

c) Muestre que las derivadas parciales de la métrica están dadas por:

$$\frac{\partial \chi^2(\vec{\theta})}{\partial \theta} = -2 \cdot \sum_{i=1}^n (y_i - \eta(x_i, \vec{\theta})) \cdot \frac{\partial \eta(x_i, \vec{\theta})}{\partial \theta}$$

tenemos que si $\chi^2(\vec{\theta})$

$$\frac{\partial \chi^2(\vec{\theta})}{\partial \theta_i} = \sum_{i=1}^n \frac{\partial}{\partial \theta_i} (y_i - \eta(x_i, \vec{\theta}))^2$$

$$\frac{\partial \chi^2(\vec{\theta})}{\partial \theta_i} = \sum_{i=1}^n (2)(y_i - \eta(x_i, \vec{\theta})) \left(- \frac{\partial \eta(x_i, \vec{\theta})}{\partial \theta_i} \right) = -2 \sum_{i=1}^n (y_i - \eta(x_i, \vec{\theta})) \frac{\partial}{\partial \theta_i}$$

Por tanto queda demostrado mediante el anterior procedimiento