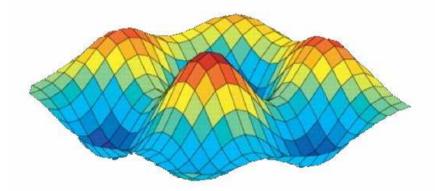
University of Franche-Comte, Master CompuPhys, Numerical methods 1

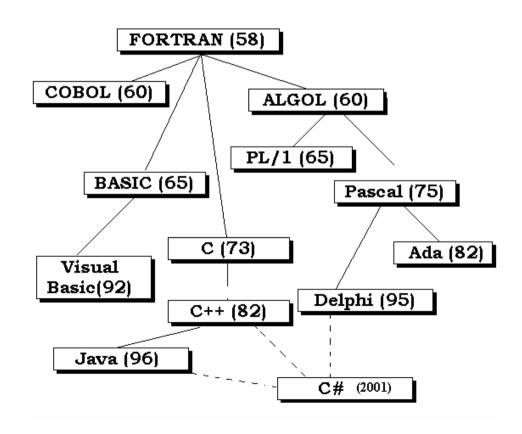
# Part III: Introduction to FORTRAN



# Introduction to FORTRAN language

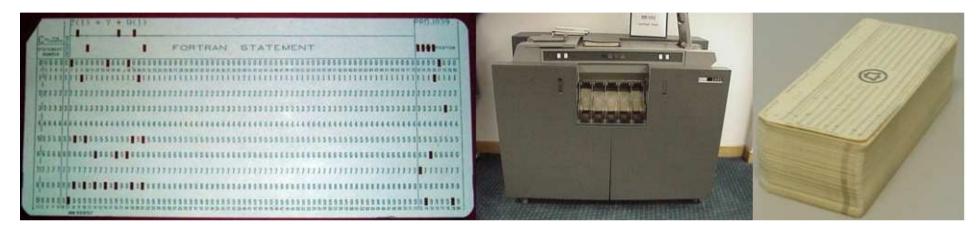
#### **FORTRAN** = **For**mula **Tran**slator

1<sup>st</sup> language of *high level*, developed from 1954 by John Backus (at IBM).



## **History**

- Fortran 66: 1st standardisation



-2d standard: Fortran 77: syntax IF-THEN-ELSE

-3d standard: **Fortran** 90 and **95:** file format .f90, modern instructions (modules, dynamic tables, ...)

-4th standard: **Fortran 2003:** numerous revisions (pointers, inter-operability with the language C, Object-Oriented programming, ...)

- 5th standard: Fortran 2008: new instructions for parallelism

## **Avantages of Fortran**

Language developed for scientific calculation (« number crunching »)

## Generates optimized high-performance code:

- compiled language
- automatic optimizations

## Simple and flexible syntax

Problems with high memory-space cost: easy dynamic management

## Good support of **mathematics**:

- numerous kinds of data (complex numbers, vectors, matrices, ...) and math functions available as standard
- compact syntax for matrix calculation (→ automatic parallelism)

#### Since Fortran 2003:

- Object-Oriented programming
- inter-operability with the language C (and Python)

## **Disadvantages of Fortran**

The language allows many obsolete instructions (supports 4 standards!) still encountered frequently in codes.

Badly adapted to anything other than scientific computing (graphical interface, access to databases, ...)

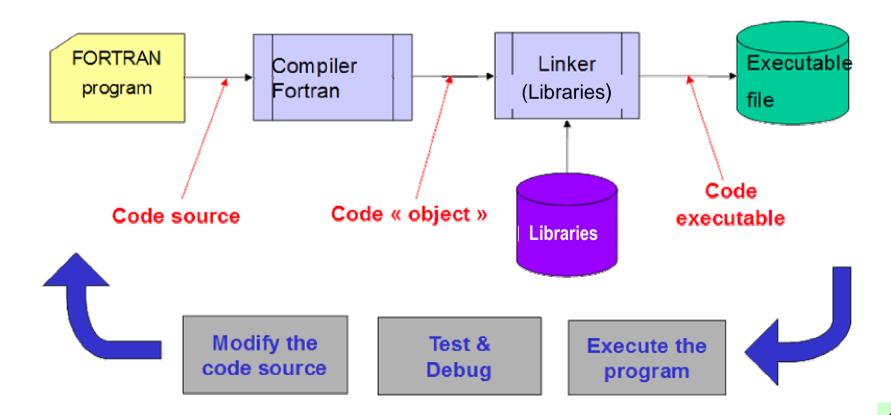
Quite small user community (compared to C)

## Advantage or disadvantage

The language evolves slowly. (→compatibility, stability)

Fortran (like C) is a compiled language.

The code-source (what we write) should be converted into machine language before being executed.



# **Basic instructions of Fortran** and first code

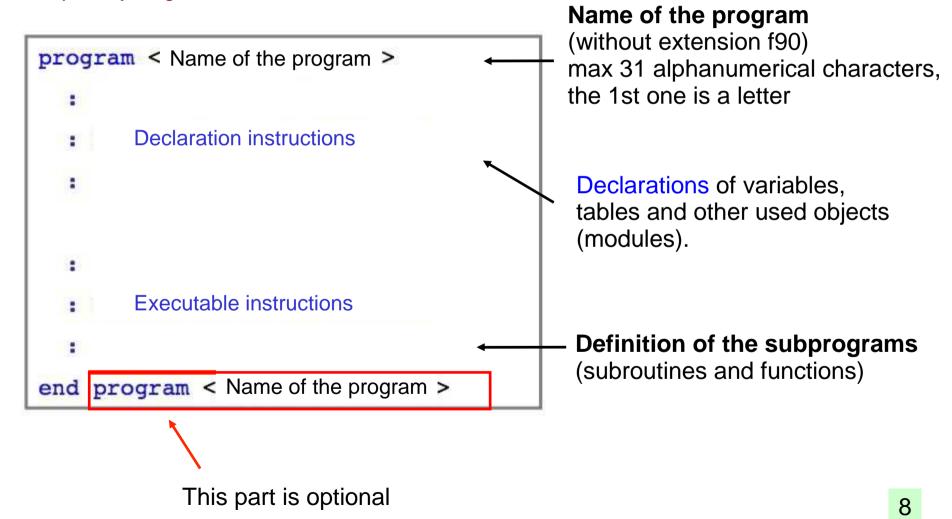
- Overview of the main instructions
- Illustration of good (and bad) programming practices

#### Note:

The language has become very complex, it is impossible to cover all the possibilities of Fortran in this course.

Source code: contained in a text file with the extension .f90

Example: MyProgram.f90



```
Example:

! Program to calculate a square root

program square_roots

implicit none
integer :: i,nroots=3
real :: value,root

print *, "Let's calculate ",nroots, " square roots"

A character! means that
the remainder of the line is a
comment

— Declarations

Instructions
```

```
print *, "Let's calculate ",nroots, " square roots"

do i=1,nroots
    print *, 'Give a number :'
    read *, value
    if (value > 0) then
        root=sqrt(value)
        print *, "The number ",value, " has the root :",root
    else
        print *, "The number ",value, " has no roots"
    end if
end do
```

end program square\_roots

max 132 characters per line



Comment your codes, but not evident things! Indent your codes!

## **Text formatting (free format)**

- Capitalization (upper / lower case) is not important
- Spaces between keywords do not count.
- Maximum 132 characters per line, but

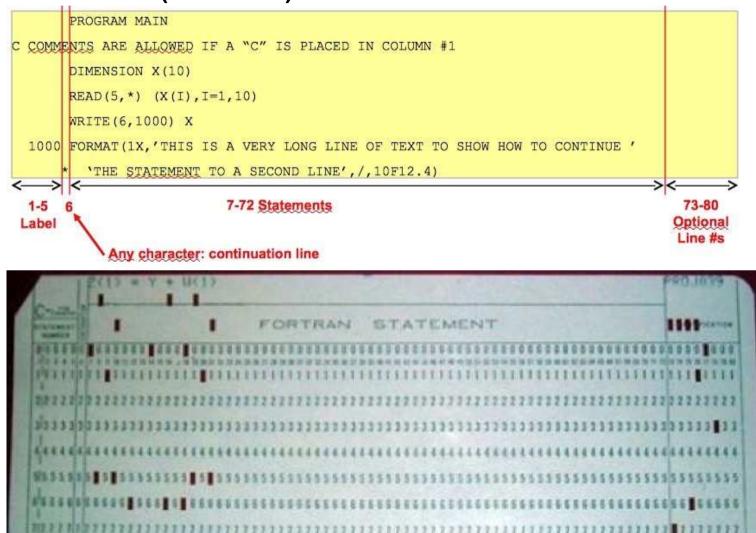
a line ending in & (ampersand) continues on the next line and the & character can be reproduced on the next line

• A semicolon (;) separates two statements on the same line

```
print *, 'Give a number'; read *, n
```

## **Text formatting**

Free format (Fortran 90 and +): file extension .f90 Fixed format (Fortran 77): file extension .f



Names of variables (and other identifiers: constants, procedures, ...)

- •They are composed of a series of alphanumerical characters
  the 1st one is a letter
  limited to 31 characters
- Concerning the letters

the underline character (\_) is considered as a letter

FORTRAN does not distinguish between uppercase and lowercase, except in strings of characters

```
Root ⇔ root
'Root' ≠ 'root'
```

# **§2** Types of variables

REAL(kind=16)

```
There are 5 basic types:
INTEGER

    integer number (positif, zero or negatif)

       • 16 bits (2 bytes): -32.768 \le i \le 32.767
       • 32 bits (4 bytes): -2.147.483.648 \le i \le 2.147.483.647
REAL(kind=4) – real number (simple precision)
       coded on 4 bytes (=32 bits): 1.2 \cdot 10^{-38} \le |x| \le 3.4 \cdot 10^{38}
       Precision: 6 significant digits
REAL(kind=8) — real number (double precision)
       coded on 8 bytes (=64 bits): 2.2 \cdot 10^{-308} \le |x| \le 1.8 \cdot 10^{308}
       Precision: 15 significant digits
COMPLEX
                       complexe number
LOGICAL

    boolean: takes the values .TRUE. or .FALSE.

CHARACTER(len=n) – string of characters (n characters)
          integer :: i = 5
Exemples:
           real(kind=4) :: epsilon = 1e-5
           real :: x ! initial value undetermined
           character(len=26) :: message = "Hello"
    REAL(kind=10) – real number (extended precision)
                                                                        13
```

real number (quadruple precision)

## **Attributes**

The declarations can use the following attributes:

**PARAMETER** : Symbolic constant

**DIMENSION** : Size of a table

**SAVE** : Static object

**EXTERNAL** : External procedure

**INTRINSIC** : Intrinsic procedure

Examples: real, parameter :: pi = 3.1415965 !def of a constant

real :: angle = 2\*pi

#### **Ancient notation (Fortran 77)**

```
! idem to real(kind=4)
real*4 value
                                      ! idem to real(kind=8)
real*8 value precise
double precision value_precise
                                     !idem to real(kind=8)
```



## Specific notation for the numerical values "double precision",

i.e. coded on 64 bits (kind=8)

Example: simple precision double precision

2.5E-82.5D-10

1.2 1.2\_8 variants: dble(1.2) [conversion] [notation F77]

1,2d0

## Code to change the precision of all variables

```
integer, parameter :: r=4 ! single line to modify
real(kind=r) :: x
                               ! num constant coded on r=4 or 8 bytes
x = 2.5 r
```

## **Complex numbers**

Notation: (real part, imaginary part)

```
Example 1: complex :: i = (0,1)

Example 2: integer, parameter :: r = 8
complex(kind=r) :: z
complex(kind=r), parameter :: i = (0_r, 1_r)

z = (3.5_r, 8e-6_r)*i !multiplication by i
```

In the expressions, one can use data of different types



# Implicit declaration versus explicit one

The variables which names start by I, K, L, M, N are considered by default as integer,

the variables starting by other letters are considered as real.

This is more harmful than helpful!

#### Solution:

Always use the implicit none instruction.

The compiler then requires all variables to be declared.

# **Compilation options**

Use:

gfortran -Wall -Wuninitialized code.f90

```
program main
implicit none
integer :: j
print *, " j= ",j
end program main
```

The value of j is not given!

#### arithmetic

Operator	Function	
**	power	T
/	division	
*	multiplication	Priority of the operation
-	substraction	
+	addition	•

Examples: 
$$3.42 + (x-y)/SIN(angle) - x*y/r**3$$
  
 $2**3**2 \Leftrightarrow 2**(3**2) = 512$  (\*\*: priority from right to left)

## **Optimisation of the arithmetic operations**

$$x = a + b*c$$
  
 $y = b*c$ 

! The multiplication is not re-calculated for the 2d time



Do not seek to optimize yourself this kind of operation. The compiler will do the job better than you!

## • arithmetic (continued)



**Trap** (language Fortran and language C)

Which value takes x at the end of the following code?

$$t = 1.0$$
  
 $x = (1/2)*9.81*t**2$  !This formula is incorrect!

The result of the division of two integers is an integer (the entire part of the quotient).

## • of comparison

Old notation	New notation	Meaning
.LT.	<	inferior to
.LE.	<=	inferior or equal to
.GT.	>	superior to
.GE.	>=	superior or equal to
.EQ.	==	equal to
.NE.	/=	different from

Examples: IF 
$$(x \ge y) \Leftrightarrow IF (x .gt. y)$$
IF  $(i/=j)$ 



Compare the real numbers via IF(x == y) is a BAD idea!

Use instead IF (abs(x-y) < 1e-7), e.g.

## • logical

Operator	Example	Meaning
.AND.	A .AND. B	logical AND
.OR.	A .OR. B	logical OR
.NEQV.	A .NEQV. B	logical inequivalence
.XOR.	A .XOR. B	exclusive OR (same as .NEQV.)
.EQV.	A .EQV. B	logical equivalence
.NOT.	.NOT. A	logical negation

## Examples:

Action of the operator .NOT. On a boolean expression 1:

1	.NOT.1	
.true.	.false.	
.false.	.true.	

## **Truth tables**

11	$\mathbf{l_2}$	$l_1$ .AND. $l_2$	$l_1$ .OR. $l_2$
.true.	.true.	.true.	.true.
.true.	.false.	.false.	.true.
.false.	.true.	.false.	.true.
.false.	.false.	.false.	.false.

$\mathbf{l_1}$	$\mathbf{l}_2$	l <sub>1</sub> .EQV. l <sub>2</sub>	l <sub>1</sub> .NEQV. l <sub>2</sub>
.true.	.true.	.true.	.false.
.true.	.false.	.false.	.true.
.false.	.true.	.false.	.true.
.false.	.false.	.true.	.false.

## §5 Tests

•Test "IF - ELSE"

IF (exp) instruction

```
[nom_bloc: ] IF( exp<sub>1</sub> )THEN
                                    bloc<sub>1</sub>
                               [ELSE IF ( exp<sub>2</sub> ) THEN [nom_bloc]
                                    bloc_2
                                    . . .
                               [ELSE [nom_bloc]
                                    bloc_n]]
                                END IF [nom_bloc]
             mom_bloc a label
             exp_i an expression of type LOGICAL,
             bloc<sub>i</sub> a series of FOTRAN instructions
In the simplest case:
```

## §5 Tests

## Multiple tests

Multiple branching based on the value of an expression

```
[ nom_bloc: ] SELECT CASE (expression)
               [ CASE (liste) [ nom_bloc ]
                    bloc<sub>1</sub>]
               [ CASE DEFAULT [ nom_bloc ]
                    bloc_n
               END SELECT [ nom_bloc ]
mom_bloc alabel
expression an expression of type
                                           INTEGER.
    LOGICAL ou CHARACTER,
liste a list of constants of the same type as that of
    expression,
```

**bloc**<sub>i</sub> a series of FOTRAN instructions

```
PROGRAM structure case
§5 Tests
                     integer :: mois, nb_jours
                     logical :: annee_bissext
                             . . .
                     SELECT CASE (mois)
                       CASE (4, 6, 9, 11)
                         nb_jours = 30
                       CASE (1, 3, 5, 7:8, 10, 12)
                         nb_jours = 31
                       CASE (2)
                       -------
                          fevrier: select case (annee_bissext)
                             case (.true.)
                              nb_jours = 29
                             case (.false.)
                              nb_jours = 28
                          end select fevrier
                       CASE DEFAULT
                         print *, ' Numéro de mois invalide'
                     END SELECT
```

END PROGRAM structure\_case

There are many kinds of iterative cycles having each the form:

```
[ block name ] DO [ loop control ]

block

END DO [ block name ]

block name is a label

loop control defines the conditions of executing and stopping the cycle

block is a series of FOTRAN instructions
```

```
1st form: cycle DO with a counter
         DO variable = beginning, end, step
PROGRAM iteration_do
        INTEGER i, somme, n
                                    Cycle on values of i from 1 to n
! affectation de n
                                   with a step of 2
        somme=0
        DO i=1,n,2
          somme=somme+i
        END DO
END PROGRAM iteration_do
```

2d form: DO WHILE (expression)

Executing of the code while the expression is valid.

To avoid infinite cycles, the expression should be able to become false in the block.

#### Example:

! Sum of the numbers from 1 to 100

```
sum = 0
i = 1
do while (i<=100)
    sum = sum + i
end do</pre>
```

**3d form:** DO (with exit via the command exit)

Execution in cycle till getting the command **EXIT** 

```
Example: x = 0.0
do
x = x + 1.0/3
if (x > 10) EXIT
end do
```



For readability, prefer loops do with a counter or do while

Note: the command STOP interrupts all the program.

## Example:

STOP 12 (<— interrupts the program giving "error 12").

#### Instruction CYCLE

CYCLE abandons the current iteration processing and moves on to the next

#### Example:

## §7 Math functions

#### **Basic**

```
absolute value of x (x integer or real)
ABS(x)
                                   square root (\sqrt{x})
SORT(x)
                                   sinus, ... (x in radian)
SIN(x), COS(x), TAN(x)
                                   hyperbolic sinus, ...
SINH(x), COSH(x), TANH(x)
                                   arcsinus, ...
ASIN(x), ACOS(x), ATAN(x)
                                   exponential
EXP(x)
                                   natural logarithm, in base 10
LOG(x), LOG10(x)
                                   modulo: rest of the entire division of a by p
MOD(a,p)
                                   maximum/minimum of x1, ..., xn
MAX(x1,...,xn), MIN(...)
```

## **Complex numbers**

```
REAL(z), AIMAG(z) real/imaginary part of z argument of the complex number (in [-\pi,\pi])
```

## **Special functions (FORTRAN 2008)**

```
\begin{array}{ll} \texttt{ERF}(\texttt{x}) \,, \; \texttt{ERFC}(\texttt{x}) & \quad \text{error function} \\ \texttt{BESSEL\_J0}(\texttt{x}) \,, \; \texttt{BESSEL\_Y0}(\texttt{x}) \,, \; ... & \quad \textbf{Bessel functions} \\ \texttt{GAMMA}(\texttt{x}) & \quad \text{gamma function} \end{array}
```

#### Conversion

```
INT(x) integer part
NINT(x) nearest integer by rounding
```

# **§8** Strings of characters

```
Examples:
           'The result is'
             "It's erroneous."
             "Hello!"
Examples of declarations: > 8 characters (=8 bytes)
character(len=8) :: inputFile, outputFile
character(len=*), parameter :: format="(f4.2,'a')"
Comparison of two strings of characters: == and /=
Concatenation (putting "end-to-end", "in parallel"): //
character(len=*) :: s1 = "Hel"
character(len=*) :: s2 = "lo"
character(len=50) :: entireword
entireword = s1 // s2
```

# §9 Input/output and formats

```
Free-format output:
                         * means that the format is determined automatically
             print *, "The calculation is finished"
             print *, 'counter=', i, '\sin(x)=', \sin(x)
                                                           format
                   print "('Energy = ',F5.1,'eV')"
Formatted output
                   gives the output: Energy = -45.0 eV
Format
             Example Comment
                      integer displayed on 4 characters
T 4
            -555
                       (sp: always display the sign +)
            +555
sp,I4
F8.3
                1.234 real (decimal notation), 8 characters with 3 decimals
             .123E+01
E8.3
                           (exponential notation)
G8.3
            1.23
                           (automatic notation dec/exp) example x=1.234
             .288E+10
                                                       example x=2.88E9
A8
            texte
                       string of characters
                       boolean (logical): T or F (example: L7 displays .false.)
```

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L1

# §9 Input/output and formats

## Formatted output (continued)

```
- leave 7 spaces

- go to the line

2E15.8 - repeat 2 times the format E15.8

3(2X,F5.1)- repeat 3 times "2 spaces and format F5.1"
```

# §9 Input/output and formats

## **Interactive input (from the keyboard)**

```
read *, variable
read "(I4,I4,I4)", i, j, k
read "(3I4)", i, j, k
repetition: 3 times

reading 3 integers
(the user enters e.g. "1 2 3")
```

# §9 Input/output and formats

#### **Files**

choose a channel number

Do not choose neither 5 (keyboard) nor 6 (screen)!

• opening:

```
open(unit=10,file="data")
```

Note: If the file does not exist, it is created.

• opening with error handling:

```
integer :: codeError
open(unit=10,file="data",iostat= codeError)
if (codeError /= 0) then
    print *, "Error no:, codeError
end if
```

reading/writing:

```
write(10,fmt='(I5)') N_particles
read (10,*,iostat=io) Length
```

• closing: close (10)

io is a variable of type integer.

io == 0 if the file is read correctly

io  $\neq$  0 if there is an error (for example, end of file)

# §9 Input/output and formats

#### Other operations with the files

• go to the beginning of the file: rewind(unit=10)

• go back one line: backspace(unit=10)

# **Tables**

Variable containing a vector, a matrix or a multi-dimensional matrix

▶ **Definition of a variable table** containing 100 elements (numbered from 1 to 100)

▶ **Definitions**: rank of a table: number of dimensions

extents of a table : number of elements for each

dimension

size of a table: total number of elements

Filling a table with initial values

mat = reshape([11,21,12,22,13,23],[2,3])

#### ► Display all the elements of a table

The display is done by varying the index 1 first, then the index 2, etc.

#### Example:

dimension(2,2)

11	12
• •	
21	22

—> display: 11 21 12 22

#### ► Assignment of values

real, dimension(10) :: a

a = 0.0

! All the elements are put to 0

a(3) = 555 ! The 3d element equals 555

a(5:10) = 1.0 ! Elements are put to 1 in a part of the table

General syntax: beginning:end:step

If omitted: beginning of the table

If omitted: end of the table

**Examples of calculations with tables:** (automatic parallelism/vectorization!)

• Algebraic operation on multiple components:

```
a(1:10) = b(5,11:20) + 4.0*c(10:1:-1)
```



The matrix multiplication is not written as a\*b but matmul(a,b)

Permutation of columns

```
integer, dimension(4) :: perm = [3, 1, 4, 2]
real, dimension(4) :: departure, arrival
arrival = departure(perm)
```

permutes the columns of departure to obtain arrival

Conditionnal operations: WHERE

#### Example:

#### Command forall: loops running through the indices

Example 1: forall (i=1:3) mat 33(i,i) = 1

Example 2: forall(i=1:N, j=1:N, a(i,j)/=0.0) & b(i,j) = 1.0/a(i,j)

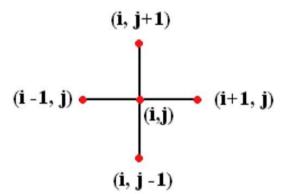
#### Exemple 3:

The command forall allows to program an operation like

$$A_{i,j} = (A_{i-1,j} + A_{i+1,j} + A_{i,j-1} + A_{i,j+1})/4$$

(A: matrix n x n)

to be done on some elements of a table



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real, dimension(n,n) :: A

forall (i=2:n-1, j=2:n-1)  

$$A(i,j) = 0.25*(A(i-1,j) + A(i+1,j) + A(i,j-1) + A(i,j+1))$$
  
end forall

#### **Intrinsic functions**

```
scalar product
DOT PRODUCT(a,b)
                               matrix product
MATMUL(a,b)
                               transposed matrix
TRANSPOSE (a)
                               norm of a vector (FOTRAN2008)
NORM2(a)
                               sum of the elements
SUM(a)
                               sum of the elements of the 2d column
SUM(a, 2)
                               product of the elements
PRODUCT(a)
                               maximal/minimal value
MAXVAL(a), MINVAL(a)
                               position of the maximal/minimal element
MAXLOC(a), MINLOC(a)
                               true if the expression is true for all elements
ALL(logical_expression)
                               true if the expression is true at least for one element
ANY(logical_expression)
COUNT(logical_expression) number of elements for which the expression is true
```

logical expression involving a table, for example a > 0

#### **Dynamic allocation of tables**

Reserve / release the memory area of a table allows to create tables of variable size (size indicated by a variable)

```
real, dimension(:,:,:), allocatable :: tableTemp
! table of rank 3 (without memory space currently associated)

n = 10; m = 5
ALLOCATE(tableTemp(100,n,m)) ! the table is now usable
! operations on the table:
DEALLOCATE(tableTemp) ! the memory space is free now
```



Make sure to respect the limits of the tables!

```
real, dimension(20) :: a
real :: b = 0
do i=1,21
a(i) = i    ! table overflow when i = 21
enddo    ! activate if necessary the option -fbounds-check of the compiler
! Now b = 21 !!!    !
```

# Subroutines and and functions

#### §11 Subroutines

The procedures such as subroutines and functions are used **to structure** long programs and avoid duplicate instructions

```
program main
   call do this(data1)
   call do this(data2)
   x = fonc1(...)
contains
   subroutine do_this(...)
   end subroutine do this
   function fonc1(...)
   end function fonc1
end program
```

Definitions of the subroutines and functions *internal* to the main program

The internal procedures have access to the variables of the main program (unless they are obscured by the declaration of a local variable)

The use of global variables (shared between the main program and the subroutines) is **not recommended**.

(—> place the procedures in a module)

#### §11 Subroutines

Attributes intent (optional attributes but recommended to improve readability)

intent(in): input variable only

The subroutine can not change the value of this variable

intent(out): **output variable** only

The input value can not be used by the subroutine

intent(inout): input and output variable

The subroutine uses the value contained in the input variable,

and modifies it during its execution

Note: A subroutine which has no side effect (no modification of global variables) is said pure.

A pure function can only modify the arguments out and inout and nothing else.

#### §11 Subroutines

```
subroutine convert (x,y,rho,theta,arq5)
                                                model arguments
      (logical_condition) return
   if
                                                 (dummy arguments)
end subroutine convert
Examples of calling a subroutine:
                                            current arguments
 call convert(10.0, 22.0, r, alpha, temp)
 call convert(50.0, -10., r2, alpha2, temp)
or with arguments key-words:
call convert (10.0, y=22.0, arg5=temp, rho=r, theta=alpha)
                                        the order is not important here
```

The command return allows completion of a subroutine run before reaching the end

#### §12 Functions

A function is used to calculate a value from one or more arguments.

Definition of a function:

```
function polynomial(x,y)
  real :: polynomial
  real, intent(in) :: x,y
  ...
  polynomial = x**2 + x*y + 3*y**2
end function polynomial
```

Example of use:

```
valeur = polynome(3., -5.)
```

Calling a function is done without the keyword call (≠ calling a subroutine)

#### Notes:

- The function and its return value have the same name
- Even if a function is allowed in principle to modify the value of arguments, this is strongly discouraged (use a procedure rather than a function)

## §13 Transmit a table as an argument

Easiest way: declare the array argument with an implicit profile

(assumed-shape array)

The compiler is responsible here to transmit to the procedure the information about the table's extents (for each dimension)

## §14 Transmit a function as an argument

In general, it is necessary to define the "interface" of the function (=its arguments and type of return value )

```
program main
   implicit none
   call integr(fonct,0.0,1.0,integral)
...

contains
   function fonct(x)
     real, intent(in) :: x
     real :: fonct
     fonct = (ln(x)/x)**2
     end function
end program
interfal

implicit none
   call integr(fonct,0.0,1.0,integral)

subrouting
   real, interfal
   interfal
   interfal
```

```
subroutine integr(f,a,b,res)
  real, intent(in) :: a,b
  real, intent(out) :: res
  interface
    function f(x)
       real, intent(in) :: x
       real :: f
    end function
  end interface
  val_1 = f(a)
  val_2 = f(b); ...
end subroutine
```

# §15 Procedures with optional arguments

A procedure (subroutine or function) may have optional arguments

```
function erf(x,accuracy)
   real, intent(in) :: x
   real, intent(in), optional :: accuracy
...
   if (present(accuracy)) then
        ...
   else
        ... !do not use accuracy here
   end if
end function
```

This function can be called via

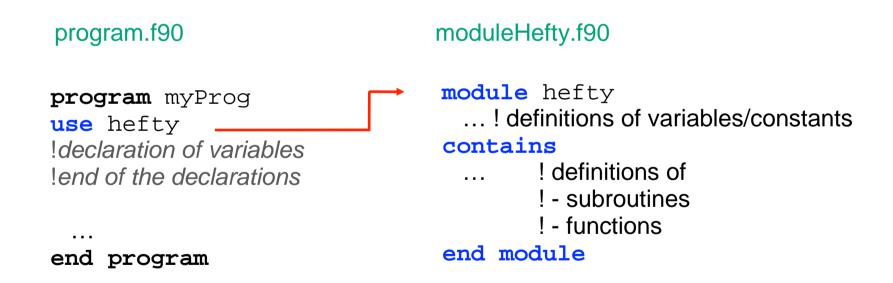
```
value = erf(x=3.)
value = erf(x=3.,accuracy=1E-6)
```

# Modules

In addition to internal procedures, we can define **external procedures**. These procedures are placed in one or more separate files.

#### Interest:

- easy reuse of procedures by other programs
- code structuring (modularity)
- separate compilation of the different files



Compilation: gfortran moduleHefty.f90 program.f90

#### General structure of a module

The quantities defined in a module are automatically accessible from outside (→ global variables) unless they have the attribute "private".

#### **Example 1**: file of constants

In the main program:

```
or use Constants, only : pi, c
```

**Example 2**: global variable declaration file

Use then use VariablesGlobales at the beginning of each file



Restrict the use of global variables as much as possible! => Prefer to explicitly pass all arguments to procedures.

#### **Example 3**:

```
module Matrices
implicit none
contains

subroutine printmat(table2D)
    real, dimension(:,:) :: table2D
    integer :: i
    do

i=lbound(table2D,dim=1),ubound(table2D,dim=1)
        print *, table2D(i,:)
    enddo
    end subroutine

end module
```

end module

#### Example 4:

```
! Note: the name histogram is already used by the function
module ModuleHisto
    implicit none
    integer, parameter:: ww = 4
contains
    function histogram(data, histoMin, histoMax, nbBins)
        real(kind=ww), dimension(:), intent(in) :: data
        real(kind=ww), intent(in) :: histoMin, histoMax
        integer, intent(in) :: nbBins
        real(kind=ww),dimension(:),allocatable :: histogram
        integer :: nbValues, bin, i
        nbValues = size(data)
        allocate(histogram(nbBins))
        histogram = 0
        do i=1,nbValues
            bin = int(1 + (data(i)-histoMin)/(histoMax - histoMin) * nbBins)
            if (bin > nbBins) &
                bin = nbBins
            histogram(bin) = histogram(bin) + 1
        enddo
        !normalisation
        do i=1,nbBins
            histogram(i) = histogram(i)/nbValeurs
        enddo
    end function
```