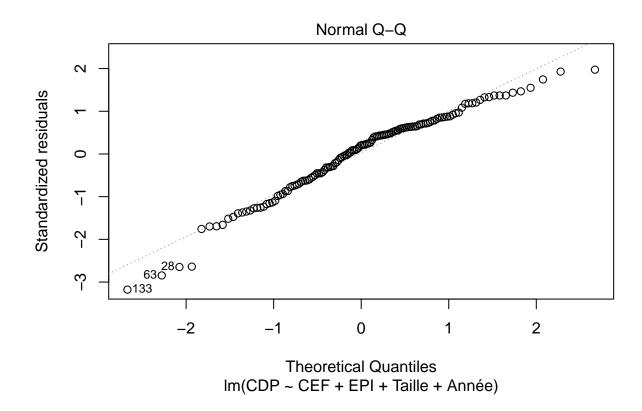
```
## 1st Qu.: 0.000
                   1st Qu.:0.0000 1st Qu.: 0.750
                                                     1st Qu.:1.000
## Median : 2.000
                   Median : 0.0000 Median : 1.500
                                                     Median :2.000
                                                     Mean :1.971
  Mean : 2.593
                    Mean :0.6286
                                  Mean : 2.964
   3rd Qu.: 4.000
                    3rd Qu.:1.0000
                                    3rd Qu.: 4.000
                                                     3rd Qu.:3.000
##
   Max. :11.000
                    Max. :8.0000
                                    Max. :16.000
                                                     Max.
                                                            :4.000
##
##
        EUR
                         EPI
                                       Taille
                                                      Taille.1
##
   Min. :0.0000
                    Min.
                           :50.74
                                   Min. :11.64
                                                   Min. :0.0
   1st Qu.:0.0000
                    1st Qu.:72.18
                                   1st Qu.:11.91
                                                   1st Qu.:0.0
  Median :0.0000
                    Median :80.59
                                   Median :12.16
                                                   Median:0.5
## Mean
         :0.4857
                    Mean
                          :78.54
                                   Mean
                                         :12.13
                                                   Mean :0.5
   3rd Qu.:1.0000
                    3rd Qu.:85.06
                                   3rd Qu.:12.35
                                                   3rd Qu.:1.0
##
##
  Max. :1.0000
                    Max.
                          :88.91
                                   Max. :12.57
                                                   Max. :1.0
##
##
       Croiss
                          Renta
##
   Min.
          :-0.35941
                      Min.
                            :-1.3200
   1st Qu.:-0.01801
                      1st Qu.: 0.2675
##
## Median : 0.02565
                    Median : 0.4850
## Mean : 0.02194
                     Mean : 0.5306
   3rd Qu.: 0.05527
                      3rd Qu.: 0.8725
##
  Max. : 0.31630
                      Max.
                           : 1.3100
##
# On détermine les meilleures variables
pred <- paste(names(coef(selection,5))[-1], collapse="+")</pre>
coef(selection,1:3)
## [[1]]
## (Intercept)
                      EPI
## -5.7425359
                0.1395829
##
## [[2]]
## (Intercept)
                      EPI
                                Année
## -15.2033431
                0.1621646
                            0.4390660
##
## [[3]]
## (Intercept)
                      CEF
                                 EPI
                                           Année
## -26.7667276
                1.0665414
                            0.1715396
                                       0.4678261
selection$which
```

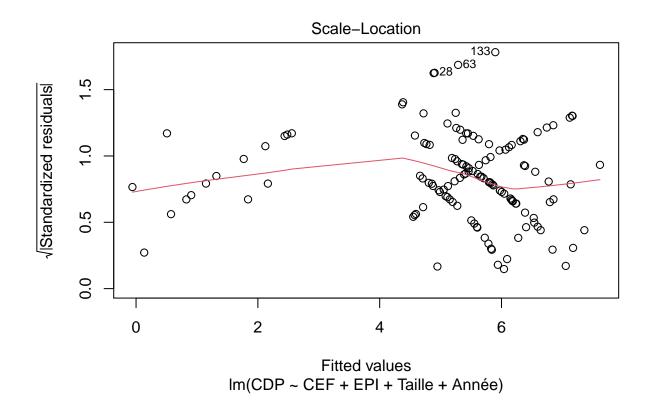
## NULL

## 6 Approfondissement de la régressions sur CDP

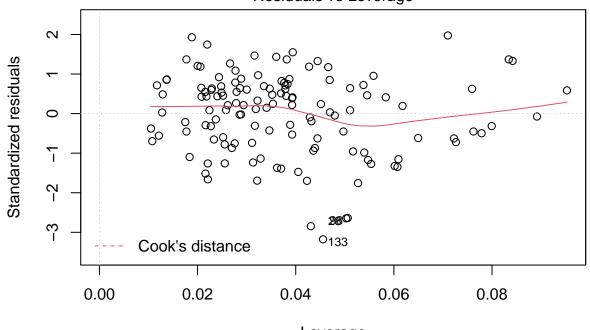
```
reg.CDP <- lm(CDP~CEF+EPI+Taille+Année, data=X)
reg.CDP.1 <- lm(CDP~FEF+CEF+EPI+Taille+Année, data=X)
reg.CDP.2 <- lm(CDP~I(-1.26*FEF+2.66*CEF)+EPI+Taille+Année, data=X)
plot(reg.CDP)</pre>
```







#### Residuals vs Leverage



Leverage Im(CDP ~ CEF + EPI + Taille + Année)

```
X[c(90,18,63),1:2] # Quelques outliers
```

##

## Residuals:

```
##
                                                     X1 Année
## 90 SMBC Group (Sumitomo Mitsui Banking Corporation)
## 18 ICBC (Industrial and Commercial Bank of China)
                                                            16
## 63
                                          BPCE/Natixis
                                                            17
X[63,]
##
                 X1 Année 2016 2017 2018 2019
                                                    FEF
                                                              CEF CDP GRI IV ERSE
## 63 BPCE/Natixis
                        17
                                   1
                                        0
                                             0 9.811167 8.967667
##
      ERSEc ECL ECLc COT EUR EPI
                                     Taille Taille.1
                                                          Croiss Renta
                            1 88.2 12.10034
                       0
                                                   0 0.01999676 0.24
summary(reg.CDP)
##
## Call:
## lm(formula = CDP ~ CEF + EPI + Taille + Année, data = X)
```

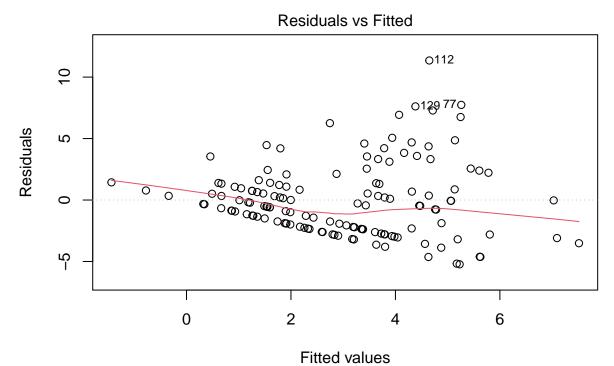
```
##
      Min
              1Q Median
                                   Max
   -5.898 -1.181 0.377
                         1.294
                                3.631
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.34280
                           11.26028
                                      0.297 0.767054
## CEF
                           0.43817
                                      3.717 0.000301 ***
                1.62888
```

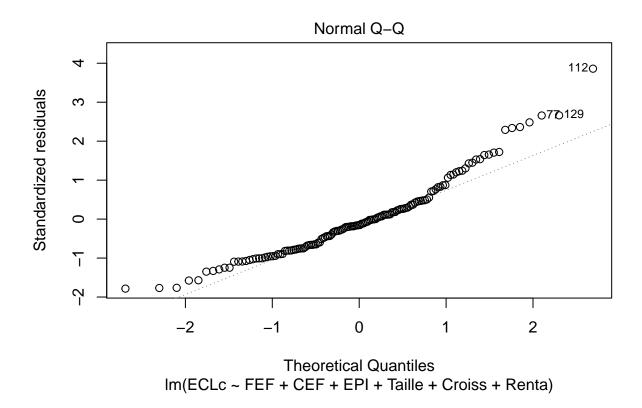
```
## EPI
              0.14011
                          0.02192
                                   6.393 2.84e-09 ***
## Taille
              -2.60030
                          0.83534 -3.113 0.002290 **
                          0.16787
## Année
              0.37910
                                  2.258 0.025632 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.9 on 127 degrees of freedom
     (8 observations deleted due to missingness)
## Multiple R-squared: 0.4152, Adjusted R-squared: 0.3968
## F-statistic: 22.54 on 4 and 127 DF, p-value: 4.38e-14
summary(reg.CDP.2) # passe de 0.30 à 0.40 en r2.adj
##
## Call:
## lm(formula = CDP \sim I(-1.26 * FEF + 2.66 * CEF) + EPI + Taille +
      Année, data = X)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -5.8651 -1.1916 0.3385 1.3022 3.7185
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               5.23288
                                        11.22465 0.466 0.641874
## I(-1.26 * FEF + 2.66 * CEF) 0.99923
                                          0.25774
                                                   3.877 0.000169 ***
## EPI
                               0.14223
                                          0.02181
                                                   6.523 1.49e-09 ***
## Taille
                              -2.56342
                                          0.82287 -3.115 0.002273 **
## Année
                               0.39740
                                          0.16717
                                                   2.377 0.018933 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.892 on 127 degrees of freedom
    (8 observations deleted due to missingness)
## Multiple R-squared: 0.4202, Adjusted R-squared: 0.4019
## F-statistic: 23.01 on 4 and 127 DF, p-value: 2.573e-14
```

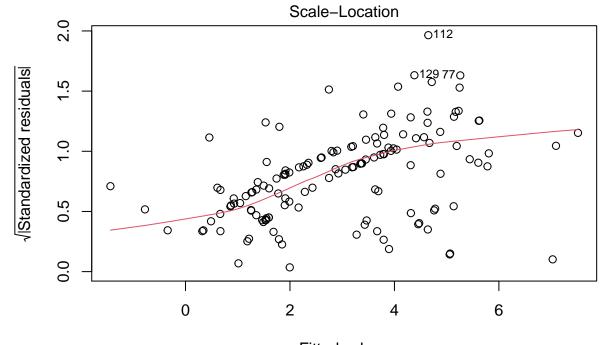
# 7 Approfondissement des autres regressions

```
et valeurs extrêmes
```

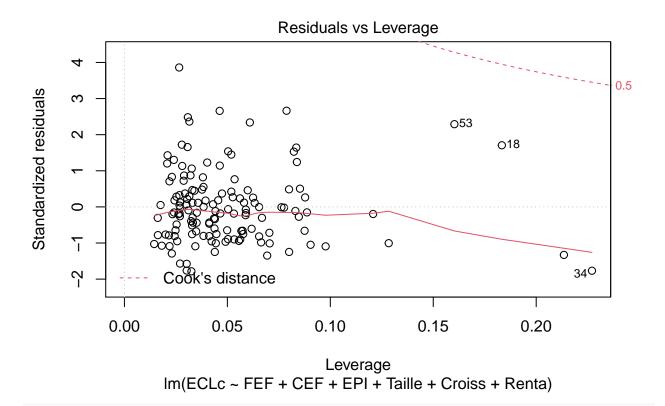
```
reg.ECLc <- lm(ECLc~FEF+CEF+EPI+Taille+Croiss+Renta, data=X)
plot(reg.ECLc)</pre>
```





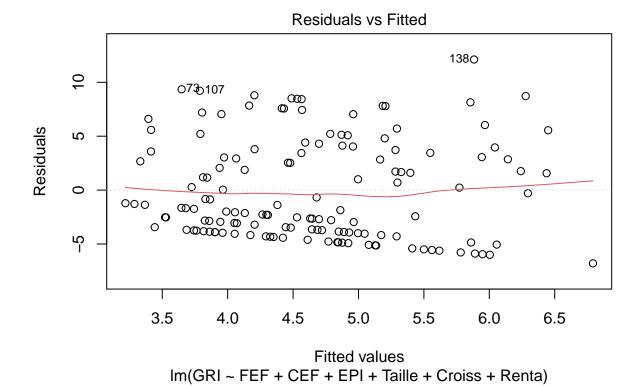


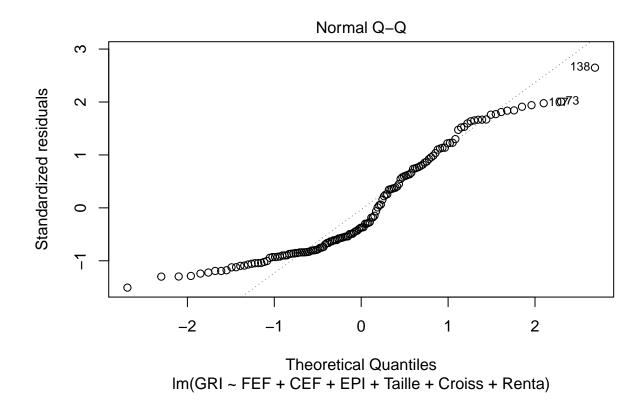
Fitted values Im(ECLc ~ FEF + CEF + EPI + Taille + Croiss + Renta)

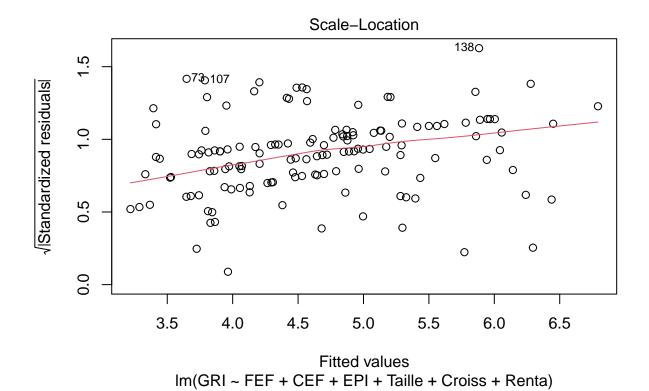


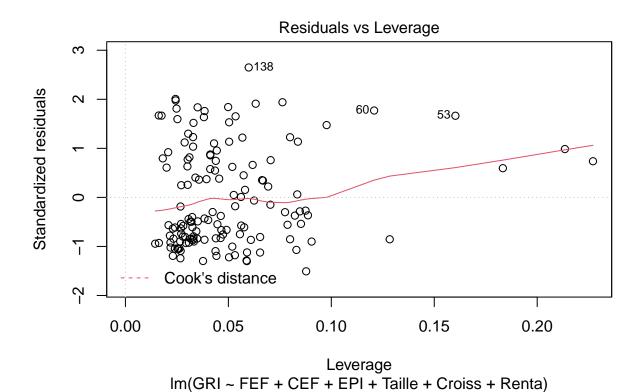
```
X[c(34,18,53),1] # Quelques outliers

## [1] "RBS "
## [2] "ICBC (Industrial and Commercial Bank of China) "
## [3] "ICBC (Industrial and Commercial Bank of China) "
reg.GRI <- lm(GRI~FEF+CEF+EPI+Taille+Croiss+Renta, data=X)
plot(reg.GRI)</pre>
```



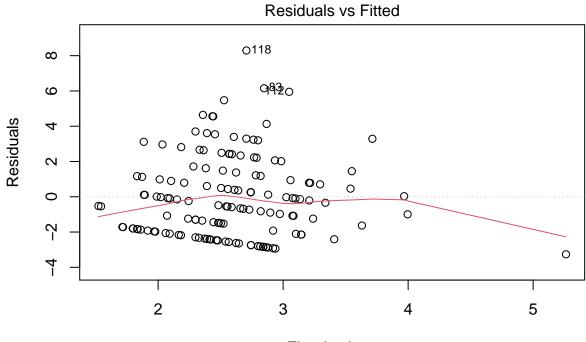




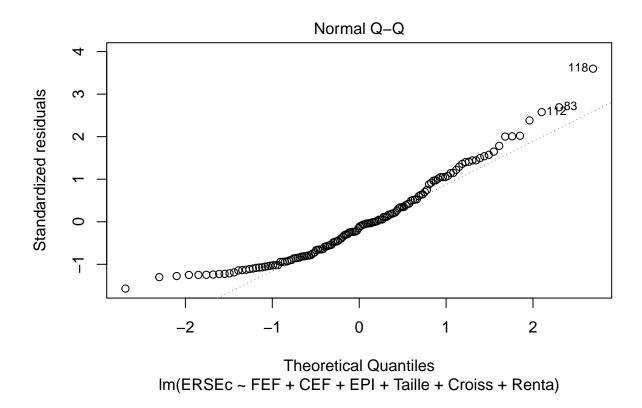


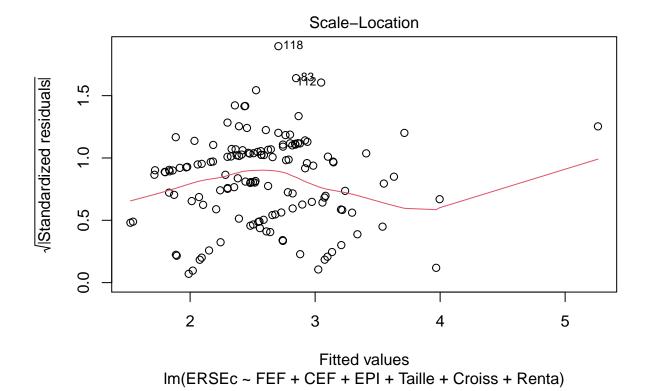
```
X[c(138,60,53),1] # Quelques outliers

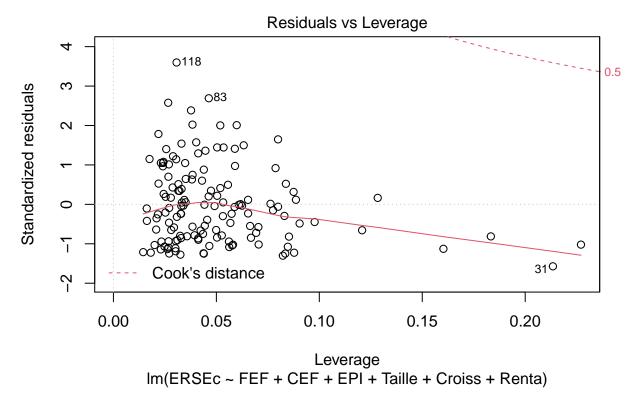
## [1] "Intesa Sanpaolo"
## [2] "ING "
## [3] "ICBC (Industrial and Commercial Bank of China) "
reg.ERSEc <- lm(ERSEc~FEF+CEF+EPI+Taille+Croiss+Renta, data=X)
plot(reg.ERSEc)</pre>
```



Fitted values Im(ERSEc ~ FEF + CEF + EPI + Taille + Croiss + Renta)







X[c(118,83,31),1] # Quelques outliers

## [1] "BNP Paribas" "BNP Paribas" "UniCredit "

Y : CDP et ECLc / GRI et ERSEc X : FEF ou CEF ; EPI ; Taille ; Croiss ; Renta

# 8 Ridge regression

### 8.1 Réduire les données

Nous devons travailler sur des données centrées réduites pour éviter que l'écrétage soit induit en erreur par des disparités d'échelles.

```
X.sc <- scale(X[,c('FEF','CEF','EPI','COT','Taille','Croiss','Renta','Année','EUR')])</pre>
Y.sc <- scale(X[,c('CDP','ECLc','GRI','ERSEc')])</pre>
#names(X)
colnames(X.sc)
## [1] "FEF"
                 "CEF"
                           "EPI"
                                     "COT"
                                               "Taille" "Croiss" "Renta"
                                                                            "Année"
## [9] "EUR"
colnames(Y.sc)
## [1] "CDP"
                         "GRI"
                                  "ERSEc"
                "ECLc"
```

#### 8.2 Load glmnet library

```
#install.packages('glmnet')
library(glmnet)

## Loading required package: Matrix

## Loaded glmnet 4.1-1
```

### 8.3 Régression Ridge sur toutes les variables Y

```
for(i in 1:ncol(Y.sc)){
cat('-----
cat("Ridge regression on variable ", colnames(Y.sc)[i],'\n')
    # detect NA
  which(is.na(Y.sc[,])) -> NA.ind
# Ajustement d'elastic cv
enet <- cv.glmnet(X.sc[-NA.ind,], Y.sc[-NA.ind,i], alpha=0)</pre>
# Fit the Ridge regression
regenet <- glmnet(X.sc[-NA.ind,], Y.sc[-NA.ind,i],
                 alpha=0, # Régression ridge
                 lambda = enet$lambda.1se)
print(coef(regenet))
#plot(regenet)
## Ridge regression on variable CDP
## 10 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept) -0.006412076
## FEF
              0.057880371
## CEF
              0.086915668
              0.211641609
## EPI
## COT
              0.010293688
## Taille
              -0.152369300
              -0.043944606
## Croiss
## Renta
              -0.059993714
               0.016250845
## Année
## EUR
              0.041309656
## Ridge regression on variable ECLc
## 10 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept) 0.01710904
## FEF
              0.11533062
## CEF
              0.13348839
              -0.07848152
## EPI
## COT
              -0.04714367
## Taille
              0.23500553
## Croiss
              -0.03478919
## Renta
              -0.12812448
```

```
0.10638887
## FUR
               0.27784517
## -----
## Ridge regression on variable GRI
## 10 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) -0.0191083967
## FEF
              -0.0009490491
## CEF
              -0.0004649658
## EPI
              0.0005381925
## COT
              -0.0001400982
## Taille
              -0.0009642353
## Croiss
              -0.0004273118
## Renta
              -0.0002733365
## Année
              -0.0004445308
## EUR
               0.0006557906
## Ridge regression on variable ERSEc
## 10 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept) -0.017669107
## FEF
              0.023139405
## CEF
              0.043086676
## EPI
              -0.000240310
## COT
              -0.014062435
## Taille
              0.025114013
## Croiss
              0.002334328
              -0.066883529
## Renta
## Année
              0.358650046
## EUR
               0.231402512
```

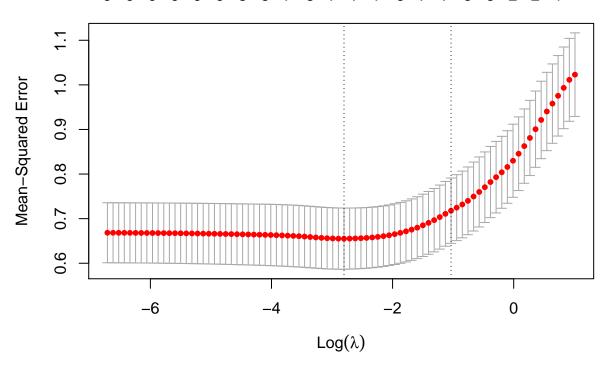
#### 8.4 Détail : Elasticnet on CDP

#### 8.4.1 Déterminer le $\lambda$

```
# Found NA
which(is.na(Y.sc[,]), arr.ind = TRUE)[,1] -> NA.CDP
## 23 25 54 60 71 95 106 130
## 23 25 54 60 71 95 106 130
# Fit elastic cv
enet <- cv.glmnet(X.sc[-NA.CDP,], Y.sc[-NA.CDP,1], alpha=0.2) # manque des CDP à voir
enet
##
## Call: cv.glmnet(x = X.sc[-NA.CDP, ], y = Y.sc[-NA.CDP, 1], alpha = 0.2)
## Measure: Mean-Squared Error
##
      Lambda Index Measure
                                SE Nonzero
## min 0.0607
             42 0.6551 0.06865
## 1se 0.3554
                23 0.7179 0.07326
```

plot(enet)

## 9 9 9 9 9 9 8 8 7 8 7 7 7 6 7 7 5 3 2 2 1

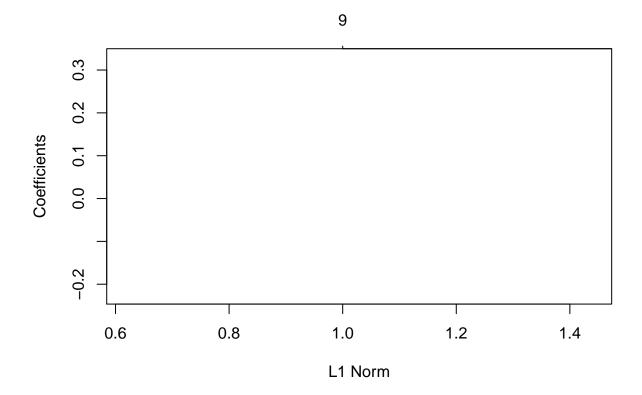


La validation croisée nous propose un  $\lambda$  optimum à 0.355379.

## 8.4.2 Ajustement CDP

On procèdera à l'ajustement avec ce lambda

```
regenet <- glmnet(X.sc[-NA.CDP,], Y.sc[-NA.CDP,1], alpha=0,</pre>
                   lambda = enet$lambda.1se)
coef(regenet)
## 10 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) -0.009851716
## FEF
                0.071864809
## CEF
                0.163346383
                0.327673331
## EPI
## COT
                0.014633740
               -0.224272664
## Taille
## Croiss
               -0.064535798
               -0.051607058
## Renta
## Année
                0.067264173
## EUR
                0.043861920
plot(regenet)
```



On observe un maintien de FEF et de CEF qui sont fortement colinéaires. Aussi l'introduction de CEF dans un modèle sortira automatiquement FEF, et inversement. Il est envisageable de les considérer comme une même variable, ou bien d'exclure FEF selon la méthode habituelle.

Les variables COT, et les 4 dernières sont peu pertinentes.

## 9 Bootstrap

## 9.1 Bootstrap sur les modèles issus de la sélection LEAPS

## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année

Définition des modèles sélectionnés :

#### 9.1.1 CDP

Fragilité de l'année. Le reste est confirmé.

```
set.seed(1)
f <- formula(paste('CDP~CEF+EPI+Taille+Croiss+Année'))
bootstrap(f, data=X)
## ------</pre>
```

```
##
                       pval stars Estim_2.5 Estim_97.5 pval_90 stars_90
               Estim
                                     -18.23
                                                  24.12 0.9218
## (Intercept) 2.22 0.8433
                                       0.64
## CEF
                1.72 0.0001
                              ***
                                                   2.86 0.0161
## EPI
                0.14 0.0000
                                       0.09
                                                   0.18 0.0000
                              ***
## Taille
               -2.60 0.0022
                                       -4.28
                                                  -1.06 0.0494
               -3.69 0.1282
                                      -8.27
                                                   0.69 0.6193
## Croiss
                0.41 0.0162
                                       0.03
                                                   0.73 0.4014
## Année
## r2 ajusté : 0.4031193
                             quantile 5\% = 0.3004187
                                                          quantile 50\% = 0.4222798
```

#### 9.1.2 ECLc

Fragilité de la cotation et de la taille. Le reste est confirmé.

```
set.seed(1)
f <- formula(paste('ECLc~FEF:CEF+EPI+COT+Taille+EUR'))
bootstrap(f, data=X)</pre>
```

```
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR
                Estim
                       pval stars Estim_2.5 Estim_97.5 pval_90 stars_90
## (Intercept) -42.30 0.0034
                                                  -21.96 0.0400
                                **
                                      -69.02
## EPI
                -0.12 0.0004
                               ***
                                       -0.18
                                                   -0.05 0.0308
## COT
                -0.48 0.0434
                                       -0.90
                                                   -0.01 0.4183
## Taille
                 2.25 0.0653
                                        0.26
                                                    4.69
                                                          0.3752
## EUR
                 5.83 0.0000
                                        4.06
                                                    7.71
                                                          0.0000
## FEF:CEF
                 0.26 0.0000
                                        0.15
                                                    0.37
                                                          0.0001
                               ***
                                                                      ***
## r2 ajusté : 0.393604
                             quantile 5\% = 0.3121403
                                                          quantile 50\% = 0.4117321
```

#### 9.1.3 ERSEc

Tout est confirmé.

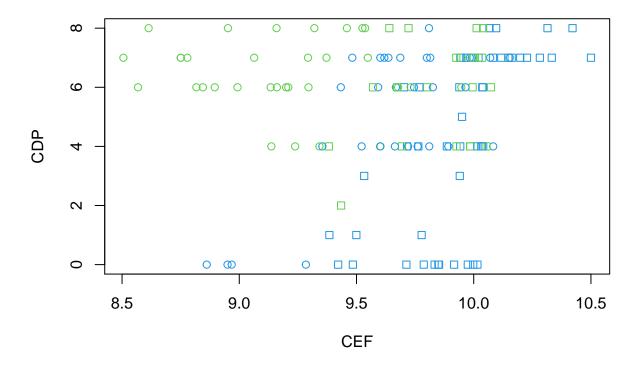
```
set.seed(1)
f <- formula(paste('ERSEc~CEF+EUR+Année'))
bootstrap(f, data=X)</pre>
```

```
## -----
## Regression : ERSEc ~ CEF + EUR + Année
##
              Estim pval stars Estim_2.5 Estim_97.5 pval_90 stars_90
## (Intercept) -35.35 0e+00
                           ***
                                  -44.52
                                            -25.72 0.0000
## CEF
                                    0.74
                                              2.35 0.0165
               1.54 2e-04
                           ***
## EUR
               2.54 0e+00
                           ***
                                    1.87
                                              3.21 0.0000
                                                               ***
               1.24 0e+00
                                    1.02
                                              1.47 0.0000
## Année
                           ***
                                                               ***
                          quantile 5\% = 0.4563583
## r2 ajusté : 0.5371633
                                                     quantile 50\% = 0.5483944
```

### 10 EUR vs NON EUR:

Comparons les régressions entre les banques EUR et non EUR. Le graphique suivant représente le CDP en fonction du CEF. Les couleurs représentent la taille, et la forme des points l'appartenance à l'europe ou pas : le champs d'investigation est caractérisé par les critères de tailles et d'appartenance à l'europe. Dans certains sous-groupes, il est possible que la variable CEF perde de son pouvoir explicatif.

```
plot(CDP~ CEF, data=X, col=Taille, pch=EUR)
```



#### 10.1 Avec les formules précédentes

```
for(frm in formules){
  f <- formula(frm)</pre>
  cat('-----
  cat('Regression : ');print(f)
  reg.eur <- lm(formula = f, data=X.eur)</pre>
  reg.noneur <- lm(formula = f, data=X.noneur)</pre>
   print(cbind(Est.eur = round(summary(reg.eur)$coefficients[,c(1)],3),
                pval.eu = round(summary(reg.eur)$coefficients[,c(4)],3),
                star.eu = star( summary(reg.eur)$coefficients[,c(4)]),
                Est.noneur = round(summary(reg.noneur)$coefficients[,c(1)],3),
                pval.noneur = round(summary(reg.noneur)$coefficients[,c(4)],3),
                star.noneur = star( summary(reg.noneur)$coefficients[,c(4)])
                ), quote=FALSE
   )
  cat('adj.r.squared = ',broom::glance(reg.eur)[[2]],' p.value = ',broom::glance(reg.eur)[['p.value
      'adj.r.squared = ',broom::glance(reg.noneur)[[2]],' p.value = ',broom::glance(reg.noneur)[['p
}
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année
               Est.eur pval.eu star.eu Est.noneur pval.noneur star.noneur
## (Intercept) 44.962 0.027
                                       -42.66
                                                  0.004
```

```
## CEF
             1.716 0.051
                                2.507
                                              0.018
## EPI
             -0.114 0.186
                                    0.201
                                              0
                                                         ***
## Taille
             -2.968 0.104
                                   -0.837
                                              0.409
             -1.852 0.634
                                   -1.651
                                              0.584
## Croiss
## Année
             -0.568 0.069
                                    1.027
## adj.r.squared = 0.05403872
                                 p.value = 0.1474141
                                                        adj.r.squared = 0.6640603
                                                                                     p.value =
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR
             Est.eur pval.eu star.eu Est.noneur pval.noneur star.noneur
## (Intercept) -41.382 0.149
                                   -32.485
                                            0.027
## EPI
             -0.27 0.004
                                    -0.076
                                              0.02
             -0.837 0.007
## COT
                                              0.158
                            **
                                    0.531
## Taille
             3.323 0.221
                                    2.531
                                              0.031
## FEF:CEF
             0.315
                                    0.08
                     0
                                              0.188
## adj.r.squared = 0.4516287
                                p.value = 1.411825e-08
                                                        adj.r.squared = 0.2887601
                                                                                     p.value =
## -----
## Regression : ERSEc ~ CEF + EUR + Année
            Est.eur pval.eu star.eu Est.noneur pval.noneur star.noneur
## (Intercept) -36.801 0
                                    -34.125
                                              0
                                                         ***
                            ***
## CEF
             1.39
                     0.009
                                    1.944
                                              0.004
                                                         **
## Année
             1.555
                     0
                            ***
                                    0.947
                                              0
                                                         ***
## adj.r.squared = 0.5203301
                                p.value = 1.595445e-11 adj.r.squared = 0.4264455
                                                                                      p.value =
```

#### 10.2 LEAPS eur

Sélection de modèle sur les banques européennes uniquement

## Selected by cp -----

## (Intercept) 11.3342 0.0047

Estimate Pr(>|t|) star

##

```
for(y in c('CDP', 'ECLc', 'GRI', 'ERSEc')){
 f <- formula(paste(y,'~CEF+EPI+COT+Taille+Croiss+Renta+Année'))</pre>
select.lm(f, data=X.eur, nvmax=7)
}
## -----
## Regression : CDP ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic
                     _____
             Estimate Pr(>|t|) star
## (Intercept) 11.3342 0.0047
## Année
            -0.3183 0.153
## adj.r.squared = 0.01733506
                              p.value = 0.1530238
##
## Selected by adjr2
                      -----
             Estimate Pr(>|t|) star
## (Intercept) 45.5208 0.0314
## CEF
             1.7423
                     0.0607
## EPI
             -0.1071 0.2432
## COT
             0.1536
                     0.4649
             -3.0691 0.0978
## Taille
## Croiss
             -3.4365 0.4005
## Renta
             0.947
                     0.2976
## Année
             -0.6083 0.0717
## adj.r.squared = 0.05162319
                                p.value = 0.1928979
##
```

```
## Année -0.3183 0.153
## adj.r.squared = 0.01733506 p.value = 0.1530238
## -----
## Regression : ECLc ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic -----
           Estimate Pr(>|t|) star
## (Intercept) -31.4858 0.0031 **
## CEF 6.434 0
## EPI -0.2786 0.0041 **
## COT -0.9179 0.0048 **
## adj.r.squared = 0.4194983 p.value = 2.802454e-08
## Selected by adjr2 -----
          Estimate Pr(>|t|) star
## (Intercept) -73.5423 0.005
## CEF 4.5693 9e-04
## EPI
          -0.2998 0.002
## COT
          -0.8627 0.0069 **
## Taille 5.1123 0.0604
## Renta -1.7222 0.1672
## adj.r.squared = 0.442993 p.value = 5.835936e-08
##
## Selected by cp -----
           Estimate Pr(>|t|) star
## (Intercept) -69.6892 0.0077 **
      4.945 3e-04
## CEF
                          ***
           -0.2795 0.0035
## EPI
## COT
           -0.8926 0.0055 **
## Taille 4.331 0.105
## adj.r.squared = 0.4345615 p.value = 3.592097e-08
##
## -----
## Regression : GRI ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic
                 -----
      Estimate Pr(>|t|) star
## (Intercept) 91.9903 0.0181 *
## Taille -7.2 0.0253
## adj.r.squared = 0.0594776 p.value = 0.02532071
##
## Selected by adjr2 -----
    Estimate Pr(>|t|) star
## (Intercept) 91.9903 0.0181 *
## Taille -7.2 0.0253 *
## adj.r.squared = 0.0594776 p.value = 0.02532071
##
## Selected by cp -----
           Estimate Pr(>|t|) star
## (Intercept) 91.9903 0.0181 *
        -7.2 0.0253 *
## Taille
## adj.r.squared = 0.0594776 p.value = 0.02532071
## -----
## Regression : ERSEc ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
```

```
## Selected by bic -----
           Estimate Pr(>|t|) star
## (Intercept) -15.9016 0.0791 .
## CEF
           1.8672 6e-04
## EPI
            -0.2019 0.0041
## Année 1.0706 0
                           ***
## adj.r.squared = 0.5721088 p.value = 1.847026e-12
## Selected by adjr2
                    -----
##
           Estimate Pr(>|t|) star
## (Intercept) -27.915 0.0802
## CEF 1.4943 0.0445
## EPI
           -0.2282 0.0018
           -0.2285 0.1968
## COT
## Taille
           1.599
                   0.2772
        1.0068 1e-04
## Année
## adj.r.squared = 0.5790275 p.value = 1.374688e-11
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -15.9016 0.0791 .
## CEF
           1.8672 6e-04
## EPI
            -0.2019 0.0041
                          **
## Année
           1.0706 0
## adj.r.squared = 0.5721088 p.value = 1.847026e-12
10.3 LEAPS non eur
for(y in c('CDP', 'ECLc', 'GRI', 'ERSEc')){
 f <- formula(paste(y,'~CEF+EPI+COT+Taille+Croiss+Renta+Année'))</pre>
select.lm(f, data=X.noneur, nvmax=7)
}
## Regression : CDP ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic -----
            Estimate Pr(>|t|) star
## (Intercept) -54.7519 0 ***
      2.7283 0.0021
## CEF
          0.2139 0 ***
## EPI
## COT
           -0.8172 0.0044 **
## Année
           1.0441 0
                          ***
## adj.r.squared = 0.7045034 p.value = 3.955286e-17
##
## Selected by adjr2
                    -----
            Estimate Pr(>|t|) star
## (Intercept) -42.3391 0.0022
## CEF
      3.248 0.0012
## EPI
           0.1871 0
                           ***
            -0.8483 0.0032
## COT
## Taille
            -1.1061 0.2467
## Année
           0.9264 1e-04
## adj.r.squared = 0.7061903 p.value = 1.40901e-16
```

##

```
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -54.7519 0 ***
       2.7283 0.0021 **
## CEF
         0.2139 0
## EPI
## COT
           -0.8172 0.0044 **
## Année 1.0441 0 ***
## adj.r.squared = 0.7045034 p.value = 3.955286e-17
## -----
## Regression : ECLc ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic -----
## Estimate Pr(>|t|) star
## (Intercept) -50.7884 0 ***
## Taille 4.3393 0
                        ***
## adj.r.squared = 0.2302393 p.value = 1.192058e-05
##
## Selected by adjr2 -----
          Estimate Pr(>|t|) star
## (Intercept) -38.4901 0.0141 *
## CEF 2.0433 0.0828 .
## EPI
          -0.0961 0.0083 **
## COT
         0.505 0.1756
## Taille 2.2272 0.0592 .
## Renta -0.9627 0.2872
## adj.r.squared = 0.2979264 p.value = 2.564575e-05
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -42.2099 0.0071 **
        2.1855 0.0539
## CEF
## EPI
           -0.0822 0.0111
         2.3511 0.0455 *
## Taille
## adj.r.squared = 0.2865195 p.value = 9.195524e-06
## -----
## Regression : GRI ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic
                  _____
##
           Estimate Pr(>|t|) star
## (Intercept) -26.0419 0.1755
## CEF 3.0388 0.117
## adj.r.squared = 0.02095156 p.value = 0.116961
## Selected by adjr2 -----
    Estimate Pr(>|t|) star
## (Intercept) -26.0419 0.1755
## CEF 3.0388 0.117
## adj.r.squared = 0.02095156 p.value = 0.116961
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -26.0419 0.1755
## CEF 3.0388 0.117
## adj.r.squared = 0.02095156 p.value = 0.116961
```

```
## -----
## Regression : ERSEc ~ CEF + EPI + COT + Taille + Croiss + Renta + Année
## Selected by bic
                  -----
            Estimate Pr(>|t|) star
## (Intercept) -34.1246 0
           1.9438 0.0041 **
## CEF
           0.9471 0
## Année
                          ***
## adj.r.squared = 0.4264455 p.value = 1.748665e-09
##
## Selected by adjr2
            Estimate Pr(>|t|) star
## (Intercept) -34.1246 0
           1.9438 0.0041 **
## CEF
          0.9471 0
## Année
                          ***
## adj.r.squared = 0.4264455 p.value = 1.748665e-09
##
## Selected by cp -----
           Estimate Pr(>|t|) star
## (Intercept) -34.1246 0
           1.9438 0.0041
## CEF
           0.9471 0
## Année
## adj.r.squared = 0.4264455 p.value = 1.748665e-09
```

#### 10.4 Formules de LEAPS

```
formules.eur <- c(
   ECLc ~ CEF+EPI + COT + Taille,
   ERSEc~ CEF + EPI + Année
)

formules.noneur <- c(
   CDP ~ CEF + EPI + COT +Année,
   ECLc ~CEF+EPI+ Taille,
   ERSEc ~ CEF + Année
)</pre>
```

# 11 Petites vs Grandes régressions

### 11.1 Avec les formules précédentes

```
star.petites = star(summary(reg.petites)$coefficients[,c(4)])
              ), quote=FALSE
   )
 }
## -----
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année
            Est.grandes pval.grandes star.grandes Est.petites pval.petites
## (Intercept) -18.227
                       0.592
                                              45.83
                                                        0.081
## CEF
            3.026
                                              0.88
                                                        0.149
## EPI
            0.167
                                              -0.063
                                                        0.305
                       0
                                   ***
## Taille
            -2.218
                       0.39
                                              -3.442
                                                        0.133
            0.999
## Croiss
                       0.736
                                              -9.707
                                                        0.016
## Année
            0.442
                       0.026
                                              -0.123
                                                        0.694
##
             star.petites
## (Intercept) .
## CEF
## EPI
## Taille
## Croiss
## Année
## adj.r.squared = 0.6784129 p.value = 1.186073e-14 adj.r.squared = 0.06290077
                                                                                 p.value =
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR
            Est.grandes pval.grandes star.grandes Est.petites pval.petites
## (Intercept) 67.749
                       0.229
                                              -26.255
                                                        0.239
## EPI
            -0.189
                       0
                                   ***
                                              -0.122
                                                        0.001
## COT
            -1.337
                       0.001
                                                        0.075
                                              0.355
## Taille
            -6.184
                       0.157
                                              2.811
                                                        0.162
            7.255
## EUR
                                   ***
                                             1.999
                                                        0.014
## FEF:CEF
            0.269
                       0.001
                                  ***
                                              0.024
                                                        0.613
             star.petites
## (Intercept)
## EPI
             ***
## COT
## Taille
## EUR
## FEF:CEF
## adj.r.squared = 0.4666383 p.value = 8.969891e-09 adj.r.squared = 0.2711434
                                                                                p.value =
## -----
## Regression : ERSEc ~ CEF + EUR + Année
##
            Est.grandes pval.grandes star.grandes Est.petites pval.petites
## (Intercept) -43.851
                       0
                                  ***
                                              -25.957
                                                        0.001
## CEF
            2.707
                       0.001
                                   ***
                                              0.272
                                                        0.691
            2.866
                                                        0.016
## EUR
                       Λ
                                   ***
                                              1.57
             1.07
                       0
                                   ***
                                              1.424
## Année
             star.petites
## (Intercept) ***
## CEF
## EUR
## Année
```

```
## adj.r.squared = 0.576268 p.value = 5.820684e-13 adj.r.squared = 0.5296455 p.value =
```

### 11.2 LEAPS grandes

Sélection de modèle sur les banques européennes uniquement

```
for(y in c('CDP', 'ECLc', 'GRI', 'ERSEc')){
 f <- formula(paste(y,'~CEF+EPI+COT+Taille+Croiss+Renta+EUR+Année'))</pre>
select.lm(f, data=X.grandes, nvmax=7)
}
## -----
## Regression : CDP ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic
                     -----
             Estimate Pr(>|t|) star
## (Intercept) -46.6102 0
## CEF
             2.9077
                     3e-04
## EPI
                     0
             0.1849
                             ***
## Année
             0.4889
                     0.0098
## adj.r.squared = 0.6848886
                             p.value = 3.505984e-16
## Selected by adjr2
                      -----
             Estimate Pr(>|t|) star
## (Intercept) -4.7998 0.8844
## CEF
             2.6829
                     0.0011
## EPI
             0.1836 0
                             ***
## COT
             0.2663 0.1974
             -3.3271 0.1832
## Taille
## Renta
             0.9469
                    0.1604
             0.5167
## Année
                     0.0094
## adj.r.squared = 0.6898852
                             p.value = 1.461173e-14
## Selected by cp -----
             Estimate Pr(>|t|) star
## (Intercept) -46.6102 0
## CEF
             2.9077 3e-04
## EPI
             0.1849
                     Ω
                             ***
## Année
             0.4889
                     0.0098
## adj.r.squared = 0.6848886
                             p.value = 3.505984e-16
##
## -----
## Regression : ECLc ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
                      _____
## Selected by bic
             Estimate Pr(>|t|) star
## (Intercept) -35.0654 0.0169
## CEF
             5.5997
                     6e-04
                             ***
             -0.1823 2e-04
## EPI
                             ***
## COT
             -1.4728 2e-04
                             ***
## Renta
            -2.3562 0.0462
             6.5462 0
## adj.r.squared = 0.4745902
                             p.value = 5.66133e-09
##
## Selected by adjr2
##
             Estimate Pr(>|t|) star
## (Intercept) -35.0654 0.0169
```

```
## CEF
           5.5997 6e-04
## EPT
           -0.1823 2e-04
                          ***
## COT
           -1.4728 2e-04
           -2.3562 0.0462
## Renta
           6.5462 0
## adj.r.squared = 0.4745902
                          p.value = 5.66133e-09
## Selected by cp -----
            Estimate Pr(>|t|) star
## (Intercept) -35.0654 0.0169 *
        5.5997 6e-04
## CEF
## EPI
           -0.1823 2e-04
                          ***
## COT
           -1.4728 2e-04
## Renta
           -2.3562 0.0462 *
## EUR
           6.5462 0
## adj.r.squared = 0.4745902 p.value = 5.66133e-09
## -----
## Regression : GRI ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic -----
           Estimate Pr(>|t|) star
## (Intercept) 14.1675 0.056
## Année -0.5905 0.1602
## adj.r.squared = 0.01451253 p.value = 0.1602059
##
## Selected by adjr2
                  -----
           Estimate Pr(>|t|) star
## (Intercept) 207.1447 0.0143
## CEF
      2.9594 0.2137
## EPI
           -0.1681 0.0626
## Taille -16.2383 0.013
## Croiss
          14.6316 0.0528
## EUR
          0.0169 0.9912
## Année
         -1.1312 0.0326
## adj.r.squared = 0.07205505 p.value = 0.09588089
## Selected by cp -----
    Estimate Pr(>|t|) star
## (Intercept) 14.1675 0.056
## Année -0.5905 0.1602
## adj.r.squared = 0.01451253 p.value = 0.1602059
## -----
## Regression : ERSEc ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
                   _____
## Selected by bic
            Estimate Pr(>|t|) star
##
## (Intercept) -43.8508 0
## CEF
           2.7073 7e-04
## EUR
           2.8662 0
                          ***
           1.0696 0
## Année
                         ***
## adj.r.squared = 0.576268
                         p.value = 5.820684e-13
## Selected by adjr2 -----
           Estimate Pr(>|t|) star
##
```

```
## (Intercept) -101.9569 0.002
      2.5802 0.0053
## CEF
## EPI
          0.0378 0.2605
## COT
           -0.251 0.2226
           4.5066 0.0626
## Taille
## EUR
           2.8976 0
                           ***
## Année 1.1478 0
                           ***
## adj.r.squared = 0.5850968 p.value = 1.146613e-11
##
## Selected by cp -----
            Estimate Pr(>|t|) star
## (Intercept) -43.8508 0 ***
            2.7073 7e-04
## CEF
                           ***
## EUR
            2.8662 0
                          ***
## Année
           1.0696 0
                          ***
## adj.r.squared = 0.576268 p.value = 5.820684e-13
11.3 LEAPS petites
```

```
for(y in c('CDP', 'ECLc', 'GRI', 'ERSEc')){
 f <- formula(paste(y,'~CEF+EPI+COT+Taille+Croiss+Renta+EUR+Année'))</pre>
select.lm(f, data=X.petites, nvmax=7)
}
## -----
## Regression : CDP ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic -----
            Estimate Pr(>|t|) star
## (Intercept) 5.8771 0
## Croiss -5.7367 0.1078
## adj.r.squared = 0.02489575 p.value = 0.1078425
##
                    -----
## Selected by adjr2
            Estimate Pr(>|t|) star
## (Intercept) 44.8105 0.0838
           0.9438 0.106
## CEF
## EPI
            -0.0466 0.299
           -3.6977 0.0902
## Taille
         -9.9116 0.0129
## Croiss
## adj.r.squared = 0.07586612
                            p.value = 0.06558045
## Selected by cp -----
            Estimate Pr(>|t|) star
## (Intercept) 40.7369 0.1112
## CEF
           1.037
                   0.0731
            -3.7503 0.0859
## Taille
## Croiss
           -8.6961 0.0218
                            p.value = 0.05066433
## adj.r.squared = 0.07441421
## -----
## Regression : ECLc ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic
                   _____
##
            Estimate Pr(>|t|) star
## (Intercept) -10.8843 4e-04
```

```
## Renta -1.4453 0.0033 **
## Année 0.7414 0 ***
                           ***
## adj.r.squared = 0.2425674 p.value = 3.3891e-05
## Selected by adjr2 -----
## Estimate Pr(>|t|) star
## (Intercept) -38.0473 0.0603
## EPI -0.0617 0.2059
## COT 0.435 0.0175
## Taille 2.9303 0.0745
## Croiss
           -5.296 0.0865
## Renta -0.7076 0.2957
## EUR 0.643 0.2723
## Année 0.5028 0.0396
## adj.r.squared = 0.3290658 p.value = 3.179603e-05
##
## Selected by cp -----
            Estimate Pr(>|t|) star
## (Intercept) -47.0448 0.0153 *
## COT 0.4536 0.0131
## Taille 2.9482 0.0706 .
## Croiss -5.694 0.061 .
## Renta -0.9878 0.0588 .
## Année 0.7458 0 ***
## adj.r.squared = 0.3284816 p.value = 9.470567e-06
## -----
## Regression : GRI ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic -----
            Estimate Pr(>|t|) star
## (Intercept) 4 1e-04 ***
       2.4286 0.0573 .
## EUR
## adj.r.squared = 0.03817324 p.value = 0.0573365
## Selected by adjr2 -----
           Estimate Pr(>|t|) star
## (Intercept) -30.9774 0.147
## CEF
         3.5351 0.1019
       5.0234 0.0143 *
## EUR
## adj.r.squared = 0.06231231 p.value = 0.04325253
## Selected by cp -----
## Estimate Pr(>|t|) star
## (Intercept) -30.9774 0.147
## CEF
            3.5351 0.1019
           5.0234 0.0143
## EUR
## adj.r.squared = 0.06231231 p.value = 0.04325253
##
## -----
## Regression : ERSEc ~ CEF + EPI + COT + Taille + Croiss + Renta + EUR + Année
## Selected by bic -----
     Estimate Pr(>|t|) star
## (Intercept) -23.3544 0 ***
## EUR
      1.3708 9e-04
```

```
## Année
            1.4284 0
                            p.value = 2.597297e-12
## adj.r.squared = 0.5355498
## Selected by adjr2
                     -----
            Estimate Pr(>|t|) star
## (Intercept) 8.4862 0.6883
            0.9894 0.1864
## CEF
            -0.1101 0.0483
## EPI
## Taille
            -2.2337 0.2247
## EUR
            2.7261 0.0011
## Année
           1.0602 1e-04
## adj.r.squared = 0.5525502
                            p.value = 3.999963e-11
## Selected by cp -----
            Estimate Pr(>|t|) star
## (Intercept) -10.5486 0.1859
## EPI
            -0.0918 0.0843
## EUR
            1.8239 2e-04
## Année
            1.108
                    0
                            ***
                            p.value = 4.308401e-12
## adj.r.squared = 0.5494837
```

#### 11.4 Formules de LEAPS

```
formules.grandes <- c(
   CDP ~ CEF+EPI+Année ,
   ECLc ~ CEF+EPI+COT+EUR,
   ERSEc~ CEF+EUR+Année
)

formules.petites <- c(
   CDP ~ CEF+Taille+Croiss ,
   ECLc ~ COT + Taille + Renta+ Croiss +Année ,
   ERSEc ~ EPI+EUR+Année
)</pre>
```

# 12 Années 0/1 dans toutes les régressions

Pas d'intervention majeure des années, sauf exception.

```
}
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année + An2016
             Estimate Pr(>|t|) star
## (Intercept) 0.228
                     0.9849
## CEF
             1.6913
                     2e-04
## EPI
             0.1386
                     0
                              ***
             -2.5612 0.0027
## Taille
                              **
## Croiss
             -3.4013 0.1747
## Année
             0.5021
                     0.0512
## An2016
             0.3018
                     0.6316
## adj.r.squared = 0.3994543
                               p.value = 15.52249
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR + An2016
##
             Estimate Pr(>|t|) star
## (Intercept) -43.2012 0.0034
             -0.1193 0.0017
## EPI
## COT
             -0.4719 0.0458
## Taille
             2.327
                     0.062
## EUR
             5.7651
                     0
             -0.1858 0.7384
## An2016
## FEF:CEF
             0.259
                     0
                              ***
## adj.r.squared = 0.3895587
                              p.value = 15.78402
## -----
## Regression : ERSEc ~ CEF + EUR + Année + An2016
             Estimate Pr(>|t|) star
## (Intercept) -40.3699 0
## CEF
             1.4396
                     4e-04
                              ***
## EUR
             2.4861
                     0
                              ***
## Année
             1.5746
                     Ω
                              ***
## An2016
            1.0973
                     0.0267
                              p.value = 43.55066
## adj.r.squared = 0.5504566
## -----
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année + An2017
             Estimate Pr(>|t|) star
## (Intercept) 1.7424
                     0.8775
## CEF
                     2e-04
             1.6951
## EPI
             0.1406
                     0
                              ***
## Taille
             -2.531
                     0.0031
## Croiss
             -3.346
                     0.179
## Année
             0.3917
                     0.0237
## An2017
             -0.2636 0.5252
## adj.r.squared = 0.4002921
                               p.value = 15.57328
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR + An2017
             Estimate Pr(>|t|) star
## (Intercept) -38.1442 0.0105
## EPI
             -0.1421 3e-04
## COT
             -0.4919 0.037
## Taille
             1.8854
                     0.1369
## EUR
             6.1091
                     0
## An2017
             0.6149
                     0.2838
## FEF:CEF
             0.2769
                     0
                              ***
```

```
## adj.r.squared = 0.3943181 p.value = 16.08223
## -----
## Regression : ERSEc ~ CEF + EUR + Année + An2017
           Estimate Pr(>|t|) star
## (Intercept) -33.7664 0
## CEF
           1.4942 3e-04
## EUR
           2.5156 0
           1.1898 0
## Année
                           ***
## An2017 -0.5485 0.0904
## adj.r.squared = 0.5435664 p.value = 42.38375
## -----
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année + An2018
            Estimate Pr(>|t|) star
## (Intercept) 1.8609 0.8697
## CEF
           1.7355 1e-04
           0.1388 0
## EPI
                           ***
## Taille
          -2.5855 0.0024
## Croiss
           -3.7251 0.1265
## Année
          0.4032 0.0194
           0.1287 0.7522
## An2018
## adj.r.squared = 0.3988257
                            p.value = 15.48448
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR + An2018
            Estimate Pr(>|t|) star
## (Intercept) -38.5776 0.0091
           -0.1396 3e-04
## EPI
## COT
           -0.4857 0.0391
## Co. ## Taille 1.500. 6.032
           1.9867 0.1104
                   0
           -0.6123 0.2709
## An2018
## FEF:CEF 0.2702 0
## adj.r.squared = 0.394608
                          p.value = 16.10055
## -----
## Regression : ERSEc ~ CEF + EUR + Année + An2018
           Estimate Pr(>|t|) star
## (Intercept) -35.4975 0
## CEF
           1.5128 3e-04
## EUR
           2.5257 0
                           ***
          1.2746 0
-0.3025 0.3527
## Année
                          ***
## An2018
## adj.r.squared = 0.5367195 p.value = 41.25855
## -----
## Regression : CDP ~ CEF + EPI + Taille + Croiss + Année + An2019
            Estimate Pr(>|t|) star
## (Intercept) 2.2065 0.8543
## CEF
           1.7226
                   2e-04
## EPI
           0.1373 0
                           ***
## Taille
           -2.6024 0.0023
                           **
## Croiss
            -3.6927 0.1342
            0.4109 0.1175
## Année
           -0.0025 0.9968
## An2019
                         p.value = 15.45542
## adj.r.squared = 0.3983443
## -----
## Regression : ECLc ~ FEF:CEF + EPI + COT + Taille + EUR + An2019
```

```
Estimate Pr(>|t|) star
## (Intercept) -43.8352 0.0035
             -0.1171 0.0027
## COT
             -0.4686 0.0476
## Taille
             2.3845
                     0.0601
## EUR
             5.7189 0
## An2019
             0.2351
                      0.6826
## FEF:CEF
           0.2557
                    0
## adj.r.squared = 0.3898151
                               p.value = 15.79997
## -----
## Regression : ERSEc ~ CEF + EUR + Année + An2019
             Estimate Pr(>|t|) star
## (Intercept) -29.9502 0
## CEF
             1.4541 4e-04
## EUR
             2.4939
                     0
                              ***
## Année
             0.9737
                     0
             0.9051
## An2019
                     0.0685
                               p.value = 42.63984
## adj.r.squared = 0.5450966
```

## 13 Régressions Simples

## EPI

## COT

## Taille

```
names(X)
   [1] "X1"
                    "Année"
                               "2016"
                                           "2017"
                                                       "2018"
                                                                   "2019"
                    "CEF"
   [7] "FEF"
                               "CDP"
                                           "GRI"
                                                       "IV"
                                                                   "ERSE"
## [13] "ERSEc"
                    "ECL"
                               "ECLc"
                                           "COT"
                                                       "EUR"
                                                                   "EPI"
## [19] "Taille"
                    "Taille.1" "Croiss"
                                           "Renta"
```

## 14 Toutes les régressions dans une boucle automatisée

Les Années ne figurent pas en variable explicative dans ce script.

```
for(y in c('CDP', 'ECLc', 'GRI', 'ERSEc')){
 f <- formula(paste(y,'~FEF*CEF+EPI+COT+Taille+Croiss+Renta+EUR'))</pre>
 cat('----\n')
 cat('Regression : ');print(f)
 reg <- lm(formula = f, data=X)</pre>
 print(cbind(summary(reg)$coefficients[,c(1,4)],
             star=star(summary(reg)$coefficients[,c(4)])
             ), quote=FALSE
 cat('adj.r.squared = ',broom::glance(reg)[[2]],' p.value = ',broom::glance(reg)[['p.value']], '\n
  #plot(reg)
}
## Regression : CDP ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR
                               Pr(>|t|)
              Estimate
## (Intercept) 416.954420825682 2.75581465206212e-06 ***
              -40.7056866074756 5.10325711465906e-06 ***
## FEF
## CEF
              -38.9001422590165 2.32250151223598e-05 ***
```

-3.35159763130775 0.000114541570295629 \*\*\*

-0.0115645471855912 0.94332733463269

```
## Croiss
## Renta
           ## EUR
           1.05312312469825 0.0757685895495297
## FEF:CEF 4.18838302412443 5.83792043075899e-06 ***
## adj.r.squared = 0.4619849 p.value = 7.922133e-15
## -----
## Regression : ECLc ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR
                     Pr(>|t|)
                                            star
           Estimate
## (Intercept) -62.7445899418481 0.593432674364401
## FEF
      1.82195888085493 0.876654230854005
## CEF
           3.09164044766154
                           0.800319608687798
## EPI
           -0.470995655750506 0.0481130773066921
## COT
## Taille
          2.22265843413532 0.0707390842851667
## Croiss
           ## Renta
           -1.39718044443081 0.0826835932372211
## EUR
           ## FEF:CEF 0.00623795696082547 0.995912410059061
## adj.r.squared = 0.3912452 p.value = 1.515575e-12
## -----
## Regression : GRI ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR
                     Pr(>|t|)
           Estimate
                                          star
## (Intercept) 130.915335042164
                           0.53826924071986
## FEF
           -11.6366793807856
                            0.584025721401927
## CEF
           -7.42113589874513
                            0.737268300872779
## EPI
           -0.00842470383745052 0.898340208205575
## COT
           ## Taille
           -2.49259787160883
                            0.260903499272662
## Croiss
           0.103383237817586
                            0.986912218524191
## Renta
           0.683328877553211
                            0.637261930304437
           1.21659266473709
## EUR
                            0.421721242392712
## FEF:CEF
           0.953798929668925
                            0.665225211489881
## adj.r.squared = -0.03131458 p.value = 0.8498094
## Regression : ERSEc ~ FEF * CEF + EPI + COT + Taille + Croiss + Renta + EUR
                     Pr(>|t|)
           Estimate
                                           star
## (Intercept) 273.428625599711 0.00136860496944672 **
## FEF
           -25.2401780892195 0.00302159509482194 **
## CEF
           -25.9634929220894 0.00337913460433893 **
## EPI
          -0.150526008083359 4.63791204513177e-08 ***
## COT
           -0.239794914271453 0.15654820778592
## Taille
           -2.48526428723792 0.00496443532719035 **
## Croiss
           4.31850222652545 0.0837195581916289
           -0.011350070061559 0.984129925198796
## Renta
## EUR
           5.10037333386347 2.49805949488928e-14 ***
## FEF:CEF
           ## adj.r.squared = 0.3639309 p.value = 2.138553e-11
```