

# CLab3 Report

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# Chapter 1

## Task1 Two-View DLT based homography estimation.

### 1.1 Selected points

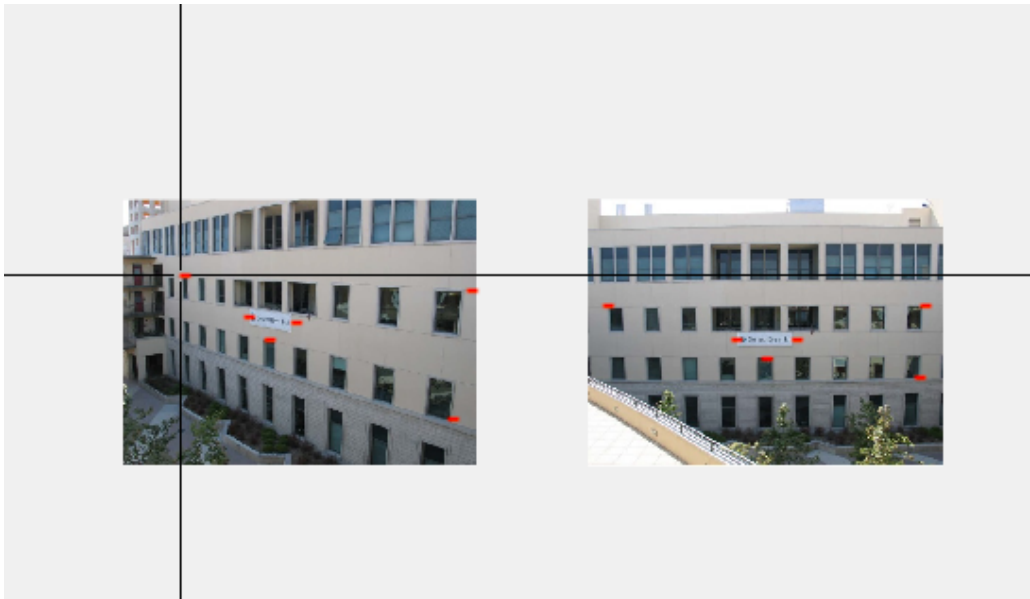


Figure 1.1: task1.4

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## 1.2 Source Code of *Homography*

```
1  function H = homography(u2Trans, v2Trans, uBase, vBase)
2  % Computes the homography H applying the Direct Linear Transformation
3  % The transformation is such that
4  %  $p = H p'$  , i.e.,:
5  %  $(uBase, vBase, 1)' = H * (u2Trans, v2Trans, 1)'$ 
6  %
7  % INPUTS:
8  % u2Trans, v2Trans - vectors with coordinates u and v of the transformed image
9  % uBase, vBase - vectors with coordinates u and v of the original base image po
10 %
11 % OUTPUT
12 % H - a 3x3 Homography matrix
13 %
14 unit=ones(6,1);
15 % image coordinates in the Base image planar
16 p1=[uBase vBase unit]';
17 % image coordinates in the Trans image planar
18 p2=[u2Trans v2Trans unit]';
19
20 [p1_norm, p1_trans]= normalise2dpts(p1);
21 [p2_norm, p2_trans]= normalise2dpts(p2);
22
23
24 % to compute the matrix H, we should construct matrix A
25 A=[];
26 tempA=[];
27 % for every point, we have only two linearly independent equations
28 % I combine them together and get a 12x9 matrix A
29 for i=1:6
30     tempA=[zeros(1,3) (-1)*p2_norm(:,i)' p1_norm(2,i)*p2_norm(:,i)';
31           p2_norm(:,i)' zeros(1,3) -p1_norm(1,i)*p2_norm(:,i)'];
32     A=[A ;tempA];
33 end
34
35 % conduct SVD on matrix A
36 [U,S,V]=svd(A);
37 % the right-most-column of V is the h with least squares
```

---

```

38 h=V(:,end);
39 H=reshape(h,[3, 3])';
40
41 % denormalise H, according to the transformation matrixs
42 H = inv(p1_trans)*H*(p2_trans);
43 end
44
45 % NORMALISE2DPTS - normalises 2D homogeneous points
46 %
47 % Function translates and normalises a set of 2D homogeneous points
48 % so that their centroid is at the origin and their mean distance from
49 % the origin is sqrt(2). This process typically improves the
50 % conditioning of any equations used to solve homographies, fundamental
51 % matrices etc.
52 %
53 % Usage: [newpts, T] = normalise2dpts(pts)
54 %
55 % Argument:
56 % pts - 3xN array of 2D homogeneous coordinates
57 %
58 % Returns:
59 % newpts - 3xN array of transformed 2D homogeneous coordinates. The
60 % scaling parameter is normalised to 1 unless the point is at
61 % infinity.
62 % T - The 3x3 transformation matrix, newpts = T*pts
63 %
64 % If there are some points at infinity the normalisation transform
65 % is calculated using just the finite points. Being a scaling and
66 % translating transform this will not affect the points at infinity.
67
68 function [newpts, T] = normalise2dpts(pts)
69
70 if size(pts,1) ~= 3
71     error('pts must be 3xN');
72 end
73
74 % Find the indices of the points that are not at infinity
75 finiteind = find(abs(pts(3,:)) > eps);
76

```

---

```

77     if length(finiteind) ~= size(pts,2)
78         warning('Some points are at infinity');
79     end
80
81     % For the finite points ensure homogeneous coords have scale of 1
82     pts(1,finiteind) = pts(1,finiteind)./pts(3,finiteind);
83     pts(2,finiteind) = pts(2,finiteind)./pts(3,finiteind);
84     pts(3,finiteind) = 1;
85
86     c = mean(pts(1:2,finiteind)')'; % Centroid of finite points
87     newp(1,finiteind) = pts(1,finiteind)-c(1); % Shift origin to centroid.
88     newp(2,finiteind) = pts(2,finiteind)-c(2);
89
90     dist = sqrt(newp(1,finiteind).^2 + newp(2,finiteind).^2);
91     meandist = mean(dist(:)); % Ensure dist is a column vector for Octave 3.0.
92
93     scale = sqrt(2)/meandist;
94
95     T = [scale    0   -scale*c(1)
96          0       scale -scale*c(2)
97          0        0        1      ];
98
99     newpts = T*pts;
100 end
101
102 function im_warped = ImageWarping(im, H)
103     [u_x, u_y] = GetPointsToTransform(size(im,2), size(im,1));
104     [v_x, v_y] = TransformPointsUsingHomography(inv(H), u_x, u_y);
105     im_warped = BuildWarpedImage(double(im), v_x, v_y);
106     im_warped = uint8(im_warped);
107 end
108
109 function [u_x, u_y] = GetPointsToTransform(width, height)
110     [u_x, u_y] = meshgrid(1:width, 1:height);
111 end
112
113 function [v_x, v_y] = TransformPointsUsingHomography(H, u_x, u_y)
114     v_x = H(1,1)*u_x + H(1,2)*u_y + H(1,3);
115     v_y = H(2,1)*u_x + H(2,2)*u_y + H(2,3);

```

---

```
116         v_z = H(3,1)*u_x + H(3,2)*u_y + H(3,3);
117
118         v_x = v_x./v_z;
119         v_y = v_y./v_z;
120     end
121
122     function im_warped = BuildWarpedImage(im, v_x, v_y)
123         h = size(v_x, 1); w = size(v_x,2);
124         im_warped(:,:,1) = reshape(interp2(im(:,:,1), v_x(:), v_y(:)), [h, w]);
125         im_warped(:,:,2) = reshape(interp2(im(:,:,2), v_x(:), v_y(:)), [h, w]);
126         im_warped(:,:,3) = reshape(interp2(im(:,:,3), v_x(:), v_y(:)), [h, w]);
127     end
```

end of matlab code.

---

### 1.3 *uv* points and $3 \times 3$ H matrix

```
1  uv =
2
3      59.6979   113.1471
4      475.3984   131.5642
5      172.8316   165.7674
6      235.9759   173.6604
7      199.1417   202.6016
8      456.9813   315.7353
9      30.5957    152.7872
10     467.6383   152.7872
11     205.9362   197.2766
12     284.4468   194.6596
13     239.9574   220.8298
14     467.6383   249.6170
15
16
17  H =
18
19     -0.2992    -0.1447   -14.6125
20      0.0745    -0.8213    41.9147
21      0.0009    -0.0004    -0.7033
```



---

## 1.4 Homography Result

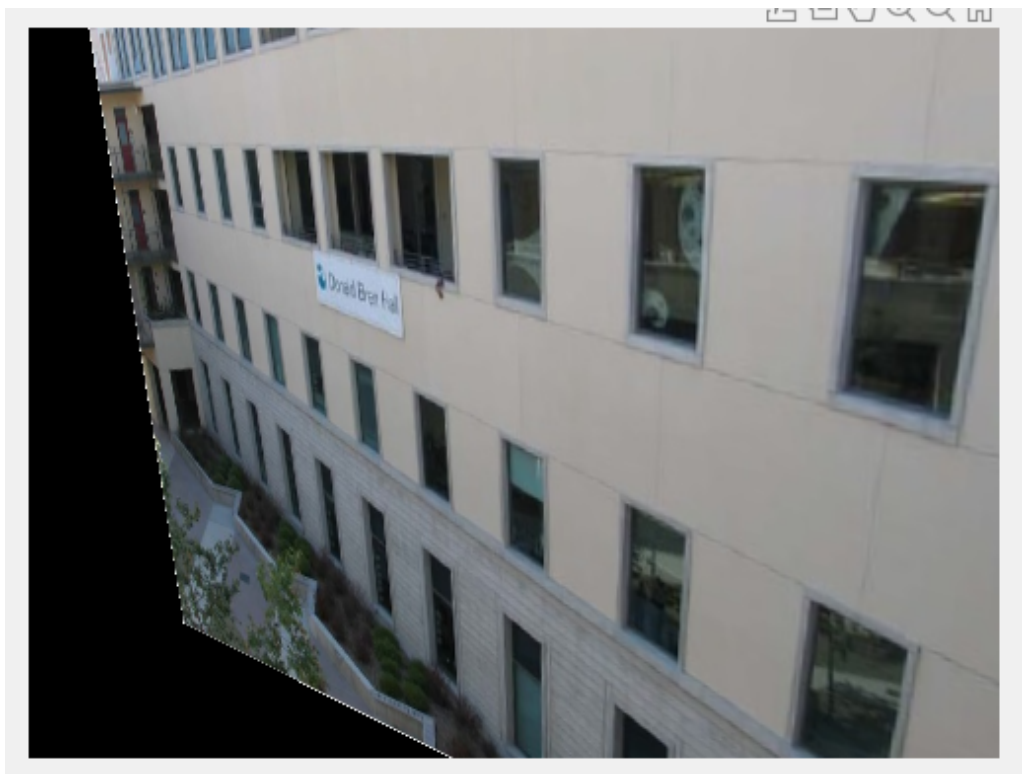


Figure 1.2: task1.4

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## 1.5 Factors of Homography Results

### 1.5.1 *Pointnumbers*

In the case where there are more than 4 point correspondences available, I took 12 points to provide more references for calculating the H matrix. And this minimizes the error generated from points. Some experiments were tried and the factors were listed.

### 1.5.2 *Distanceofselectedpoints*

The simplest way to minimize the error is to minimize the algebraic distance of selected points. To ensure that the  $h$  selected isn't the zero vector we add the constraint that  $\|h\| = 1$ . The unit singular vector corresponding to the smallest singular value of A. This can be found using SVD. However, this is not so geometrically meaningful.

### 1.5.3 *Geometricdistance*

The geometric distance measures the Euclidian image distance between where the homography maps a point and where the point's correspondence was originally found. This defines the transfer error.

The correspondences  $\mathbf{x}_i \rightarrow \mathbf{x}'_i$  is:

$$\sum_i d(\mathbf{x}'_i, H\mathbf{x}_i)^2$$

Where d is the geometry distance. With consider of forward and backward transpose,

$$\sum_i d(\mathbf{x}'_i, H\mathbf{x}_i)^2 + d(\mathbf{x}_i, H^{-1}\mathbf{x}'_i)^2$$

## Chapter 2

# 3D-2D Camera Calibration

### 2.1 Implementation of Calibrate

```
1  %% Task 2
2  img_a = imread('CLab3_Materiala/stereo2012a.jpg');
3  XYZ = load(CLab3_Materiala/XYZ.txt)
4  [u, v] = load(CLab3_Materiala/ux.txt)
5  plot(u, v, 'ro');
6
7  C = calibrate(img_a,XYZ,[u,v]);
8  disp(C);
9  %% calc K, R, T
10 [K, R, t] = vgg_KR_from_P(C);
11 disp('K = ');
12 disp(K);
13 disp('R = ');
14 disp(R);
15 disp('t = ');
16 disp(t);
17 %calculate focal
18 alpha = K(1,1);
19 gama = K(1,2);
20 thelta = acot(gama/-alpha);
21 fx = abs(alpha);
22 fy = abs(K(2,2)*sin(thelta));
23 f = sqrt(fx^2+fy^2);
```

---

```

24 disp(['fx: ',num2str(fx)]);
25 disp(['fy: ',num2str(fy)]);
26 disp(['focal: ',num2str(f)]);
27
28 %% calibrate function
29 function C = calibrate(im, XYZ, uv)
30 [len,~] = size(uv);
31
32 A = zeros(len*2,12);
33
34 for tmp = 1:len
35     %get the 3D vertices and their 2D corresponding points
36     X = XYZ(tmp,1);
37     Y = XYZ(tmp,2);
38     Z = XYZ(tmp,3);
39
40     u = uv(tmp,1);
41     v = uv(tmp,2);
42
43     A(tmp*2-1,:) = [X,Y,Z,1,0,0,0,0,-u*X,-u*Y,-u*Z,-u];
44     A(tmp*2,:) = [0,0,0,0,X,Y,Z,1,-v*X,-v*Y,-v*Z,-v];
45 end
46 [~,~,V] = svd(A);
47
48 C = V(:,end);
49 C = C/C(end);
50 C = reshape(C,[4 3]);
51 C = C';
52
53 imshow(im);
54 hold on;
55 plot(uv(:,1),uv(:,2),'ro');
56 hold on;
57 xyz1 = [XYZ,ones(tmp,1)]';
58 xy = C*xyz1;
59
60 xy(1,:) = xy(1,:)./xy(3,:);
61 xy(2,:) = xy(2,:)./xy(3,:);
62

```

---

```
63 distance = (xy(1:2,:) - uv').^2;
64 distance = mean(sum(distance));
65 disp(['Mean Square Error: ',num2str(distance)]);
66
67 plot(xy(1,:),xy(2:,:), 'g+');
68 end
```

## 2.2 Experiment Result of 2012a

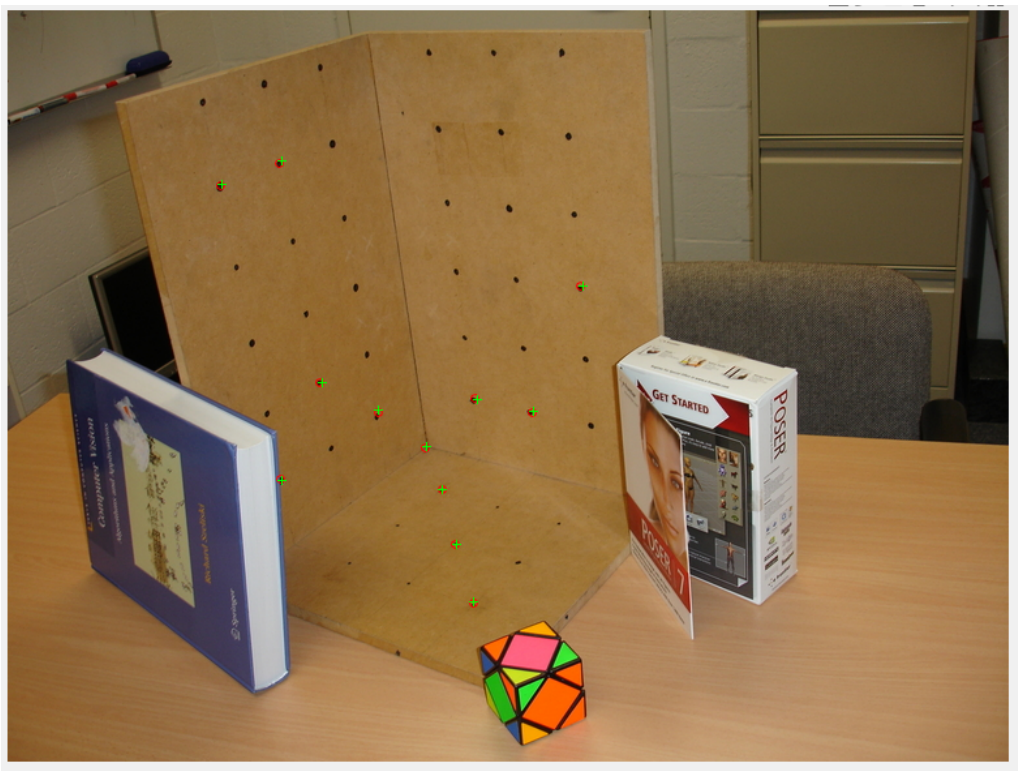


Figure 2.1: task2

---

## 2.3 $3 \times 4$ Matrix C

```
1 C =
2 -15.5043 -10.7309 -6.9259 315.9230
3 -16.4116 -10.9395 -7.3210 325.9015
4 -0.0475 -0.0323 -0.0234 1.0000
5
6 MSE =
7 2.7535
```

## 2.4 Matrix K, R, t

Decompose the C matrix into K, R, t, such that  $C = K[R|t]$

```
1 K =
2 5.4072 9.9570 323.7067
3 0 10.9062 339.0619
4 0 0 1.0000
5
6 R =
7 0.4505 -0.8528 0.2642
8 -0.4590 0.0326 0.8878
9 -0.7657 -0.5213 -0.3767
10
11 t =
12 -2.2690
13 19.8003
14 20.0155
```

---

## 2.5 Focal length and Angle

### 2.5.1 what is the focal length of the camera, and in what unit of measurement?

```
1  fx: 5.4072
2  fy: 5.2047
3  focal: 7.5051
```

The focal length of the camera is 7.5 cm.

### 2.5.2 what is the pitch angle of the camera with respect to the X-Z plane in the world coordinate system?

```
1  theta =
2  88.995
```

The angle of the camera should be around 90 degree to X-Z plane.