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An Introduction to R and Python For Data Analysis: A Side By Side Approach

To my son,
without whom I should have finished this book two years earlier

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Welcome

A Sample Course

Please email me for access to a private Github repository with course materials such as a syllabus, course schedule, and assignments.

Assignments are written with automatic grading in mind. R scripts are graded with the `gradeR` package (Brown, 2020), and Python scripts with the `otter-grader` library¹ (Pyles, 2019). The quickest way to create your own autograding bundles is to use the tool here (TODO).

Become a Contributor

Spot a typo, or have a suggestion? Feel free to post an **issue here**². You may also submit pull requests through Github. I'll be happy to take a look.

¹<https://otter-grader.readthedocs.io/en/latest/>

²https://github.com/tbrown122387/r_and_python_book/issues

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Preface

About this book

This book is written to be used in a one-semester statistical computing class that teaches both R and Python to graduate students in a statistics or data science department. This book is written for students that do not necessarily possess any previous familiarity with writing code.

- If you are using them for analyzing data, R and Python do a lot of the same things in pretty similar ways, so it does not always make sense to teach one language after the other. Imagine learning about vectorization, say, in R, and then several weeks later learning about the same concept in Python. You might end up spending a lot of time refreshing your memory before getting started for the second time. The side-by-side approach ought to help reinforce shared concepts. In my opinion, it also helps to highlight key differences.
- This text does not describe statistical modeling techniques in detail, although many exercises will be motivated by different statistical techniques. Rather, it teaches a.) important data types, b.) the basics of common procedures such as data “cleaning”, “munging” and manipulation, and c.) some background on object-oriented programming and functional programming. This is largely motivated by the setup of many graduate programs in statistics and data science. Many of these departments organize their classes by sub-discipline (e.g. time series, linear models, Bayesian, etc.). When this is the case, departments tend to compartmentalize the programming courses. The orga-

nization of this text aims to complement this kind of course offering structure.

- This book is written for aspiring data scientists, not necessarily aspiring software developers. Why do I draw the distinction? When discussing different types, for example, I do not discuss data structures in any depth. Rather, I discuss examples of applications where different types would be most useful.
- This book does not attempt to be an authoritative reference. This is my attempt at balancing depth and breadth for a one-semester course. Plenty of discovery will be left to the reader. For instance, hyperlinks are provided to support self-guided exploration, and second many exercises are designed to motivate further questions.
- Generally speaking, chapters should be read in order. However, some jumping around may be useful. (TODO update after re-organizing) (sub-)sections within a chapter are carefully ordered. Say, for instance, a topic in R is discussed first. If the Python discussion comes second, that discussion will reference and make comparisons with details mentioned in the R section. So read sections and subsections in order.

Conventions

Sometimes R and Python code look very similar, or even identical. This is why I usually separate R and Python code into separate sections. However, sometimes I do not, so whenever it is necessary to prevent confusion, I will remind you what language is being used in comments (more about comments in 0.2).

```
# in python
print('hello world')
## hello world
```



```
# in R
print('hello world')
## [1] "hello world"
```

Installing the Required Software

To get started, you must install both R and Python. The installation process depends on what kind of machine you have (e.g. what type of operating system your machine is running, is your processor 32 or 64 bit, etc.).

Below, I suggest running R with RStudio, and Python with Anaconda, and I provide some helpful links. I suggest downloading these two bundles separately; however, I should note that the recommendation below is not the only installation method. For example: - one can run R and Python without downloading RStudio or Anaconda, - one can install RStudio with Anaconda, - one can run Python from within Rstudio, - one can run Python from within Rstudio that is managed by Anaconda, etc., and - options and procedures are very likely to change over time.

Instructors can prefer alternative strategies, if they wish. If they do, they should verify that Python's version is ≥ 3.6 , and R's is $\geq 4.0.0$. If so, all the code in this book should run.

Installing R (and RStudio)

It is recommended that you install R and *RStudio Desktop*. *RStudio Desktop* is a graphical user interface with many tools that making writing R easier and more fun.

Install R from the Comprehensive R Archive Network (CRAN).

You can access instructions for your specific machine by clicking [here](#).³

You can get RStudio Desktop directly from the company's website⁴.

0.0.1 Installing Python by Installing Anaconda {-}

It is recommended that you install *Anaconda*, which is a package manager, environment manager, and Python distribution with many third party open source packages. It provides a graphical user interface for us, too, just as RStudio does. You can access instructions for your specific machine and OS by clicking [here](#)⁵.

³<https://cran.r-project.org/>

⁴<https://www.rstudio.com/products/rstudio/download/#download>

⁵<https://docs.anaconda.com/anaconda/install/#>

Part I

Part I



0

Introduction

Now that you have both R and Python installed, we can get started by taking a tour of our two different **integrated development environments environments** (IDEs) RStudio and Spyder.

In addition, I will also discuss a few topics superficially, so that we can get our feet wet:

- printing,
- creating variables, and
- calling functions.

0.1 Hello World in R

Go ahead and open up RStudio. It should look something like this

I changed my “Editor Theme” from the default to “Cobalt” because it’s easier on my eyes. If you are opening RStudio for the first time, you probably see a lot more white. You can play around with the theme, if you wish, after going to `Tools -> Global Options -> Appearance`.

The **console**, which is located by default on the lower left panel, is the place that all of your code gets run. For short one-liners, you can type code directly into the console. Try typing the following code in there. Here we are making use of the `print()` function.

In R, functions are “first-class objects,” which means can refer to the name of a function without asking it to do anything. However, when we *do* want to use it, we put parentheses after the name.

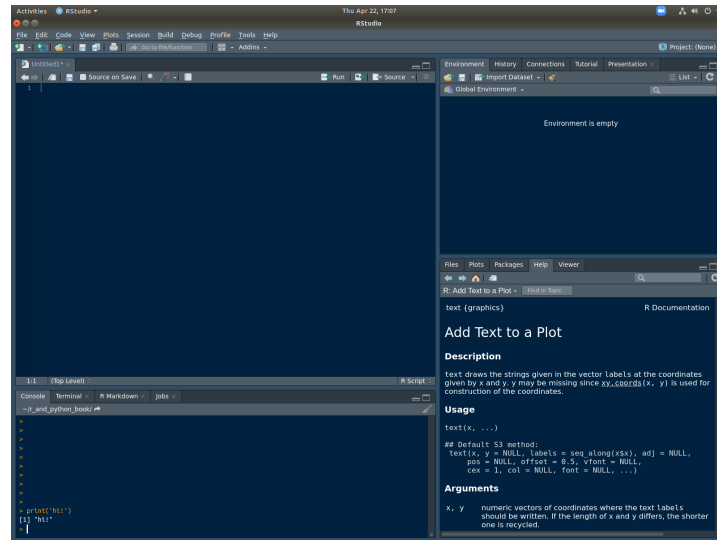


FIGURE 1: RStudio

This is called **calling** the function or **invoking** the function. If a function call takes any **arguments** (aka inputs), then the programmer supplies them between the two parentheses. A function may **return** values to be subsequently used, or it may just produce a “side-effect” such as printing some text, displaying a chart, or read/writing information to an external data source.

```
print('hello R world')
## [1] "hello R world"
```

During the semester, we will write more complicated code. Complicated code is usually written incrementally and stored in a text file called a **script**. Click **File** -> **New File** -> **R Script** to create a new script. It should appear at the top left of the RStudio window (see Figure 1). After that, copy and paste the following code into your script window.

```
print('hello world')
print("this program")
```

```
print('is not incredibly interesting')
print('but it would be a pain')
print('to type it all directly into the console')
myName <- "Taylor"
print(myName)
```

This script will run five print statements, and then create a variable called `myName`. The print statements are of no use to the computer and will not affect how the program runs. They just display messages to the human running the code.

The variable created on the last line is more important because it is used by the computer, and so it can affect how the program runs. The operator `<-` is the **assignment operator**⁶. It takes the character constant `"Taylor"`, which is on the right, and stores it under the name `myName`. If we added lines to this program, we could refer to the variable `myName` in subsequent calculations.

Save this file wherever you want on your hard drive. Call it `awesomeScript.R`. Personally, I saved it to my desktop.

After we have a saved script, we can run it by sending all the lines of code over to the console. One way to do that is by clicking the **Source** button at the top right of the script window (see Figure 1).

Another way is that we can use R's `source()` function. We can run the following code in the console.

```
# Anything coming after the pound/hash-tag symbol
# is a comment to the human programmer.
# These lines are ignored by R
setwd("/home/taylor/Desktop/")
source("awesomeScript.R")
```

⁶<https://stat.ethz.ch/R-manual/R-devel/library/base/html/assignOps.html>

The first line changes the **working directory**⁷ to `Desktop/`. You, dear reader, should change this line by replacing `Desktop/` to whichever folder you chose to save `awesomeScript.R` in. If you would like to find out what your working directory is currently set to, you can use `getwd()`.

Every computer has a different folder/directory structure—that is why it is highly recommended you refer to file locations as seldom as possible in your scripts. This makes your code more *portable*. When you send your file to someone else (e.g. your instructor or your boss), she will have to remove or change every mention of any directory. This is because those directories (probably) won't exist on her machine.

The second line calls `source()`. This function finds the script file and executes all the commands found in that file sequentially.

A third way is to tell R to run `awesomeScript.R` from the command line. We will describe this approach in more detail in section 0.52

0.2 Hello World in Python

First, start by opening *Anaconda Navigator*. It should look something like this:

Recall that we will exclusively assume the use of *Spyder* in this textbook. Open that up now. It should look something like this:

It looks a lot like RStudio, right? The script window is still on the left hand side, but it takes up the whole height of the window this time. However, you will notice that the console window has moved. It's over on the bottom right now.

Again, you might notice a lot more white when you open this for the first time. Just like last time, I changed my color scheme. You

⁷<https://stat.ethz.ch/R-manual/R-devel/library/base/html/getwd.html>

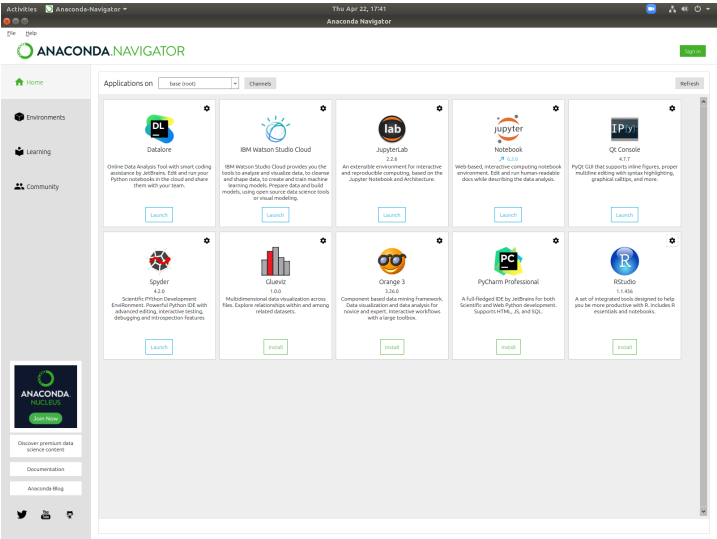


FIGURE 2: Anaconda Navigator

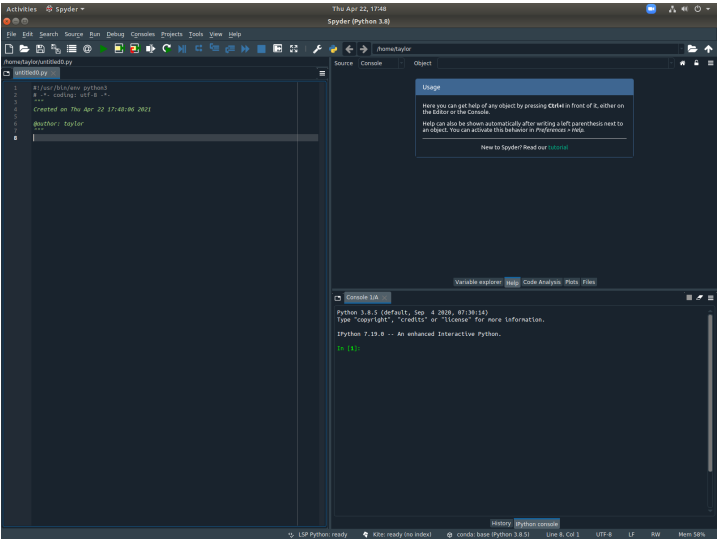


FIGURE 3: Spyder

can change yours by going to **Tools -> Preferences** and then exploring the options available under the **Appearances** tab.

Try typing the following line of code into the console.

```
# this looks like R code but it's Python code!
print("hello Python world")
## hello Python world
```

Already we have many similarities between our two languages. Both R and Python have a `print()` function, and they both use the same symbol to start a comment: `#`. Finally, they both define character/string constants with quotation marks. In both languages, you can use either single or double quotes.

We will also show below that both languages share the same three ways to run scripts. Nice!

Let's try writing our first Python script. R scripts end in `.r` or `.R`, while Python scripts end in `.py`. Call this file `awesomeScript.py`.

```
# save this as awesomeScript.py
print('hello world')
print("this program")
print('is pretty similar to the last program')
print('it is not incredibly interesting, either')
my_name = "Taylor"
print(my_name)
```

Notice that the assignment operator is different in Python. It's an `=`⁸.

Just like RStudio, Spyder has a button that runs the entire script from start to finish. It's the green triangle button (see Figure 3).

You can also write code to run `awesomeScript.py`. There are a few ways to do this, but here's the easiest.

⁸You can use this symbol in R, too, but it is less common.

```
import os
os.chdir('/home/taylor/Desktop')
runfile("awesomeScript.py")
```

This is also pretty similar to the R code from before. `os.chdir()` sets our working directory to the `Desktop`. Then `runfile()` runs all of the lines in our program, sequentially, from start to finish.

The first line is new, though. We did not mention anything like this in R, yet. We will talk more about `importing` modules in section 0.42. Suffice it to say that we imported the `os` module to make the `chdir()` function available to us.

Third, we can tell Python to run `awesomeScript.py` from the command line. We will describe this approach in more detail in chapter [@\(running-scripts-from-the-command-line\)](#)

0.3 Getting Help

0.3.1 Reading Documentation

Programming is not about memorization. Nobody can memorize, for example, every function and all of its arguments. Nobody can do that. Not even close. So what do programmers do when they get stuck? The primary way is to read the documentation.

0.3.1.1 In R

Getting help in R is easy. If you want to know more about a function, type into the console the name of the function with a leading question mark. For example, `?print` or `?setwd`. You can also use `help()` and `help.search()` to find out more about functions (e.g. `help(print)`). Sometimes you will need to put quotation marks around the name of the function (e.g. `?":"`).

This will not open a separate web browser window, which is very convenient. If you are using RStudio, you have some extra benefits. Everything will look very pretty, and you can search through the text by typing phrases into the search bar in the “Help” window.

0.3.1.2 In Python

In Python, the question mark comes *after* the name of the function⁹ (e.g. `print?`), and you can use `help(print)` just as in R.

In Spyder, if you want the documentation to appear in the Help window (it looks prettier), then you can type the name of the function, and then `Ctrl-i` (`Cmd-i` on a mac keyboard).

0.3.2 Understanding File Paths

File paths look different on different operating systems. Mac and Linux machines tend to have forward slashes (i.e. `/`), while Windows machines tend to use backslashes (i.e. `\`).

Depending on what kind of operating system is running your code, you will need to change the file paths. It is important for everyone writing R and Python code to understand how things work on both types of machines—just because you’re writing code on a Windows machine doesn’t mean that it won’t be run on a Mac, or vice versa.

0.3.2.1 *nix Machines

The directory repeatedly mentioned in the code above was `/home/taylor/Desktop`. This is a directory on my machine which is running Ubuntu Linux. The leading forward slash is the *root directory*. Inside that is the directory `home/`, and inside that is `taylor/`, and inside that is `Desktop/`. If you are running MacOS, these file paths will look very similar. The folder `home/` will most likely be replaced with `Users/`.

⁹If you did not install Anaconda, then this may not work for you because this is an IPython (<https://ipython.org>) feature.

0.3.2.2 Windows Machines

On Windows, things are a bit different. For one, a full path starts with a drive (e.g. `C:`). Second, there are backslashes (not forward slashes) to separate directory names (e.g. `C:\Users\taylor\Desktop`).

Unfortunately, backslashes are a special character in both R and Python. Whenever you type a `\`, it will change the meaning of whatever comes after it. In other words, `\` is known as an **escape character**.

In both R and Python, the backslash character is used to start an “escape” sequence. You can see some examples in R by clicking here¹⁰, and some examples in Python by clicking here¹¹. In Python it may also be used to allow long lines of code to take up more than one line in a text file.¹²

The recommended way of handling this is to just use forward slashes instead. For example, if you are running Windows, `C:/Users/taylor/Desktop/myScript.R` will work in R, and `C:/Users/taylor/Desktop/myScript.py` will work in Python.

You may also use “raw string constants” (e.g. `r'C:\Users\taylor\Desktop\my_file.txt'`). “Raw” means that `\` will be treated as a literal character instead of an escape character.

Alternatively, you can “escape” the backslashes by replacing each single backslash with a double backslash.

¹⁰<https://stat.ethz.ch/R-manual/R-devel/library/base/html/Quotes.html>

¹¹https://docs.python.org/3/reference/lexical_analysis.html

¹²https://docs.python.org/3/reference/lexical_analysis.html#explicit-line-joining





Part II

Part I: Data Types



0

Basic Types

In every programming language, data is stored in different ways. Writing a program that manipulates data requires understanding all of the choices. That is why we must be concerned with the different **types** of data in our R and Python programs. Different types are suitable for different purposes.

There are similarities between Python's and R's type systems. However, there are many differences as well. Be prepared for these differences. There are many more of them in this chapter than there were in the previous chapter!

If you're ever unsure what type a variable has, use `type()` (in Python) or `typeof()` (in R) to query it.

Storing an individual piece of information is simple in both languages. However, while Python has scalar types, R does not draw as strong of a distinction between scalar and compound types.

0.4 Basic Types In Python

In Python, the simplest types we frequently use are `str` (short for string), `int` (short for integer), `float` (short for floating point) and `bool` (short for Boolean). This list is not exhaustive, but these are a good collection to start thinking about. For a complete list of built-in types in Python, click here¹³.

¹³<https://docs.python.org/3/library/stdtypes.html>

```
print(type('a'), type(1), type(1.3))  
## <class 'str'> <class 'int'> <class 'float'>
```

Strings are useful for processing text data such as names of people/places/things and messages such as texts, tweets and emails. If you are dealing with numbers, you need floating points if you have a number that might have a fractional part after its decimal; otherwise you'll need an integer. Booleans are useful for situations where you need to record whether something is true or false. They are also important to understand for control-flow in section 0.42.1.

In the next section we will discuss the Numpy library. This library has a broader collection¹⁴ of basic types that allows for finer control over any script you write.

0.4.1 Type Conversions in Python

We will often have to convert between types in a Python program. This is called **type conversion**, and it can be either implicitly or explicitly done.

For example, ints are often implicitly converted to floats, so that arithmetic operations work.

```
my_int = 1  
my_float = 3.2  
my_sum = my_int + my_float  
print("my_int's type", type(my_int))  
## my_int's type <class 'int'>  
print("my_float's type", type(my_float))  
## my_float's type <class 'float'>  
print(my_sum)  
## 4.2
```

¹⁴<https://numpy.org/doc/stable/user/basics.types.html>

```
print("my_sum's type", type(my_sum))
## my_sum's type <class 'float'>
```

You might be disappointed if you always count on this behavior, though.

```
3.2 + "3.2"
## Error in py_call_impl(callable, dots$args, dots$keywords): TypeError: unsupported operand type(s) for +: float and str
##
## Detailed traceback:
##   File "<string>", line 1, in <module>
```

Explicit conversions occur when we as programmers explicitly ask Python to perform a conversion. We will do this with the functions such as `int()`, `str()`, `float()`, and `bool()`.

```
my_date = "5/2/2021"
month_day_year = my_date.split('/')
my_year = int(month_day_year[-1])
print('my_year is equal to ', my_year, 'and its type is ', type(my_year))
## my_year is equal to 2021 and its type is <class 'int'>
```

0.5 Basic Types In R

In R, the names of basic types are only slightly different. They are `logical` (instead of `bool`), `integer` (instead of `int`), `double` or `numeric` (instead of `float`)¹⁵, `character` (instead of `str`), `complex` (for calculations involving imaginary numbers), and `raw` (useful for working with bytes).

¹⁵“double” is short for “double precision floating point.” In other programming languages, the programmer might choose how many decimal points of precision he or she wants.

```
# cat() is kind of like print()
cat(typeof('a'), typeof(1), typeof(1.3))
## character double double
```

In this case R automatically upgraded 1 to a double. If you wanted to force it to be an integer, you can add a capital “L” to the end of the number.

```
# cat() is kind of like print()
cat(typeof('a'), typeof(1L), typeof(1.3))
## character integer double
```

0.5.1 Type Conversions in R

You can explicitly and implicitly convert types in R just as you did in Python. Implicit conversion looks like this.

```
myInt = 1
myDouble = 3.2
mySum = myInt + myDouble
print(paste0("my_int's type is ", typeof(myInt)))
## [1] "my_int's type is double"
print(paste0("my_float's type is ", typeof(myDouble)))
## [1] "my_float's type is double"
print(mySum)
## [1] 4.2
print(paste0("my_sum's type is ", typeof(mySum)))
## [1] "my_sum's type is double"
```

Explicit conversion can be achieved with functions such as `as.integer`, `as.logical`, `as.double`, etc.

```
print(typeof(1))
## [1] "double"
```

```
print(typeof(as.logical(1)))  
## [1] "logical"
```

0.5.2 R's Simplification

The basic types of R are a little different than the basic types of Python. On the one hand, Python has basic types for individual elements, and it uses separate types as containers for storing many elements. On the other, R uses the same type to store a single element as it does to store many elements. Strictly speaking, R does not have a scalar type.

Technically, all of the examples we just did in R are using length one **vectors**—`logical`, `integer`, `double`, `character`, `complex`, and `raw` are the possible **modes** of a vector. **vectors** will be discussed further section 0.6.6.2.

Think about which option you prefer. What are the benefits of using separate types for scalars and collections? What are the benefits of using the same type?

0.6 Exercises

0.6.1 Easier R Questions

1. Which R base type is ideal for each piece of data? Assign your answers to a `character vector` of length four called `questionOne`.
 - An individual's IP address
 - whether or not an individual attended a study
 - the number of seeds found in a plant
 - the amount of time it takes for a car to race around a track

2. Floating points are weird. What gets printed is not the same as what is stored! In R, you can control how many digits get printed by using the `options` function.
 - Assign `a` to `2/3`
 - `print a`, and copy/paste what you see into the variable `aPrint`. Make sure it is a character.
 - Take a look at the documentation for `options`. Assign the value of `options()$digits` to `numDigitsStart`
 - Change the number of digits to 22
 - Again, `print, a` and copy/paste what you see into the variable `aPrintv2`. Make sure it is a character.
 - Assign the output of `options()$digits` to `numDigitsEnd`
3. Floating points are weird. What gets stored might not be what you want. “The only numbers that can be represented exactly in R’s numeric type are integers and fractions whose denominator is a power of 2.”¹⁶
 - Assign the square root of 2 to `mySqrt`
 - Print the square of this variable
 - Test (using `==`) that this variable is equal to 2. Assign the result of this test to `isTwoRecoverable`
 - Test for near equality (using `all.equal`) that this variable is “equal” to 2. Assign the result of this test to `closeEnough`. Make sure to read the documentation for this function because the return type can be tricky!
4. Let’s flip some coins! Generate a thousand flips of a fair coin. Use `rbinom`, and let heads be coded as 1 and tails coded as 0.
 - Assign the thousand raw coin flips to a variable

¹⁶https://cran.r-project.org/doc/FAQ/R-FAQ.html#Why-doesn_0027t-R-think-these-numbers-are-equal_003f

- flips. Make sure the elements are integers, and make sure you flip a “fair” coin ($p = .5$).
- Create a length 1000 logical vector called `isHeads`. Whenever you get a heads, make sure the corresponding element is `TRUE` and `FALSE` otherwise.
 - Create a variable called `numHeads` by tallying up the number of heads.
 - Calculate the percent of time that the number changes in `flips`. Assign your number to `acceptanceRate`. Try to write only one line of code to do this.

0.6.2 Easier Python Questions

1. Which Python type is ideal for each piece of data? Assign your answers to a list of strings called `question_one`.
 - An individual’s IP address
 - whether or not an individual attended a study
 - the number of seeds found in a plant
 - the amount of time it takes for a car to race around a track
2. Floating points are weird. What gets printed is not the same as what is stored! In Python, you need to edit a class’s `__str__` method if you want to control how many digits get printed, but we won’t do that. Instead, we’ll use `str.format()`¹⁷ to return a string directly (instead of copy/paste-ing it).
 - Assign `a` to `2/3`
 - print `a`, and copy/paste what you see into the variable `a_print`
 - Create a `str` that displays 22 digits of `2/3`. Call it `a_printv2`
 - print the above string

¹⁷<https://docs.python.org/3/library/stdtypes.html#str.format>

3. Floating points are weird. What gets stored might not be what you want. The Python documentation has an excellent discussion of how storage behavior can be surprising. Click here¹⁸ to read it.
 - Assign the square root of 2 to `my_sqrt`
 - `print` the square of this variable
 - Test (using `==`) that this variable is equal to 2. Assign the result of this test to `is_two_recoverable`
 - Test for near equality (using `np.isclose`) that this variable is “equal” to 2. Assign the result of this test to `close_enough`.
4. Let’s flip some coins (again)! Generate a thousand flips of a fair coin. Use `np.random.binomial`, and let heads be coded as 1 and tails coded as 0.
 - Assign the thousand raw coin flips to a variable `flips`. Make sure the elements are integers, and make sure you flip a “fair” coin ($p = .5$).
 - Create a length 1000 list of bools called `is_heads`. Whenever you get a heads, make sure the corresponding element is `True` and `False` otherwise.
 - Create a variable called `num_heads` by tallying up the number of heads.
 - Calculate the percent of time that the number changes in `flips`. Assign your number to `acceptance_rate`. Try to write only one line of code to do this.

0.6.3 More Difficult R Questions

0.6.3.1 Examining a vector

1. Say you have a vector of prices of some financial asset:

¹⁸<https://docs.python.org/3/tutorial/floatingpoint.html>


```
prices <- c(100.10, 95.98, 100.01, 99.87)
```

Convert this vector into a vector of *log returns*. Call the variable `logReturns`. If p_t is the price at time t , the log return ending at time t is

$$r_t = \log \left(\frac{p_t}{p_{t-1}} \right) = \log p_t - \log p_{t-1}$$

2. Do the same for *arithmetic returns*. These are regular percent changes if you scale by 100. Call the variable `arithReturns`. The mathematical formula you need is

$$a_t = \left(\frac{p_t - p_{t-1}}{p_{t-1}} \right) \times 100$$

0.6.3.2 Some Monte Carlo

Consider another **mixture density** $f(y) = \int f(y | x)f(x)dx$ where

$$Y | X \sim \text{Normal}(0, x^2)$$

and

$$X \sim \text{half-Cauchy}(0, 1).$$

This distribution is a special case of a prior distribution that is used in Bayesian statistics (Carvalho et al., 2009).

Suppose further that you are interested in calculating the probability that one of these random variables ends up being too far from the median:

$$\mathbb{P}[|Y| > 1] = \int_{y:|y|>1} f(y)dy = \int_{y:|y|>1} \int_{-\infty}^{\infty} f(y | x)f(x)dx dy.$$

1. Simulate X_1, \dots, X_{5000} from a half-Cauchy(0, 1) and call these samples `xSamps`. Hint: you can simulate from a t distribution with one degree of freedom to sample from a

Cauchy. Once you have regular Cauchy samples, take the absolute value of each one.

2. Simulate $Y_1 \mid X_1, \dots, Y_{5000} \mid X_{5000}$ and call the samples `ySamps`.
3. Calculate the approximate probability using `ySamps` and call it `approxProbDev1`.
4. Why is simply “ignoring” `xSamps`, the samples you condition on, “equivalent” to “integrating out x ”? Store a string response as a length 1 character vector called `integratingOutResp`.
5. Calculate another **Rao-Blackwellized** Monte Carlo estimate of $\mathbb{P}[|Y| > 1]$ from `xSamps`. Call it `approxProbDev2`. Hint: $\mathbb{P}[|Y| > 1] = \mathbb{E}[\mathbb{P}(|Y| > 1 \mid X)]$. Calculate $\mathbb{P}(|Y| > 1 \mid X = x)$ with pencil and paper, notice it is a function in x , apply that function to each of `xSamps`, and average all of it together.
6. Are you able to calculate an exact solution to $\mathbb{P}[|Y| > 1]$?

0.6.3.3 Playing Around with Some Letters

1. Store the ordered uppercase letters of the alphabet in a length 26 character vector called `myUppcaseLetters`. Do not hardcode this. Use a function, along with the variable `letters`.
2. Create a new vector called `withReplacements` that’s the same as the previous vector, but replace all vowels with “---”. Again, do not hardcode this. Find a function that searches for patterns and performs a replacement whenever that pattern is found.
3. Create a length 26 logical vector that is `TRUE` whenever an element of `letters` is a consonant, and `FALSE` everywhere else. Call it `consonant`.

0.6.4 More Difficult Python Questions

0.6.5 Examining a **Series** taken from a **DataFrame**

1. Use `pd.read_csv` to correctly read in "2013-10-Citi_Bike_trip_data_20K.csv" as a data frame called `my_df`. Make sure to read `autograding_tips.html`.
2. extract the "starttime" column into a separate **Series** called `s_times`
3. extract date strings of those elements into a **Series** called `date_strings`
4. extract time strings of those elements into a **Series** called `time_strings`

0.6.6 Monte Carlo Integration

0.6.6.1 Approximating Probabilities

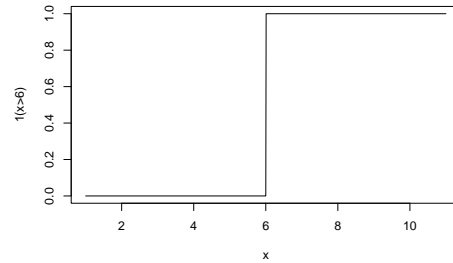
We will make use of the *Monte Carlo* (Robert and Casella, 2005) method below. It is a technique to approximate expectations and probabilities. If n is a large number, and X_1, \dots, X_n is a random sample drawn from the distribution of interest, then

$$\mathbb{P}(X > 6) \approx \frac{1}{n} \sum_{i=1}^n \mathbf{1}(X_i > 6).$$

If you haven't seen an **indicator function** before, it is defined as

$$\mathbf{1}(X_i > 6) = \begin{cases} 1 & X_i > 6 \\ 0 & X_i \leq 6 \end{cases}.$$

If you wanted to visualize it, $\mathbf{1}(x > 6)$ looks like this.



So, the sum in this expression is just a count of the number of elements that are greater than 6.

1. Evaluate exactly the probability that a normal random variable with mean 5 and standard deviation 6 is greater than 6. Assign it to the variable `exact_exceedance_prob` in Python.
2. Simulate `1e3` times from a standard normal distribution (mean 0 and variance 1). Call the samples `stand_norm_samps`
3. Calculate a Monte Carlo estimate of $\mathbb{P}(X > 6)$ from these samples. Call it `approx_exceedance_prob1`.
4. Simulate `1e3` times from a normal distribution with mean 5 and standard deviation 6. Call the samples `norm_samps`. Don't use the old samples in any way.
5. Calculate a Monte Carlo estimate of $\mathbb{P}(X > 6)$ from these new `norm_samps`. Call it `approx_exceedance_prob2`.

0.6.6.2 Approximating Expectations

Alternatively, we can approximate expectations. If $\mathbb{E}[f(X)]$ exists, n is a large number, and W_1, \dots, W_n is a random sample drawn from the distribution of interest, then

$$\mathbb{E}[f(W)] \approx \frac{1}{n} \sum_{i=1}^n f(W_i).$$

Here's a new distribution. It is a **mixture distribution**, specifi-

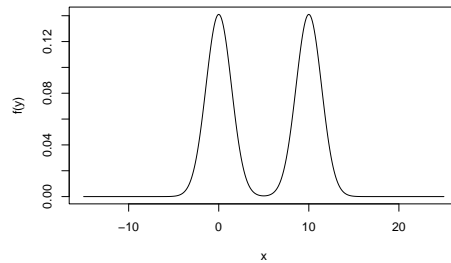
cally a **finite mixture of normal distributions**: $f(y) = f(y | X = 1)P(X = 1) + f(y | X = 0)P(X = 0)$ where

$$Y | X = 0 \sim \text{Normal}(0, 2) \quad Y | X = 1 \sim \text{Normal}(10, 2)$$

and

$$X \sim \text{Bernoulli}(.5).$$

Both $f(y | X = 0)$ and $f(y | X = 1)$ are bell-curved, and $f(y)$ looks like this



1. Evaluate exactly $\mathbb{E}[Y]$. Assign it to the variable `exact_mean` in Python.
2. Simulate `1e3` times from the Bernoulli distribution. Call the samples `bernoulli_flips`
3. Simulate $Y_1 | X_1, \dots, Y_{1000} | X_{1000}$ and call the samples `cond_norm_samps`.
4. Calculate a Monte Carlo estimate of $\mathbb{E}[Y]$ from `cond_norm_samps`. Call it `approx_ave_1`. Why is simply “ignoring” `bernoulli_flips`, the samples you condition on, “equivalent” to “integrating them out?”
5. Calculate a **Rao-Blackwellized** Monte Carlo estimate of $\mathbb{E}[Y]$ from `bernoulli_flips`. Call it `approx_ave_2`. Hint: $\mathbb{E}[Y] = \mathbb{E}[\mathbb{E}(Y | X)]$. Calculate $\mathbb{E}(Y | X_i)$ exactly, and evaluate that function on each X_i sample, and then average them together. Rao-Blackwellization is a variance-reduction technique that allows you come up with lower-variance estimates given a fixed computational budget.



0

R vectors versus Numpy arrays and Pandas' Series

This section is for describing the data types that let us store collections of elements that all **share the same type**. Data is very commonly stored in this fashion, so this section is quite important. Once we have one of these collection objects in a program, we will be interested in learning how to extract and modify different elements in the collection, as well as how to use the entire collection in an efficient calculation.

0.7 Overview of R

In the previous section, I mentioned that R does not have scalar types—it just has **vectors**¹⁹. So, whether you want to store one number (or `logical`, or `character`, or ...), or many numbers, you will need a **vector**.

For many, the word “vector” evokes an impression that these objects are designed to be used for performing matrix arithmetic (e.g. inner products, transposes, etc.). You can perform these operations on **vectors**, but in my opinion, this preconception can be misleading, and I recommend avoiding it. Most of the things you can do with **vectors** in R have little to do with linear algebra!

How do we create one of these? There are many ways. One common

¹⁹<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Vector-objects>

way is to read in elements from an external data set. Another way is to generate vectors from code.

```
1:10          # consecutive integers
## [1] 1 2 3 4 5 6 7 8 9 10
seq(1,10,2)   # arbitrary sequences
## [1] 1 3 5 7 9
rep(2,5)      # repeating numbers
## [1] 2 2 2 2 2
c("5/2/2021", "5/3/2021", "5/4/2021") # combine elements without relying on a pattern
## [1] "5/2/2021" "5/3/2021" "5/4/2021"
rnorm(10)     # generate Gaussian random variables
## [1] 0.6708303 -1.3901584 2.3564705 -0.5026985 -2.8020787 -1.6232026 0.27457
## [10] -1.7146973
```

`c()` is short for “combine”. `seq()` and `rep()` are short for “sequence” and “replicate”, respectively. `rnorm()` samples normal (or Gaussian) random variables. There is plenty more to learn about these functions, so I encourage you to take a look at their documentation.

I should mention that functions such as `rnorm()` don’t create truly random numbers, just *pseudorandom* ones. Pseudorandom numbers are nearly indecipherable from truly random ones, but the way the computer generates them is actually deterministic.

First, a *seed*, or starting number is chosen. Then, the *pseudorandom number generator (PRNG)* maps that number to another number. The sequence of all the numbers appears to be random, but is actually deterministic.

Sometimes you will be interested in setting the seed on your own because it is a cheap way of sharing and communicating data with others. If two people use the same starting seed, and the same PRNG, then they should simulate the same data. This can be important if you want to help other people reproduce the results of code you share. Most of the time, though, I don’t set the seed, and

I don't think about the distinction between random and pseudo-random numbers.

0.8 Overview of Python

If you want to store many elements of the same type (and size) in Python, you will probably need a Numpy array. Numpy is a highly-regarded third party library (Harris et al., 2020) for Python. Its array objects store elements of the same type, just as R's vectors do.

There are five ways to create numpy arrays (source²⁰). Here are some examples that complement the examples from above.

```
import numpy as np
np.array([1,2,3])
## array([1, 2, 3])
np.arange(1,12,2)
## array([ 1,  3,  5,  7,  9, 11])
np.random.normal(size=3)
## array([0.68142417, 0.54087541, 1.23369108])
```

Another option for storing a homogeneous collection of elements in Python is a Series object²¹ from the Pandas library. The benefit of these is that they play nicely with Pandas' data frames (more information about Pandas' data frames can be found in 0.32), and that they have more flexibility with accessing elements by name (see here²² for more information).

²⁰<https://numpy.org/doc/stable/user/basics.creation.html>

²¹<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.Series.html#pandas-series>

²²<https://jakevdp.github.io/PythonDataScienceHandbook/03.01-introducing-pandas-objects.html#Series-as-generalized-NumPy-array>

```
import pandas as pd
first = pd.Series([2, 4, 6])
second = pd.Series([2, 4, 6], index = ['a','b','c'])
print(first[0])
## 2
print(second['c'])
## 6
```

0.9 Vectorization in R

An operation in R is **vectorized** if it applies to all of the elements of a **vector** at once. An operator that is not vectorized can only be applied to individual elements. In that case, the programmer would need to write more code to instruct the function to be applied to all of the elements of a vector. You should prefer writing vectorized code because it is usually easier to read. Moreover, many of these vectorized functions are written in compiled code, so they can often be much faster.

Arithmetic (e.g. `+`, `-`, `*`, `/`, `^`, `%%`, `%/%`, etc.) and logical (e.g. `!`, `|`, `&`, `>`, `>=`, `<`, `<=`, `==`, etc.) operators are commonly applied to one or two vectors. Arithmetic is usually performed *element-by-element*. Numeric vectors are converted to logical vectors if they need to be. Be careful of operator precedence if you seek to minimize your use of parentheses.

Note that there are an extraordinary amount of named functions (e.g. `sum()`, `length()`, `cumsum()`, etc.) that operate on entire vectors, as well. Here are some examples.

```
(1:3) * (1:3)
## [1] 1 4 9
(1:3) == rev(1:3)
```

```
## [1] FALSE TRUE FALSE
sin( (2*pi/3)*(1:5))
## [1]  8.660254e-01 -8.660254e-01 -2.449294e-16  8.660254e-01 -8.660254e-01
```

In the last example, there is **recycling** happening. $(2\pi/3)$ is taking three length-one vectors and producing another length-one vector. The resulting length-one vector is multiplied by a length five vector `1:5`. The single element in the length one vector gets *recycled* so that its value is multiplied by every element of `1:5`. This makes sense most of the time, but sometimes recycling can be tricky. Notice that the following code does not produce an error—just a warning.

```
(1:3) * (1:4)
## Warning in (1:3) * (1:4): longer object length is not a multiple of shorter obj
## [1] 1 4 9 4
```

0.10 Vectorization in Python

The Python’s Numpy library makes extensive use of vectorization as well. Vectorization in Numpy is accomplished with **universal functions**²³, or “ufuncs” for short. Some ufuncs can be invoked using the same syntax as in R (e.g. `+`). You can also refer to function by its name (e.g. `np.sum()` instead of `+`). Mixing and matching is allowed, too.

Ufuncs are called *unary* if they take in one array, and *binary* if they take in two. At the moment, there are fewer than 100 available²⁴, all performing either mathematical operations, boolean-emitting comparisons, or bit-twiddling operations. For an exhaustive list

²³<https://numpy.org/doc/stable/reference/ufuncs.html>

²⁴<https://numpy.org/doc/stable/reference/ufuncs.html#available-ufuncs>

of Numpy's universal functions, click here.²⁵ Here are some code examples.

```
np.arange(1,4)*np.arange(1,4)
## array([1, 4, 9])
np.zeros(5) > np.arange(-3,2)
## array([ True,  True,  True, False, False])
np.exp( -.5 * np.linspace(-3, 3, 10)**2) / np.sqrt( 2 * np.pi)
## array([0.00443185, 0.02622189, 0.09947714, 0.24197072, 0.37738323,
##        0.37738323, 0.24197072, 0.09947714, 0.02622189, 0.00443185])
```

Instead of calling it “recycling”, Numpy calls reusing elements of a shorter array in a binary operation **broadcasting**²⁶. It's the same idea as in R, but in general, Python is stricter and disallows more scenarios.

```
np.arange(1,3)*np.arange(1,4)
## Error in py_call_impl(callable, dots$args, dots$keywords): ValueError: operands
##
## Detailed traceback:
##   File "<string>", line 1, in <module>
```

If you are working with string arrays, Numpy has a `np.char` module with many useful functions²⁷.

```
a = np.array(['a','b','c'])
np.char.upper(a)
## array(['A', 'B', 'C'], dtype='<U1')'
```

Then there are the `Series` objects from Pandas. Ufuncs continue to

²⁵<https://numpy.org/doc/stable/reference/ufuncs.html#available-ufuncs>

²⁶<https://numpy.org/devdocs/user/theory.broadcasting.html>

²⁷<https://numpy.org/doc/stable/reference/routines.char.html#module-numpy.char>

work in the same way on `Series` objects, and they respect common index values²⁸.

```
s1 = pd.Series(np.repeat(100,3))
s2 = pd.Series(np.repeat(10,3))
s1 + s2
## 0    110
## 1    110
## 2    110
## dtype: int64
```

If you feel more comfortable, and you want to coerce these `Series` objects to Numpy arrays before working with them, you can do that. For example, the following works.

```
s = pd.Series(np.linspace(-1,1,5))
np.exp(s.to_numpy())
## array([0.36787944, 0.60653066, 1.          , 1.64872127, 2.71828183])
```

In addition, `Series` objects possess many extra attributes and methods²⁹.

```
ints = pd.Series(np.arange(10))
ints.abs()
## 0    0
## 1    1
## 2    2
## 3    3
## 4    4
## 5    5
## 6    6
## 7    7
```

²⁸<https://jakevdp.github.io/PythonDataScienceHandbook/03.03-operations-in-pandas.html>

²⁹<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.Series.html#pandas-series>

liv

R vectors versus Numpy arrays and Pandas' Series

```
## 8      8
## 9      9
## dtype: int64
ints.mean()
## 4.5
ints.floordiv(2)
## 0      0
## 1      0
## 2      1
## 3      1
## 4      2
## 5      2
## 6      3
## 7      3
## 8      4
## 9      4
## dtype: int64
```

Series objects that have text data³⁰ are a little bit different. For one, you have to access the `.str` attribute of the `Series` before calling any vectorized methods³¹. Here are some examples.

```
s = pd.Series(['a','b','c','33'])
s.dtype
```

```
## dtype('O')
```

```
s.str.isdigit()
```

```
## 0      False
## 1      False
```

³⁰https://pandas.pydata.org/pandas-docs/stable/user_guide/text.html#working-with-text-data

³¹<https://jakevdp.github.io/PythonDataScienceHandbook/03.10-working-with-strings.html>

```
## 2    False
## 3     True
## dtype: bool
```

```
s.str.replace('a', 'z')
```

```
## 0      z
## 1      b
## 2      c
## 3     33
## dtype: object
```

String operations can be a big game changer, and we discuss text processing strategies in more detail in section [@ \(working-with-text-data\)](#).

0.11 Indexing Vectors in R

It is very common to want to extract or modify a subset of elements in a vector. There are a few ways to do this. All of the ways I discuss will involve the square bracket operator (i.e. `[]`). Feel free to retrieve the documentation by typing `?['`.

```
allElements <- 1:6
allElements[seq(2,6,2)] # extract evens
## [1] 2 4 6
allElements[-seq(2,6,2)] <- 99 # replace all odds with 99
allElements[allElements > 2] # get nums bigger than 2
## [1] 99 99 4 99 6
```

To access the first element, we use the index 1. To access the second, we use 2, and so on. Also, the `-` sign tells R to remove elements. Both of these functionalities are *very different* from Python, as we will see shortly.

We can use names to access elements, too, but only if the elements are named.

```
sillyVec <- c("favorite"=1, "least favorite" = 2)
sillyVec['favorite']
## favorite
##      1
```

0.12 Indexing Numpy arrays

Indexing Numpy arrays³² is very similar to indexing vectors in R. You use the square brackets, and you can do it with logical arrays or index arrays. There are some important differences, though.

For one, indexing is 0-based in Python. The 0th element is the first element of an array. Another key difference is that the - isn't used to remove elements like it is in R, but rather to count backwards. Third, using one or two : inside square brackets is more flexible in Python. This is syntactic sugar for using the `slice()` function, which is similar to R's `seq()` function.

```
one_through_ten = np.arange(1, 11)
one_through_ten[np.array([2,3])]
## array([3, 4])
one_through_ten[1:10:2] # evens
## array([ 2,  4,  6,  8, 10])
one_through_ten[::-1] # reversed
## array([10,  9,  8,  7,  6,  5,  4,  3,  2,  1])
one_through_ten[-2] = 99 # second to last
one_through_ten
## array([ 1,  2,  3,  4,  5,  6,  7,  8, 99, 10])
```

³²<https://numpy.org/doc/stable/user/basics.indexing.html>


```
one_through_ten[one_through_ten > 3] # bigger than three
## array([ 4,  5,  6,  7,  8, 99, 10])
```

0.13 Indexing Pandas' Series

At a minimum, there is little that is new that you *need* to learn to go from Numpy arrays to Pandas' Series objects. They still have the `[]` operator, and many methods are shared across these two types³³. The following is almost equivalent to the code above, and the only apparent difference is that the results are printed a little differently.

```
import pandas as pd
one_through_ten = pd.Series(np.arange(1, 11))
one_through_ten[np.array([2,3])]
## 2      3
## 3      4
## dtype: int64
one_through_ten[1:10:2] # evens
## 1      2
## 3      4
## 5      6
## 7      8
## 9     10
## dtype: int64
one_through_ten[::-1] # reversed
## 9     10
## 8      9
## 7      8
## 6      7
```

³³<https://pandas.pydata.org/docs/reference/api/pandas.Series.html>

```
## 5      6
## 4      5
## 3      4
## 2      3
## 1      2
## 0      1
## dtype: int64
one_through_ten[-2] = 99 # second to last
one_through_ten
## 0      1
## 1      2
## 2      3
## 3      4
## 4      5
## 5      6
## 6      7
## 7      8
## 8      9
## 9     10
## -2     99
## dtype: int64
one_through_ten[one_through_ten > 3] # bigger than three
## 3      4
## 4      5
## 5      6
## 6      7
## 7      8
## 8      9
## 9     10
## -2     99
## dtype: int64
one_through_ten.sum()
## 154
```

However, Pandas' Series have `.loc` and `.iloc` methods³⁴. We won't talk much about these two methods now, but they will become very important when we start to discuss Pandas' data frames in section 0.32.

```
one_through_ten.iloc[2]
## 3
one_through_ten.loc[2]
## 3
```

0.14 Some Gotchas

0.14.1 Shallow versus Deep Copies

In R, assignment usually produces a **deep copy**. In the code below, we create `b` from `a`. If we modify `b`, these changes don't affect `a`. This takes up more memory, but our program is easier to follow as we don't have to keep track of connections between objects.

```
# in R
a <- c(1,2,3)
b <- a
b[1] <- 999
a # still the same!
## [1] 1 2 3
```

With Numpy arrays in Python, “shallow copies” can be created by simple assignment, or by explicitly constructing a **view**³⁵. In the code below, `a`, `b`, `c`, and `d` all share the same data. If you modify one, you change all the others. This can make the program more

³⁴https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#different-choices-for-indexing

³⁵<https://numpy.org/devdocs/user/quickstart.html#copies-and-views>

confusing, but on the other hand, it can also improve computational efficiency.

```
# in python
a = np.array([1,2,3])
b = a # b is an alias
c = a.view() # c is a view
d = a[:]
b[0] = 999
a # two names for the same object in memory
## array([999,  2,  3])
b
## array([999,  2,  3])
c
## array([999,  2,  3])
d
## array([999,  2,  3])
```

It's the same story with Pandas' Series objects. You're usually making a “shallow” copy.

```
# in python
import pandas as pd
s1 = pd.Series(np.array([100.0,200.0,300.0]))
s2 = s1
s3 = s1.view()
s4 = s1[:]
s1[0] = 999
s1
## 0    999.0
## 1    200.0
## 2    300.0
## dtype: float64
s2
## 0    999.0
## 1    200.0
```

```
## 2      300.0
## dtype: float64
s3
## 0      999.0
## 1      200.0
## 2      300.0
## dtype: float64
s4
## 0      999.0
## 1      200.0
## 2      300.0
## dtype: float64
```

If you want a “deep copy” in Python, you usually want a function or method called `copy()`. Use `np.copy` or `np.ndarray.copy`³⁶ when you have a Numpy array.

```
# in python
a = np.array([1,2,3])
b = np.copy(a)
c = a.copy()
b[0] = 999
a
## array([1, 2, 3])
b
## array([999,  2,  3])
c
## array([1, 2, 3])
```

Use `pandas.Series.copy`³⁷ with Pandas’ Series objects. Make sure not to set the `deep` argument to `False`. Otherwise you’ll get a shallow copy.

³⁶<https://numpy.org/doc/stable/reference/generated/numpy.ndarray.copy.html#numpy-ndarray-copy>

³⁷<https://pandas.pydata.org/docs/reference/api/pandas.Series.copy.html#pandas-series-copy>

```
# in python
s1 = pd.Series(np.array([1,2,3]))
s2 = s1.copy()
s3 = s1.copy(deep=False)
s1[0] = 999
s1
## 0    999
## 1     2
## 2     3
## dtype: int64
s2
## 0     1
## 1     2
## 2     3
## dtype: int64
s3
## 0    999
## 1     2
## 2     3
## dtype: int64
```

0.15 How do R and Python handle missing values?

R has `NULL`, `NaN`, and `NA`. Python has `None` and `np.nan`. If your eyes are glazing over already and you're thinking "they all look like the same"—they are not.

R's `NULL` and Python's `None` are similar. Both represent "nothingness." This is *not* the same as `0`, or an empty string, or `FALSE/False`. This is commonly used to detect if a user fails to pass in an argument to a function, or if a function fails to "return" (more information on functions can be found in section 0.20) anything meaningful.

In R, for example, if a function fails to return anything, then it actually returns a `NULL`. A `NULL` object has its own type.³⁸

```
NULL == FALSE
## logical(0)
NULL == NULL
## logical(0)
# create a function that doesn't return anything
# more information on this later
doNothingFunc <- function(a){}
thing <- doNothingFunc() # call our new function
is.null(thing)
## [1] TRUE
typeof(NULL)
## [1] "NULL"
```

In Python, we have the following.

```
None == False
## False
None == None
# create a function that doesn't return anything
# more information on this later
## True
def do_nothing_func():
    pass
thing = do_nothing_func()
if thing is None:
    print("thing is None!")
## thing is None!
type(None)
## <class 'NoneType'>
```

“NaN” abbreviates “not a number.” NaN is an object of type dou-

³⁸<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#NULL-object>

ble in R, and `np.nan` is of type `float` in Python. It can come in handy when you (deliberately or accidentally) perform undefined calculations such as $0/0$ or $\infty - \infty$.

```
# in R
0/0
## [1] NaN
Inf/Inf
## [1] NaN
is.na(0/0)
## [1] TRUE
```

```
# in Python
0/0
## Error in py_call_impl(callable, dots$args, dots$keywords): ZeroDivisionError: a
##
## Detailed traceback:
##   File "<string>", line 1, in <module>
import numpy as np
np.inf/np.inf
## nan
np.isnan(np.nan)
## True
```

“NA” is short for “not available.” Missing data is a fact of life in data science. Observations are often missing in data sets, introduced after joining/merging data sets together (more on this in section 0.48), or arise from calculations involving underflow and overflow. There are many techniques designed to estimate quantities in the presence of missing data. When you code them up, you’ll need to make sure you deal with NAs properly.

```
# in R
babyData <- c(0,-1,9,NA,21)
NA == TRUE
```



```
## [1] NA
is.na(babyData)
## [1] FALSE FALSE FALSE TRUE FALSE
typeof(NA)
## [1] "logical"
```

Unfortunately, Python’s support of an NA-like object is more limited. There is no NA object in base Python. And often NaNs will appear in place of an NA. There are a few useful tools, though. The Numpy library offers “masked arrays”³⁹, for instance.

Also, as of version 1.0.0, the pandas library⁴⁰ has an experimental `pd.NA` object. However, they warn⁴¹ that “the behaviour of `pd.NA` can still change without warning.”

```
import numpy as np
import numpy.ma as ma
baby_data = ma.array([0,-1,9,-9999, 21]) # -9999 "stands for" missing
baby_data[3] = ma.masked
np.average(baby_data)
## 7.25
```

Be careful of using extreme values to stand in for what should be an NA. Be aware that some data providers will follow this strategy. I recommend that you avoid it yourself. Failing to represent a missing value correctly would lead to extremely wrong calculations!

³⁹<https://numpy.org/devdocs/reference/maskedarray.html>

⁴⁰https://pandas.pydata.org/docs/user_guide/index.html#user-guide

⁴¹https://pandas.pydata.org/pandas-docs/dev/user_guide/missing_data.html#missing-data-na



0

Numpy's ndarrays versus R's matrices and arrays

Sometimes you want a collection of elements that are *all the same type*, but you want to store them in a two- or three-dimensional structure. For instance, say you need to use matrix multiplication for some linear regression software you're writing, or that you needed to use tensors for a computer vision project you're working on.

0.16 Numpy **ndarrays** In Python

In Python, you could still use arrays for these kinds of tasks. You will be pleased to learn that the Numpy arrays we discussed earlier are a special case of Numpy's N-dimensional arrays⁴². Each array will come with an enormous amount of methods⁴³ and attributes⁴⁴ (more on object-oriented program in chapter IV) attached to it. A few are demonstrated below.

```
import numpy as np
a = np.array([[1,2],[3,4]], np.float)
a
```

⁴²<https://numpy.org/doc/stable/reference/arrays.ndarray.html>

⁴³<https://numpy.org/doc/stable/reference/arrays.ndarray.html#array-methods>

⁴⁴<https://numpy.org/doc/stable/reference/arrays.ndarray.html#array-attributes>

```
## array([[1., 2.],
##        [3., 4.]])
a.shape
## (2, 2)
a.ndim
## 2
a.dtype
## dtype('float64')
a.max()
## 4.0
a.resize((1,4)) # modification is **in place**
a
## array([[1., 2., 3., 4.]])
```

0.17 The `matrix` and `array` classes in R

In Python, adding a dimension to your “container” is simple. You keep using Numpy arrays, and you just change the `.shape` attribute (perhaps with a call to `.reshape()` or something similar). In R, there is a stronger distinction between 1-, 2-, and 3-dimensional containers. Each has its own class. 2-dimensional containers that store objects of the same type are of the `matrix` class. Containers with 3 or more dimensions are of the `array` class. In this section, I will provide a quick introduction to using these two classes. For more information, see chapter 3 of (Matloff, 2011).

Just like `vectors`, `matrix` objects do not necessarily have to be used to perform matrix arithmetic. Yes, they require all the elements are of the same type, but it doesn't really make sense to “multiply” `matrix` objects that hold onto characters.

I usually create `matrix` objects with the `matrix()` function or the `as.matrix()` function. `matrix()` is to be preferred in my opinion.

The first argument is explicitly a `vector` of all the flattened data that you want in your `matrix`. On the other hand, `as.matrix()` is more flexible; it takes in a variety of R objects (e.g. `data.frames`), and tries to figure out what to do with them on a case-by-case basis. In other words, `as.matrix()` is a *generic function*. More information about generic functions is provided in 0.54.2.

Some other things to remember with `matrix()`: `byrow=` is `FALSE` by default, and you will also need to specify either `ncol=` and/or `nrow=` if you want anything that isn't a 1-column `matrix`.

```
A <- matrix(1:4)
A
##           [,1]
## [1,]      1
## [2,]      2
## [3,]      3
## [4,]      4
matrix(1:4, ncol = 2)
##           [,1] [,2]
## [1,]      1    3
## [2,]      2    4
matrix(1:4, ncol = 2, byrow = T)
##           [,1] [,2]
## [1,]      1    2
## [2,]      3    4
as.matrix(data.frame(firstCol = c(1,2,3), secondCol = c("a","b","c"))) # coerces n
##           firstCol secondCol
## [1,] "1"         "a"
## [2,] "2"         "b"
## [3,] "3"         "c"
dim(A)
## [1] 4 1
nrow(A)
## [1] 4
ncol(A)
## [1] 1
```

I use `array()` to create `array` objects. Personally, I rarely use this type, but this doesn't mean you should avoid learning about it. Rather, this is a reflection of what kind of data sets I prefer to work with, and the fact that you can't matrix-multiply `arrays` together. You won't be able to avoid 3-d data sets (3-dimensions, not a 3-column `matrix`) forever, though, particularly if you're working in an area such as neuroimaging or computer vision.

```
myArray <- array(rep(1:3, each = 4), dim = c(2,2,3))
myArray
## , , 1
##
##      [,1] [,2]
## [1,]    1    1
## [2,]    1    1
##
## , , 2
##
##      [,1] [,2]
## [1,]    2    2
## [2,]    2    2
##
## , , 3
##
##      [,1] [,2]
## [1,]    3    3
## [2,]    3    3
```

You can matrix-multiply `matrix` objects together with the `%*%` operator. If you're working on this, then the transpose operator (i.e. `t()`) comes in handy, too. You can still use element-wise (Hadamard) multiplication. This is defined with the more familiar multiplication operator `*`.

```
# calculate a quadratic form y'Qy
y <- matrix(c(1,2,3))
```

```
Q <- diag(1, 3) # diag() gets and sets diagonal matrices
t(y) %*% Q %*% y
##      [,1]
## [1,]  14
```

Sometimes you need to access or modify individual elements of a `matrix` object. You can use the familiar `[]` and `[]=` operators to do this. Here is a setting example. You don't need to worry about coercion to different types here.

```
Qcopy <- Q
Qcopy[1,1] <- 3
Qcopy[2,2] <- 4
Qcopy
##      [,1] [,2] [,3]
## [1,]    3    0    0
## [2,]    0    4    0
## [3,]    0    0    1
```

Here are some extraction examples. Notice that, if it can, `[]` will coerce a `matrix` to `vector`. If you wish to avoid this, you can specify `drop=FALSE`.

```
Q
##      [,1] [,2] [,3]
## [1,]    1    0    0
## [2,]    0    1    0
## [3,]    0    0    1
Q[1,1]
## [1] 1
Q[2,]
## [1] 0 1 0
Q[2,,drop=FALSE]
##      [,1] [,2] [,3]
## [1,]    0    1    0
```

```
class(Q)
## [1] "matrix" "array"
class(Q[2,])
## [1] "numeric"
class(Q[2,,drop=FALSE])
## [1] "matrix" "array"
row(Q) > 1
##          [,1] [,2] [,3]
## [1,] FALSE FALSE FALSE
## [2,]  TRUE  TRUE  TRUE
## [3,]  TRUE  TRUE  TRUE
Q[row(Q) > 1] # column-wise ordering
## [1] 0 0 1 0 0 1
```

There are other functions that operate on one or more `matrix` objects in more interesting ways, but much of this will be covered in future sections. For instance, we will describe how `apply()` works with `matrix`s in section 0.55, and we will discuss combining `matrix` objects in different ways in section 0.45.2.

0

R's lists versus Python's lists and dictionaries

When you need to store elements in a container, but you can't guarantee that these elements all have the same type, or you can't guarantee that they all have the same size, then you need a `list` in R. In Python, you might need a `list` or `dict` (short for dictionary).

0.18 Lists In R

`lists` are one of the most flexible data types in R. You can access individual elements in many different ways, each element can be of different size, and each element can be of a different type.

```
myList <- list(c(1,2,3), "May 5th, 2021", c(TRUE, TRUE, FALSE))
myList[1] # length-1 list; first element is length 3 vector
## [[1]]
## [1] 1 2 3
myList[[1]] # length-3 vector
## [1] 1 2 3
```

If you want to extract an element, you need to decide between using single square brackets or double square brackets. The former returns a `list`, while the second returns the type of the individual element.

You can also name the elements of a list. This can lead to more readable code. To see why, examine the example below. The `lm()`

function estimates a linear regression model. It returns a list with plenty of components.

```
dataSet <- read.csv("data/cars.csv")
results <- lm(log(Horsepower) ~ Type, data = dataSet)
length(results)
## [1] 13
names(results)
## [1] "coefficients" "residuals" "effects" "rank" "fitted.va
## [7] "qr" "df.residual" "contrasts" "xlevels" "call"
## [13] "model"
results$contrasts
## $Type
## [1] "contr.treatment"
results['rank']
## $rank
## [1] 6
results[['terms']]
## log(Horsepower) ~ Type
## attr("variables")
## list(log(Horsepower), Type)
## attr("factors")
##           Type
## log(Horsepower) 0
## Type            1
## attr("term.labels")
## [1] "Type"
## attr("order")
## [1] 1
## attr("intercept")
## [1] 1
## attr("response")
## [1] 1
## attr("Environment")
## <environment: R_GlobalEnv>
## attr("predvars")
```

```
## list(log(Horsepower), Type)
## attr("dataClasses")
## log(Horsepower)           Type
##      "numeric"      "character"
```

`results` is a `list` (`is.list(results)` returns `TRUE`), but to be more specific, it is an S3 object of class `lm`. If you do not know what this means, do not worry! S3 classes are discussed more in a later chapter. Why is this important? For one, I mention it so that you aren't confused if you type `class(results)` and see `lm` instead of `list`. Second, the fact that the authors of `lm()` wrote code that returns `result` as a “fancy list” suggests that they are encouraging another way to access elements of the `results`: to use specialized functions! For example, you can use `residuals(results)`, `coefficients(results)`, and `fitted.values(results)`. These functions do not work for all lists in R, but when they do work (for `lm` and `glm` objects only), you can be sure you are writing the kind of code that is encouraged by the authors of `lm()`.

0.19 Lists In Python

Python `lists`⁴⁵ are very flexible, too. There are fewer choices for accessing and modifying elements of lists in Python—you'll most likely end up using the square bracket operator. Elements can be different sizes and types, just like they were with R's lists.

Unlike in R, however, you cannot name elements of lists. If you want a container that allows you to access elements by name, look into Python dictionaries⁴⁶ (see section 0.20) or Pandas' `Series` objects (see section 0.8).

From the example below, you can see that we've been introduced

⁴⁵<https://docs.python.org/3/library/stdtypes.html#lists>

⁴⁶<https://docs.python.org/3/library/stdtypes.html#mapping-types-dict>

to lists already. We have been constructing Numpy arrays from them.

```
another_list = [np.array([1,2,3]), "May 5th, 2021", True, [42,42]]
another_list[2]
## True
another_list[2] = 100
another_list
## [array([1, 2, 3]), 'May 5th, 2021', 100, [42, 42]]
```

Python lists have methods attached to them⁴⁷, which can come in handy.

```
another_list
## [array([1, 2, 3]), 'May 5th, 2021', 100, [42, 42]]
another_list.append('new element')
another_list
## [array([1, 2, 3]), 'May 5th, 2021', 100, [42, 42], 'new element']
```

Creating lists can be done as above, with the square bracket operators. They can also be created with the `list()` function, and by creating a *list comprehension*. List comprehensions are discussed more in 0.44.

```
my_list = list(('a','b','c')) # converting a tuple to a list
your_list = [i**2 for i in range(3)] # list comprehension
my_list
## ['a', 'b', 'c']
your_list
## [0, 1, 4]
```

⁴⁷<https://docs.python.org/3/tutorial/datastructures.html#more-on-lists>

0.20 Dictionaries In Python

Dictionaries⁴⁸ in Python provide a container of key-value pairs. The keys are *unique*, and they must be *immutable*. **strings** are the most common key type, but **ints** can be used as well.

Here is an example of creating a **dict** with curly braces (i.e. `{}`). This **dict** stores the current price of a few popular cryptocurrencies. Accessing an individual element's value using its key is done with the square bracket operator (i.e. `[]`), and deleting elements is done with the **del** keyword.

```
current_crypto_prices = {'BTC': 38657.14, 'ETH': 2386.54, 'DOGE': .308122}
current_crypto_prices['DOGE'] # get the current price of Dogecoin
## 0.308122
del current_crypto_prices['BTC'] # remove the current price of Bitcoin
current_crypto_prices.keys()
## dict_keys(['ETH', 'DOGE'])
current_crypto_prices.values()
## dict_values([2386.54, 0.308122])
```

You can also create **dicts** using **dictionary comprehensions**. Just like list comprehensions, these are discussed more in 0.44.

```
incr_cryptos = {key:val*1.1 for (key,val) in current_crypto_prices.items()}
incr_cryptos
## {'ETH': 2625.194, 'DOGE': 0.3389342}
```

Personally, I don't use dictionaries as much as lists. If I have a dictionary, I usually convert it to a pandas data frame (more information on those in 0.32).

⁴⁸<https://docs.python.org/3/tutorial/datastructures.html#dictionaries>

```
import pandas as pd
df_from_dict = pd.DataFrame({ 'col1': [1,2,3], 'col2' : ['a','b','c']})
df_from_dict
##      col1 col2
## 0      1    a
## 1      2    b
## 2      3    c
```

0

Functions

This text has already covered how to *use* functions that come to us pre-made. At least we have discussed how to use them in a one-off way—just write the name of the function, write some parentheses after that name, and then plug in any requisite arguments by writing them in a comma-separated way between those two parentheses. This is how it works in both R and Python.

In this section we take a look at how to *define* our own functions. This will not only help us to understand pre-made functions, but it will also be useful if we need some extra functionality that isn't already provided to us.

Writing our own functions is also useful for “packaging up” computations. The utility of this will become very apparent in chapter 0.55. Consider the task of estimating a regression model. Would you want to write that program using only arithmetic operators? Would it be simpler if you could use matrix multiplications? Would you want your function to work on different types of inputs? Would you want it to estimate several regression models and choose the “best” one?

Thankfully, R functions are very similar to Python functions. In both languages, functions are **first-class objects**. This means that, no matter which of these two languages you are using, functions

- can be passed as arguments to other functions,
- can be returned as values from other functions, and
- can be assigned to variables and stored in containers (Abelson and Sussman, 1996)

0.21 Defining R Functions

To create a function in R, we need another function called `function`. We give the output of `function` a name in the same way we give names to any other variable in R, by using the assignment operator `<-`. Here's an example of a toy function called `addOne`. Here `myInput` is a placeholder that refers to whatever the user of the function ends up plugging in.

```
addOne <- function(myInput){ # define the function
  myOutput <- myInput + 1
  return(myOutput)
}
addOne(41) # call/invoke/use the function
## [1] 42
```

Below the definition, the function is called with an input of 41. When this happens, the following sequence of events occurs

- The value 41 is assigned to `myInput`
- `myOutput` is given the value 42
- `myOutput`, which is 42, is returned from the function
- the temporary variables `myInput` and `myOutput` are destroyed.

We get the desired answer, and all the unnecessary intermediate variables are cleaned up and thrown away after they are no longer needed.

0.22 Defining Python Functions

To create a function in Python, we use the `def` statement (instead of the `function` function in R). The desired name of the func-

tion comes next. After that, the formal parameters come, comma-separated inside parentheses, just like in R.

Defining a function in Python is a little more concise. There is no assignment operator like there is in R, there are no curly braces, and `return` isn't a function like it is in R, so there is no need to use parentheses after it. There is one syntactic addition, though—we need a colon (`:`).

Here is an example of a toy function called `add_one`.

```
def add_one(my_input): # define the function
    my_output = my_input + 1
    return my_output
add_one(41) # call/invoke/use the function
## 42
```

Below the definition, the function is called with an input of 41. When this happens, the following sequence of events occurs

- The value 41 is assigned to `my_input`
- `my_output` is given the value 42
- `my_output`, which is 42, is returned from the function
- the temporary variables `my_input` and `my_output` are destroyed.

We get the desired answer, and all the unnecessary intermediate variables are cleaned up and thrown away after they are no longer needed.

0.23 More details on R's user-defined functions

Technically, in R, functions are defined as three things bundled together⁴⁹:

⁴⁹<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Function-objects>

1. a **formal argument list** (also known as *formals*),
2. a **body**, and
3. a **parent environment**.

The *formal argument list* is exactly what it sounds like. It is the list of arguments a function takes. You can access a function's formal argument list using the `formals()` function. Note that it is not the *actual* arguments a user will plug in—that isn't knowable at the time the function is created in the first place.

Here is another function that takes a **default argument** called `whichNumber`. If the user of the function doesn't specify how much she wants to add to `myInput`, `addNumber` will use 1 as the default. This default value shows up in the output of `formals(addNumber)`.

```
addNumber <- function(myInput, whichNumber = 1){  
  myOutput <- myInput + whichNumber  
  return(myOutput)  
}  
addNumber(3) # no second argument being provided by the user here  
## [1] 4  
formals(addNumber)  
## $myInput  
##  
##  
## $whichNumber  
## [1] 1
```

The function's *body* is also exactly what it sounds like. It is the work that a function performs. You can access a function's body using the `body()` function.

```
addNumber <- function(myInput, whichNumber = 1){  
  myOutput <- myInput + whichNumber  
  return(myOutput)  
}  
body(addNumber)
```

```
## {  
##   myOutput <- myInput + whichNumber  
##   return(myOutput)  
## }
```

Every function you create also has a *parent environment*⁵⁰. You can get/set this using the `environment()` function. Environments help a function know which variables it is allowed to use and how to use them. The parent environment of a function is where the function was *created*, and it contains variables outside of the body that the function can also use. The rules of which variables a function can use are called *scoping*. When you create functions in R, you are primarily using **lexical scoping**. To understand functions well in R, these examples are important to understand, so I provide more detail in 0.25.

There is a lot more information about environments that isn't provided in this text. For instance, a user-defined function also has binding, execution, and calling environments associated with it⁵¹, and environments are used in creating package namespaces, which are important when two packages each have a function with the same name.

0.24 More details on Python's user-defined functions

Roughly, Python functions have the same things R functions have. They have a **formal parameter list**, a body, and there are namespaces⁵² created that help organize which variables the function can

⁵⁰Primitive functions are functions that contain no R code and are internally implemented in C. These are the only type of function in R that don't have a parent environment.

⁵¹<http://adv-r.had.co.nz/Environments.html#function-envs>

⁵²<https://docs.python.org/3/tutorial/classes.html#python-scopes-and-namespaces>

access, as well as which pieces of code can call this new function. These three concepts are analogous to those in R. The names are just a bit different sometimes, and it isn't organized in the same way. To access these bits of information, you need to access the *special attributes* of a function. User-defined functions in Python have a lot of pieces of information attached to them. If you'd like to see all of them, you can visit this page of documentation⁵³.

So, for instance, let's try to find the *formal parameter list* of a user-defined function below. This is, again, the collection of inputs a function takes. Just like in R, this is not the *actual* arguments a user will plug in—that isn't knowable at the time the function is created.⁵⁴ Here we have another function called `add_number()` that takes a **default argument** called `which_number`.

```
def add_number(my_input, which_number = 1): # define a function
    my_output = my_input + which_number
    return my_output
add_number(3) # no second argument being provided by the user here
## 4
add_number.__code__.co_varnames # note this also contains *my_output*
## ('my_input', 'which_number', 'my_output')
add_number.__defaults__
## (1,)
```

The code attribute has much more to offer. To see a list of names of all its contents, you can use `dir(add_number.__code__)`.

Don't worry if the notation `add_number.__code__` looks strange. The dot (`.`) operator will become more clear in the future chapter on *object-oriented programming*. For now, just think of `__code__` as being an object *belonging to* `add_number`. Objects that belong to

⁵³<https://docs.python.org/3/reference/datamodel.html#objects-values-and-types>

⁵⁴You might have noticed that Python uses two different words to prevent confusion. Unlike R, Python uses the word “parameter” (instead of “argument”) to refer to the inputs a function takes, and “arguments” to the specific values a user plugs in.

other objects are called **attributes** in Python. The dot operator helps us access attributes *inside* other objects.

0.25 Function Scope in R

R uses **lexical scoping**.

R functions can use variables that are defined in the function body, and variables that were defined in the environment that the function itself was defined in. R functions **cannot** necessarily find variables in an environment where the function was *called* in. Code outside the body of a function cannot access variables inside the body of a function.

```
a <- 3
sillyFunction <- function(){
  return(a + 20)
}
environment(sillyFunction) # the env. it was defined in contains a
## <environment: R_GlobalEnv>
sillyFunction()
## [1] 23
```

From the point of view of the function, when it attempts to access a variable, it first looks in its own body. In the example below, there are two variables named `a`, but they exist in different environments. Inside the function, the innermost one gets used. Outside the function, the global variable gets used.

```
a <- 3
sillyFunction <- function(){
  a <- 20
  return(a + 20)
}
```

```
sillyFunction()
## [1] 40
print(a)
## [1] 3
```

The same concept applies if you create functions within functions. The inner function looks “inside-out” for variables. Below we call `outerFunc()`, which calls `innerFunc()`. `innerFunc()` can refer to the variable `b`, because it lies in the same environment in which `innerFunc()` was created. Interestingly, `innerFunc()` can also refer to the variable `a`, because that variable was captured by `outerFunc`, which provides access to `innerFunc`.

```
a <- "outside both"
outerFunc <- function(){
  b <- "inside one"
  innerFunc <- function(){
    print(a)
    print(b)
  }
  return(innerFunc())
}
outerFunc()
## [1] "outside both"
## [1] "inside one"
```

If we ask `outerFunc` to return the function `innerFunc` (functions are objects!), then we might be surprised to see that `innerFunc()` can still successfully refer to `b`, even though it doesn’t exist inside the *calling environment*. But don’t be surprised! What matters is what was available when the function was *created*. In this example, `outerFuncV2` is sometimes called a *function factory*. More information about this is provided in 0.55.

```

outerFuncV2 <- function(){
  b <- "inside one"
  innerFunc <- function(){
    print(b)
  }
  return(innerFunc) # note the missing inner parentheses!
}
myFunc <- outerFuncV2() # get a new function
ls(environment(myFunc)) # list all data attached to this function
## [1] "b"          "innerFunc"
myFunc()
## [1] "inside one"

```

Sometimes, in R, functions are called **closures** to emphasize that they are capturing variables from the parent environment in which they were created, to emphasize the data that they are bundled with.

0.26 Function Scope in Python

Python uses **lexical scoping** just like R! There's a famous acronym for the concept in Python: **LEGB**.

- L: Local,
- E: Enclosing,
- G: Global, and
- B: Built-in.

A Python function will search for a variable in these namespaces⁵⁵ in this order.⁵⁶

⁵⁵<https://docs.python.org/3/tutorial/classes.html#python-scopes-and-namespaces>

⁵⁶Functions aren't the only thing that get their own namespace. For in-

“*Local*” refers to variables that are defined inside of the function’s block. The function below uses the local `a` over the global one.

```
a = 3
def silly_function():
    a = 22 # local a
    print("local variables are ", locals())
    return a + 20
silly_function()
## local variables are  {'a': 22}
## 42
silly_function.__code__.co_nlocals # number of local variables
## 1
silly_function.__code__.co_varnames # names of local variables
## ('a',)
```

“*Enclosing*” refers to variables that were defined in the enclosing namespace, but not the global namespace. These variables are sometimes called **free variables**. In the example below, there is no local `a` variable for `inner_func`. But there is a global one and one in the enclosing namespace. It chooses the one in the enclosing namespace.

```
a = "outside both"
def outer_func():
    a = "inside one"
    def inner_func():
        print(a)
    return inner_func
my_new_func = outer_func()
my_new_func()
## inside one
my_new_func.__code__.co_freevars
## ('a',)
```

stance, classes do as well⁵⁷. More information on classes is provided in Chapter IV

“*Global*” scope contains variables defined in the module-level namespace. If the below example code was the entirety of your script, then `a` would be a global variable.

```
a = "outside both"
def outer_func():
    b = "inside one"
    def inner_func():
        print(a)
        inner_func()
    outer_func()
## outside both
```

Just like in R, Python functions **cannot** necessarily find variables in an environment where the function was *called* in. For example, here is some code that mimics the above R example. Both `a` and `b` are accessible from within `inner_func`. That is due to LEGB.

```
a = "outside both"
def outer_func():
    b = "inside one"
    def inner_func():
        print(a)
        print(b)
    return inner_func()
outer_func()
```

```
## outside both
## inside one
```

However, if we start using `outer_func` inside another function, *calling* it in another function, when it was *defined* somewhere else, well then it doesn’t have access to some variables. You might be surprised at how the following code functions. Does this print the right string: “this is the `a` I want to use now!” No!

```
def third_func():  
    a = "this is the a I want to use now!"  
    outer_func()  
third_func()
```

```
## outside both  
## inside one
```

Again, these examples get at *functional programming*, which is discussed more in depth in chapter 0.55. There it will describe strategies to make your code easier to maintain (e.g. keep your functions “pure”!)

0.27 Modifying a Function’s Arguments

Can/should we modify a function’s argument? The flexibility to do this sounds empowering; however, not doing it is recommended because it makes programs easier to reason about.

0.27.1 Passing By Value In R

In R, it is *difficult* for a function to modify the variable that a user plugs in to a function as its argument.⁵⁸ Consider the following code.

```
a <- 1  
f <- function(arg){  
    arg <- 2  
    return(arg)  
}  
print(a)
```

⁵⁸There are some exceptions to this, but it’s generally true.

```
## [1] 1
print(f(a))
## [1] 2
print(a)
## [1] 1
```

The function `f` has an argument called `arg`. When `f(a)` is performed, changes are made to a *copy* of `a`. When a function constructs a copy of all input variables inside its body, this is called **pass-by-value** semantics. This copy is a temporary intermediate value that only serves as a starting point for the function to produce a return value of 2.

`arg` could have been called `a`, and the same behavior will take place. However, giving these two things different names is helpful to remind you and others that R copies its arguments.

It is still possible to modify `a`, but I don't recommend doing this either. I will discuss this more in subsection 0.27.

0.27.2 Passing By Assignment In Python

The story is more complicated in Python. Python functions have **pass-by-assignment** semantics. This is something that is very unique to Python. What this means is that your ability to modify the arguments of a function depends on

- what the type of the argument is, and
- what you're trying to do to it.

We will go through some examples first, and then explain why this works the way it does. Here is some code that is analogous to the example above.

```
a = 1
def f(arg):
    arg = 2
```

```
    return arg

print(type(a))
## <class 'int'>
print(a)
## 1
print(f(a))
## 2
print(a)
## 1
```

In this case, `a` is not modified. That is because `a` is an `int`. `ints` are **immutable** in Python, which means that their value⁵⁹ cannot be changed after they are created, either inside or outside of the function's scope. However, consider the case when `a` is a `list`, which is a **mutable** type. A mutable type is one that can have its value changed after its created.

```
a = [999]
def f(arg):
    arg[0] = 2
    return arg

print(type(a))
## <class 'list'>
print(a)
## [999]
print(f(a))
## [2]
print(a)
## [2]
```

In this case `a` *is* modified. Changing the value of the argument

⁵⁹<https://docs.python.org/3/reference/datamodel.html#objects-values-and-types>

inside the function effects changes to that variable outside of the function.

Ready to be confused? What happens if we take in a list, but try to do something else with it.

```
a = [999]
def f(arg):
    arg = [2]
    return arg

print(a)
## [999]
print(f(a))
## [2]
print(a)
## [999]
```

That time `a` did not permanently change in the global scope. Why does this happen? I thought lists were mutable!

The reason behind all of this doesn't even have anything to do with functions, per se. Rather, it has to do with how Python manages, objects, values, and types⁶⁰. It also has to do with what happens during assignment⁶¹.

Let's revisit the above code, but bring everything out of a function. Python is pass-by-assignment, so all we have to do is understand how assignment works. Starting with the immutable `int` example, we have the following.

```
# old code:
# a = 1
# def f(arg):
```

⁶⁰<https://docs.python.org/3/reference/datamodel.html#objects-values-and-types>

⁶¹<https://docs.python.org/3/reference/executionmodel.html#naming-and-binding>

```
#   arg = 2
#   return arg
a = 1    # still done in global scope
arg = a  # arg is a name that is bound to the object a refers to
arg = 2  # arg is a name that is bound to the object 2
print(arg is a)
## False
print(id(a), id(arg))
## 140510223533408 140510223533440
print(a)
## 1
```

The `id()`⁶² function returns the **identity** of an object, which is kind of like its memory address. Identities of objects are unique and constant. If two variables, `a` and `b` say, have the same identity, `a is b` will evaluate to `True`. Otherwise, it will evaluate to `False`.

In the first line, the *name* `a` is bound to the *object* 1. In the second line, the name `arg` is bound to the *object* that is referred to by the *name* `a`. After the second line finishes, `arg` and `a` are two names for the same object (a fact that you can confirm by inserting `arg is a` immediately after this line).

In the third line, `arg` is bound to 2. The variable `arg` can be changed, but only by re-binding it with a separate object. Re-binding `arg` does not change the value referred to by `a` because `a` still refers to 1, an object separate from 2. There is no reason to re-bind `a` because it wasn't mentioned at all in the third line.

If we go back to the first function example, it's basically the same idea. The only difference, however, is that `arg` is in its own scope. Let's look at a simplified version of our second code chunk that uses a mutable list.

```
a = [999]
# old code:
```

⁶²<https://docs.python.org/3/library/functions.html#id>

```
# def f(arg):  
#     arg[0] = 2  
#     return arg  
arg = a  
arg[0] = 2  
print(arg)  
## [2]  
print(a)  
## [2]  
print(arg is a)  
## True
```

In this example, when we run `arg = a`, the name `arg` is bound to the same object that is bound to `a`. This much is the same. The only difference here, though, is that because lists are mutable, changing the first element of `arg` is done “in place”, and all variables can access the mutated object.

Why did the third example produce unexpected results?

```
a = [999]  
# old code  
# def f(arg):  
#     arg = [2]  
#     return arg  
arg = a  
arg = [2]  
print(arg is a)  
## False  
print(a)  
## [999]  
print(arg)  
## [2]
```

The difference is in the line `arg = [2]`. This rebinds the name `arg` to a different variable. Lists are still mutable, but this has nothing

to do with re-binding–re-binding a name works no matter what type of object you’re binding it to. In this case we are re-binding `arg` to a completely different list.

0.28 Accessing and Modifying Non-Local Variables

In the last subsection, we were talking about variables that were passed in as arguments to a function. Here we are talking about variables that are not, but are still referred to inside a function’s body.

In general, even though it is possible to access and modify non-local variables in both languages, it is not a good idea.

0.28.1 Accessing and Modifying Non-Local Variables in R

As Hadley Wickham writes in his book⁶³, “[l]exical scoping determines where, but not when to look for values.” R has **dynamic lookup**, meaning code inside a function will only try to access a referred-to variable when the function is *running*, not when it is defined.

Consider the R code below.

```
# R
missileLaunchCodesSet <- TRUE
everythingIsSafe <- function(){
  return(!missileLaunchCodesSet)
}
missileLaunchCodesSet <- FALSE
# everythingIsSafe() # what happens if we call it?
```

`everythingIsSafe` is created in the global environment, and the

⁶³<https://adv-r.hadley.nz/functions.html#dynamic-lookup>

global environment contains a Boolean variable called `missile-LaunchCodesAreSet`.

Now imagine sharing some code with a collaborator. Imagine, further, that your collaborator is the subject-matter expert, and knows little about R programming. Suppose that he changes a global variable in the script. Shouldn't this induce a relatively trivial change to the overall program?

Let's explore this hypothetical further. Consider what could happen if any of the following (very typical) conditions are true:

- you or your collaborators aren't sure what `everythingIsSafe` will return because you don't understand dynamic lookup, or
- it's difficult to visually keep track of all assignments to `missile-LaunchCodesAreSet` (e.g. your script is quite long or it changes often), or
- you are not running code sequentially (e.g. you are testing chunks at a time instead of clearing out your memory and `source()`ing from scratch, over and over again).

In each of these situations, understanding of the program would be compromised. However, if you follow the above principle of never referring to non-local variables in function code, all members of the group could do their own work separately, minimizing the dependence on one another.

Another reason violating this could be troublesome is if you define a function that refers to a nonexistent variable. *Defining* the function will never throw an error because R will assume that variable is defined in the global environment. *Calling* the function might throw an error, unless you accidentally defined the variable, or if you forgot to delete a variable whose name you no longer want to use.

```
# R
myFunc <- function(){
  return(varigbleNameWithTypo)
}
```

Running the above code to define `myFunc` will not throw an error, even if you think it should!

0.28.2 Accessing and Modifying Non-Local Variables in Python

It is the same exact situation in Python. Consider `everything_is_safe`, a function that is analogous to `everythingIsSafe`.

```
# python
missile_launch_codes_set = True
def everything_is_safe():
    return not missile_launch_codes_set

missile_launch_codes_set = False
everything_is_safe()
## True
```

We can also define `my_func`, which is analogous to `myFunc`. Defining this function doesn't throw an error either!

```
# python
def my_func():
    return varigble_name_with_typo
```

So stay away from referring to variables outside the body of your function!

0.28.3 Modifying Non-Local Variables In R

Now what if we want to be extra bad, and in addition to *accessing* global variables, we *modify* them, too.

```
a <- 1
f <- function(arg){
```

```
    arg <- 2
    a <<- arg
    # return(arg) # no return value
}
print(a)
## [1] 1
print(f(a))
## [1] 2
print(a)
## [1] 2
```

In the program above, `arg` creates a copy of `a`. It assigns 2 to that copy. Then it takes that 2 and writes it to the global variable in the parent environment. Notice that the function can take in different inputs, but the global assignment is hard-coded.

0.28.4 Modifying Non-Local Variables In Python

Finally, there is something in Python that is like R's super assignment operator (`<<-`). It is the `global` keyword. This will let you *modify* global variables.

Referring to global variables *without* modifying them was always allowed, even without using the `global` keyword. This keyword should be used sparingly, and when it is used, it identifies that a function causes **side effects**, which are changes in some variable defined outside of the function's scope.

```
a = 1
def increment_a():
    global a
    a += 1
increment_a()
increment_a()
increment_a()
```

```
print(a)
## 4
```

Here's a last example that will be important for us in particular. Notice that Numpy arrays are mutable.

```
import numpy as np
my_array = np.array([1,2,3])
def make_calc(arr):
    arr[0] = np.average(my_array)
    return 2*arr
result = make_calc(my_array)
print(result)
## [4 4 6]
print(my_array) # watch out: side effect
## [2 2 3]
```

0

Categorical Data

0.29 Categorical Data in R

Categorical data is typically stored in a `factor`⁶⁴ variable in R. For example, say we asked three people what their favorite season was. The data might look something like this.

```
responses <- factor(c("autumn", "summer", "summer"),
                    levels = c("autumn", "summer", "spring", "winter"))
levels(responses)
## [1] "autumn" "summer" "spring" "winter"
contrasts(responses)
##           summer spring winter
## autumn         0      0      0
## summer         1      0      0
## spring         0      1      0
## winter         0      0      1
is.factor(responses)
## [1] TRUE
is.ordered(responses)
## [1] FALSE
```

factors have a `levels` attribute, which is comprised of all the possible values that each response could be. They also have a `contrasts` attribute, which will be important once you start using factors as inputs to functions such as `lm`. In the case of using factors as in-

⁶⁴<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Factors>

puts to `lm()`, the `factor` would tell `lm()` *how* to create the dummy predictors in a linear regression model. It's perfectly fine if you're rusty on regression—the reason I mention this is that in Python, dummy variable construction is done more explicitly/manually.

In the above example, there wasn't at least one person who prefers each season (that's a confusing sentence). Here, if we did not specify a `levels` argument, there would only be two levels. This is a common source of bugs! Another source of bugs: what if some people say "autumn" and others say "fall"?

`factors` can be ordered or unordered. Ordered `factors` are for ordinal data. As another example, say we asked ten people how much they liked programming, and they could only respond "love it", "hate it", or "it's okay". The data might look something like this.

```
responses <- factor(c("love it", "it's okay", "love it",
                     "love it", "it's okay", "love it",
                     "love it", "love it", "it's okay",
                     "it's okay"),
                  levels = c("hate it", "it's okay", "love it"),
                  ordered = TRUE)

levels(responses)
## [1] "hate it" "it's okay" "love it"
contrasts(responses)
##           .L           .Q
## [1,] -7.071068e-01  0.4082483
## [2,] -7.850462e-17 -0.8164966
## [3,]  7.071068e-01  0.4082483
is.factor(responses)
## [1] TRUE
is.ordered(responses)
## [1] TRUE
```

Whether a `factor` is ordered or not can affect its `contrasts` and the behavior of functions it is fed into. Intuitively, it should be clear when to impose ordering or not. In the first example, there isn't a clear ordering of the seasons (which one should come first?). In

the second example, we are looking at responses to a “how much” question.

Here’s a third example. We can take non-categorical data, and cut it into something categorical.

```
stockReturns <- rnorm(10) # not categorical here
typeOfDay <- cut(stockReturns, breaks = c(-Inf, 0, Inf))
typeOfDay
## [1] (-Inf,0] (-Inf,0] (0, Inf] (-Inf,0] (-Inf,0] (-Inf,0] (-Inf,0] (-Inf,0] (-
## Levels: (-Inf,0] (0, Inf]
levels(typeOfDay)
## [1] "(-Inf,0]" "(0, Inf]"
is.factor(typeOfDay)
## [1] TRUE
is.ordered(typeOfDay)
## [1] FALSE
```

0.30 Categorical Data in Python

Categorical data can be handled with the pandas library⁶⁵, which takes a lot of inspiration from R. We’ve talked about `Series` objects before in section 0.10, and here we will use them again. All we have to do to make a `Series` object categorical is to change its `dtype`. The `dtype` we provide will control the categories (like levels in R), and whether it’s ordered or not.

```
import pandas as pd
from pandas.api.types import CategoricalDtype

cat_type = CategoricalDtype(categories=["autumn", "summer", "spring", "winter"],
```

⁶⁵https://pandas.pydata.org/pandas-docs/stable/user_guide/categorical.html

```
ordered=False)
responses = pd.Series(["autumn", "summer", "summer"],
                      dtype = cat_type)

responses
## 0    autumn
## 1    summer
## 2    summer
## dtype: category
## Categories (4, object): ['autumn', 'summer', 'spring', 'winter']
responses.cat.categories
## Index(['autumn', 'summer', 'spring', 'winter'], dtype='object')
responses.cat.ordered
## False
```

The pandas library also provides a `pd.cut()` function, which can return either of these types, or even a regular Numpy array.

```
stock_returns = np.random.normal(size=10) # not categorical here
type_of_day = pd.cut(stock_returns, [-np.inf, 0, np.inf], labels = ['bad day', 'good day'])
type_of_day
## ['bad day', 'bad day', 'bad day', 'bad day', 'bad day', 'good day', 'bad day', 'good day', 'bad day', 'good day']
## Categories (2, object): ['bad day' < 'good day']
type(type_of_day)
## <class 'pandas.core.arrays.categorical.Categorical'>
type_of_day = pd.Series(type_of_day)
type(type_of_day)
## <class 'pandas.core.series.Series'>
type_of_day.cat.categories
## Index(['bad day', 'good day'], dtype='object')
type_of_day.cat.ordered
## True
```

You'll notice that, in this instance, `pd.cut` did not return a `Series` object. It can, but `pd.cut`'s return type will depend on the inputs

you feed in. In this case, it returned a `Categorical`⁶⁶, which is not the same thing as a `Series`. In the code above, I had to convert it back before accessing the `cat` attribute.

⁶⁶<http://pandas-docs.github.io/pandas-docs-travis/reference/api/pandas.Categorical.html#pandas.Categorical>



0

Data Frames

The rectangular array (e.g. an Excel spreadsheet) of information is what many think of when they hear the word “data.” Each column contains elements of a shared data type, and these data types can vary from column to column.

There is a type for this in R and Python: a data frame. It might even be the most common way that data is stored in both R and Python scripts because many functions that read in data from an external source return objects of this type (e.g. `read.csv()` in R and `pd.read_csv()` in Python).

0.31 Data Frames in R

Let’s consider as an example Fisher’s “Iris” data set obtained from (Dua and Graff, 2017). We will read this data set in from a comma separated file (more on input/output in chapter III). This file can be downloaded from this link: <https://archive.ics.uci.edu/ml/datasets/iris>.

```
irisData <- read.csv("data/iris.csv", header = F)
head(irisData)
##      V1  V2  V3  V4      V5
## 1 5.1 3.5 1.4 0.2 Iris-setosa
## 2 4.9 3.0 1.4 0.2 Iris-setosa
## 3 4.7 3.2 1.3 0.2 Iris-setosa
## 4 4.6 3.1 1.5 0.2 Iris-setosa
```

```
## 5 5.0 3.6 1.4 0.2 Iris-setosa
## 6 5.4 3.9 1.7 0.4 Iris-setosa
typeof(irisData)
## [1] "list"
class(irisData) # we'll talk more about classes later
## [1] "data.frame"
dim(irisData)
## [1] 150 5
nrow(irisData)
## [1] 150
ncol(irisData)
## [1] 5
```

Do not rely on the default arguments of `read.csv` or `read.table`! After you read in a data frame, always check the first few rows to make sure that

1. The number of columns is correct because the correct column *separator* was used (c.f. `sep=`),
2. column names were parsed correctly, if there were some in the raw text file,
3. the first row of data wasn't used as a column name sequence, if there weren't column names in the text file, and
4. the last few rows aren't reading in empty spaces
5. character columns are read in correctly (c.f. `stringsAsFactors=`), and
6. special characters signifying missing data were correctly identified (c.f. `na.strings=`).

There are some exceptions, but most data sets can be stored as a `data.frame`. This is because usually a data set comes in a two-dimensional shape. Looking at one particular row gives you an observation with all its variables. Looking at a particular column gives you one particular variable for each observation.

A `data.frame` is a special case of a `list`⁶⁷. Every element of the list is a column. Columns can be vectors or factors, and they can all be of a different type. This is one of the biggest differences between data frames and `matrix`s. They are both two-dimensional, but a `matrix` needs elements to be all the same type. Unlike a general `list`, a `data.frame` requires all of its columns to have the same number of elements. In other words, the `data.frame` is not a “ragged” list.

Often times you will need to extract pieces of information from a `data.frame`. This can be done in many ways. If the columns have names, you can use the `$` operator to access a single column. Accessing a single column might be followed up by creating a new vector. You can also use the `[]` operator to access multiple columns by name.

```
colnames(irisData) <- c("sepal.length", "sepal.width", "petal.length", "petal.width")
firstCol <- irisData$sepal.length
head(firstCol)
## [1] 5.1 4.9 4.7 4.6 5.0 5.4
firstTwoCols <- irisData[c("sepal.length", "sepal.width")]
head(firstTwoCols)
##      sepal.length sepal.width
## 1           5.1           3.5
## 2           4.9           3.0
## 3           4.7           3.2
## 4           4.6           3.1
## 5           5.0           3.6
## 6           5.4           3.9
```

The `[]` operator is also useful for selecting rows and columns by index numbers, or by some logical criteria.

⁶⁷<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Data-frame-objects>

```

topLeft <- irisData[1,1] # first row, first col
topLeft
## [1] 5.1
firstThreeRows <- irisData[1:3,] # rows 1-3, all cols
firstThreeRows
##      sepal.length sepal.width petal.length petal.width      species
## 1           5.1           3.5           1.4           0.2 Iris-setosa
## 2           4.9           3.0           1.4           0.2 Iris-setosa
## 3           4.7           3.2           1.3           0.2 Iris-setosa
setosaOnly <- irisData[irisData$species == "Iris-setosa",] # rows where species co
head(setosaOnly)
##      sepal.length sepal.width petal.length petal.width      species
## 1           5.1           3.5           1.4           0.2 Iris-setosa
## 2           4.9           3.0           1.4           0.2 Iris-setosa
## 3           4.7           3.2           1.3           0.2 Iris-setosa
## 4           4.6           3.1           1.5           0.2 Iris-setosa
## 5           5.0           3.6           1.4           0.2 Iris-setosa
## 6           5.4           3.9           1.7           0.4 Iris-setosa

```

In the code above, `irisData$species == "Iris-setosa"` creates a logical vector (try it!) using the vectorized `==` operator. The `[]` operator selects the rows for which the corresponding element of this logical vector is `TRUE`.

Be careful: depending on how you use the square brackets, you can either get a `data.frame` or a vector. As an example, try both `class(irisData[,1])` and `class(irisData[,c(1,2)])`.

In R, `data.frames` have row names. You can get/set this character vector with the `rownames()` function. You can access rows by name using the square bracket operator. Personally, I don't typically use this functionality that often.

```

head(rownames(irisData))
## [1] "1" "2" "3" "4" "5" "6"
rownames(irisData) <- as.numeric(rownames(irisData)) + 1000
head(rownames(irisData))

```

```
## [1] "1001" "1002" "1003" "1004" "1005" "1006"
irisData["1002",]
##      sepal.length sepal.width petal.length petal.width      species
## 1002           4.9           3           1.4           0.2 Iris-setosa
```

0.32 Data Frames in Python

The pandas library in Python has data frames that are modeled after R's.

```
import pandas as pd
iris_data = pd.read_csv("data/iris.csv", header = None)
iris_data.head()
##      0      1      2      3      4
## 0  5.1  3.5  1.4  0.2  Iris-setosa
## 1  4.9  3.0  1.4  0.2  Iris-setosa
## 2  4.7  3.2  1.3  0.2  Iris-setosa
## 3  4.6  3.1  1.5  0.2  Iris-setosa
## 4  5.0  3.6  1.4  0.2  Iris-setosa
iris_data.shape
## (150, 5)
len(iris_data) # num rows
## 150
len(iris_data.columns) # num columns
## 5
iris_data.dtypes
## 0      float64
## 1      float64
## 2      float64
## 3      float64
## 4      object
## dtype: object
```

The structure is very similar to that of R's data frame. It's two dimensional, and you can access columns and rows by name or number.⁶⁸ Each column is a `Series` object, and each column can have a different `dtype`, which is analogous to R's situation. Again, because the elements need to be the same type along columns only, this is a big difference between 2-d Numpy arrays and `DataFrames`.

Just like in R, you can access columns by name. You do that using square brackets. Observe how similar this code is to the corresponding R code above.

```
iris_data.columns = ["sepal.length", "sepal.width", "petal.length",
                    "petal.width", "species"]
first_col = iris_data['sepal.length']
first_col.head()
## 0      5.1
## 1      4.9
## 2      4.7
## 3      4.6
## 4      5.0
## Name: sepal.length, dtype: float64
first_two_cols = iris_data[["sepal.length", "sepal.width"]]
first_two_cols.head()
##      sepal.length  sepal.width
## 0              5.1           3.5
## 1              4.9           3.0
## 2              4.7           3.2
## 3              4.6           3.1
## 4              5.0           3.6
```

Notice that `iris_data['sepal.length']` returns a `Series` and `iris_data[["sepal.length", "sepal.width"]]` returns a `Pandas`

⁶⁸https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html

`DataFrame`. This behavior is similar to what happened in R's. For more details, click here⁶⁹.

You can select columns and rows by number with the `.iloc` method⁷⁰. `iloc` is (probably) short for “integer location.”

```
# specify rows/cols by number
top_left = iris_data.iloc[0,0]
top_left
## 5.1
first_three_rows = iris_data.iloc[:3,]
first_three_rows
#setosa_only = iris_data[iris_data$species == "Iris-setosa",] # easier with loc?
#head(setosa_only)
##      sepal.length  sepal.width  petal.length  petal.width      species
## 0           5.1           3.5           1.4           0.2  Iris-setosa
## 1           4.9           3.0           1.4           0.2  Iris-setosa
## 2           4.7           3.2           1.3           0.2  Iris-setosa
```

Selecting columns by anything besides integer number can be done with the `.loc()` method⁷¹. You should generally prefer this method to access columns because accessing things by *name* instead of *number* is more readable. Here are some examples.

```
sepal_w_to_petal_w = iris_data.loc['sepal.width':'petal.width']
sepal_w_to_petal_w
## Empty DataFrame
## Columns: [sepal.length, sepal.width, petal.length, petal.width, species]
## Index: []
setosa_only = iris_data.loc[iris_data['species'] == "Iris-setosa",]
setosa_only.head()
```

⁶⁹https://pandas.pydata.org/pandas-docs/stable/user_guide/dsintro.html#indexing-selection

⁷⁰<https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.iloc.html>

⁷¹<https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.loc.html>

##	sepal.length	sepal.width	petal.length	petal.width	species
## 0	5.1	3.5	1.4	0.2	Iris-setosa
## 1	4.9	3.0	1.4	0.2	Iris-setosa
## 2	4.7	3.2	1.3	0.2	Iris-setosa
## 3	4.6	3.1	1.5	0.2	Iris-setosa
## 4	5.0	3.6	1.4	0.2	Iris-setosa

Notice we used a `slice` to access many columns by only referring to the left-most and the right-most. This does not work with the regular square bracket operator. The second example filters out the rows where the "species" column elements are equal to "Iris-setosa".

Each `DataFrame` in pandas comes with an `.index` attribute. This is analogous to a row name in R, but it's much more flexible because the index can take on a variety of types. This can help us highlight the difference between `.loc` and `.iloc`. Recall that `.loc` was label-based selection. Labels don't necessarily have to be strings. Consider the following example

```
iris_data.index
## RangeIndex(start=0, stop=150, step=1)
iris_data = iris_data.set_index(iris_data.index[::-1]) # reverse the index
iris_data.head(2)
##      sepal.length  sepal.width  petal.length  petal.width  species
## 149           5.1           3.5           1.4           0.2  Iris-setosa
## 148           4.9           3.0           1.4           0.2  Iris-setosa
iris_data.tail(2)
##      sepal.length  sepal.width  petal.length  petal.width  species
## 1             6.2           3.4           5.4           2.3  Iris-virginica
## 0             5.9           3.0           5.1           1.8  Iris-virginica
iris_data.loc[0]
## sepal.length           5.9
## sepal.width             3
## petal.length           5.1
## petal.width            1.8
```

```
## species      Iris-virginica
## Name: 0, dtype: object
iris_data.iloc[0]
## sepal.length      5.1
## sepal.width       3.5
## petal.length      1.4
## petal.width       0.2
## species      Iris-setosa
## Name: 149, dtype: object
```

`iris_data.loc[0]` selects the 0th index. The second line reversed the indexes, so this is actually the last row. If you want the first row, use `iris_data.iloc[0]`.

0.33 Row Names and Indexes

In Python, Pandas' DataFrames have an

```
iris_data.index
## RangeIndex(start=149, stop=-1, step=-1)
```

0.34 Getting Versus Setting



Part III

Part 2: Common Tasks and Patterns



0

Input and Output

0.35 General Input Considerations

So far we have been creating small pieces of data within our scripts. This is primarily for pedagogical purposes. In real life, we can have

- data read in from a data set saved on our machine’s hard drive (e.g. `my_data.csv` or `log_file.txt`),
- data read in from a database (e.g. MySQL, PostgreSQL, etc.), or
- data created in a script (either deterministic or random).

I focus mostly on the first category in this section. Here are my reasons for doing so:

1. text-files are more readily-available to students than databases,
2. teaching the second category requires teaching SQL, and that would introduce conceptual overlap,
3. the third category is programmatically self-explanatory.

The third reason does not imply data created by code is unimportant. For example, it is the most common approach to create data used in *simulation studies*. Authors writing statistical papers need to demonstrate that their techniques work on “nice” data: data simulated from a known data-generating process. In a simulation study, unlike in the “real-world,” you have access to the parameters generating your data, and you can examine data that might otherwise be unobserved or hidden. Further, with data from the

real-world, there is no guarantee your model correctly matches the true model.

Can your code/technique/algorithm, at the very least, obtain parameter estimates that are “in-line” with the parameters your code is using to simulate data? Are forecasts or predictions obtained by your method accurate? These kinds of questions can often only be answered by simulating fake data. Programmatically, simulating data like this largely involves calling functions that we have seen before (e.g. `rnorm()` in R or `np.random.choice()` in Python). This may or may not involve setting a pseudorandom number seed, first, for reproducibility.

Also, *benchmark data sets* are often readily available through specialized function calls.

Even though this chapter is written to teach you how to read in files into R and Python, you should not expect that you will know how to read in *all* data sets after reading this section. For both R and Python, there are an enormous amount of functions, different functions have different return types, different functions are suited for different file types, many functions are spread across a plethora of third party libraries, and many of these functions have an enormous amount of arguments. You will probably not be able to memorize everything. In my very humble opinion, I doubt you should want to.

Instead, **focus on developing your ability to identify and diagnose data input problems**. Reading in a data set correctly is often a process of trial-and-error. After attempting to read in a data set, always check the following items. Many of these points were previously mentioned in section [@\(data-frames-in-r\)](#).

1. **The correct column *separator* was used, or the correct “fixed-width format” was expected.** If mistakes are made, columns are going to be combined in weird ways, and often the wrong types are going to be used for pieces of data (e.g. “2,3” instead of 2 and 3.) Also, watch out for when separators are found inside data

elements or column names. For example, sometimes it's unclear whether people's names in the "last, first" format can be stored in one or two columns. Also, text data might surprise you with unexpected spaces or other whitespace is a common separator.

2. **The column names were parsed correctly.** Column names should not be stored as data in R/Python. Functions should not expect column names when they don't exist in the actual file.
3. **Empty space and metadata was ignored correctly.** Empty space between column names and data shouldn't be stored. Data descriptions are sometimes stored in the same file as the data itself, and that should be skipped over when it's being read in. This can occur at the beginning of the file, and even at the end of the file.
4. **Type choice is performed correctly.** Are letters stored as strings or as something else such as an R factor? Are dates and times stored as a special date/time type, or as strings? Is missing data correctly identified? Sometimes data providers use outrageous numbers like `-9999` to represent missing data—don't store that as a float or integer!

I realize that this is no small task. To make matters worse:

- you can't edit the raw data to suit your needs, to make it easier to read in. You have to work with what you're given. If you were allowed to edit, say, a text file you downloaded onto your own machine, you shouldn't—it will lead to code that doesn't run anywhere else. If you abuse write privileges on your company's database, say, well then that's definitely going to be catastrophic.
- Data sets are often quite large, so manually checking each element is often impossible. In this situation you will have to resign yourself to checking the top and bottom of a data set, or maybe anticipate a specific place where problems are likely to appear.

0.36 Reading in Text Files with R

You’ve seen examples of `read.csv()` used earlier in the book, so it should not surprise you that this is one of the most common ways to read in data in R. Another important function is `read.table()`. Actually, if you look at the source code for `read.csv()` (type the name of the function without parentheses into the console and press `)`, you will see it calls `read.table()`. The primary difference between these functions is default arguments. **Mind the default arguments.** Do not be completely averse to writing a long-line of code to read in a data set correctly. Or do, and choose the function with the best default arguments.

Consider the “Challenger USA Space Shuttle O-Ring Data Set”⁷² from (Dua and Graff, 2017). The first ten rows looks like this.

```
6 0 66 50 1
6 1 70 50 2
6 0 69 50 3
6 0 68 50 4
6 0 67 50 5
6 0 72 50 6
6 0 73 100 7
6 0 70 100 8
6 1 57 200 9
6 1 63 200 10
```

It does not use commas as separators, and there is no header information, so `read.csv()` used with its default arguments will produce an incorrect result. It will miss the first row by counting it as a column name, and store everything in one column with the wrong type.

⁷²<https://archive.ics.uci.edu/ml/datasets/Challenger+USA+Space+Shuttle+O-Ring>

```
d <- read.csv("data/o-ring-erosion-only.data")
head(d)
##      X6.0.66..50..1
## 1   6 1 70  50  2
## 2   6 0 69  50  3
## 3   6 0 68  50  4
## 4   6 0 67  50  5
## 5   6 0 72  50  6
## 6   6 0 73 100  7
dim(d)
## [1] 22  1
typeof(d[,1])
## [1] "character"
```

Specifying `header=FALSE` fixes the column name issue, but `sep = " "` does not fix the separator issue.

```
d <- read.csv("data/o-ring-erosion-only.data", header=FALSE, sep = " ")
head(d)
##      V1 V2 V3 V4 V5 V6 V7
## 1   6  0 66 NA 50 NA  1
## 2   6  1 70 NA 50 NA  2
## 3   6  0 69 NA 50 NA  3
## 4   6  0 68 NA 50 NA  4
## 5   6  0 67 NA 50 NA  5
## 6   6  0 72 NA 50 NA  6
dim(d)
## [1] 23  7
str(d)
## 'data.frame':    23 obs. of  7 variables:
##  $ V1: int  6 6 6 6 6 6 6 6 6 6 ...
##  $ V2: int  0 1 0 0 0 0 0 0 1 1 ...
##  $ V3: int 66 70 69 68 67 72 73 70 57 63 ...
##  $ V4: int NA NA NA NA NA NA 100 100 200 200 ...
##  $ V5: int 50 50 50 50 50 50 NA NA NA 10 ...
```

```
## $ V6: int NA NA NA NA NA NA 7 8 9 NA ...
## $ V7: int 1 2 3 4 5 6 NA NA NA NA ...
```

One space is strictly one space. Some rows have two, though. After digging into the documentation a bit further, you will notice that `""` works for “one or more spaces, tabs, newlines or carriage returns.” This is why `read.table()`, with its default arguments, works well.

```
d <- read.table("data/o-ring-erosion-only.data")
head(d)
##    V1 V2 V3 V4 V5
## 1  6  0 66 50  1
## 2  6  1 70 50  2
## 3  6  0 69 50  3
## 4  6  0 68 50  4
## 5  6  0 67 50  5
## 6  6  0 72 50  6
dim(d)
## [1] 23  5
str(d)
## 'data.frame':    23 obs. of  5 variables:
## $ V1: int  6 6 6 6 6 6 6 6 6 6 6 ...
## $ V2: int  0 1 0 0 0 0 0 0 1 1 ...
## $ V3: int 66 70 69 68 67 72 73 70 57 63 ...
## $ V4: int 50 50 50 50 50 50 100 100 200 200 ...
## $ V5: int  1 2 3 4 5 6 7 8 9 10 ...
```

This data set has columns whose widths are “fixed”, too. It is in “fixed width format” because any given column has all its elements take up a constant amount of characters. The third column has integers with two or three digits, but no matter what, each row has the same number of characters. The annoying thing about this method, though, is you have to specify what those widths are. This can be quite tedious if your data set has many columns and/or many rows. The upside though, is that the files can be a

little bit smaller, because the data provider does not have to waste characters on separators.

```
d <- read.fwf("data/o-ring-erosion-only.data", widths = c(1,1,2,3,2), sep = "")
str(d)
## 'data.frame':   23 obs. of  4 variables:
## $ V1: int  6 6 6 6 6 6 6 6 6 6 ...
## $ V2: int  0 1 0 0 0 0 0 0 1 1 ...
## $ V3: int 66 70 69 68 67 72 73 70 57 63 ...
## $ V4: int  5 5 5 5 5 5 10 10 20 20 ...
```

0.37 Reading in Text Files with Python

TODO

0.38 Output

After we have created something useful, we might be interested in storing our results. We can write out to a database, a text file, or we can save a digitized version of our work space.



0

Using Third-Party Code

Before using third-party code, it must first be installed. After it is installed, it must be “loaded in” to your session. I will describe both of these steps in R and Python.

0.39 Installing Packages In R

In R, there are thousands of user-created **packages**. You can download most of these from the *Comprehensive R Archive Network*⁷³. You can also download packages from other publishing platforms like Bioconductor⁷⁴, or Github⁷⁵. Installing from CRAN is more commonplace, and extremely easy to do. Just use the `install.packages()` function. This can be run inside your R console, so there is no need to type things into the command line.

```
install.packages("thePackage")
```

⁷³<https://cran.r-project.org/>

⁷⁴<https://www.bioconductor.org/>

⁷⁵<https://github.com/>

0.40 Installing Packages In Python

In Python, installing packages is more complicated. Commands must be written in the command line, and there are multiple package managers. This isn't surprising, because Python is used more extensively than R in fields other than data science.

If you followed the suggestions provided in 0.0.1, then you installed Anaconda. This means you will usually be using the `conda` command⁷⁶. Point-and-click interfaces are made available as well.

```
conda install the_package
```

There are some packages that will not be available using this method. For more information on that situation, see here.⁷⁷

0.41 Loading Packages In R

After they are installed on your machine, third-party code will need to be “loaded” into your R or Python session.

Loading in a package is relatively simple in R, however complications can arise when different variables share the same name. This happens relatively often because

- it's easy to create a variable in the global environment that has the same name as another object you don't know about, and
- different packages you load in sometimes share names accidentally.

⁷⁶<https://docs.anaconda.com/anaconda/user-guide/tasks/install-packages/>

⁷⁷<https://conda.io/projects/conda/en/latest/user-guide/tasks/manage-pkgs.html#install-non-conda-packages>

Starting off with the basics, here's how to load in a package of third-party code. Just type the following into your R console.

```
library(thePackage)
```

You can also use the `require()` function, which has slightly different behavior when the requested package is not found.

To understand this more deeply, we need to talk about **environments** again. We discussed these before in 0.23, but only in the context of user-defined functions. When we load in a package with `library()`, we make its contents available by putting it all in an environment for that package.

An environment⁷⁸ holds the names of objects. There are usually several environments, and each holds a different set of functions and variables. All the variables you define are in an environment, every package you load in gets its own environment, and all the functions that come in R pre-loaded have their own environment.

Formally, each environment is pair of two things: a **frame** and an **enclosure**. The frame is the set of symbol-value pairs, and the enclosure is a pointer to the parent environment. If you've heard of a *linked list* in a computer science class, it's the same thing.

Moreover, all of these environments are connected in a chain-like structure. To see what environments are loaded on your machine, and what order they were loaded in, use the `search()` function. This displays the **search path**⁷⁹, or the ordered sequence of all of your environments.

```
search()
## [1] ".GlobalEnv"          "package:R6"           "package:Matrix"       "package:Hm
## [5] "package:ggplot2"      "package:Formula"      "package:survival"      "package:la
## [9] "package:reticulate"   "tools:rstudio"        "package:stats"         "package:gr
```

⁷⁸<https://cran.r-project.org/doc/manuals/R-lang.html#Environment-objects>

⁷⁹<https://cran.r-project.org/doc/manuals/R-lang.html#Search-path>

```
## [13] "package:grDevices" "package:utils"      "package:datasets"  "package:me
## [17] "Autoloads"         "package:base"
```

Alternatively, if you're using RStudio, the search path, and the contents of each of its environments, are displayed in the "Environment" window. You can choose which environment you'd like to look at by selecting it from the drop-down menu. This allows you to see all of the variables in that particular environment. The **global environment** (i.e. ".GlobalEnv") is displayed by default, because that is where you store all the objects you are creating in the console.

```
r      anaconda-navigator,    fig.cap='Anaconda Navigator',
out.width='80%', fig.asp=.75, fig.align='center', echo=F
```

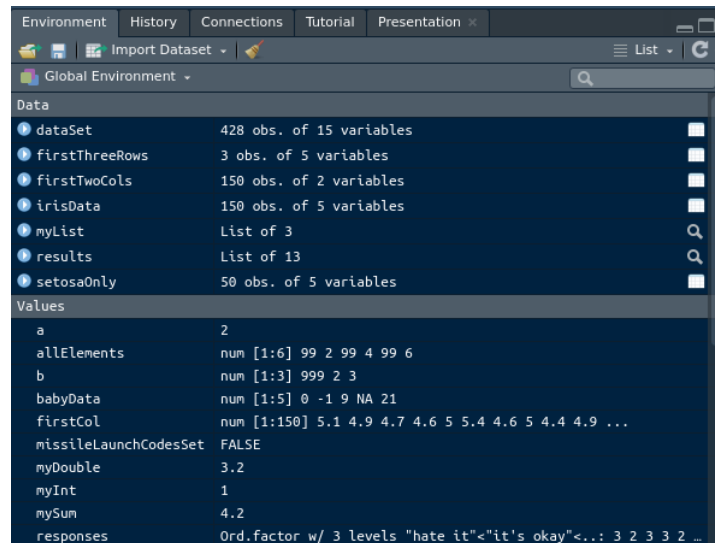


FIGURE 4: The Environment Window in RStudio

When you call `library(thePackage)`, the package has an environment created for it, and it is *inserted between the global environment, and the most recently loaded package*. When you want to access an object by name, R will first search the global environ-

ment, and then it will traverse the environments in the search path in order. These has a few important implications.

- First, **don't define variables in the global environment that are already named in another environment.** There are many variables that come pre-loaded in the `base` package (to see them, type `ls("package:base")`), and if you like using a lot of packages, you're increasing the number of names you should avoid using.
- Second, **don't `library` in a package unless you need it, and if you do, be aware of all the names it will mask its packages you loaded in before.** The good news is that `library` will often print warnings letting you know which names have been masked. The bad news is that it's somewhat out of your control—if you need two packages, then they might have a shared name, and the only thing you can do about it is watch the ordering you load them in.
- Third, don't use `library()` inside code that is `source'd` in other files. For example, if you attach a package to the search path from within a function you defined, anybody that uses your function loses control over the order of packages that get attached.

All is not lost if there is a name conflict. The variables haven't disappeared. It's just slightly more difficult to refer to them. For instance, if I load in `Hmisc` (TODO cite), I get the warning warning that `format.pval` and `units` are now masked because they were names that were in `"package:base"`. I can still refer to these masked variables with the double colon operator (`::`).

```
library(Hmisc)
# format.pval refers to Hmisc's format.pval because it was loaded more recently
# Hmisc::format.pval in this case is the same as above
# base::format.pval this is the only way you can get base's format.pval function
```

0.42 Loading Packages In Python

In Python, you use the `import` statement to access objects defined in another file. It is slightly more complicated than R's `library()` function, but it is also more flexible. To make the contents of a package called, say, `the_package` available, type *one of the following* inside a Python session.

```
import the_package
import the_package as tp
from the_package import *
```

To describe the difference between these three approaches, as well as to highlight the important takeaways and compare them with the important takeaways in the last section, we need to discuss what a Python module is, what a package is, and what a Python namespace is.⁸⁰

- A Python **module**⁸¹ is a separate (when I say separate, I mean separate from the script file you're currently editing) `.py` file with function and/or object definitions in it.⁸²
- A package⁸³ is a group of modules.⁸⁴
- A **namespace**⁸⁵ is “a mapping from names to objects.”

With these definitions, we can define `importing`. According to the

⁸⁰I am avoiding any mention of R's namespaces and modules. These are things that exist, but they are different from Python's namespaces and modules, and are not within the scope of this text.

⁸¹<https://docs.python.org/3/tutorial/modules.html>

⁸²The scripts you write are modules. They come with the intention of being run from start to finish. Other non-script modules are just a bag of definitions to be used in other places.

⁸³<https://docs.python.org/3/tutorial/modules.html#packages>

⁸⁴Sometimes a package is called a *library* but I will avoid this terminology.

⁸⁵<https://docs.python.org/3/tutorial/classes.html#python-scopes-and-namespaces>

Python documentation⁸⁶, “[t]he import statement combines two operations; it searches for the named module, then it binds the results of that search to a name in the local scope.”

The sequence of places Python looks for a module is called the search path. This is not the same as R’s search path, though. In Python, the search path is a list of places to look for *modules*, not a list of places to look for variables. To see it, `import sys`, then type `sys.path`.

After a module is found, the variable names in the found module become available in the `importing` module. These variables are available in the global scope, but the names you use to access them will depend on what kind of `import` statement you used. From there, you are using the same scoping rules that we described in 0.26, which means the LEGB acronym still applies.

Here are a few important takeaways that might not be readily apparent:

- Python namespaces are unlike R environments in that they are not arranged into a sorted list.
- Unlike in R, there is no *masking*, and you don’t have to worry about the *order* of `importing` things.
- However, you do have to worry about *how* you’re `importing` things. If you use the `from the_package import thingone, thingtwo` format of `importing`, you are at risk of re-assigning either `thingone` or `thingtwo`, if they already exist. As a rule of thumb, **you should never use this form of `importing`**.
- These differences might explain why Python packages tend to be larger than R packages.

0.42.1 `importing` Examples

In the example below, we import the entire `numpy` package in a way that lets us refer to it as `np`. This reduces the amount of typing that

⁸⁶<https://docs.python.org/3/reference/import.html#the-import-system>

is required of us, but it also protects against variable name clashing. We then use the `normal()` function to simulate normal random variables. This function is in the `random` sub-module⁸⁷, which is a sub-module in `numpy` that collects all of the pseudorandom number generation functionality together.

```
import numpy as np # import all of numpy
np.random.normal(size=10)
## array([-0.27765344, -0.47933331,  0.35239385,  1.29126942, -1.14823749,
##          0.45079581, -0.16164364,  1.61077554,  0.19163947,  0.8018418 ])
```

This is one use of the dot operator (`.`). It is also used to access attributes and methods of objects (more information on that will come later in chapter IV). `normal` is *inside of* `random`, which it itself inside of `np`.

As a second example, suppose we were interested in the `stats` sub-module⁸⁸ found inside the `scipy` package. We could import all of `scipy`, but just like the above example, that would mean we would need to consistently refer to a variable's module, the sub-module, and the variable name. For long programs, this can become tedious if we had to type `scipy.stats.norm` over and over again. Instead, let's import the sub-module (or sub-package) and ignore the rest of `scipy`.

```
from scipy import stats
stats.norm().rvs(size=10)
## array([-0.60424474,  1.10574136, -0.03758288,  0.74888149, -1.26213601,
##          -0.40244042, -0.39630302,  0.20299809,  1.33581446, -0.31943598])
```

So we don't have to type `scipy` every time we use something in `scipy.stats`.

Finally, we can import the function directly, and refer to it with

⁸⁷<https://numpy.org/doc/stable/reference/random/index.html?highlight=random#module-numpy.random>

⁸⁸<https://docs.scipy.org/doc/scipy/reference/tutorial/stats.html>

only one letter. This is highly discouraged, though. We are much more likely to accidentally use the name `n` twice. Further, `n` is not a very descriptive name, which means it could be difficult to understand what your program is doing later.

```
from numpy.random import normal as n
n(size=10)
## array([-0.00206196, -0.30941862,  1.31168263, -0.55416485,  0.48026473,
##        0.27260937, -1.26977766,  0.18755715,  0.67696992, -0.65171426])
```

Keep in mind, you're always at risk of accidentally re-using names, even if you aren't importing anything. For example, consider the following code.

```
# don't do this!
sum = 3
```

This is very bad, because now you cannot use the `sum` function that was named in the built-in module. To see what is in your built in module, type the following into your Python interpreter: `dir(__builtins__)`.



0

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0.43 Conditional Logic

We discussed Boolean objects in II. We used these for

- counting up number of times a condition appeared, and
- subsetting.

Another way to use them is to conditionally execute code, depending on whether or truth condition of a Boolean.

In R,

```
myName <- "Clare"
if(myName != "Taylor"){
  print("you are not Taylor")
}
## [1] "you are not Taylor"
```

In Python⁸⁹, you don't need curly braces, but the indentation needs to be just right, and you need a colon.

```
my_name = "Taylor"
if my_name == "Taylor":
    print("hi Taylor")
## hi Taylor
```

There can be more than one truth test. To test alternative Boolean

⁸⁹<https://docs.python.org/3/tutorial/controlflow.html#if-statements>

conditions, you can add one or more `else if` (in R) or `elif` (in Python) blocks. The first block with a Boolean that is found to be true will execute, and none of the resulting conditions will be checked.

If no `if` block or `else if/elif` block executes, an `else` block will always execute. That's why `else` blocks don't need to look at a Boolean. Whether they execute only depends on the Booleans in the previous blocks.

```
food <- "muffin"
if(food == "apple"){
  print("an apple a day keeps the doctor away")
}else if(food == "muffin"){
  print("muffins have a lot of sugar in them")
}else{
  print("neither an apple nor a muffin")
}
## [1] "muffins have a lot of sugar in them"
```

```
my_num = 42.999
if my_num % 2 == 0:
  print("my_num is even")
elif my_num % 2 == 1:
  my_num += 1
  print("my_num was made even")
else:
  print("you're cheating by not using integers!")
## you're cheating by not using integers!
```

0.44 Loops

One line of code generally does one “thing,” unless you’re using loops. Code written inside a loop will execute many times.

The most common loop for us will be a `for` loop. A simple `for` loop in R might look like this

```
myLength <- 9
r <- vector(mode = "numeric", length = myLength)
for(i in seq_len(myLength)){
  r[i] <- i
}
r
## [1] 1 2 3 4 5 6 7 8 9
```

1. `seq_len(myLength)` gives us a `vector`
2. `i` is a variable that takes on the values found in the `vector`
3. Code inside the loop (inside the curly braces), is repeatedly executed, and it may or may not reference the dynamic variable `i`

In Python⁹⁰

```
my_length = 9
r = []
for i in range(my_length):
    r.append(i)
r
## [0, 1, 2, 3, 4, 5, 6, 7, 8]
```

1. Unsurprisingly, Python’s syntax opts for indentation and colons instead of curly braces and parentheses,

⁹⁰<https://docs.python.org/3/tutorial/controlflow.html#for-statements>

2. Code inside the loop (inside the curly braces), is repeatedly executed, and it may or may not reference the dynamic variable `i`
3. `for` loops in Python are more flexible because they iterate over many different types of data structures,
4. The `range`⁹¹ doesn't generate all the numbers in the sequence at once, so it saves on memory. This can be quite useful for certain applications. However, `r` is a list that *does* store all the consecutive integers.

Loop tips:

1. If you find yourself copy/paste-ing code, changing only a small portion of text on each line of code, you should consider using a loop,
2. If a `for` loop works for something you are trying to do, first try to find a replacement function that does what you want. The examples above just made a `vector/list` of consecutive integers. There are many built in functions that accomplish this. Avoiding loops in this case would make your program shorter, easier to read, and (potentially) much faster.
3. A third option between looping, and a built-in function, is to try the functional approach. This will be explained more in the last chapter.
4. Watch out for **off-by-one** errors⁹². Iterating over the wrong sequence is a common mistake, considering
 - Python starts counting from 0, while R starts counting from 1
 - sometimes iteration `i` references the `i-1`th element of a container
 - The behavior of loops is sometimes more difficult to understand if they're using `break` or `continue/next` statements

⁹¹<https://docs.python.org/3/tutorial/controlflow.html#the-range-function>

⁹²https://en.wikipedia.org/wiki/Off-by-one_error

5. *Don't hardcode variables.* Minimize the number of places you have to make changes to your code. You will change your code consistently, so save your future self some time.

The last point bears repeating: *don't hardcode variables*. In statistical programs, there are often “tuning parameters,” for instance that must be changed frequently to affect the overall behavior of the program. If these variables only need to be changed in one location, that saves you a lot of time and gives you more flexibility.

In the example above, the `myLength` or `my_length` variable could be referenced in many places throughout the entire program. If you wanted to change the number of iterations in your program (which happens all the time), and you *did* hardcode the length in a bunch of places throughout the program, you would need to hunt down all those changes!

Python provides an alternative way to construct lists similar to the one we constructed in the above example. They are called **list comprehensions**⁹³. You can incorporate iteration and conditional logic in one line of code.

```
[3*i for i in range(10) if i%2 == 0]
## [0, 6, 12, 18, 24]
```

You might also have a look at *generator expressions*⁹⁴ and *dictionary comprehensions*⁹⁵.

R can come close to replicating the above behavior with vectorization, but the conditional part is hard to achieve without subsetting.

```
3*seq(0,9)[seq(0,9)%2 == 0]
## [1] 0 6 12 18 24
```

⁹³<https://docs.python.org/3/tutorial/datastructures.html#list-comprehensions>

⁹⁴<https://www.python.org/dev/peps/pep-0289/>

⁹⁵<https://www.python.org/dev/peps/pep-0274/>

0.45 A Longer Example

0.45.1 Description of Accept-Reject Sampling

An example of an algorithm that uses conditional logic is the **accept-reject sampling method** (Robert and Casella, 2005). This is useful for when we want to sample from a *target probability density* $p(x)$, using another distribution called a *proposal distribution* $q(x)$.

$q(x)$ is probably a distribution that is easy to sample from and is easy to evaluate pointwise. For example, a uniform distribution satisfies these criteria because both R and Python have functions that accomplish these two things (e.g. sampling can be done with `runif` in R and `np.random.uniform` in Python). $p(x)$ is generally more “complicated.” If it wasn’t, we would try to find some built-in function for it.

One common way a distribution can be complicated is that it can have an unknown **normalizing constant**—one that is difficult or impossible to solve using calculus. This happens a lot in *Bayesian Statistics*, for example.⁹⁶ We might write down

$$p(x) = \frac{f(x)}{\int f(x)dx},$$

and this is guaranteed to be a probability density function as long as $f(x) \geq 0$ and $\int f(x)dx < \infty$, but we might have no idea how to solve the denominator. In this case, $f(x)$ is easy to evaluate pointwise, but $p(x)$ is not.

This algorithm makes use of an auxiliary random variable that is sampled from a Bernoulli(p) distribution. As long as $0 < p < 1$, a Bernoulli random variable Y is either 0 or 1. The probability it takes the value 1 is p , while the probability that it takes the

⁹⁶The posterior distribution is usually the object of interest in Bayesian statistics. According to Bayes’ Rule, the unnormalized posterior is usually the product of two “easy” functions. However, integrating the product is not always possible!

value 0 is $1 - p$. A coin flip is a good example use-case for this distribution. Coin flips are commonly assumed to be distributed as `Bernoulli(.5)`. At least for fair coins, there is an equal chance that the coin lands heads (i.e. 0) or tails (i.e. 1).

The most difficult part about using this algorithm is that one must calculate the probability parameter of this Bernoulli random variable. This involves calculating (by hand) an upper bound M for the ratio $f(x)/q(x)$. This bound has to hold uniformly, meaning that it is a constant number that is greater than the ratio no matter what x we plug in.

Below is one step of the accept-reject algorithm.

Algorithm 1: Accept-Reject Sampling (One Step)

1. Calculate $M > \frac{f(x)}{q(x)}$ (the smaller the better)
 2. Sample X from $q(x)$
 3. Sample $Y \mid X$ from `Bernoulli` $\left(\frac{f(X)}{q(X)M}\right)$
 4. If $Y = 1$, then return X
 5. Otherwise, return nothing
-

Multiple samples will be required, so this process needs to be iterated many times. There are two ways to do this. If you want to iterate a fixed number of times, you can use a `for` loop. However, in that case, you will end up with a random number of samples. On the other hand, if you want a nonrandom number of samples, you will probably want a `while` loop. This is the approach the example below takes. The `while` loop will continue iterating until a condition is false. In our case, we want to loop until we receive the total number of samples we requested.

0.45.2 A Specific Example

Here is a specific example. Let's say our target⁹⁷ is

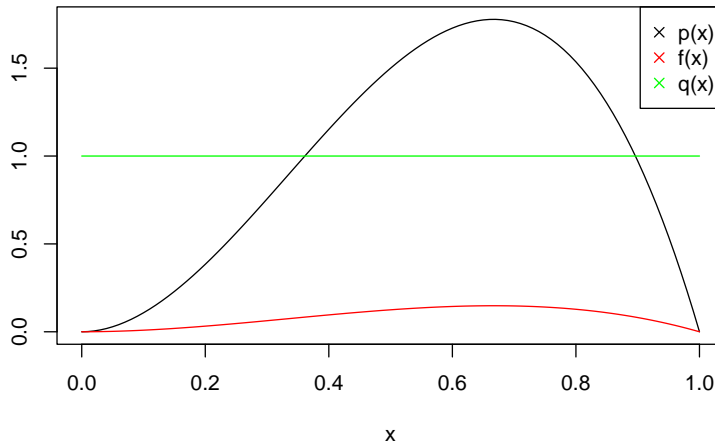
$$p(x) = \begin{cases} \frac{x^2(1-x)}{\int_0^1 x^2(1-x)dx} & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}.$$

The denominator, $\int_0^1 x^2(1-x)dx$, is the target's normalizing constant. You might know how to solve this integral, but let's pretend for the sake of our example that it's too difficult for us. We want to sample from $p(x)$ while only being able to evaluate (not sample) from its normalized version.

Next, let's choose a uniform distribution for our proposal distribution:

$$q(x) = \begin{cases} 1 & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$

We can plot all three functions.



Here's some Python code that attempts to sample once from $p(x)$. Sometimes proposals are not accepted. When that happens, the function returns None.

⁹⁷This is the density of a Beta(3,2) random variable, if you're curious.


```

import numpy as np

def f(samp):
    """the unnormalized density"""
    return (1-samp)*(samp**2)

def attempt_one_samp():
    """attempts to sample from target distribution, using uniform as a proposal"""
    x = np.random.uniform()
    M = 4/27
    bern_prob_param = f(x)/M
    accept = np.random.binomial(1, bern_prob_param) == 1
    if accept:
        return x

```

```

def sample_from_target(num_times):
    """sample num_times from the target distribution"""
    samps = []
    while len(samps) < num_times:
        potential_samp = attempt_one_samp()
        if potential_samp is not None:
            samps.append(potential_samp)
    return samps

```

1. we used a while loop instead of a for loop because we did not know how many iterations it would take to get num_times samples
2. We are following the Python style guide⁹⁸ and using the is not keyword to check if something is None

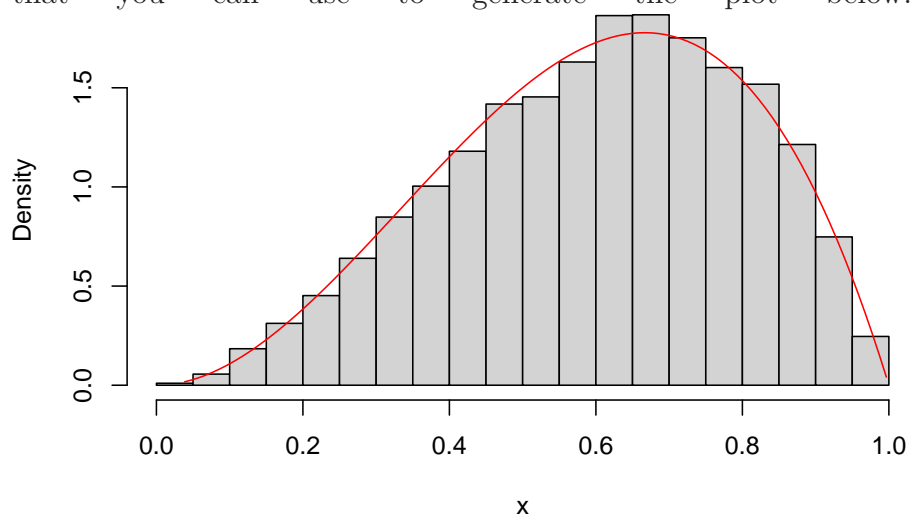
In chapter 0.49.2, we'll show you the code

⁹⁸<https://www.python.org/dev/peps/pep-0008/#other-recommendations>

cxlvi

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that you can use to generate the plot below.



0

Reshaping and Combining Data Sets

0.46 Ordering and Sorting Data

Sorting a data set, in ascending order, say, is a common task. You might need to do it because

1. ordering and ranking is commonly done in *nonparametric statistics*,
2. you want to inspect the most “extreme” observations in a data set,
3. it’s a pre-processing step before generating visualizations.

In R, it all starts with *vectors*. There are two common functions you should know: `sort` and `order`. `sort` returns the sorted *data*, while `order` returns the *order indexes*.

```
sillyData <- rnorm(5)
print(sillyData)
## [1] -0.64581828  0.07525966 -0.23188324  0.51466673  1.06266555
sort(sillyData)
## [1] -0.64581828 -0.23188324  0.07525966  0.51466673  1.06266555
order(sillyData)
## [1] 1 3 2 4 5
```

`order` is useful if you’re sorting a data frame by a particularly column. Below, we inspect the top 5 most expensive cars. Notice that we need to clean up the `MSRP` (a *character vector*) a little first. We use the function `gsub` to find patterns in the text, and replace them with the empty string.

```
carData <- read.csv("data/cars.csv")
noDollarSignMSRP <- gsub("$", "", carData$MSRP, fixed = TRUE)
carData$cleanMSRP <- as.numeric(gsub(",", "", noDollarSignMSRP, fixed = TRUE))
rowIndices <- order(carData$cleanMSRP, decreasing = TRUE)[1:5]
carData[rowIndices, c("Make", "Model", "MSRP", "cleanMSRP")]
```

##	Make	Model	MSRP	cleanMSRP
## 335	Porsche	911 GT2 2dr	\$192,465	192465
## 263	Mercedes-Benz	CL600 2dr	\$128,420	128420
## 272	Mercedes-Benz	SL600 convertible 2dr	\$126,670	126670
## 271	Mercedes-Benz	SL55 AMG 2dr	\$121,770	121770
## 262	Mercedes-Benz	CL500 2dr	\$94,820	94820

In Python, Numpy has `np.argsort`⁹⁹ and `np.sort`¹⁰⁰.

```
import numpy as np
silly_data = np.random.normal(size=5)
print(silly_data)
## [-2.35016726 -0.75361656  0.477097   -0.27210408 -1.06733766]
np.sort(silly_data)
## array([-2.35016726, -1.06733766, -0.75361656, -0.27210408,  0.477097   ])
np.argsort(silly_data)
## array([0, 4, 1, 3, 2])
```

For pandas' DataFrames, most of the functions I find useful are methods attached to the DataFrame class. That means that, as long as something is inside a DataFrame, you can use dot notation.

```
import pandas as pd
car_data = pd.read_csv("data/cars.csv")
car_data['no_dlr_msrp'] = car_data['MSRP'].str.replace("$", "", regex = False)
car_data['clean_MSRP'] = car_data['no_dlr_msrp'].str.replace(",", "").astype(float)
```

⁹⁹<https://numpy.org/doc/stable/reference/generated/numpy.argsort.html>

¹⁰⁰<https://numpy.org/doc/stable/reference/generated/numpy.sort.html>

```
car_data = car_data.sort_values(by='clean_MSRP', ascending = False)
car_data[["Make", "Model", "MSRP", "clean_MSRP"]].head(5)
```

##	Make	Model	MSRP	clean_MSRP
## 334	Porsche	911 GT2 2dr	\$192,465	192465.0
## 262	Mercedes-Benz	CL600 2dr	\$128,420	128420.0
## 271	Mercedes-Benz	SL600 convertible 2dr	\$126,670	126670.0
## 270	Mercedes-Benz	SL55 AMG 2dr	\$121,770	121770.0
## 261	Mercedes-Benz	CL500 2dr	\$94,820	94820.0

pandas' `DataFrames` and `Series` have a `replace`¹⁰¹ method. We use this to remove dollar signs and commas from the `MSRP` column. Note that we had to access the `.str` attribute of the `Series` column before we used it. After the string was processed, we converted it to a `Series` of floats with the `astype` method.

Finally, sorting the overall data frame could have been done with the same approach as the code we used in R (i.e. raw subsetting by row indexes), but there is a built in method called `sort_values` that will do it for us.

0.47 Stacking Data Sets and Placing them Shoulder to Shoulder

Stacking data sets on top of each other is a common task. You might need to do it if

1. you need to add new a new row (or many rows) to a data frame,
2. you need to recombine data sets (e.g. recombine a train/test split), or
3. you're creating a matrix in a step-by-step way.

¹⁰¹<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.replace.html>

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Reshaping and Combining Data Sets

In R, this can be done with `rbind` (short for “row bind”)

```
realEstate <- read.csv("data/albemarle_real_estate.csv")
train <- realEstate[-1,]
test <- realEstate[1,]
head(rbind(test, train))
```

##	YearBuilt	YearRemodeled	Condition	NumStories	FinSqFt	Bedroom	FullBath	HalfBat
## 1	2006	0	Average	1.00	1922	3	3	
## 2	2003	0	Average	1.00	1848	3	2	
## 3	1972	0	Average	1.00	1248	2	1	
## 4	1998	0	Good	1.00	1244	1	1	
## 5	1886	0	Average	1.86	1861	4	1	
## 6	1910	0	Fair	1.53	1108	3	1	

##	TotalValue	City
## 1	409900	CROZET
## 2	523100	CROZET
## 3	180900	EARLYSVILLE
## 4	620700	CROZET
## 5	162500	CROZET
## 6	167200	CROZET

```
sum(rbind(test, train) != realEstate)
## [1] 0
```

The above example was with `data.frames`. This example of `rbind` is with `matrix` objects.

```
rbind(matrix(1,nrow = 2, ncol = 3),
      matrix(2,nrow = 2, ncol = 3))
```

##	[,1]	[,2]	[,3]
## [1,]	1	1	1
## [2,]	1	1	1
## [3,]	2	2	2
## [4,]	2	2	2

In Python, you can stack data frames with `pd.concat`¹⁰². It has a lot of options, so feel free to peruse those. You can also replace the call to `pd.concat` below with `test.append(train)`¹⁰³.

```
import pandas as pd
real_estate = pd.read_csv("data/albemarle_real_estate.csv")
train = real_estate.iloc[1:,]
test = real_estate.iloc[[0],] # need the extra brackets!
pd.concat([test,train], axis=0).head() # also
##      YearBuilt  YearRemodeled Condition  ...  LotSize  TotalValue      City
##  0         2006              0  Average  ...    5.000    409900    CROZET
##  1         2003              0  Average  ...   61.189    523100    CROZET
##  2         1972              0  Average  ...    1.760    180900  EARLYSVILLE
##  3         1998              0    Good   ...   50.648    620700    CROZET
##  4         1886              0  Average  ...    3.880    162500    CROZET
##
## [5 rows x 12 columns]
(pd.concat([test,train], axis=0) != real_estate).sum().sum()
## 0
```

Take note of the extra square brackets when we create `test`. If you use `real_estate.iloc[0,]` instead, it will return a `Series` with all the elements coerced to the same type, and this won't `pd.concat` properly with the rest of the data!

0.48 Merging or Joining Data Sets

If you have two different data sets that provide different information about the same things, you put them together using a **merge** (aka **join**) statement. The resulting data set is wider, and possi-

¹⁰²<https://www.google.com/search?client=safari&rls=en&q=pandas+concat&ie=UTF-8&oe=UTF-8>

¹⁰³<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.append.html>

bly with fewer rows. In R, you can use the `merge` function¹⁰⁴. In Python, you can use the `merge` method¹⁰⁵.

Suppose you have two sets of supposedly anonymized data about individual accounts on some online platforms.

```

baby1 <- read.csv("data/baby1.csv", stringsAsFactors = FALSE)
baby2 <- read.csv("data/baby2.csv", stringsAsFactors = FALSE)
head(baby1)
##      idnum height.inches.      email_address
## 1      1           74 fakeemail123@gmail.com
## 2      3           66  anotherfake@gmail.com
## 3      4           62    notreal@gmail.com
## 4     23           62    notreal@gmail.com
head(baby2)
##      idnum      phone      email
## 1 3901283 5051234567    notreal@gmail.com
## 2  41823 5051234568 notrealeither@gmail.com
## 3 7198273 5051234568  anotherfake@gmail.com

```

The first thing you need to ask yourself is “which column is the unique identifier that is shared between these two data sets?” In our case, they both have an “identification number” column, could that be it? Let’s suppose for the sake of argument that these two data sets are coming from different online platforms, and these two places use different schemes to number their users.

In this case, they both share a column with (possibly) the same information about email addresses. They are named differently in each data set, so we must specify both column names.

```

# in R
merge(baby1, baby2, by.x = "email_address", by.y = "email")

```

¹⁰⁴<https://www.rdocumentation.org/packages/base/versions/3.6.2/topics/merge>

¹⁰⁵<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.merge.html#pandas-dataframe-merge>

##	email_address	idnum.x	height.inches.	idnum.y	phone
## 1	anotherfake@gmail.com	3	66	7198273	5051234568
## 2	notreal@gmail.com	4	62	3901283	5051234567
## 3	notreal@gmail.com	23	62	3901283	5051234567

In Python, `merge` is a method attached to each `DataFrame` instance.

```
# in Python
baby1.merge(baby2, left_on = "email_address", right_on = "email")
##      idnum_x  height(inches)  ...      phone      email
## 0         3             66  ...  5051234568  anotherfake@gmail.com
## 1         4             62  ...  5051234567    notreal@gmail.com
## 2        23             62  ...  5051234567    notreal@gmail.com
##
## [3 rows x 6 columns]
```

The email addresses `anotherfake@gmail.com` and `notreal@gmail.com` exist in both data sets, so each of these email addresses will end up in the result data frame. The rows in the result data set are wider and have more attributes for each individual.

Notice the duplicate email address, too. In this case, either the user signed up for two accounts using the same email, or one person signed up for an account with another person's email address. In the case of duplicates, both rows will match with the same rows in the other data frame.

Also, in this case, all email addresses that weren't found in both data sets were thrown away. This does not necessarily need to be the intended behavior. For instance, if we wanted to make sure no rows were thrown away, that would be possible. In this case, though, for email addresses that weren't found in both data sets, some information will be missing. Recall that Python and R handle missing data differently (see 0.15).

```
# in R
merge(baby1, baby2,
      by.x = "email_address", by.y = "email",
      all.x = TRUE, all.y = TRUE)
##           email_address idnum.x height.inches. idnum.y      phone
## 1  anotherfake@gmail.com      3           66 7198273 5051234568
## 2   fakeemail123@gmail.com      1           74      NA      NA
## 3    notreal@gmail.com      4           62 3901283 5051234567
## 4    notreal@gmail.com     23           62 3901283 5051234567
## 5 notrealeither@gmail.com    NA           NA   41823 5051234568
```

```
# in Python
baby1.merge(baby2,
            left_on = "email_address", right_on = "email",
            how = "outer")
##      idnum_x  height(inches)  ...      phone      email
## 0         1.0           74.0  ...      NaN      NaN
## 1         3.0           66.0  ...  5.051235e+09  anotherfake@gmail.com
## 2         4.0           62.0  ...  5.051235e+09    notreal@gmail.com
## 3        23.0           62.0  ...  5.051235e+09    notreal@gmail.com
## 4         NaN           NaN  ...  5.051235e+09  notrealeither@gmail.com
##
## [5 rows x 6 columns]
```

You can see it's slightly more concise in Python. If you are familiar with SQL, you might have heard of inner and outer joins. This is where pandas takes some of its argument names from¹⁰⁶.

¹⁰⁶<https://pandas.pydata.org/pandas-docs/version/0.15/merging.html#database-style-dataframe-joining-merging>

0.49 Long Versus Wide Data

0.49.1 Long Versus Wide in R

Many types of data can be stored in either a **wide** or **long** format.

The classical example is data from a *longitudinal study*. If an experimental unit (in the example below a person) is repeatedly measured over time, each row would correspond to an experimental unit *and* an observation time in a data set in a long form.

```
fake_long_data1 <- data.frame(person = c("Taylor", "Taylor", "Charlie", "Charlie"),
                              timeObserved = c(1, 2, 1, 2),
                              nums = c(100, 101, 300, 301))

fake_long_data1
##      person timeObserved nums
## 1  Taylor           1    100
## 2  Taylor           2    101
## 3 Charlie           1    300
## 4 Charlie           2    301
```

A long format can also be used if you have multiple observations (at a single time point) on an experimental unit. Here is another example.

```
fake_long_data2 <- data.frame(person = c("Taylor", "Taylor", "Charlie", "Charlie"),
                              attributeName = c("attrA", "attrB", "attrA", "attrB"),
                              nums = c(100, 101, 300, 301))

fake_long_data2
##      person attributeName nums
## 1  Taylor           attrA   100
## 2  Taylor           attrB   101
## 3 Charlie           attrA   300
## 4 Charlie           attrB   301
```

If you would like to reshape the long data sets into a wide format, you can use the `reshape` function. You will need to specify which columns correspond with the experimental unit, and which column is the “factor” variable.

```
fake_wide_data1 <- reshape(fake_long_data1,
                           direction = "wide",
                           timevar = "timeObserved",
                           idvar = "person",
                           varying = c("before", "after")) # col names in new data
```

```
fake_long_data1
##      person timeObserved nums
## 1  Taylor           1   100
## 2  Taylor           2   101
## 3  Charlie          1   300
## 4  Charlie          2   301
fake_wide_data1
##      person before after
## 1  Taylor    100   101
## 3  Charlie   300   301
```

```
fake_wide_data2 <- reshape(fake_long_data2,
                           direction = "wide",
                           timevar = "attributeName", # timevar is kind of a misnomer
                           idvar = "person",
                           varying = c("attribute A", "attribute B"))
```

```
fake_long_data2
##      person attributeName nums
## 1  Taylor           attrA   100
## 2  Taylor           attrB   101
## 3  Charlie          attrA   300
## 4  Charlie          attrB   301
fake_wide_data2
##      person attribute A attribute B
## 1  Taylor           100           101
## 3  Charlie          300           301
```

reshape will also go in the other direction: it can take wide data and convert it into long data

```
reshape(fake_wide_data1,
        direction = "long",
        idvar = "person",
        varying = list(c("before","after")),
        v.names = "nums")
##           person time nums
## Taylor.1  Taylor    1  100
## Charlie.1 Charlie    1  300
## Taylor.2  Taylor    2  101
## Charlie.2 Charlie    2  301
fake_long_data1
##   person timeObserved nums
## 1 Taylor          1  100
## 2 Taylor          2  101
## 3 Charlie         1  300
## 4 Charlie         2  301
reshape(fake_wide_data2,
        direction = "long",
        idvar = "person",
        varying = list(c("attribute A","attribute B")),
        v.names = "nums")
##           person time nums
## Taylor.1  Taylor    1  100
## Charlie.1 Charlie    1  300
## Taylor.2  Taylor    2  101
## Charlie.2 Charlie    2  301
fake_long_data2
##   person attributeName nums
## 1 Taylor          attrA  100
## 2 Taylor          attrB  101
## 3 Charlie         attrA  300
## 4 Charlie         attrB  301
```

0.49.2 Long Versus Wide in Python

With pandas, we can take make wide data long with `pd.DataFrame.pivot`¹⁰⁷, and we can go in the other direction with `pd.DataFrame.melt`¹⁰⁸.

When going from wide to long, make sure to use the `pd.DataFrame.reset_index()`¹⁰⁹ method afterwards to reshape the data and remove the index. Here is an example similar to the one above.

```
import pandas as pd
fake_long_data1 = pd.DataFrame({'person' : ["Taylor","Taylor","Charlie","Charlie"],
                                'time_observed' : [1, 2, 1, 2],
                                'nums' : [100,101,300,301]})

fake_long_data1
##      person  time_observed  nums
## 0   Taylor              1   100
## 1   Taylor              2   101
## 2  Charlie              1   300
## 3  Charlie              2   301
pivot_data1 = fake_long_data1.pivot(index='person', columns='time_observed', values='nums')
pivot_data1
## time_observed      1      2
## person
## Charlie          300   301
## Taylor           100   101
fake_wide_data1 = pivot_data1.reset_index()
fake_wide_data1
## time_observed  person      1      2
```

¹⁰⁷<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.pivot.html#>

¹⁰⁸<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.melt.html?highlight=melt>

¹⁰⁹https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.reset_index.html#

```
## 0          Charlie  300  301
## 1          Taylor  100  101
```

Here's one more example showing the same functionality—going from wide to long format.

```
fake_long_data2 = pd.DataFrame({'person' : ["Taylor","Taylor","Charlie","Charlie"],
                                'attribute_name' : ['attrA', 'attrB', 'attrA', 'attrB'],
                                'nums' : [100,101,300,301]})
fake_wide_data2 = fake_long_data2.pivot(index='person',
                                         columns='attribute_name',
                                         values='nums').reset_index()

fake_wide_data2
## attribute_name  person  attrA  attrB
## 0          Charlie    300    301
## 1          Taylor    100    101
```

Here are some examples of going in the other direction: from wide to long with `pd.DataFrame.melt`¹¹⁰. The first example specifies value columns by integers.

```
fake_wide_data1
## time_observed  person    1    2
## 0          Charlie    300    301
## 1          Taylor    100    101
fake_wide_data1.melt(id_vars = "person", value_vars = [1,2])
##      person time_observed  value
## 0  Charlie            1    300
## 1  Taylor            1    100
## 2  Charlie            2    301
## 3  Taylor            2    101
```

The second example uses strings to specify value columns.

¹¹⁰<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.melt.html?highlight=melt>

clx

Reshaping and Combining Data Sets

```
fake_wide_data2
## attribute_name person attrA attrB
## 0             Charlie    300    301
## 1             Taylor     100    101
fake_wide_data2.melt(id_vars = "person", value_vars = ['attrA','attrB'])
##      person attribute_name value
## 0  Charlie             attrA    300
## 1  Taylor             attrA    100
## 2  Charlie             attrB    301
## 3  Taylor             attrB    101
```


0

Visualization

I describe a few plotting paradigms in R and Python below. Note that these descriptions are extremely thin. More depth could easily turn any of these subsections into an entire textbook!

0.50 Base R Plotting

R comes with some built-in functions `plot`, `hist`, `boxplot`, etc. Many of these reside in `package:graphics`, which comes pre-loaded into the search path. `plot` on the other hand, is higher up the search path in `package:base`—it is a generic method whose methods might be in `package:graphics` or some place else.

Base plotting covers most needs, so that’s what we spend most time with. However, there are a large number of third-party libraries for plotting that you might consider looking into if you want to follow a certain aesthetic, or if you want plotting specialized for certain cases (e.g. geospatial plots).

Recall our Albemarle Real Estate data set.

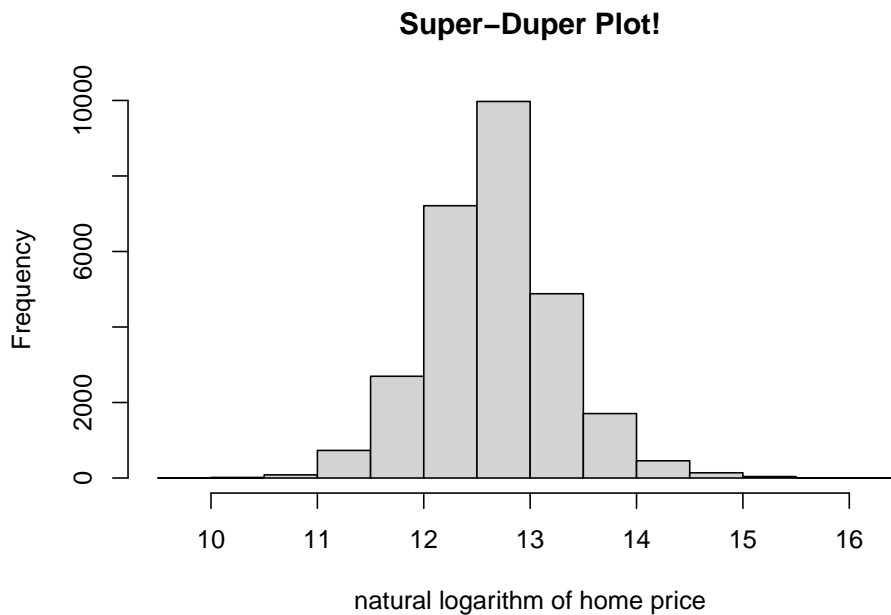
```
df <- read.csv("data/albemarle_real_estate.csv")
head(df)
```

##	<i>YearBuilt</i>	<i>YearRemodeled</i>	<i>Condition</i>	<i>NumStories</i>	<i>FinSqFt</i>	<i>Bedroom</i>	<i>FullBath</i>	<i>HalfBat</i>
## 1	2006	0	Average	1.00	1922	3	3	
## 2	2003	0	Average	1.00	1848	3	2	
## 3	1972	0	Average	1.00	1248	2	1	

## 4	1998	0	Good	1.00	1244	1	1
## 5	1886	0	Average	1.86	1861	4	1
## 6	1910	0	Fair	1.53	1108	3	1
##	TotalValue	City					
## 1	409900	CROZET					
## 2	523100	CROZET					
## 3	180900	EARLYSVILLE					
## 4	620700	CROZET					
## 5	162500	CROZET					
## 6	167200	CROZET					

If we wanted to get a general idea of how expensive homes were in Albemarle County, we could use a histogram. This helps us visualize a univariate numerical variable/column. Below I plot the (natural) logarithm of home prices.

```
hist(log(df$TotalValue),
      xlab = "natural logarithm of home price", main = "Super-Duper Plot!")
```

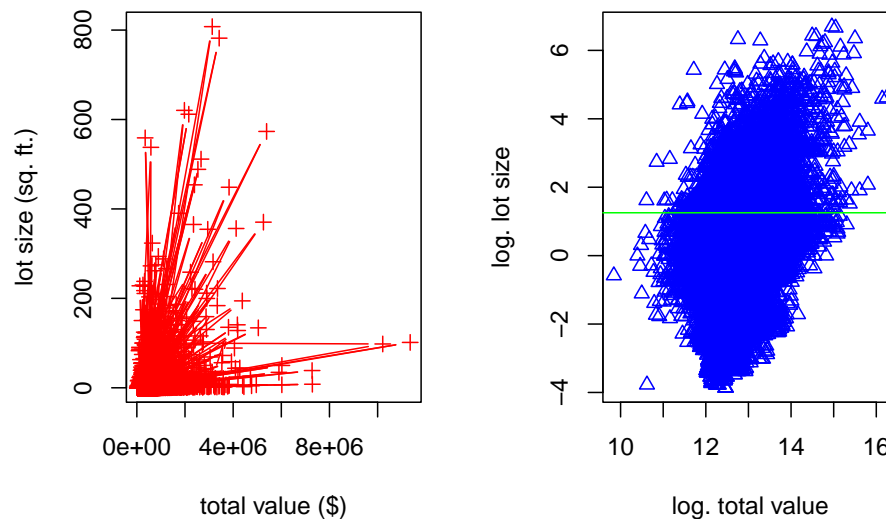


I specified the `xlab=` and `main=` arguments, but there are many

more that could be tweaked. Make sure to skim the options in the documentation (`?hist`).

`plot` is useful for plotting two univariate numerical variables. This can be done in time series plots (variable versus time) and scatter plots (one variable versus another).

```
par(mfrow=c(1,2))
plot(df$TotalValue, df$LotSize,
     xlab = "total value ($)", ylab = "lot size (sq. ft.)",
     pch = 3, col = "red", type = "b")
plot(log(df$TotalValue), log(df$LotSize),
     xlab = "log. total value", ylab = "log. lot size",
     pch = 2, col = "blue", type = "p")
abline(h = log(mean(df$LotSize)), col = "green")
```



```
par(mfrow=c(1,1))
```

I use some of the many arguments available (type `?plot`). `xlab=` and `ylab=` specify the x- and y-axis labels, respectively. `col=` is short for “color.” `pch=` is short for “point character.” Changing this will change the symbol shapes used for each point. `type=` is more

general than that, but it is related. I typically use it to specify whether or not I want the points connected with lines.

I also use a couple other functions. `abline` is used to superimpose lines over the top of a plot. They can be horizontal, vertical, or you can specify them in slope-intercept form, or by providing a linear model object. I also used `par` to set a graphical parameter. The graphical parameter `par()$mfrow` sets the layout of a multiple plot visualization. I then set it back to the standard 1×1 layout afterwards.

0.51 Plotting with `ggplot2`

`ggplot2`¹¹¹ is a popular third-party visualization package for R. There are also libraries in Python (e.g. `plotnine`¹¹²) that look and feel quite similar. This subsection provides a short tutorial on how to use `ggplot2` in R, and it is primarily based off of the material provided in (Wickham, 2016). An online version of this text is provided here¹¹³.

`ggplot2` code looks a lot different than the code in the above section¹¹⁴. There, we would write a series of function calls, and each would change some state in the current figure. Here, we call different `ggplot2` functions that create S3 objects with special behavior (more information about S3 objects in subsection 0.54.2), and then we “add” (i.e. we use the `+` operator) them together.

This new design is not to encourage you to think about S3 object-oriented systems. Rather, it is to get you thinking about making visualizations using the “grammar of graphics” (Wilkinson, 2005).

¹¹¹<https://ggplot2.tidyverse.org/index.html>

¹¹²<https://plotnine.readthedocs.io/en/stable/#>

¹¹³<https://ggplot2-book.org>

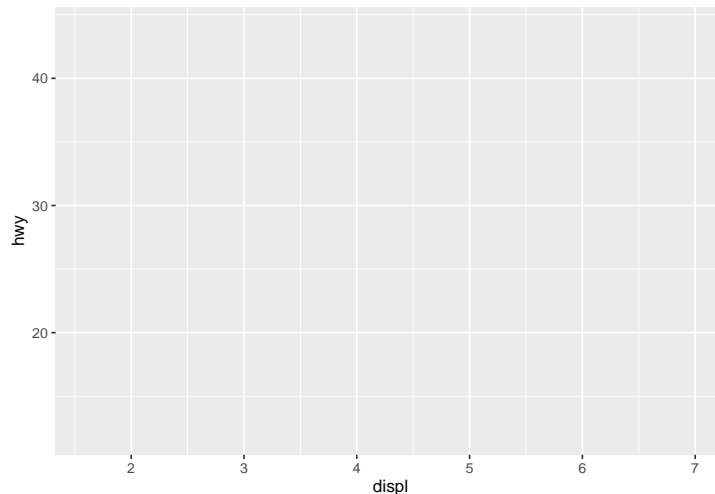
¹¹⁴Personally, I find its syntax more confusing, and so I tend to prefer base graphics. However, it is popular at the moment, and so I do believe that it is important to mention here in this text.

ggplot2 makes use of its own specialized vocabulary that is taken from this book. As we get started, I will try to introduce some of this vocabulary slowly.

The core function is the `ggplot` function¹¹⁵. This is the function that figures are initialized with; it is the function that will take in information about *which* data set you want to plot, and *how* you want to plot it. The raw data is provided in the first argument. The second argument, `mapping=`, is more confusing. The argument should be constructed with the `aes` function. In the parlance of ggplot2, `aes` constructs an **aesthetic mapping**. Think of the “aesthetic mapping” as stored information that can be used later on—it “maps” data to visual properties of a figure.

Consider this first example.

```
library(ggplot2)
ggplot(mpg, aes(x = displ, y = hwy))
```



You’ll notice a few things about the code and the result produced:

1. No geometric shapes show up!

¹¹⁵<https://www.rdocumentation.org/packages/ggplot2/versions/3.3.5/topics/ggplot>

2. A Cartesian coordinate system is displayed, and the x-axis and y-axis were created based on aesthetic mapping provided (confirm this by typing `summary(mpg$displ)` and `summary(mpg$hwy)`).
3. The axis labels are taken from the column names provided to `aes`.

To plot geometric shapes (*geoms* in the parlance of `ggplot2`), we need to add **layers**¹¹⁶ to it. “Layers” is quite a broad term—it does not only apply to geometric objects. In fact, in `ggplot2`, a layer can be pretty much anything: raw data, summarized data, transformed data, annotations, etc. However, the functions that add geometric object layers usually start with the prefix `geom_`. In RStudio, after loading `ggplot2`, type `geom_`, and then press <Tab> (autocomplete) to see some of the options.

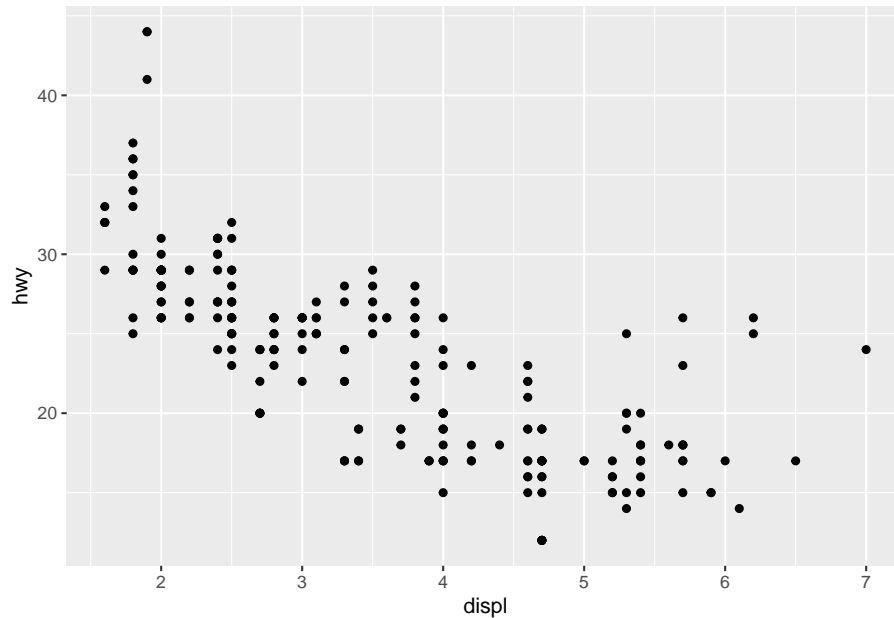
Consider the function `geom_point`¹¹⁷. It too returns an S3 instance that has specialized behavior. In the parlance of `ggplot2`, it adds a scatterplot¹¹⁸ layer to the figure.

```
library(ggplot2)
ggplot(mpg, aes(x = displ, y = hwy)) +
  geom_point()
```

¹¹⁶<https://ggplot2-book.org/toolbox.html#toolbox>

¹¹⁷https://www.rdocumentation.org/packages/ggplot2/versions/3.3.5/topics/geom_point

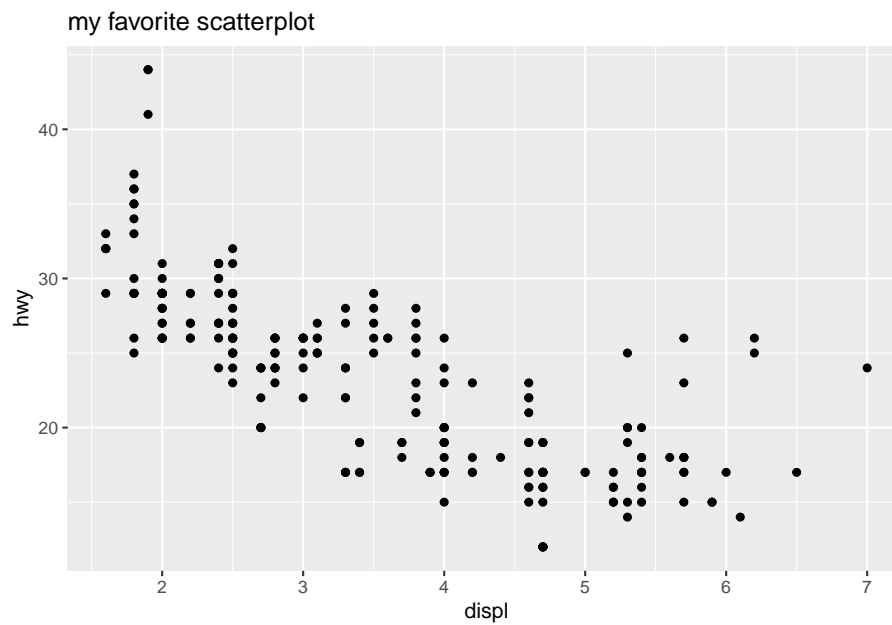
¹¹⁸<https://ggplot2-book.org/getting-started.html#basic-use>



Notice that we did not need to provide any arguments to `geom_point`. The aesthetic mappings were used by the new layer.

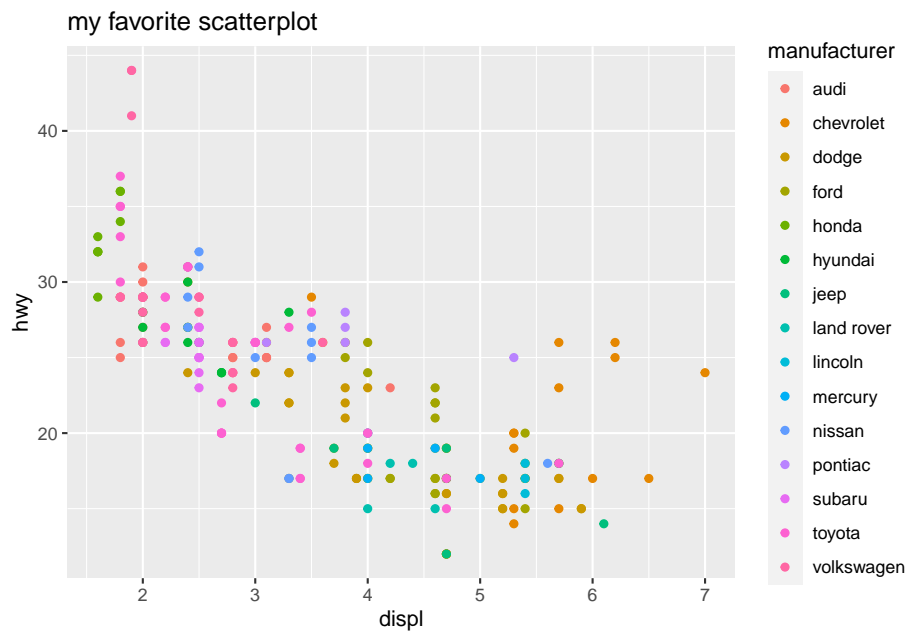
There are *many* types of layers that you can add to a plot, and you're not limited to any number of them in a given plot. For example, if we wanted to add a title, we could use the `ggtitle` function to add a title layer. Unlike `geom_point`, this function will need to take an argument because the desired title is not stored as an aesthetic mapping.

```
ggplot(mpg, aes(x = displ, y = hwy)) +  
  geom_point() +  
  ggtitle("my favorite scatterplot")
```



Additionally, notice that the same layer will behave much differently if we change the aesthetic mapping.

```
ggplot(mpg, aes(x = displ, y = hwy, color = manufacturer)) +  
  geom_point() +  
  ggtitle("my favorite scatterplot")
```

If we want tighter control on the aesthetic mapping, we can use **scales**¹¹⁹. Syntactically, these are things we “add” (+) to the figure, just like layers. However, these scales are constructed with a different set of functions, many of which start with the prefix `scale_`.

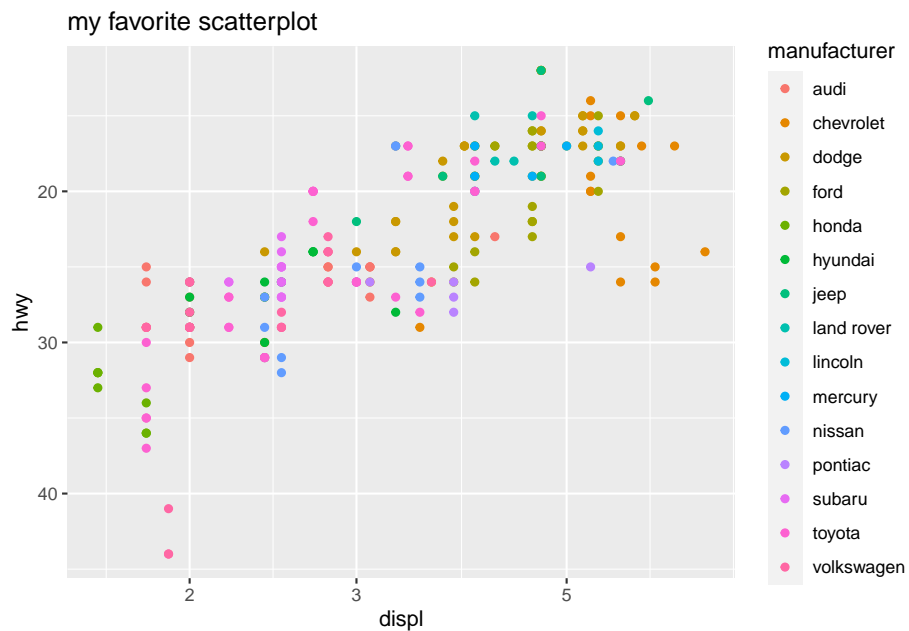
We can change attributes of the axes like this.

```
base_plot <- ggplot(mpg, aes(x = displ, y = hwy, color = manufacturer)) +
  geom_point() +
  ggtitle("my favorite scatterplot")
base_plot + scale_x_log10() + scale_y_reverse()
```

¹¹⁹<https://ggplot2-book.org/scales.html#scales>

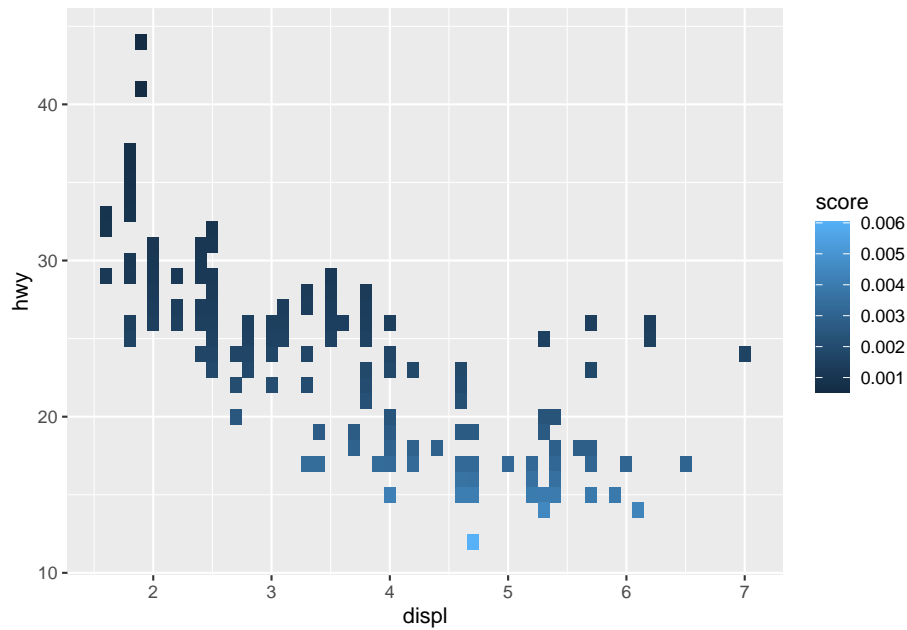
clxx

Visualization



We can also change plot colors with scale layers. Let's add an aesthetic called `fill` so we can use colors to denote the value of a numerical (not categorical) column. This data set doesn't have any more unused numerical columns, so let's create a new one called `score`. We also use a new geom layer from a function called `geom_tile()`.

```
mpg$score <- 1/(mpg$displ^2 + mpg$hwy^2)
ggplot(mpg, aes(x = displ, y = hwy, fill = score)) +
  geom_tile()
```

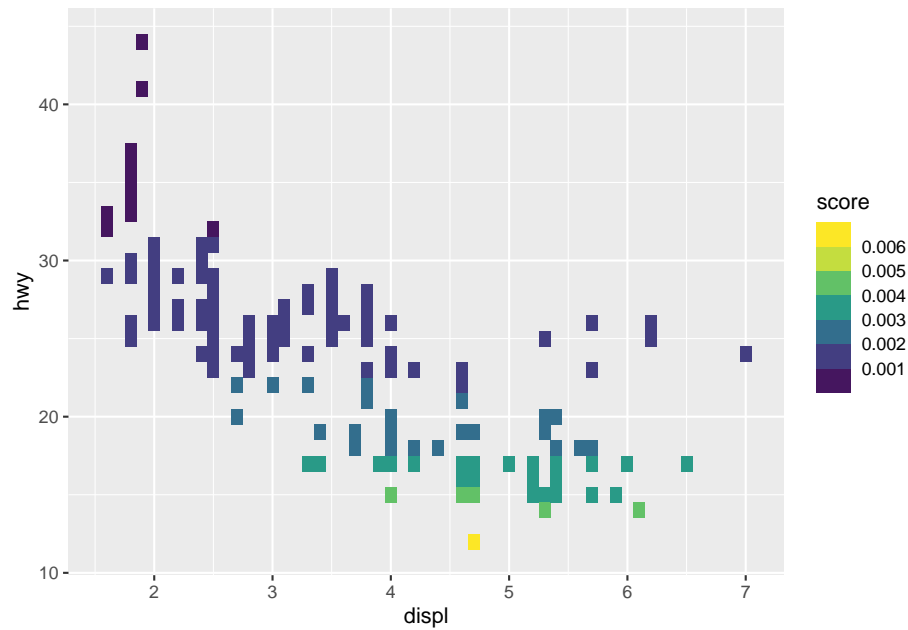


If we didn't like these colors, we could change them with a scale layer. Personally, I like this one.

```
mpg$score <- 1/(mpg$displ^2 + mpg$hwy^2)
ggplot(mpg, aes(x = displ, y = hwy, fill = score )) +
  geom_tile() +
  scale_fill_viridis_b()
```

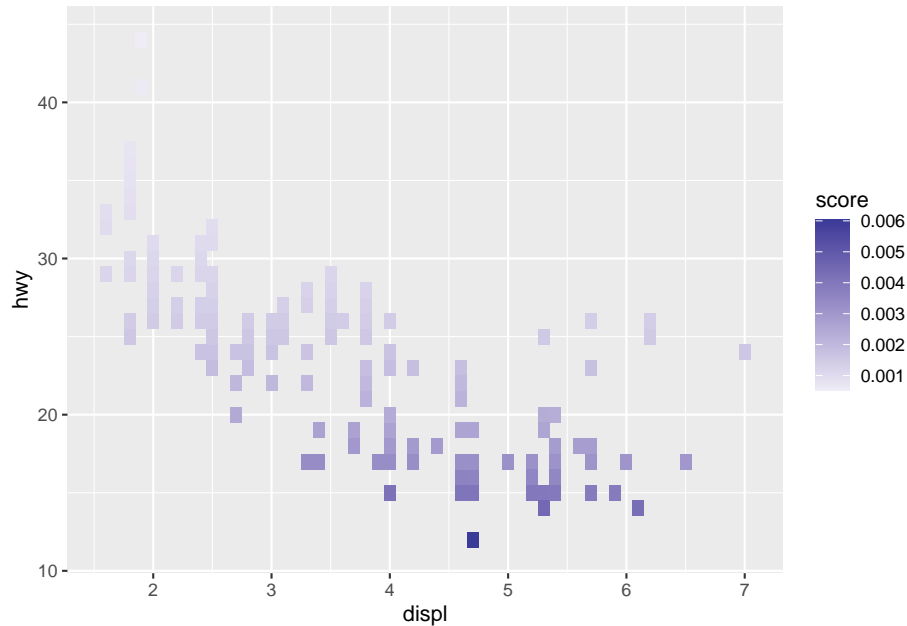
clxxii

Visualization



There are many to choose from, though. Here's another one.

```
mpg$score <- 1/(mpg$displ^2 + mpg$hwy^2)
ggplot(mpg, aes(x = displ, y = hwy, fill = score )) +
  geom_tile() +
  scale_fill_gradient2()
```



0.52 Plotting with Matplotlib

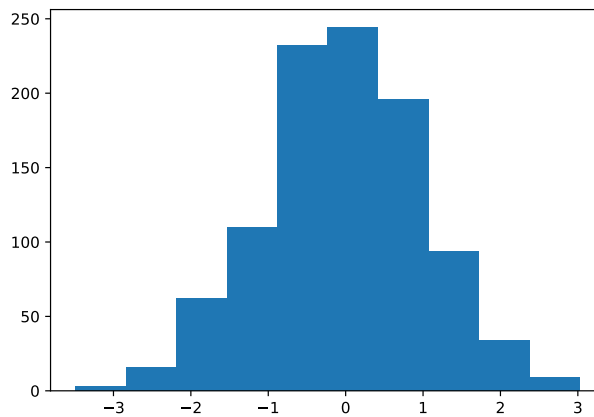
Matplotlib (Hunter, 2007) is a third-party visualization library in Python. It’s the oldest and most heavily-used, so it’s the best way to start making graphics in Python, in my humble opinion. It also comes installed with Anaconda. This short introduction borrows heavily from the myriad of tutorials¹²⁰ on Matplotlib’s website. I will start off making a simple plot, and commenting on each line of code.

You can use either “pyplot-style” (e.g. `plt.plot()`) or “object-oriented-style” to make figures in Matplotlib. Even though using the first type is faster to make simple plots, I will only describe the second one. It is the recommended approach because it is more extensible. However, the first one resembles the syntax of MATLAB.

¹²⁰<https://matplotlib.org/stable/tutorials/index.html>

If you're familiar with MATLAB, you might consider learning a little about the first style, as well.

```
import matplotlib.pyplot as plt      # 1
import numpy as np                   # 2
fig, ax = plt.subplots()             # 3
ax.hist(np.random.normal(size=1000)) # 4
## (array([ 3., 16., 62., 110., 232., 244., 196., 94., 34., 9.]), array([-3.
##      -0.23234771,  0.4186806 ,  1.06970891,  1.72073721,  2.37176552,
##      3.02279383]), <a list of 10 Patch objects>)
```



In the first line, we import the `pyplot` submodule of `matplotlib`. We rename it to `plt`, which is short, and will save us some typing. It also follows the most commonly-used convention.

Second, we import Numpy in the same way we always have. Matplotlib is written to work with Numpy arrays. If you want to plot some data, and it isn't in a Numpy array, you should convert it first.

Third, we call the `subplots` function, and use *sequence unpacking* to unpack the returned container into individual objects without storing the overall container. “Subplots” sounds like it will make many different plots all on one figure, but if you look at the docu-

mentation¹²¹ the number of rows and columns defaults to one and one, respectively.

`plt.subplots` returns a tuple¹²²¹²³ of two things: a `Figure` object, and one or more `Axes` object(s). These two classes will require some explanation.

1. A `Figure` object¹²⁴ is the overall visualization object you're making. It holds onto all of the plot elements. If you want to save all of your progress (e.g. with `fig.savefig('my_picture.png')`), you're saving the overall `Figure` object.
2. One or more `Axes` objects¹²⁵ are contained in a `Figure` object. Each is "what you think of as 'a plot'¹²⁶." They hold onto two `Axis` objects (in the case of 2-dimensional plots) or three (in the case of 3-dimensional arguments). We are usually calling the methods of these objects to effect changes on a plot.

In line four, we call the `hist()` method¹²⁷ of the `Axes` object called `ax`. There are many more plots available than plain histograms. Each one has its own method, and you can peruse the options in the documentation¹²⁸.

¹²¹https://matplotlib.org/stable/api/_as_gen/matplotlib.pyplot.subplots.html#matplotlib-pyplot-subplots

¹²²<https://docs.python.org/3.3/library/stdtypes.html?highlight=tuple#tuple>

¹²³We didn't talk about tuples in chapter 2, but you can think of them as being similar to lists. They are containers that can hold elements of different types. There are a few key differences, though: they are made with parentheses (e.g. `('a')`) instead of square brackets, and they are immutable instead of mutable.

¹²⁴https://matplotlib.org/stable/api/figure_api.html#matplotlib.figure.Figure

¹²⁵https://matplotlib.org/stable/api/axes_api.html#the-axes-class

¹²⁶<https://matplotlib.org/stable/tutorials/introductory/usage.html#axes>

¹²⁷https://matplotlib.org/stable/api/_as_gen/matplotlib.axes.Axes.hist.html#matplotlib.axes.Axes.hist

¹²⁸https://matplotlib.org/stable/api/axes_api.html#plotting

If you want to make figures more elaborate, just keep calling different methods of `ax`. If you want to fit more subplots to the same figure, add more Axes objects. Here is an example using some code from one of the official Matplotlib tutorials¹²⁹.

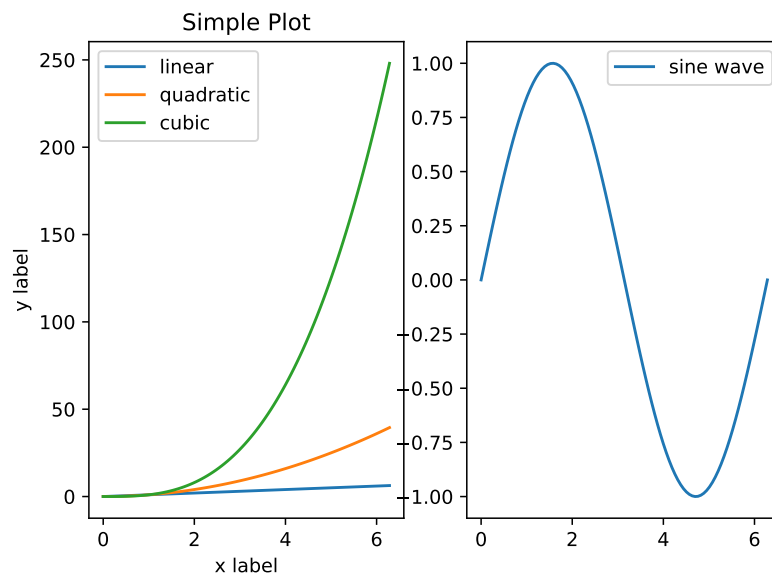
```
x = np.linspace(0, 2*np.pi, 100) # x values grid shared by both subplots

# create two subplots...one row two columns
fig, myAxes = plt.subplots(1, 2) # kind of like par(mfrow=c(1,2)) in R

# first subplot
myAxes[0].plot(x, x, label='linear') # Plot some data on the axes.
myAxes[0].plot(x, x**2, label='quadratic') # Plot more data on the axes...
myAxes[0].plot(x, x**3, label='cubic') # ... and some more.
myAxes[0].set_xlabel('x label') # Add an x-label to the axes.
myAxes[0].set_ylabel('y label') # Add a y-label to the axes.
myAxes[0].set_title("Simple Plot") # Add a title to the axes.
myAxes[0].legend() # Add a legend.

# second subplot
myAxes[1].plot(x, np.sin(x), label='sine wave')
myAxes[1].legend()
```

¹²⁹<https://matplotlib.org/stable/tutorials/introductory/usage.html#the-object-oriented-interface-and-the-pyplot-interface>



```
import numpy as np my_inputs = np.linspace(start = 0, stop = 2*np.pi) outputs = np.sin(my_inputs)
```

```
import matplotlib.pyplot as plt plt.plot(my_inputs, outputs)
```

very good! <https://jakevdp.github.io/PythonDataScienceHandbook/04.12-three-dimensional-plotting.html>



0

Working With Text Data

TODO

- regular expressions



0

Dates and Times

TODO



0

Running Scripts from the Command Line

TODO





Part IV

Part 3: Programming Styles



0

An Introduction to Object-Oriented Programming

Object-Oriented Programming (OOP) is a way of thinking about how to organize programs. This way of thinking focuses on objects. In the next chapter, we focus on organizing programs by functions, but for now we stick to objects. We already know about objects from the last chapter, so what's new here?

The difference is that we're creating our own *types* now. In the last chapter we learned about built-in types: floating point numbers, lists, arrays, functions, etc. Now we will discuss broadly how one can create his own types in both R and Python. These user-defined types can be used as cookie cutters. Once we have the cookie cutter, we can make as many cookies as we want!

TODO: image of cookie cutter

We will not go into this too deeply, but it is important to know how code works so that we can use it more effectively. For instance, in Python, we frequently write code like `my_data_frame.doSomething()`. The material in this chapter will go a long way to describe how we can make our own types with custom behavior.

Here are a few abstract concepts that will help thinking about OOP. They are not mutually exclusive, and they aren't unique to OOP, but understanding these words will help you understand the purpose of OOP. Later on, when we start looking at code examples, I will alert you to when these concepts are coming into play.

- **Composition** refers to the idea when one type of object *contains*

an object of another type. For example, a linear model object could hold onto estimated regression coefficients, residuals, etc.

- **Inheritance** takes place when an object can be considered to be of another type(s). For example, an analysis of variance linear regression model might be a special case of a general linear model.
- **Polymorphism** is the idea that the programmer can use the same code on objects of different types. For example, built-in functions in both R and Python can work on arguments of a wide variety of different types.
- **Encapsulation** is another word for complexity hiding. Do you have to understand every line of code in a package you're using? No, because a lot of details are purposefully hidden from you.
- **Modularity** is an idea related to encapsulation—it means splitting something into independent pieces. How you split code into different files, different functions, different classes—all of that has to do with modularity. It promotes encapsulation, and it allows you to think about only a few lines of code at a time.
- The **interface**, between you and the code you're using, describes *what* can happen, but not *how* it happens. In other words, it describes some functionality so that you can decide whether you want to use it, but there are not enough details for you to make it work yourself. For example, all you have to do to be able to estimate a complicated statistical model is to look up some documentation.¹³⁰ In other words, you only need to be familiar with the interface, not the implementation.
- The **implementation** of some code you're using describes *how* it works in detail. If you are a package author, you can change your code's implementation “behind the scenes” and ideally, your end-users would never notice.

¹³⁰Just because you can do this, doesn't mean you *should*, though!

0.53 OOP In Python

0.53.1 Overview

In Python, classes¹³¹ are user-defined types. When you define your own class, you describe what kind of information it holds onto, and how it behaves.

To define your own type, use the `class` keyword¹³². Objects created with a user-defined class are sometimes called **instances**. They behave according to the rules written in the class definition—they always have data and/or functions bundled together in the same way, but these instances do not all have the same data.

To be more clear, classes may have the following two things in their definition.

- **Attributes** are pieces of data “owned” by an instance created by the class.
- **(Instance) methods** are functions “owned” by an instance created by the class. They can use and/or modify data belonging to the class.

0.53.2 A First Example

Here’s a simple example. Say we are interested in calculating, from numerical data x_1, \dots, x_n , a sample mean:

$$\bar{x}_n = \frac{\sum_{i=1}^n x_i}{n}.$$

In Python, we can usually calculate this one number very easily using `np.average`. However, this function requires that we pass into it all of the data at once. What if we don’t have all the data

¹³¹<https://docs.python.org/3/tutorial/classes.html>

¹³²<https://docs.python.org/3/tutorial/classes.html#class-definition-syntax>

at any given time? In other words, suppose that the data arrive intermittently. We might consider taking advantage of a recursive formula for the sample means.

$$\bar{x}_n = \frac{(n-1)\bar{x}_{n-1} + x_n}{n}$$

How would we program this in Python? A first option: we might create a variable `my_running_ave`, and after every data point arrives, we could

```
my_running_ave = 1.0
my_running_ave
## 1.0
my_running_ave = ((2-1)*my_running_ave + 3.0)/2
my_running_ave
## 2.0
my_running_ave = ((3-1)*my_running_ave + 2.0)/3
my_running_ave
## 2.0
```

There are a few problems with this. Every time we add a data point, the formula slightly changes. Every time we update the average, we have to write a different line of code. This opens up the possibility for more bugs, and it makes your code less likely to be used by other people and more difficult to understand. And if we were trying to code up something more complicated than a running average? That would make matters even worse.

A second option: write a class that holds onto the running average, and that has

1. an `update` method that updates the running average every time a new data point is received, and
2. a `get_current_xbar` method that gets the most up-to-date information for us.

Using our code would look like this:

```
my_ave = RunningMean() # create running average object
my_ave.get_current_xbar() # no data yet!
my_ave.update(1.) # first data point
my_ave.get_current_xbar() # xbar_1
## 1.0
my_ave.update(3.) # second data point
my_ave.get_current_xbar() # xbar_2
## 2.0
my_ave.n # my_ave.n instead of self.n
## 2
```

There is a Python convention that stipulates class names should be written in *UpperCamelCase* (e.g. *RunningMean*).

That's much better! Notice the *encapsulation*. Looking at this code we don't need to think about the mathematical formula and the data being received. We only need to think about the latter. In other words, the *implementation* is separated from the *interface*. The interface in this case, is just the name of the class methods, and the arguments they expect. That's all we need to know about to use this code.

Classes (obviously) need to be defined before they are used, so here is the definition of our class.

```
class RunningMean:
    """Updates a running average"""
    def __init__(self):
        self.current_xbar = 0.0
        self.n = 0
    def update(self, new_x):
        self.n += 1
        self.current_xbar = (self.current_xbar*(self.n - 1) + new_x) / self.n
    def get_current_xbar(self):
        if self.n == 0:
            return None
```

```
else:  
    return self.current_xbar
```

Methods that look like `__init__`, or that possess names that begin and end with two underscores, are called **dunder (double underscore) methods**, **special methods** or **magic methods**. There are many that you can take advantage of! For more information see this¹³³.

Here are the details of the class definition:

1. Defining class methods looks exactly like defining functions! The primary difference is that the first argument must be `self`. If the definition of a method refers to `self`, then this allows the class instance to refer to its own (heretofore undefined) data attributes. Also, these method definitions are indented inside the definition of the class.
2. This class owns two data attributes. One to represent the number of data points seen up to now (`n`), and another to represent the current running average (`current_xbar`).
3. Referring to data members requires dot notation. `self.n` refers to the `n` belonging to any instance. This data attribute is free to vary between all the objects instantiated by this class.
4. The `__init__` method performs the setup operations that are performed every time any object is instantiated.
5. The `update` method provides the core functionality using the recursive formula displayed above.
6. `get_current_xbar` simply returns the current average. In the case that this function is called before any data has been seen, it returns `None`.

¹³³<https://docs.python.org/3/reference/datamodel.html#special-method-names>

A few things you might find interesting:

- i. Computationally, there is never any requirement that we must hold *all* of the data points in memory. Our data set could be infinitely large, and our class will hold onto only one floating point number, and one integer.
- ii. This example is generalizable to other statistical methods. In a mathematical statistics course, you will learn about a large class of models having *sufficient statistics*. Most sufficient statistics have recursive formulas like the one above. Second, many algorithms in *time series analysis* have recursive formulas and are often needed to analyze large streams of data. They can all be wrapped into a class in a way that is similar to the above example.

0.53.3 Adding Inheritance

How can we use inheritance in statistical programming? A primary benefit of inheritance is code re-use, so one example of inheritance is writing a generic algorithm as a base class, and a specific algorithm as a class that inherits from the base class. For example, we could re-use the code in the `RunningMean` class in a variety of other classes.

Let's make some assumptions about a *parametric model* that is generating our data. Suppose I assume that the data points x_1, \dots, x_n are a “random sample”¹³⁴ from a normal distribution with mean μ and variance $\sigma^2 = 1$. μ is assumed to be unknown (this is, after all, and interval for μ), and σ^2 is assumed to be known, for simplicity.

A 95% confidence interval for the true unknown population mean μ is

$$\left[\bar{x} - 1.96\sqrt{\frac{\sigma^2}{n}}, \bar{x} + 1.96\sqrt{\frac{\sigma^2}{n}} \right].$$

The width of the interval shrinks as we get more data (as $n \rightarrow \infty$).

¹³⁴Otherwise known as an independent and identically distributed sample

We can write another class that, not only calculates the center of this interval, \bar{x} , but also returns the interval endpoints.

If we wrote another class from scratch, then we would need to rewrite a lot of the code that we already have in the definition of `RunningMean`. Instead, we'll use the idea of *inheritance*¹³⁵.

```
import numpy as np
class RunningCI(RunningMean):
    """Updates a running average and gives you a known-variance confidence interval"""
    def __init__(self, known_var):
        super().__init__()
        self.known_var = known_var
    def get_current_interval(self):
        if self.n == 0:
            return None
        else:
            half_width = 1.96 * np.sqrt(self.known_var / self.n)
            return np.array([self.current_xbar - half_width, self.current_xbar + half_width])
```

The parentheses in the first line of the class definition signal that this new class definition is inheriting from `RunningMean`. Inside the definition of this new class, when I refer to `self.current_xbar` Python knows what I'm referring to because it is defined in the base class. Last, I am using `super()` to access the base class's methods, such as `__init__`.

```
my_ci = RunningCI(1) # create running average object
my_ci.get_current_xbar() # no data yet!
my_ci.update(1.)
my_ci.get_current_interval()
## array([-0.96,  2.96])
my_ci.update(3.)
my_ci.get_current_interval()
## array([0.61407071,  3.38592929])
```

¹³⁵<https://docs.python.org/3/tutorial/classes.html#inheritance>

This example also demonstrates **polymorphism**. Polymorphism comes from the Greek for “many forms.” “Forms” means “type” or “class” in this case. If the same code (usually a function or method) works on objects of different types, that’s polymorphic. Here, the `update` method worked on an object of class `RunningCI`, as well as an object of `RunningMean`.

Why is this useful? Consider this example.

```
for datum in time_series:
    for thing in obj_list:
        thing.update(xt)
```

Inside the inner `for` loop, there is no need to include conditional logic that tests for what kind of type each `thing` is. We can iterate through time more succinctly.

```
for datum in time_series:
    for thing in obj_list:
        if isinstance(thing, class1):
            thing.updatec1(xt)
        if isinstance(thing, class2):
            thing.updatec2(xt)
        if isinstance(thing, class3):
            thing.updatec3(xt)
        if isinstance(thing, class4):
            thing.updatec4(xt)
        if isinstance(thing, class5):
            thing.updatec5(xt)
        if isinstance(thing, class6):
            thing.updatec6(xt)
```

If, in the future, you add a new class called `class7`, then you need to change this inner `for` loop, as well as provide new code for the class.

0.53.4 Adding in Composition

Composition also enables code re-use. Inheritance ensures an “is a” relationship between base and derived classes, and composition promotes a “has a” relationship. Sometimes it can be tricky to decide which technique to use, especially when it comes to statistical programming.

Regarding the example above, you might argue that a confidence interval isn’t a particular type of a sample mean. Rather, it only *has a* sample mean. If you believe this, then you might opt for a composition based model instead. With composition, the derived class (the confidence interval class) will be decoupled from the base class (the sample mean class). This decoupling will have a few implications. In general, composition is more flexible, but can lead to longer, uglier code.

1. You will lose polymorphism.
2. Your code might become less re-usable.
 - You have to write any derive class methods you want because you don’t inherit any from the base class. For example, you won’t automatically get the `.update()` or the `.get_current_xbar()` method for free. This can be tedious if there are a lot of methods you want both classes to have that should work the same exact way for both classes. If there are, you would have to re-write a bunch of method definitions.
 - On the other hand, this could be good if you have methods that behave completely differently. Each method you write can have totally different behavior in the derived class, even if the method names are the same in both classes. For instance, `.update()` could mean something totally different in these two classes. Also, in the derive class, you can still call the base class’s `.update()` method.
3. Many-to-one relationships are easier. It’s generally easier

to “own” many base class instances rather than inherit from many base classes at once. This is especially true if this is the only book on programming you plan on reading—I completely avoid the topic of multiple inheritance!

Sometimes it is very difficult to choose between using composition or using inheritance. However, this choice should be made very carefully. If you make the wrong one, and realize too late, *refactoring* your code might be very time consuming!

Here is an example implementation of a confidence interval using composition. Notice that this class “owns” a `RunningMean` instance called `self.mean`. This is contrast with *inheriting* from the `RunningMean` class.

```
class RunningCI2:
    """Updates a running average and gives you a known-variance confidence interval"""
    def __init__(self, known_var):
        self.mean = RunningMean()
        self.known_var = known_var
    def update(self, new_x):
        self.mean.update(new_x)
    def get_current_interval(self):
        if self.n == 0:
            return None
        else:
            half_width = 1.96 * np.sqrt(self.known_var / self.n)
            return np.array([self.mean.get_current_xbar() - half_width, self.mean.get_cu
```

0.54 OOP In R

R, unlike Python, has many different kinds of classes. In R, there is not only one way to make a class. There are many! This list isn't exhaustive, but I will discuss

- S3 classes
- S4 classes
- Reference classes, and
- R6 classes.

If you like how Python does OOP, you will like reference classes and R6 classes, while S3 and S4 classes will feel strange to you.

It's best to learn about them chronologically, in my opinion. S3 classes came first, S4 classes sought to improve upon those. Reference classes rely on S4 classes, and R6 classes are an improved version of Reference classes.

TODO a picture of a wide variety of choices

0.54.1 S3 objects: The Big Picture

With S3 (and S4) objects, calling a method `print` will not look like this.

```
my_obj.print()
```

Instead, it will look like this:

```
print(my_obj)
```

The primary goal of S3 is *polymorphism*. We want functions like `print`, `summary` and `plot` to behave differently when objects of a different type are passed in to them. Printing a linear model should look a lot different than printing a data frame, right? So we can write code like the following, we only have to remember fewer functions as an end-user, and the “right” thing will always happen. If you're writing a package, it's also nice for your users that

they’re able to use the regular functions that they’re familiar with. For instance, I allow users of my package `cPseudoMaRg`¹³⁶ (Brown, 2021) to call `print` on objects of type `cpmResults`. In section 0.51, `ggplot2` instances, which are much more complicated than plain numeric vectors, are `+`ed together.

```
# print works on pretty much everything
print(myObj)
print(myObjOfADifferentClass)
print(aThirdClassObject)
```

This works because these “high-level” functions (like `print`), will look at its input and choose the most appropriate function to call, based on what kind of type the input has. `print` is the high-level function. When you run some of the above code, it might not be obvious which specific function `print` chooses for each input. You can’t see that happening, yet.

Last, recall that this discussion only applies to S3 objects. Not all objects are S3 objects, though. To find out if an object `x` is an S3 object, use `is.object(x)`.

0.54.2 Using S3 objects

Using S3 objects is so easy that you probably don’t even know that you’re actually using them. You can just try to call functions on objects, look at the output, and if you’re happy with it, you’re good. However, if you’ve ever asked yourself: “why does `print` (for another function) do different things all the time?” then this section will be useful for you to read.

TODO: picture of looking into one door but going down a lot of avenues

`print` is a **generic function**¹³⁷ which is a function that looks at

¹³⁶<https://cran.r-project.org/web/packages/cPseudoMaRg/index.html>

¹³⁷<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Method-dispatching>

the type of its first argument, and then calls another, more specialized function depending on what type that argument is. Not all functions in R are generic, but some are. In addition to `print`, `summary` and `plot` are the most ubiquitous generic functions. Generic functions are an *interface*, because the user does not need to concern himself with the details going on behind the scenes.

In R, a **method** is a specialized function that gets chosen by the generic function for a particular type of input. The method is the *implementation*. When the generic function chooses a particular method, this is called **method dispatch**.

If you look at the definition of a generic function, let's take `plot` for instance, it has a single line that calls `UseMethod`.

```
plot
```

```
## function (x, y, ...)
## UseMethod("plot")
## <bytecode: 0x55f51c399030>
## <environment: namespace:base>
```

`UseMethod` performs method dispatch. Which methods can be dispatched to? To see that, use the `methods` function.

```
methods(plot)
```

```
##      [1] plot,ANY-method                plot,color-
method      plot.aareg*
##  [4] plot.acf*                      plot.agnes*      plot.areg*
##  [7] plot.areg.boot*                plot.aregImpute* plot.biVar*
## [10] plot.clusGap*                  plot.cox.zph*    plot.curveRep*
## [13] plot.data.frame*              plot.decomposed.ts* plot.default
## [16] plot.dendrogram*              plot.density*    plot.describe*
## [19] plot.diana*                    plot.drawPlot*   plot.ecdf
## [22] plot.factor*                  plot.formula*    plot.function
## [25] plot.gbayes*                   plot.ggplot*     plot.gtable*
## [28] plot.hcl_palettes*            plot.hclust*     plot.histogram*
```



```
## [31] plot.HoltWinters*      plot.isoreg*          plot.lm*
## [34] plot.medpolish*       plot.mlm*             plot.mona*
## [37] plot.numpy.ndarray*   plot.partition*       plot.ppr*
## [40] plot.prcomp*          plot.princomp*        plot.profile.nls*
## [43] plot.Quantile2*       plot.R6*              plot.raster*
## [46] plot.rm.boot*         plot.rpart*           plot.shingle*
## [49] plot.silhouette*     plot.spec*            plot.spline*
## [52] plot.stepfun          plot.stl*             plot.summary.formula.respo
## [55] plot.summary.formula.reverse* plot.summaryM*         plot.summaryP*
## [58] plot.summaryS*        plot.Surv*            plot.survfit*
## [61] plot.table*          plot.trans*           plot.transcan*
## [64] plot.trellis*        plot.ts               plot.tskernel*
## [67] plot.TukeyHSD*       plot.varclus*         plot.xyVector*
## see '?methods' for accessing help and source code
```

All of these S3 class methods share the same naming convention. Their name has the generic function’s name as a prefix, then a dot (`.`), then the name of the class that they are specifically written to be used with.

R’s dot-notation is nothing like Python’s dot-notation! In R, functions do not *belong* to types/classes like they do in Python!

Method dispatch works by looking at the `class` attribute of an S3 object argument. An object in R may or may not have a set of **attributes**¹³⁸, which are a collection of name/value pairs that give a particular object extra functionality. Regular **vectors** in R don’t have attributes (e.g. try running `attributes(1:3)`), but objects that are “embellished” versions of a **vector** might (e.g. run `attributes(factor(1:3))`).

`class` will return misleading results if it’s called on an object that isn’t an S3 object. Make sure to check with `is.object` first.

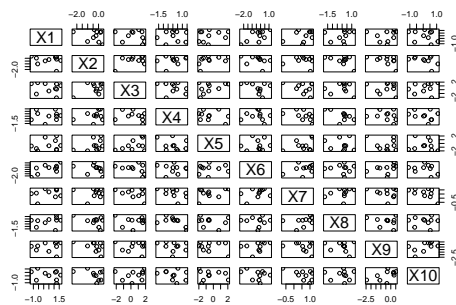
Also, these methods are not *encapsulated* inside a class definition like they are in Python, either. They just look like loose functions—the method definition for a particular class is not defined inside

¹³⁸<https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Attributes>

the class. These class methods can be defined just as ordinary functions, out on their own, in whatever file you think is appropriate to define functions in.

As an example, let's try to plot some specific objects.

```
aDF <- data.frame(matrix(rnorm(100), nrow = 10))
is.object(aDF) # is this s3?
## [1] TRUE
class(aDF)
## [1] "data.frame"
plot(aDF)
```



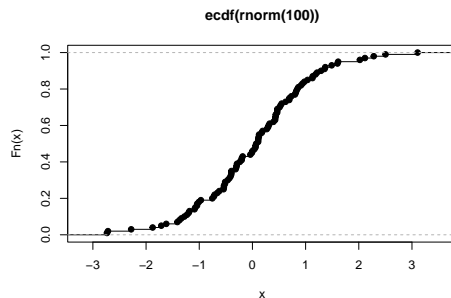
Because `aDF` has its `class` set to `data.frame`, this causes `plot` to try to find a `plot.data.frame` method. If this method was not found, R would attempt to find/use a `plot.default` method. If no default method existed, an error would be thrown.

As another example, we can play around with objects created with the `ecdf` function. This function computes an *empirical cumulative distribution function*, which takes a real number as an input, and outputs the proportion of observations that are less than or equal to that input¹³⁹

```
myECDF <- ecdf(rnorm(100))
is.object(myECDF)
## [1] TRUE
```

¹³⁹It's defined as $\hat{F}(x) = \frac{1}{n} \sum_{i=1}^n \mathbf{1}(X_i \leq x)$.

```
class(myECDF)
## [1] "ecdf"      "stepfun"    "function"
plot(myECDF)
```



This is how *inheritance* works in R. The `ecdf` class inherits from the `stepfun` class, which in turn inherits from the `function` class. When you call `plot(myECDF)`, ultimately `plot.ecdf` is used on this object. However, if `plot.ecdf` did not exist, `plot.stepfun` would be tried. S3 inheritance in R is much simpler than Python's inheritance!

0.54.3 Creating S3 objects

Creating an S3 object is very easy, and is a nice way to spruce up some bundled up object that you're returning from a function, say. All you have to do is tag an object by changing its class attribute. Just assign a character vector to it!

Here is an example of creating an object of `CoolClass`.

```
myThing <- 1:3
attributes(myThing)
## NULL
class(myThing) <- "CoolClass"
attributes(myThing) # also try class(myThing)
## $class
## [1] "CoolClass"
```

`myThing` is now an instance of `CoolClass`, even though I never defined what a `CoolClass` was ahead of time! If you're used to Python, this should seem very strange. Compared to Python, this approach is very flexible, but also, kind of dangerous, because you can change the classes of existing objects. You shouldn't do that, but you could if you wanted to.

After you start creating your own S3 objects, you can write your own methods associated with these objects. That way, when a user of your code uses typical generic functions, such as `summary`, on your S3 object, you can control what interesting things will happen to the user of your package. Here's an example.

```
summary(myThing)
## [1] "No summary available!"
## [1] "Cool Classes are too cool for summaries!"
## [1] ":",)
```

The `summary` method I wrote for this class is the following.

```
summary.CoolClass <- function(object,...){
  print("No summary available!")
  print("Cool Classes are too cool for summaries!")
  print(":",)
}
```

When writing this, I kept the signature the same as `summary`'s.

0.54.4 S4 objects: The Big Picture

S4 was developed after S3. If you look at your search path (type `search()`), you will see `package:methods`. That's where all the code you need to do S4 is.

Here are the similarities and differences between S3 and S4:

- they both use generic functions and methods work in the same way
- unlike in S3, S4 classes allow you to use multiple dispatch, which means the generic function can dispatch on multiple arguments, instead of just the first argument
- S4 class definitions are strict. They aren't just name tags like in S3.
- S4 inheritance feels more like Python's. You can think of a base class object living inside a child class object.
- S4 classes can have default data members via `prototypes`.

Much more information about S4 classes can be obtained by reading Chapter 15 in Hadley Wickham's book.¹⁴⁰

0.54.5 Using S4 objects

One CRAN package that uses S4 is the `Matrix` package.¹⁴¹ S4 objects are also extremely popular in packages hosted on Bioconductor¹⁴².

Bioconductor is kind of like CRAN, but its software has a much more specific focus on bioinformatics. To download packages from Bioconductor, you can check out the installation instructions provided here¹⁴³.

```
library(Matrix)
M <- Matrix(10 + 1:28, 4, 7)
isS4(M)
## [1] TRUE
M
## 4 x 7 Matrix of class "dgeMatrix"
```

¹⁴⁰<https://adv-r.hadley.nz/s4.html>

¹⁴¹<https://cran.r-project.org/web/packages/Matrix/vignettes/Intro2Matrix.pdf>

¹⁴²<https://www.bioconductor.org/>

¹⁴³<https://bioconductor.org/help/course-materials/2017/Zurich/S4-classes-and-methods.html>

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## [1,]  11  15  19  23  27  31  35
## [2,]  12  16  20  24  28  32  36
## [3,]  13  17  21  25  29  33  37
## [4,]  14  18  22  26  30  34  38
M@Dim
## [1] 4 7
```

Inside an S4 object, data members are called **slots**, and they are accessed with the `@` operator (instead of the `$` operator). Objects can be tested if they are S4 with the function `isS4`. Otherwise, they look and feel just like S3 objects.

0.54.6 Creating S4 objects

Here are the key takeaways

- create a new S4 class with `setClass`
- create a new S4 object with `new`
- S4 classes have a fixed amount of slots, a name, and a fixed inheritance structure

Let's do an example that resembles the example we did in Python, where we defined a `RunningMean` class and a `RunningCI` class.

```
setClass("RunningMean",
        slots = list(n = "integer",
                     currentXbar = "numeric"))
setClass("RunningCI",
        slots = list(knownVar = "numeric"),
        contains = "RunningMean")
```

Here, unlike in S3 class's, we actually have to define a class with `setClass`. In the parlance of S4, `slots` are a class' data members, and `contains` signals that one class inherits from another (even though it kind of sounds like *composition*).

New objects can be created with the `new` function after this is accomplished.

```
new("RunningMean", n = 0L, currentXbar = 0)
new("RunningCI", n = 0L, currentXbar = 0, knownVar = 1.0)
```

Let's set one of those up. To achieve we want this `update` method to be generic, and it will work on objects of type "RunningMean" and "RunningCI".

Next we want to define an `update` generic function that will work on objects of both types. This is what gives us *polymorphism*. The generic `update` will call specialized methods for objects of class "RunningMean" and "RunningCI".

Recall that in the Python example, each class had its own `update` method. Here, we still have a specialized method for each class, but S4 methods don't have to be defined inside the class definition, as we can see below.

```
setGeneric("update", function(oldMean, newNum) {
  standardGeneric("update")
})
## [1] "update"
setMethod("update",
  c(oldMean = "RunningMean", newNum = "numeric"),
  function(oldMean, newNum) {
    oldN <- oldMean@n
    oldAve <- oldMean@currentXbar
    newAve <- (oldAve*oldN + newNum)/(oldN + 1)
    newN <- oldN + 1L
    return(new("RunningMean", n = newN, currentXbar = newAve))
  }
)
setMethod("update",
  c(oldMean = "RunningCI", newNum = "numeric"),
  function(oldMean, newNum) {
```

```

        oldN <- oldMean@n
        oldAve <- oldMean@currentXbar
        newAve <- (oldAve*oldN + newNum)/(oldN + 1)
        newN <- oldN + 1L
        return(new("RunningCI", n = newN, currentXbar = newAve, knownVar = old
    )
    }
)

```

Here's a demonstration of using these two classes that mirrors the example in subsection 0.53.3

```

myAve <- new("RunningMean", n = 0L, currentXbar = 0)
myAve <- update(myAve, 3)
myAve
## An object of class "RunningMean"
## Slot "n":
## [1] 1
##
## Slot "currentXbar":
## [1] 3
myAve <- update(myAve, 1)
myAve
## An object of class "RunningMean"
## Slot "n":
## [1] 2
##
## Slot "currentXbar":
## [1] 2

myCI <- new("RunningCI", n = 0L, currentXbar = 0, knownVar = 1.0)
myCI <- update(myCI, 3)
myCI
## An object of class "RunningCI"
## Slot "knownVar":
## [1] 1

```



```
##
## Slot "n":
## [1] 1
##
## Slot "currentXbar":
## [1] 3
myCI <- update(myCI, 1)
myCI
## An object of class "RunningCI"
## Slot "knownVar":
## [1] 1
##
## Slot "n":
## [1] 2
##
## Slot "currentXbar":
## [1] 2
```

This looks more *functional* (more information on functional programming is available in chapter 0.55) than the Python example because the `update` function does not change a *mutable* object with a side-effect. Instead, it takes the old object, changes it, returns the new object, and uses assignment to overwrite the object. The benefit of this approach is that the assignment operator (`<-`) signals to us that something is changing. However, there is more data copying involved, so the program is presumably slower than it needs to be.

The big takeaway here is that S3 and S4 don't feel like Python's encapsulated OOP. If we wanted to write stateful programs, we might consider using Reference Classes, or R6 classes.

0.54.7 Reference Classes: The Big Picture

Reference Classes.¹⁴⁴ are built on top of S4 classes, and were released in late 2010¹⁴⁵. They feel very different from S3 and S4 classes, and they more closely resemble Python classes, because

1. their method definitions are *encapsulated* inside class definitions like in Python, and
2. the objects they construct are *mutable*.

So it will feel much more like Python's class system. Some might say using reference classes that will lead to code that is not very R-ish, but it can be useful for certain types of programs (e.g. long-running code, code that performs many/high-dimensional/complicated simulations, or code that circumvents storing large data set in your computer's memory all at once).

0.54.8 Creating Reference Classes

Creating reference classes is done with the function `setRefClass`. I create a class called `RunningMean` that produces the same behavior as that in the previous example.

```
RunningMeanRC <- setRefClass("RunningMeanRC",  
                             fields = list(current_xbar = "numeric",  
                                           n = "integer"),  
                             methods = list(  
                               update = function(new_x){  
                                 n <- n + 1L  
                                 current_xbar <- (current_xbar*(n - 1) + new_x) / n  
                               })
```

This tells us a few things. First, data members are called *fields*

¹⁴⁴<https://www.rdocumentation.org/packages/methods/versions/3.6.2/topics/ReferenceClasses>

¹⁴⁵<https://stat.ethz.ch/pipermail/r-announce/2010/000529.html>

now. Second, changing class variables is done with the `<<-`. We can use it just as before.

```
my_ave <- RunningMeanRC$new(current_xbar=0, n=0L)
my_ave
## Reference class object of class "RunningMeanRC"
## Field "current_xbar":
## [1] 0
## Field "n":
## [1] 0
my_ave$update(1.)
my_ave$current_xbar
## [1] 1
my_ave$n
## [1] 1
my_ave$update(3.)
my_ave$current_xbar
## [1] 2
my_ave$n
## [1] 2
```

Compare how similar this code looks to the code in 0.53.2! Note the paucity of assignment operators, and plenty of side-effects.

0.54.9 Creating R6 Classes

I quickly implement the above example as an R6 class. A more detailed introduction to R6 classes is provided in the vignette from the package authors.¹⁴⁶

You'll notice the reappearance of the `self` keyword. R6 classes have a `self` keyword just like in Python. They are similar to reference classes, but there are a few differences:

¹⁴⁶<https://r6.r-lib.org/articles/Introduction.html>

1. they have better performance than reference classes¹⁴⁷,
and
2. they don't make use of the <- operator.

```
library(R6)

RunningMeanR6 <- R6Class("RunningMeanR6",
  public = list(
    current_xbar = NULL,
    n = NULL,
    initialize = function(current_xbar = NA, n = NA) {
      self$current_xbar <- current_xbar
      self$n <- n
    },
    update = function(new_x) {
      self$n <- self$n + 1L
      self$current_xbar <- (self$current_xbar*(self$n - 1) + new_x)
    }
  )
)

my_r6_ave <- RunningMeanR6$new(current_xbar=0, n=0L)
my_r6_ave
## <RunningMeanR6>
##   Public:
##     clone: function (deep = FALSE)
##     current_xbar: 0
##     initialize: function (current_xbar = NA, n = NA)
##     n: 0
##     update: function (new_x)
my_r6_ave$update(1.)
my_r6_ave$current_xbar
## [1] 1
my_r6_ave$n
## [1] 1
```

¹⁴⁷<https://r6.r-lib.org/articles/Performance.html>

```
my_r6_ave$update(3.)
my_r6_ave$current_xbar
## [1] 2
my_r6_ave$n
## [1] 2
```

TODO a more detailed

<https://adv-r.hadley.nz/r6.html>

<https://adv-r.hadley.nz/r6.html#why-r6>

0.55 Exercises

All answers to questions related to R should be written in a file named `data_types_exercises.R`. All answers to questions related to Python should be written in a file named `data_types_exercises.py`.

1. In Python, write a class that implements a running sample variance.⁴
2. In Python, write a class that estimates a linear regression model.

Let

- Let $\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_{10} \end{bmatrix}$ be a 10×1 vector of predictor variables.
- $\mathbf{X} = \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ \vdots & \vdots \\ 1 & x_{10} \end{bmatrix}$ be a 10×2 “design matrix”,

- $\mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_{10} \end{bmatrix}$ be a 10×1 vector of dependent observations, and
- $\epsilon = \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \vdots \\ \epsilon_{10} \end{bmatrix}$ be a 10×1 vector of mean 0 random errors. The assumed regression model can be written as

$$\mathbf{y} = \mathbf{X}\beta + \epsilon,$$

and the estimate for the coefficient vector can be written as $\hat{\beta} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$.

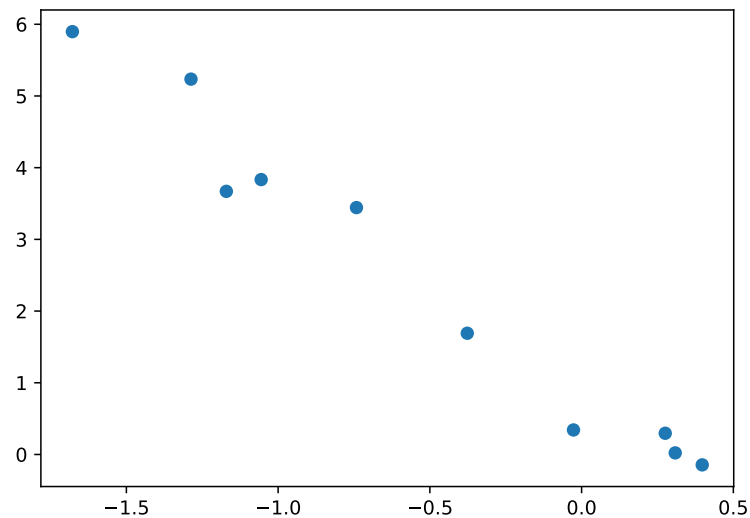
- Make the class called `LinearModel`, and use only the numpy package
- have the only attribute be a numpy array of estimated coefficients `coeffs`
- have one method called `fit` that takes a numpy arrays `x` (the design matrix), and `y`
- every time `fit` is called, reset the `coeffs` using the formula above

```
import numpy as np
import matplotlib.pyplot as plt

# don't hardcode variables!
num_rows = 10
num_predictors = 1
num_x_columns = num_predictors + 1

# generate fake data
true_coefficients = np.array([1,-3]).reshape((num_x_columns,1))
x_array = np.empty((num_rows, num_x_columns))
x_array[:,0] = 1
x_array[:,1] = np.random.normal(size=num_rows)
y_array = np.dot(x_array, true_coefficients)
y_array = y_array + np.random.normal(scale = .3, size = num_rows).reshape((num_row
```

```
# plot fake data  
plt.scatter(x_array[:,1], y_array)
```



Here is an example class definition, and then its use. The class holds onto

3. Come up with a list of Python classes that are written in third party libraries, and that you will find useful in the future!
4. Come up with a list of R classes that are written in third party libraries, and that you will find useful in the future!
5. Finish the R6 class example by adding a method `get_current_xbar` that takes no arguments, and returns `NULL` if `n` is equal to 0, and `n` otherwise. This class should behave exactly the same as the Python class that goes by the same name.
6. Come up with some ideas for (base class, derived class, object) triples.

7. Come up with some examples of when composition would be better than inheritance, and vice versa.

0

Functional Programming

Functional Programming (FP) is another way of thinking about how to organize programs. We talked about OOP in the last chapter (chapter IV), so how do OOP and FP differ? To put it simply, FP focuses on functions instead of objects. Because we are talking a lot about functions in this chapter, we will assume you have read and understood section 0.20.

Neither R nor Python is a purely functional language. For us, FP is a style that we can choose to let guide us, or that we can disregard. You can choose to employ a more functional style, or you can choose to use a more object-oriented style, or neither. Some people tend to prefer one style to other styles, and others prefer to decide which to use depending on the task at hand.

More specifically, a functional programming style takes advantage of **first-class functions** and favors functions that are **pure**.

1. **First-class functions** are functions that
 - can be passed as arguments to other functions,
 - can be returned from other functions, and
 - can be assigned to variables or stored in data structures.
2. **Pure functions**
 - return the same output if they are given the same input, and
 - do not produce **side-effects**.

Side-effects are changes made to non-temporary variables, to the “state” of the program.

We discussed (1) in the beginning of chapter 0.20. If you have not

used any other programming languages before, you might even take (1) for granted. However, if you have written C code before, you might remember how difficult it is to use functions as inputs to other functions!

There is more to say about point (2). This means you should keep your functions as *modular* as possible, unless you want your overall program to be much more difficult to understand. FP stipulates that

- **ideally functions will not refer to non-local variables;**
- **ideally functions will not (refer to and) modify non-local variables; and**
- **ideally functions will not modify their arguments.**

Unfortunately, violating the first of these three criteria is very easy to do in both of our languages. Recall our conversation about *dynamic lookup* in subsection 0.28. Both R and Python use dynamic lookup, which means you can't reliably control *when* functions look for variables. Typos in variable names easily go undiscovered, and modified global variables can potentially wreak havoc on your overall program.

Fortunately it is difficult to modify global variables inside functions in both R and Python. This was also discussed in subsection 0.28. In Python, you need to make use of the `global` keyword (mentioned in section 0.27.2), and in R, you need to use the rare super assignment operator (it looks like `<<-`, and it was mentioned in 0.27.1). Because these two symbols are so rare, they can serve as signals to viewers of your code about when and where (in which functions) global variables are being modified.

Last, violating the third criterion is easy in Python and difficult in R. This was discussed earlier in 0.27. Python can mutate/change arguments that have a mutable type because it has *pass-by-assignment* semantics (mentioned in section 0.27.2, and R generally can't modify its arguments at all because it has *pass-by-value* semantics 0.27.1).

This chapter avoids the philosophical discussion of FP. Instead, it takes the applied approach, and provides instructions on how to use FP in your own programs. I try to give examples of *how* you can use FP, and *when* these tools are especially suitable.

One of the biggest tip-offs that you should be using functional programming is if you need to evaluate a single function many times, or in many different ways. This happens quite frequently in statistical computing. Instead of copy/pasting similar-looking lines of code, you might consider *higher-order* functions that take your function as an input, and intelligently call it in all the many ways you want it to. A third option you might also consider is to use a loop (c.f. 0.44). However, that approach is not very functional, and so it will not be heavily-discussed in this section.

Another tip-off that you need FP is if you need many different functions that are all “related” to one another. Should you define each function separately, using excessive copy/paste-ing? Or should you write a function that can elegantly generate any function you need?

Not repeating yourself and re-using code is a primary motivation, but it is not the only one. Another motivation for **functional programming** is clearly explained in Advanced R¹⁴⁸¹⁴⁹:

A functional style tends to create functions that can easily be analysed in isolation (i.e. using only local information), and hence is often much easier to automatically optimise or parallelise.

¹⁴⁸<https://adv-r.hadley.nz/fp.html>

¹⁴⁹Even though this book only discusses *one* of our languages of interest, this quote applies to both languages.

All of these sound like a good things to have in our code, so let's get started with some examples!

0.56 Functions as Function Inputs in R

Many of the most commonly-used functionals in R have names that end in “apply”. The ones I discuss are `sapply`, `vapply`, `lapply`, `apply`, `tapply` and `mapply`. Each of these takes a function as one of its arguments. Recall that this is made possible by the fact that R has first-class functions.

0.56.1 `sapply` and `vapply`

Suppose we have a `data.frame` that has 10 rows and 100 columns. What if we want to take the mean of each column?

An amateurish way to do this would be something like the following.

```
myFirstMean <- mean(myDF[,1])
mySecondMean <- mean(myDF[,2])
myThirdMean <- mean(myDF[,3])
# ....
# so on and so forth
# ....
myThirdMean <- mean(myDF[,100])
```

You will need one line of code for each column in the data frame. For data frames with a lot of columns, this becomes quite tedious. You should also ask yourself what happens to you and your collaborators when the data frame changes even slightly, or if you want to apply a different function to its columns. Third, the results are not stored in a single container. You are making it difficult on

yourself if you want to use these variables in subsequent pieces of code.

“Don’t repeat yourself” (DRY) is an idea that’s been around for a while and is widely accepted (Hunt and Thomas, 2000). DRY is the opposite of WET¹⁵⁰.

Instead, prefer the use of `sapply` in this situation. The “s” in `sapply` stands for “simplified.” In this bit of code `mean` is called on each column of the data frame. `sapply` applies the function over columns, instead of rows, because data frames are internally a list of columns.

```
myMeans <- sapply(myDF, mean)
head(myMeans)
##           X1           X2           X3           X4           X5           X6
## 0.09039357 -0.92846760  0.30457418 -0.04405609 -0.09384464  0.45688472
```

Each call to `mean` returns a double vector of length 1. This is necessary if you want to collect all the results into a vector—remember, all elements of a vector have to have the same type. To get the same behavior, you might also consider using `vapply(myDF, mean, numeric(1))`.

In the above case, “simplify” referred to how one-hundred length-1 vectors were simplified into one length-100 vector. However, “simplified” does not necessarily imply that all elements will be stored in a vector. Consider the `summary` function, which returns a double vector of length 6. In this case, one-hundred length-6 vectors were simplified into one 6×100 matrix.

```
mySummaries <- sapply(myDF, summary)
is.matrix(mySummaries)
## [1] TRUE
dim(mySummaries)
## [1]  6 100
```

¹⁵⁰https://en.wikipedia.org/wiki/Don%27t_repeat_yourself#WET

Another function that is worth mentioning is `replicate`—it is a wrapper for `sapply`. Consider a situation where you want to call a function many times with the same inputs. You might try something like `sapply(1:100, function(elem) { return(myFunc(someInput)) })`. Another, more readable, way to do this is `replicate(100, myFunc(someInput))`.

0.56.2 `lapply`

For functions that do not return amenable types that fit into a vector, matrix or array, they might need to be stored in `list`. In this situation, you would need `lapply`. The “l” in `lapply` stands for “list”. `lapply` always returns a `list` of the same length as the input.

```
regress <- function(y){ lm(y ~ 1) }
myRegs <- lapply(myDF, regress)
length(myRegs)
## [1] 100
class(myRegs[[1]])
## [1] "lm"
summary(myRegs[[12]])
##
## Call:
## lm(formula = y ~ 1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.44489 -0.78635 -0.03176  0.38692  1.87463
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.2658      0.3189  -0.833   0.426
##
## Residual standard error: 1.008 on 9 degrees of freedom
```

0.56.3 apply

I use `sapply` and `lapply` the most, personally. The next most common function I use is `apply`. I use it to apply functions to *rows* instead of columns. However, it can also apply functions over columns, just as the other functions we discussed can.¹⁵¹

```
dim(myDF)
## [1] 10 100
apply(myDF, 1, mean)
## [1] 0.18780324 -0.05832272 -0.17120024 -0.08014775 0.04603083 -0.10057438 -0.04301368
## [9] -0.08449865 -0.04301368
```

Another example where it can be useful to apply a function to rows is **predicate functions**. A predicate function is just a fancy name for a function that returns a Boolean. I use them to filter out rows of a `data.frame`. Without a predicate function, filtering rows might look something like this.

```
albRealEstate <- read.csv("data/albemarle_real_estate.csv")
subDF <- albRealEstate[(albRealEstate$YearBuilt == 2006 & albRealEstate$Condition == "Average")]
head(subDF)
```

##	YearBuilt	YearRemodeled	Condition	NumStories	FinSqFt	Bedroom	FullBath	HalfBath
## 1	2006	0	Average	1.00	1922	3	3	
## 2	2003	0	Average	1.00	1848	3	2	
## 4	1998	0	Good	1.00	1244	1	1	
## 5	1886	0	Average	1.86	1861	4	1	
## 6	1910	0	Fair	1.53	1108	3	1	
## 8	1975	1982	Average	1.00	1520	3	1	
##	TotalValue	City						
## 1	409900	CROZET						

¹⁵¹`apply` is everyone's favorite whipping boy whenever it comes to comparing `apply` against the other `*apply` functions. This is because it is generally a little slower—it is written in R and doesn't call out to compiled C code. However, in my humble opinion, it doesn't matter all that much because the fractions of a second saved don't always add up in practice.

```
## 2      523100 CROZET
## 4      620700 CROZET
## 5      162500 CROZET
## 6      167200 CROZET
## 8      151900 CROZET
```

Complicated filtering criteria can become quite wide, so I prefer to break the above code into three steps.

- Step 1: write a predicate function that returns TRUE or FALSE;
- Step 2: construct a logical vector by applying the predicate over rows;
- Step 3: plug the logical vector into the `[` operator to remove the rows.

```
pred <- function(row){
  (row['YearBuilt'] == 2006 & row['Condition'] == "Average") | row['City'] == "CROZET"
}
whichRows <- apply(albRealEstate, 1, pred)
subDF <- albRealEstate[whichRows,]
head(subDF)
```

##	YearBuilt	YearRemodeled	Condition	NumStories	FinSqFt	Bedroom	FullBath	HalfBath
## 1	2006	0	Average	1.00	1922	3	3	
## 2	2003	0	Average	1.00	1848	3	2	
## 4	1998	0	Good	1.00	1244	1	1	
## 5	1886	0	Average	1.86	1861	4	1	
## 6	1910	0	Fair	1.53	1108	3	1	
## 8	1975	1982	Average	1.00	1520	3	1	

```
##      TotalValue      City
## 1      409900 CROZET
## 2      523100 CROZET
## 4      620700 CROZET
## 5      162500 CROZET
## 6      167200 CROZET
## 8      151900 CROZET
```


0.56.4 **tapply**

`tapply` can be very handy when you need it. First, we’ve alluded to the definition before in subsection 0.31, but a **ragged array** is a collection of arrays that all have potentially different lengths. I don’t typically construct such an object and then pass it to `tapply`. Rather, I let `tapply` construct the ragged array for me. The first argument it expects is “typically vector-like”, while the second tells us how to break that **vector** into chunks. The third argument is a function that gets applied to each **vector** chunk.

If I wanted the average home price for each city, I could use something like this.

```
head(albRealEstate)
##      YearBuilt YearRemodeled Condition NumStories FinSqFt Bedroom FullBath HalfBat
## 1      2006           0 Average         1.00    1922         3         3
## 2      2003           0 Average         1.00    1848         3         2
## 3      1972           0 Average         1.00    1248         2         1
## 4      1998           0 Good           1.00    1244         1         1
## 5      1886           0 Average         1.86    1861         4         1
## 6      1910           0 Fair           1.53    1108         3         1
##      TotalValue      City
## 1      409900      CROZET
## 2      523100      CROZET
## 3      180900 EARLYSVILLE
## 4      620700      CROZET
## 5      162500      CROZET
## 6      167200      CROZET
unique(albRealEstate$City)
## [1] "CROZET"      "EARLYSVILLE" "CHARLOTTESVILLE" "SCOTTSVILLE" "NO
## [6] "KESWICK"
tapply(albRealEstate$TotalValue, list(albRealEstate$City), mean)
## CHARLOTTESVILLE      CROZET      EARLYSVILLE      KESWICK      NORTH GARDEN
##      381933.0      380425.7      439141.0      540532.6      366597.8
```

You might be wondering why we put `albRealEstate$City` into a `list`. That seems kind of unnecessary. This is because `tapply` can

be used with multiple factors—this will break down the vector input into a finer partition. The second argument must be one object, though, so all of these factors must be collected into a list. The following code produces a “pivot table.”

```
tapply(albRealEstate$TotalValue, list(albRealEstate$City, albRealEstate$Condition),
##
## Average Excellent Fair Good Poor Substandard
## CHARLOTTESVILLE 337913.4 491702.4 229336.2 444325.5 202420.00 457500
## CROZET 342133.4 552081.6 198009.5 390657.7 203806.25 53450
## EARLYSVILLE 365990.6 652387.4 230646.2 470554.7 372442.86 160400
## KESWICK 392998.6 871719.8 172790.9 672510.7 100337.50 NA
## NORTH GARDEN 241187.7 966528.6 131997.0 440503.1 151187.50 NA
## SCOTTSVILLE 214046.9 502273.8 157438.0 374600.4 95377.78 NA
```

For functions that return higher-dimensional output, you will have to use something like `by` or `aggregate` in place of `tapply`.

0.56.5 `mapply`

The documentation of `mapply`¹⁵² states `mapply` is a multivariate version of `sapply`. `sapply` worked with univariate functions; the function was called multiple times, but each time with a single argument. If you have a function that takes multiple arguments, and you want those arguments to change each time the function is called, then you might be able to use `mapply`.

Here is a short example. Regarding the `n=` argument of `rnorm`, the documentation explains, “[i]f `length(n) > 1`, the length is taken to be the number required.” This would be a problem if we want to sample a.) three times from a mean 0 normal, b.) twice from a mean 100 normal, and c.) once from a mean −100 normal distribution.

¹⁵²<https://stat.ethz.ch/R-manual/R-devel/library/base/html/mapply.htm>

```

rnorm(n = c(3,2,1), mean = c(0,100,-100), sd = c(.01, .01, .01))

## [1] 0.01339378 99.99952118 -99.99995760

mapply(rnorm, n = c(3,2,1), mean = c(0,100,-100), sd = c(.01, .01, .01))

## [[1]]
## [1] 0.014982930 0.006057215 0.005257986
##
## [[2]]
## [1] 99.99486 100.00275
##
## [[3]]
## [1] -100.02

```

0.56.6 Reduce and do.call

In section 0.45.2 we talked about several different ways of “combining” data sets. We discussed stacking data sets on top of one another with `rbind` (c.f. subsection 0.47), stacking them side-by-side with `cbind` (also in 0.47), and intelligently joining them together with `merge` (c.f. 0.48). Consider the task of combining *many* data sets. How do we write DRY code and abide by the DRY principle?

We can use either `Reduce` or `do.call` as a higher-order function. Just like the aforementioned `*apply` functions, they take in either `cbind`, `rbind`, or `merge` as a function input. Which one do we pick, though? The answer to that question deals with how many arguments our lower-order functions take.

Take a look at the documentation to `rbind`. Its first argument is `...`, which is the dot-dot-dot¹⁵³ symbol. This means `rbind` can take a varying number of `data.frames` to stack on top of each other. In other words, `rbind` is *variadic*.

¹⁵³https://cran.r-project.org/doc/manuals/r-release/R-lang.html#Dot_002ddot_002ddot

On the other hand, take a look at the documentation of `merge`. It only takes two `data.frames` at a time¹⁵⁴.

If we want to combine many data sets, `merge` This is the difference between `Reduce` and `do.call`.

`do.call` calls a function once on many arguments, so its function must be able to handle many arguments. On the other hand, `Reduce` calls a binary function many times on pairs of arguments. `Reduce`'s function argument gets called on the first two elements, then on the first output and the third element, then on the second output and fourth element, and so on.

TODO diagram

Here is an initial example that makes use of four data sets `d1.csv`, `d2.csv`, `d3.csv`, and `d4.csv`. To start, ask yourself how we would read all of these in. There is a temptation to copy and paste `read.csv` calls, but that would violate the DRY principle. Instead, let's use `lapply` an anonymous function that constructs a file path string, and then uses it to read in the data set the string refers to.

```
numDataSets <- 4
dataSets <- paste0("d",1:numDataSets)
dfs <- lapply(dataSets,
              function(name) read.csv(paste0("data/", name, ".csv")))
head(dfs[[3]])
##      id obs3
## 1  a      7
## 2  b      8
## 3  c      9
```

Notice how the above code would only need to be changed by one character if we wanted to increase the number of data sets being read in!

¹⁵⁴Although, it is still variadic. The difference is that the dot-dot-dot symbol does not refer to a varying number of `data.frames`...just a varying number of other things we don't care about at the present moment.

Next, `cbinding` them all together can be done as follows. `do.call` will call the function only once. `cbind` takes many arguments at once, so this works.

```
do.call(cbind, dfs) # DRY! :)
##   id obs1 id obs2 id obs3 id obs4
## 1  a    1  b    5  a    7  a   10
## 2  b    2  a    4  b    8  b   11
## 3  c    3  c    6  c    9  c   12
# cbind(df1,df2,df3,df4) # WET! :(
```

This code is even better than the above code in that if `dfs` becomes longer, or changes at all, *nothing* will need to be changed.

What if we wanted to `merge` all these data sets together? After all, the `id` column appears to be repeating itself, and some data from `d2` isn't lining up.

```
Reduce(merge, dfs)
##   id obs1 obs2 obs3 obs4
## 1  a    1    4    7   10
## 2  b    2    5    8   11
## 3  c    3    6    9   12
```

Again, this is very DRY code. Nothing would need to be changed if `dfs` grew. Furthermore, trying to `do.call` the `merge` function wouldn't work because it can only take two data sets at a time.

0.57 Another Example in R

Consider another common example: plotting scalar-valued multivariate functions. Let's try to plot a bivariate Gaussian distribution.

$$f(x, y) = \frac{1}{2\pi} \exp \left[-\frac{x^2 + y^2}{2} \right]$$

The random elements x and y , in this particular case, are uncorrelated, each have unit variance, and zero mean. This density is a surface in 3-d dimensional space. To visualize this, we would need to

1. generate a “grid” of points in \mathbb{R}^2 ,
2. evaluate our function on each point, and then
3. call some plotting function that takes this all and makes a pretty picture.

There are a couple ways you could write this function. One way might take two arguments, and another might take one argument. If we are to use `mapply`, we need the function to take two arguments.

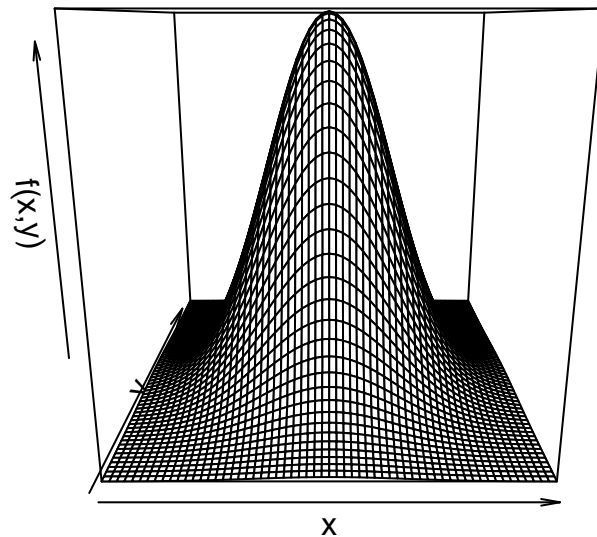
```
fTwoArgs <- function(x,y){  
  exp(-.5*(x^2 + y^2)) / 2 / pi  
}
```

We can construct every possible point on a grid with the `expand.grid` function.

```
xGrid <- seq(-3,3,.1)  
yGrid <- seq(-3,3,.1)  
grid <- expand.grid(xGrid, yGrid)  
head(grid)  
##      Var1 Var2  
## 1 -3.0    -3  
## 2 -2.9    -3  
## 3 -2.8    -3  
## 4 -2.7    -3  
## 5 -2.6    -3  
## 6 -2.5    -3
```

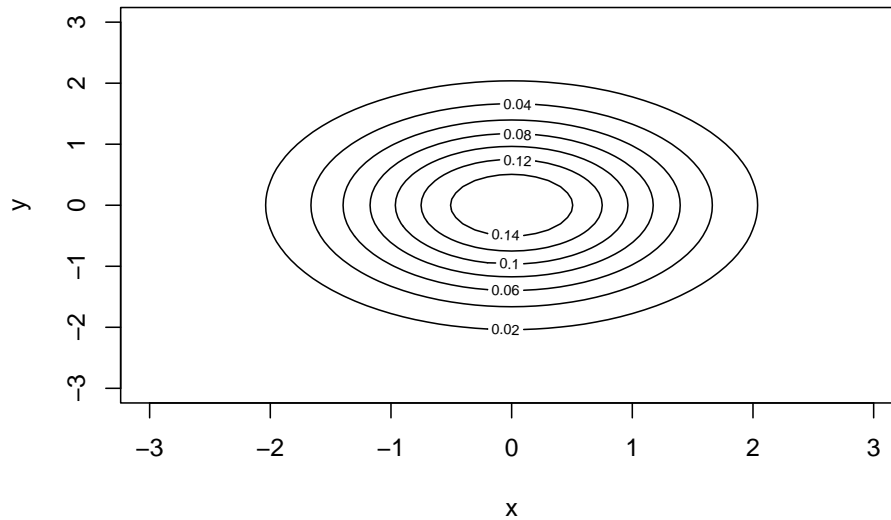
`mapply` would take `fTwoArgs`, and effectively call it on every row pair. The pairs do not need to be organized in a `data.frame`, though.

```
funcOut1 <- mapply(fTwoArgs, grid[,1], grid[,2])
head(funcOut1)
## [1] 1.964128e-05 2.638072e-05 3.508008e-05 4.618400e-05 6.019766e-05 7.768277e-05
rectangularOutput <- matrix(funcOut1, ncol = length(xGrid))
persp(xGrid, yGrid, rectangularOutput,
      zlab = "f(x,y)", xlab = "x", ylab = "y")
```



If you prefer using `apply`, that is also possible, but you would need to rewrite the function to take one (length-two) argument.

```
fOneArg <- function(vec){
  exp(-sum(vec^2)/2)/2/pi
}
funcOut2 <- apply(grid, 1, fOneArg)
moreRectOut <- matrix(funcOut2, ncol = length(xGrid))
contour(xGrid, yGrid, moreRectOut, xlab = "x", ylab = "y")
```



0.58 Functions as Function Inputs in Base Python

I discuss two functions from base Python that take functions as input. Neither return a `list` or a `np.array`, but they do return different kinds of **iterables**, which are “objects capable of returning their members one at a time,” according to the Python documentation.¹⁵⁵ `map`, the function, will return objects of type `map`. `filter`, the function, will return objects of type `filter`. Often times we will just convert these to the container we are more familiar with.

0.58.1 `map`

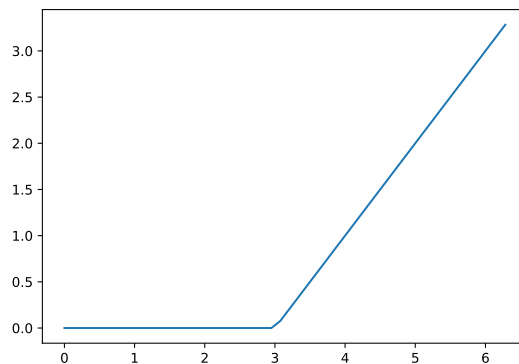
`map`¹⁵⁶ can call a function repeatedly using elements of a container as inputs. Here is an example of calculating outputs of a *spline* function, which can be useful for coming up with predictors in regression models. This particular spline function is $f(x) = (x - k)1(x \geq k)$, where k is some chosen “knot point.”

¹⁵⁵<https://docs.python.org/3/glossary.html>

¹⁵⁶<https://docs.python.org/3/library/functions.html#map>


```
import numpy as np
my_inputs = np.linspace(start = 0, stop = 2*np.pi)
def spline(x):
    knot = 3.0
    if x >= knot:
        return x-knot
    else:
        return 0.0
output = list(map(spline, my_inputs))
```

We can visualize the mathematical function by plotting its outputs against its inputs. More information on visualization was given in subsection 0.49.2.



`map` can also be used like `maply`. In other words, you can apply it to two containers,

```
import numpy as np
x = np.linspace(start = -1., stop = 1.0)
y = np.linspace(start = -1., stop = 1.0)
def f(x):
    np.log(x**2 + y**2)
output = list(map(spline, my_inputs))
```

0.58.2 filter

`filter`¹⁵⁷ helps remove unwanted elements from a container. It returns an iterable of type `filter`, which we can iterate over or convert to a more familiar type of container. In this example, I iterate over it without converting it.

```
raw_data = np.arange(0,1.5,.01)
for elem in filter(lambda x : x**2 > 2, raw_data):
    print(elem)
## 1.42
## 1.43
## 1.44
## 1.45
## 1.46
## 1.47
## 1.48
## 1.49
```

0.59 Functions as Function Inputs in Numpy

Numpy provides a number of functions¹⁵⁸ that facilitate working with `np.ndarrays` in a functional style. For example, `np.apply_along_axis`¹⁵⁹ is similar to R's `apply`. `apply` had a `MARGIN` argument (1 sums rows, 2 sums columns), whereas this function has a `axis=` argument (0 sums columns, 1 sums rows).

```
import numpy as np
my_array = np.arange(6).reshape((2,3))
```

¹⁵⁷<https://docs.python.org/3/library/functions.html#filter>

¹⁵⁸<https://numpy.org/doc/stable/reference/routines.functional.html>

¹⁵⁹https://numpy.org/doc/stable/reference/generated/numpy.apply_along_axis.html

```
my_array
## array([[0, 1, 2],
##        [3, 4, 5]])
np.apply_along_axis(sum, 0, my_array) # summing columns
## array([3, 5, 7])
np.apply_along_axis(sum, 1, my_array) # summing rows
## array([ 3, 12])
```

```
my_array = np.random.normal(size=(10,1000))
np.apply_along_axis(sum, 0, my_array).shape
## (1000,)
np.apply_along_axis(sum, 1, my_array).shape
## (10,)
```

0.60 Functional Methods in pandas

pandas' DataFrames have an `.apply` method¹⁶⁰ that is very similar to `apply` in R,¹⁶¹ but again, just like the above function, you have to think about an `axis=` argument instead of a `MARGIN=` argument.

```
import pandas as pd
alb_real_est = pd.read_csv("data/albemarle_real_estate.csv")
alb_real_est.shape
## (27943, 12)
alb_real_est.apply(len, axis=0) # length of columns
## YearBuilt      27943
```

¹⁶⁰<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.apply.html>

¹⁶¹You should know that a lot of special-case functions that you typically apply to rows or columns come built-in as `DataFrame` methods. For instance, `.mean` would allow you to do something like `my_df.mean()`.

```
## YearRemodeled      27943
## Condition           27943
## NumStories          27943
## FinSqFt             27943
## Bedroom             27943
## FullBath            27943
## HalfBath            27943
## TotalRooms          27943
## LotSize             27943
## TotalValue          27943
## City                27943
## dtype: int64
type(alb_real_est.apply(len, axis=1)) # length of rows
## <class 'pandas.core.series.Series'>
```

Another thing to keep in mind is that `DataFrames`, unlike `ndarrays`, don't have to have the same type for all elements. If you have mixed column types, then summing rows, for instance, might not make sense. This just requires subsetting columns before `.apply`ing a function to rows. Here is an example of computing each property's "score".

```
import pandas as pd
# alb_real_est.apply(sum, axis=1) # can't add letters to numbers!
def get_prop_score(row):
    return 2*row[0] + 3*row[1]
alb_real_est['Score'] = alb_real_est[['FinSqFt', 'LotSize']].apply(get_prop_score,
alb_real_est[['FinSqFt', 'LotSize', 'Score']].head(2)
##      FinSqFt  LotSize      Score
## 0      1922     5.000  3859.000
## 1      1848    61.189  3879.567
```

`.apply` also works with more than one function at a time.

```
alb_real_est[['FinSqFt','LotSize']].apply([sum, len])
##      FinSqFt      LotSize
## sum  55559801  97856.8384
## len    27943  27943.0000
```

If you do not want to waste two lines defining a function with `def`, you can use an anonymous (unnamed) **lambda function**¹⁶². Be careful, though—if your function is complex enough, then your lines will get quite wide. For instance, this example is pushing it.

```
alb_real_est[['FinSqFt','LotSize']].apply(lambda row : sum(row*[2,3]), 1)[:4]
## 0      3859.000
## 1      3879.567
## 2      2501.280
## 3      2639.944
## dtype: float64
```

If you want to apply a (scalar-valued) function that takes only individual elements, you should try to use a unary function (recall that this was discussed in TODO). If no such unary function exists, you can apply it with `.applymap`¹⁶³.

```
alb_real_est[['FinSqFt','LotSize']].applymap(lambda e : e + 1).head(2)
##      FinSqFt  LotSize
## 0         1923     6.000
## 1         1849    62.189
```

Last, we have a `.groupby`¹⁶⁴ method, which can be used to mirror the behavior of R's `tapply`, `aggregate` or `by`. It can take the `DataFrame` it belongs to, and group its rows into multiple sub-

¹⁶²<https://docs.python.org/3/tutorial/controlflow.html#lambda-expressions>

¹⁶³<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.applymap.html#pandas.DataFrame.applymap>

¹⁶⁴<https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.groupby.html>

`DataFrames`. The collection of sub-`DataFrames` has a lot of the same methods that an individual `DataFrame` has (e.g. the subsetting operators, and the `.apply()` method), which can all be used in a second step of calculating things on each sub-`DataFrame`.

```
type(alb_real_est.groupby(['City']))
## pandas.core.groupby.generic.DataFrameGroupBy
type(alb_real_est.groupby(['City'])['TotalValue'])
## pandas.core.groupby.generic.SeriesGroupBy
```

Here is an example that models some pretty typical functionality. It shows two ways to get the average home price by city. The first line groups the rows by which `City` they are in, extracts the `TotalValue` column in each sub-`DataFrame`, and then `.apply()`s the `np.average()` function on the sole column found in each sub-`DataFrame`. The second `.apply()`s a lambda function to each sub-`DataFrame` directly.

```
alb_real_est.groupby(['City'])['TotalValue'].apply(np.average)
## City
## CHARLOTTESVILLE    381932.962760
## CROZET                380425.678927
## EARLYSVILLE          439140.987124
## KESWICK               540532.605905
## NORTH GARDEN         366597.750865
## SCOTTSVILLE        268407.384615
## Name: TotalValue, dtype: float64
alb_real_est.groupby(['City']).apply(lambda df : np.average(df['TotalValue']))
## City
## CHARLOTTESVILLE    381932.962760
## CROZET                380425.678927
## EARLYSVILLE          439140.987124
## KESWICK               540532.605905
## NORTH GARDEN         366597.750865
## SCOTTSVILLE        268407.384615
## dtype: float64
```

More tips on this programming pattern can be found here¹⁶⁵.

0.61 Functions as Function Inputs (miscellany)

functools.reduce

operator module

0.62 Functions as Function Outputs in R

Functions that create and return other functions are sometimes called **function factories**. Functions are first-class objects in R, so it's easy to return them. What's more interesting is that supposedly temporary objects inside the outer function can be accessed during the call of the inner function after it's returned.

Here is a first quick example.

```
funcFactory <- function(greetingMessage){  
  function(name){  
    paste(greetingMessage, name)  
  }  
}  
greetWithHello <- funcFactory("Hello")  
greetWithHello("Taylor")  
## [1] "Hello Taylor"  
greetWithHello("Charlie")  
## [1] "Hello Charlie"
```

¹⁶⁵https://pandas.pydata.org/pandas-docs/stable/user_guide/groupby.html

The `greetingMessage` argument that is passed in, "Hello", isn't temporary anymore.

Here is an example that implements a variance reduction technique called **common random numbers**.

Suppose $X \sim \text{Normal}(\mu, \sigma^2)$, and we are interested in approximating an expectation of a function of this random variable. Suppose that we don't know that

$$\mathbb{E}[\sin(X)] = \sin(\mu) \exp\left(-\frac{\sigma^2}{2}\right)$$

for any particular choice of μ and σ^2 , and instead, we choose to use the Monte Carlo method:

$$\hat{\mathbb{E}}[\sin(X)] = \frac{1}{n} \sum_{i=1}^n \sin(X^i)$$

where $X^1, \dots, X^n \stackrel{\text{iid}}{\sim} \text{Normal}(\mu, \sigma^2)$ is a large collection of draws from the appropriate normal distribution. In real life, the theoretical expectation might not be tractable (either because the random variable has a complicated distribution, or maybe because the functional is very complicated) and Monte Carlo, or some other approximation algorithm, might be our only hope!

Here are two functions that calculate the above quantities for $n = 100$. `actualExpectSin` is a function that computes the theoretical expectation for any particular parameter pair. `monteCarloSin` is a function that implements the Monte Carlo approximate expectation.

```
n <- 1000 # don't hardcode variables that aren't passed as arguments!
actualExpectSin <- function(params){
  stopifnot(params[2] > 0) # second parameter is sigma
  sin(params[1])*exp(-.5*(params[2]^2))
}
monteCarloSin <- function(params){
  stopifnot(params[2] > 0)
  mean(sin(rnorm(n = n, mean = params[1], sd = params[2])))
```

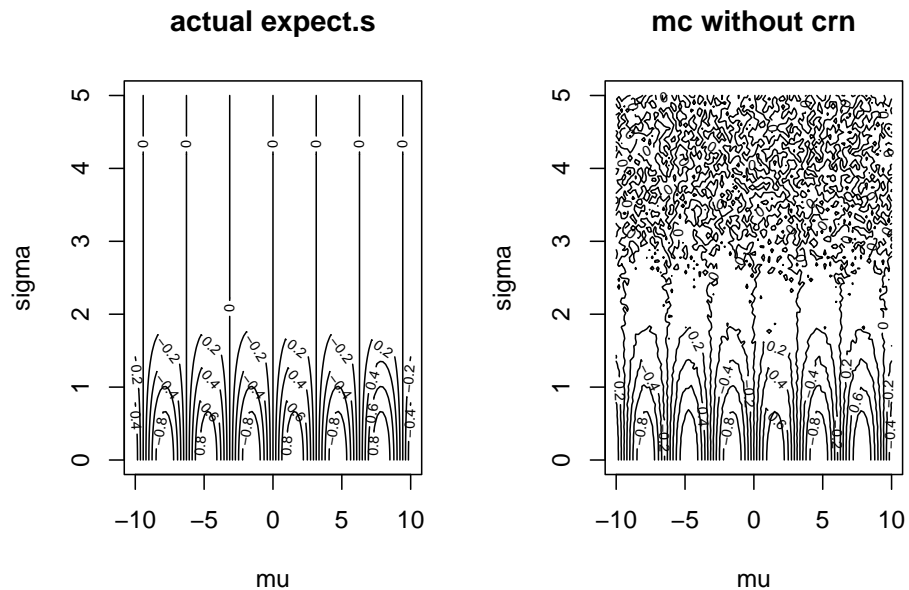


```
}
# monteCarloSin(c(10,1))
```

One-off approximations aren't as interesting as visualizing many expectations for many parameter inputs. On the left, we have the true expectation function plotted with a contour plot. On the right,

```
muGrid <- seq(-10,10, length.out = 100)
sigmaGrid <- seq(.001, 5, length.out = 100)
muSigmaGrid <- expand.grid(muGrid, sigmaGrid)
actuals <- matrix(apply(muSigmaGrid, 1, actualExpectSin), ncol = length(muGrid))
mcApprox <- matrix(apply(muSigmaGrid, 1, monteCarloSin), ncol = length(muGrid))

par(mfrow=c(1,2))
contour(muGrid, sigmaGrid, actuals, xlab = "mu", ylab = "sigma", main = "actual ex
contour(muGrid, sigmaGrid, mcApprox, xlab = "mu", ylab = "sigma", main = "mc witho
```



```
par(mfrow=c(1,1))
```

If we wanted to use common random numbers, we could generate $Z^1, \dots, Z^n \stackrel{\text{iid}}{\sim} \text{Normal}(0, 1)$, and use the fact that $X^i = \mu + \sigma Z^i$

This leads to the Monte Carlo estimate

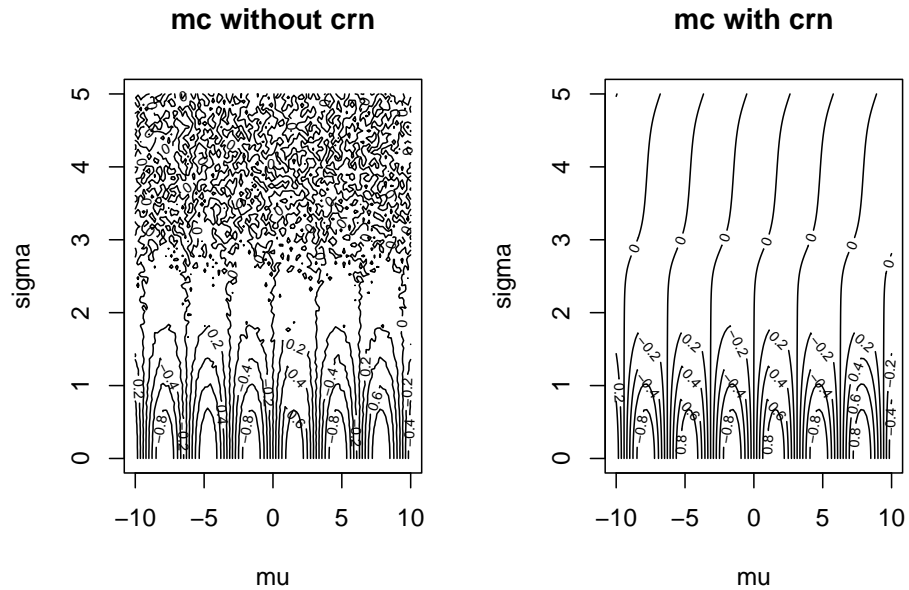
$$\tilde{\mathbb{E}}[\sin(X)] = \frac{1}{n} \sum_{i=1}^n \sin(\mu + \sigma Z^i)$$

Here is one function that naively implements Monte Carlo with common random numbers. We generate the collection of standard normal random variables once, globally. Each time you call `monteCarloSinCRNv1(c(10,1))`, you get the same answer.

```
commonZs <- rnorm(n=n)
monteCarloSinCRNv1 <- function(params){
  stopifnot(params[2] > 0)
  mean(sin(params[1] + params[2]*commonZs))
}
# monteCarloSinCRNv1(c(10,1))
```

Let's compare using common random numbers to going without. As you can see, common random numbers make the plot look "smoother."

```
mcApproxCRNv1 <- matrix(apply(muSigmaGrid, 1, monteCarloSinCRNv1), ncol = length(muSigmaGrid[,1]),
  par(mfrow=c(1,2))
contour(muGrid, sigmaGrid, mcApprox, xlab = "mu", ylab = "sigma", main = "mc without CRN")
contour(muGrid, sigmaGrid, mcApproxCRNv1, xlab = "mu", ylab = "sigma", main = "mc with CRN")
```

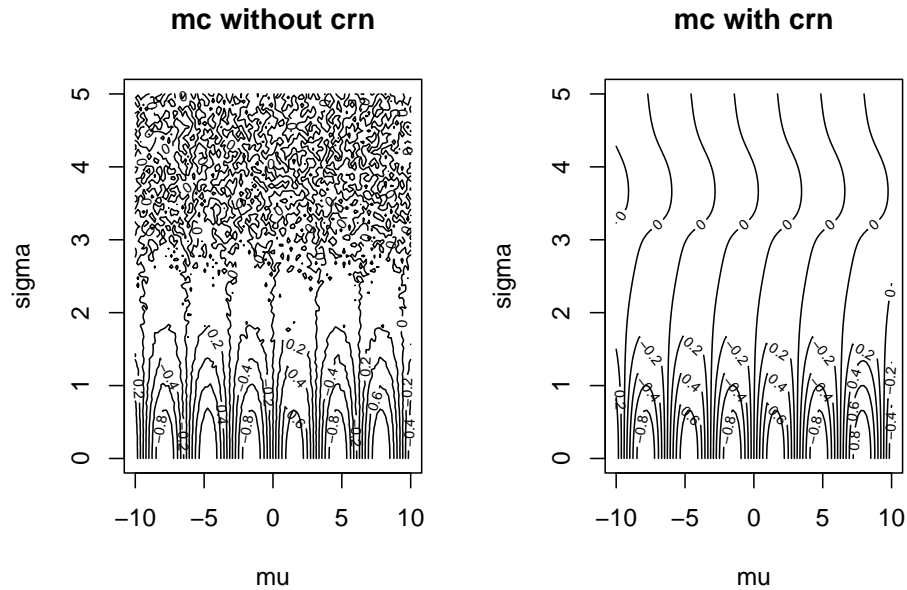


```
par(mfrow=c(1,1))
```

The downside to this implementation is that we have a bunch of samples floating around in the global environment. We can implement this much more nicely with a function factory.

```
makeMCFunc <- function(){
  commonZs <- rnorm(n=n)
  function(params){
    stopifnot(params[2] > 0)
    mean(sin(params[1] + params[2]*commonZs))
  }
}
monteCarloSinCRNv2 <- makeMCFunc()
# monteCarloSinCRNv2(c(10,1))
```

Much better! Let's just make sure this function works by comparing its output to the known true function.



0.63 Functions as Function Outputs in Python

Returning functions from functions, explaining mechanics

`np.vectorize`¹⁶⁶ is something that I use quite often.

decorators!

TODO Both R and Python have reduce functions. R has `Reduce`, while Python has `reduce`.

In R

`reduce`,

¹⁶⁶<https://numpy.org/doc/stable/reference/generated/numpy.vectorize.html#numpy.vectorize>

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