JMO Spectrum Library Documentation

Version 1.3, July 18th, 2020

Julius Muschaweck, JMO GmbH, Zugspitzstr. 66, 82131 Gauting, Germany. julius@jmoptics.de

Rationale

We deal routinely with spectra in illumination optics. We need to analyze LED spectra, compute color coordinates and color rendering values from spectra, integrate them, add spectra, multiply spectra with scalar weights and with other spectra (like transmission spectra), interpolate a given measured spectrum with non-equidistant wavelength values to a regular 1 nm array, and so on.

In practice, this is tedious: spectra come in various formats, and the problem of dealing with two spectra als tabulated values which have two different sets of wavelengths is annoying. In addition, many colorimetric calculations, from computing simple x/y coordinates all the way to the color rendering index, are not easily accessable.

This open source Matlab library is designed to make these engineering tasks easy and transparent. It is compatible with GNU Octave, and with Matlab for Mac and Linux.

License -- public domain

I release this software into the public domain under CC0

Version history

Version 1.3

Revised PlanckSpectrum to include refractive index.

Added RGBLEDSpectrum class to model spectra of RGB LEDs under actual operating conditions, based on data sheet and binning information only.

Added ShiftToLDom function, shifting a spectrum such that the result has a desired dominant wavelength

Version 1.24, July 4, 2020

Fixed bug in AddSpectra, where two spectra with different additional fields could not be added.

Version 1.23, Jan 25, 2020

Fixed a bug in CRI (van Kries transformation was first computed but then ignored).

Added Integrate Spectrum, to integrate a spectrum, with an optional weighting spectrum

Version 1.22, Jan 24, 2020

Added ComputeSpectrumColorimetry, convenience function to compute XYZ, CCT and color rendering values in one call

Added Vlambda, returning V(lambda), CIE 1924 as a spectrum

Added PlotClExyBorder, plotting the CIE x/y "color horseshoe", with optional ticks and other options

MakeSpectrum now accepts optional Name/Value pairs to set fields like e.g. 'name'

CCT and CCT_from_xy have additional return values ok and errmsg, to suppress errors and warnings if desired

Version 1.21, Jan 24, 2020

Added CCT, convenience function to compute CCT from spectrum directly, not via x/y

Added Example_WhiteLED.m as an example script composing a white LED from blue and yellow, with supporting spectra blue.sre and yellow.sre

Added LDomPurity, to compute dominant wavelength and purity of a spectrum

Added ReadLightToolsSpectrumFile, to read LightTools .sre files, as supplied by many LED vendors. Reads also simple ASCII 2-column tables with any text header

Version 1.2, Jan. 22, 2020

Added CIE standard illuminants

Added CRI (color rendering index) computations

Added AssignNewWavelength function

Version 1.01, Oct. 13:

Added WriteLightToolsSpectrumFile

Version 1.0, Sept. 9, 2019: Initial version

Getting started

To define a spectrum and compute its CIE xy color coordinates, simply say

```
clear s;
s.lam = [360 830];
s.val = [1 1];
% this is a flat spectrum, known as CIE standard illuminant E.
% By definition, it should have color coordinates x == y == 1/3-
s.XYZ = CIE1931_XYZ(s);
% This is a common pattern: Compute information from a spectrum, and then
% add this information to the same spectrum as an additional field
s
```

```
s = struct with fields:
    lam: [360 830]
    val: [1 1]
    XYZ: [1×1 struct]
```

s.XYZ

```
ans = struct with fields:
    X: 106.8654
    Y: 106.8569
    Z: 106.8919
    x: 0.3333
    y: 0.3333
```

Design decisions

val: [1 1]

hopp: "topp"

name: "CIE standard illuminant E"

Spectrum

In this library, a *spectrum* is a struct with at least two fields named lam and val, which meet the following requirements:

- 1. 1am is a 1D vector of numeric values which are not complex, > 0, and strictly ascending
- 2. val is a 1D vector of numeric values which are not complex.
- 3. 1am and val are of same length and have at least two elements

It is desirable for lam and val to be column vectors.

There is a function rv = SpectrumSanityCheck(rhs), which tests all these requirements and, if met, returns the same struct except that lam and val are converted to column vectors if necessary.

A *spectrum* models the function S(lambda) which represents a physical scalar function of wavelength. Like spectral radiant flux, spectral irradiance, spectral radiant intensity, spectral radiance, spectral transmission, spectral absorption, spectral efficiency. The tabulated values in val are linearly interpolated. Outside the range given by lam, S(lambda) == 0. Accordingly, there are no spectra consisting of truly monochromatic lines in this library. If you want to approximate line spectra, make very narrow triangles. Spectra are continuous, except at the wavelength boundaries, where the jump to zero

lam is considered to have units of nanometers in all library functions that make use of this unit, e.g. color calculations.

Why structs and not classes? Classes are nice to guarantee that properties like 1am and val always are present, and would allow methods which operate directly on spectra. However, structs are simpler and more versatile. I, as the library designer, cannot know which additional information a user (I myself, for example), wants to attach to a given spectrum. Name, date, name of LED, color coordinates and more. To make a spectrum s, I can simply say

```
clear s
nfig = 0; %figure number to be used in examples
s.lam = [360 830];
s.val = [1 1];
s.name = "CIE standard illuminant E";
s.hopp = "topp";
s

s = struct with fields:
    lam: [360 830]
```

to give it an appropriate name and an arbitrary value in an arbitrary additional field. Of course, a user can always create a subclass to add properties to a given class, but it is just so much simpler to assign to an

additional struct field in a single line. In my experience, these conventions for spectra are simple and few enough to be easily remembered and adhered to.

Conventions

In my code, I like to have long unabbreviated variable and function names. Except for a few standards:

rv is my name for the return value of a function

spec is my name for a single spectrum argument of a function.

1hs and rhs are short for 'left hand side' and 'right hand side', the arguments of a binary function.

Proper library function names start with capital letters, e.g. MakeSpectrum. Internal helper functions start with a small "i", e.g. iLinInterpolProto.

A spectrum struct is valid if it has fields lam and val which fulfill the requirements above. In addition, I assume a spectrum may have the following fields:

name: A short character string with a name.

description: A longer character string with a description.

XYZ: A struct with tristimulus and color coordinate fields X, Y, Z, x, y, z, typically created by code like s.XYZ = CIE1931 XYZ(s)

Function reference

Alphabetic list

AddSpectra adds two spectra

AddWeightedSpectra adds multiple spectra with weights

AssignNewWavelength replaces the wavelength of a spectrum, interpolating the values correctly

CCT, convenience function to compute CCT from spectrum directly, not via x/y

CCT_from_xy computes correlated color temperature and uv-distance to Planck locus from spectrum

CIE1931_lam_x_y_z.mat contains CIE 1931 data for color matching functions, monochromatic border and Planck locus

CIE1931_XYZ computes CIE 1931 XYZ color coordinates and tristimulus values from spectrum

CIE_Illuminant returns a large selection of CIE standard illuminants

CIE_Illuminant_D computes the CIE standard daylight spectrum as function of color temperature

CODATA2018 returns a struct with CODATA 2018 values for relevant physical constants (speed of light, Boltzmann constant etc.)

ComputeSpectrumColorimetry, convenience function to compute XYZ, CCT and color rendering values in one call

CRI computes Color Rendering Index values according to CIE 13.3-1995

Example_WhiteLED.m as an example script composing a white LED from blue and yellow, with supporting spectra blue.sre and yellow.sre

GaussSpectrum creates a Gaussian spectrum for given mean and standard deviation

IntegrateSpectrum, integrate a spectrum, with an optional weighting spectrum

IsOctave determines if running on GNU Octave or Matlab

IsSpectrum checks if a spectrum is valid

LDomPurity, to compute dominant wavelength and purity of a spectrum

LinInterpol computes linear interpolation like interp1, but about five times faster on Matlab on Windows

LinInterpolAdd4Async computes linear interpolation of the sum of four functions

MakeSpectrum creates a valid spectrum from wavelength and value data

MultiplySpectra multiplies two spectra, e.g. an LED spectrum with a transmission spectrum

PlanckLocus returns a wealth of information about the Planck locus, including interpolation function objects and Judd lines of equal CCT

PlanckSpectrum creates a blackbody spectrum with various normalizations to choose from

PlotCIExyBorder, plotting the CIE x/y "color horseshoe", with optional ticks and other options

ReadLightToolsSpectrumFile, to read LightTools .sre files, as supplied by many LED vendors. Reads also simple ASCII 2-column tables with any text header

RGBLEDSpectrum is a class to model RGB LED spectra at operating conditions, based solely on data sheet information

ShiftToLDom shifts the wavelengths of a given spectrum such that a desired dominant wavelength results

SpectrumSanityCheck performs a detailed diagnosis if a spectrum fails to fulfill the requirements, returns a sanitized spectrum otherwise

TestLinInterpol tests the LinInterpol function

Vlambda, returning V(lambda), CIE 1924 as a spectrumCRI is a class for computing color rendering index values

WriteLightToolsSpectrumFile writes a spectrum to an ASCII file in LightTools® format.

AddSpectra

Adds two spectra without weights. Convenience function with simpler interface than AddWeightedSpectra

% function rv = AddSpectra(lhs, rhs)

Input: 1hs, rhs: Both must be valid spectra.

Output: rv: Sum of rhs + 1hs. When both spectra do not overlap, the wavelength ranges are concatenated, and the range in between is padded with zero. If they do overlap, then rv.lam contains all values from both input spectra, with duplicate values removed, and what is added are the linearly interpolated values from both input spectra. Thus, the sum spectrum is a perfect model of the underlying continuous function which is the sum of the continuous, linearly interpolated input spectra.

Additional fields present in 1hs or rhs will be stripped, rv will have only fields 1am and val.

Usage Example:

```
clear s1 s2 sumspec
s1 = MakeSpectrum([400,500,600],[1, 2, 4]);
s2 = MakeSpectrum([400,560,610],[4, 4, 1]);
sumspec = AddSpectra(s1,s2);
nfig = nfig + 1;
figure(nfig);
clf;
hold on;
plot(s1.lam, s1.val, 'Marker', 'x');
plot(s2.lam, s2.val, 'Marker', 'x');
plot(sumspec.lam, sumspec.val, 'Marker', 'x');
legend({'s1','s2','sumspec'},'Location','NorthWest');
axis([390 610 0 8]);
grid on;
xlabel('lam');
ylabel('val');
title('AddSpectra demo');
```

AddWeightedSpectra

Computes weighted sum of several spectra.

```
% function rv = AddWeightedSpectra(spectra,weights)
```

Input:

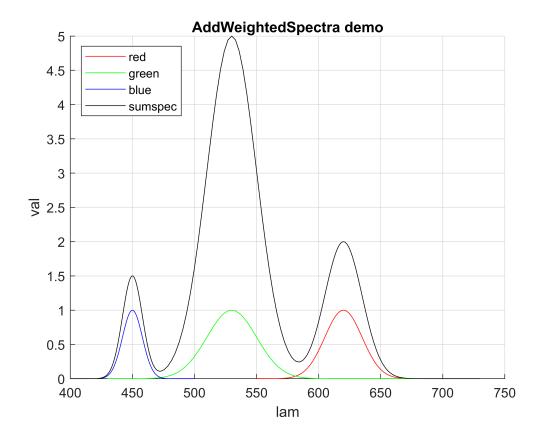
spectra: Nonempty cell array of spectra

weights: Vector of numeric non-complex values, same length as spectra.

Output: rv: Weighted sum of input spectra. When spectra do not overlap, the wavelength ranges are concatenated, and the range in between is padded with zero. If they do overlap, then rv.lam contains all values from all input spectra, with duplicate values removed, and sorted, and what is added are the linearly interpolated values from all input spectra. Thus, the sum spectrum is a perfect model of the function which is the sum of the continuous, linearly interpolated input spectra.

Additional fields present in spectra will be stripped, rv will have only fields lam and val.

```
clear red green blue sumspec
red = GaussSpectrum(linspace(550,700),620,15);
green = GaussSpectrum(linspace(430,730),530,20);
blue = GaussSpectrum(linspace(400,500),450,8);
sumspec = AddWeightedSpectra({red, green, blue},[2, 5, 1.5]);
nfig = nfig + 1;
figure(nfig);
clf;
hold on;
plot(red.lam, red.val, 'r');
plot(green.lam, green.val, 'g');
plot(blue.lam, blue.val, 'b');
plot(sumspec.lam, sumspec.val, 'k');
legend({'red', 'green', 'blue', 'sumspec'}, 'Location', 'NorthWest');
grid on;
xlabel('lam');
ylabel('val');
title('AddWeightedSpectra demo');
```



AssignNewWavelength

Assign a new wavelength vector to a spectrum, interpolating the old values.

```
% function rv = AssignNewWavelength(spectrum, lam_new)
```

Input:

spectrum: a spectrum

lam_new: the new wavelength array, ascending doubles.

Output:

rv: A copy of the old spectrum with all fields, but lam is replaced and val is interpolated. For lam_new values outside the old interval, val(i) == 0

Usage Example:

```
s_old = MakeSpectrum([400 500], [0 100]);
s_new = AssignNewWavelength(s_old, [450 451 452])

s_new = struct with fields:
    lam: [450 451 452]
    val: [50 51 52]
```

CCT

convenience function to compute CCT from spectrum directly, not via x/y

```
% function [iCCT, dist_uv, ok, errmsg] = CCT(spectrum)
```

Input:

spectrum: a spectrum with fields lam and val

Output:

iCCT: Correlated color temperature in Kelvin

dist_uv: Distance to Planck locus in u/v color space. When dist_uv>0.05, a warning is issued, when dist_uv > 0.09, an error. Positive when x/y is above Planck locus (on the "green" side), negative when below.

ok: true if CCT can be properly computed, i.e. dist_uv <= 0.9 and CCT within 1000..Inf range. false if something went really wrong

errmsg: empty '' if everything is ok, 'error: ...' if ok==false, 'warning: ...' e.g. if dist_uv > 0.05', which makes the CCT computation technically illegal.

If ok is not queried as a return value, warnings and errors are raised. If ok is queried, they are suppressed.

Usage Example:

```
test = CIE_Illuminant('D65'); % 6500K CIE daylight spectrum, slightly above Planck
[iCCT, dist_uv] = CCT(test) %#ok<ASGLU> % not exactly 6500, depends on step size of XYZ integral
iCCT = 6.5008e+03
dist_uv = 0.0032
```

CCT_from_xy

Compute correlated color temperature of an xy color point. Uses parabolic interpolation between nearest Planck locus points

```
% function [CCT, dist_uv, ok, errmsg] = CCT_from_xy(x,y)
```

Input: x, y scalar numbers, x/y color coordinates

Output:

CCT: Correlated color temperature in Kelvin

dist_uv: Distance to Planck locus in u/v color space. When dist_uv>0.05, a warning is issued, when dist_uv > 0.09, an error. Positive when x/y is above Planck locus (on the "green" side), negative when below.

ok: true if CCT can be properly computed, i.e. dist_uv <= 0.9 and CCT within 1000..lnf range. false if something went really wrong

errmsg: empty '' if everything is ok, 'error: ...' if ok==false, 'warning: ...' e.g. if dist_uv > 0.05', which makes the CCT computation technically illegal.

If ok is not queried as a return value, warnings and errors are raised. If ok is queried, they are suppressed.

Usage Example:

```
clear T pl jl uv den x y CCT dist_uv
T = 3456;
pl = PlanckLocus;
jl = pl.JuddLine_func(T);
% compute uv coordinates for color point with CCT == T,
% 0.04 away from Planck
uv = [jl.u, jl.v] + 0.04 * [jl.du, jl.dv];
% compute xy coordinates by standard transformation
den = 2*uv(1) - 8*uv(2) + 4;
x = 3*uv(1)/den;
y = 2 * uv(2) / den;
% compute CCT
[iCCT, dist_uv] = CCT_from_xy(x,y);
iCCT - T % should be zero, is about 1.3 mK
```

```
ans = 0.0013
```

```
dist_uv - 0.04 % should be zero
```

```
ans = -4.3835e-07
```

CIE1931_lam_x_y_z.mat

A .mat file which contains a struct named 'CIE1931XYZ' with CIE 1931 data: x/y/z color matching functions, monochromatic border x/y coordinates with corresponding wavelengths, and coordinates of the Planck locus with corresponding absolute temperatures.

```
clear CIE1931XYZ;
```

```
load('CIE1931_lam_x_y_z.mat','CIE1931XYZ')
CIE1931XYZ
```

```
CIE1931XYZ = struct with fields:
    lam: [471×1 double]
        x: [471×1 double]
        y: [471×1 double]
        z: [471×1 double]
        xBorder: [471×1 double]
        yBorder: [471×1 double]
        yBorder: [1001×1 double]
        PlanckT: [1001×1 double]
        Plancky: [1001×1 double]
```

CIE1931_XYZ

Computes CIE 1931 color coordinates.

```
% function rv = CIE1931_XYZ(spec)
```

Input: spec is a *spectrum* struct, see above for requirements.

Output: A struct with fields X Y Z x y z.

Capital X Y Z are the CIE tristimulus values, i.e. the result of integrating spec with the CIE 1931 standard x y z color matching functions.

x y z are the corresponding color coordinates, x = X / (X + Y + Z) etc.

Usage example:

```
clear s;
s.lam = [360 830];
s.val = [1 1];
% this is a flat spectrum, known as CIE standard illuminant E.
% By definition, it should have color coordinates x == y == 1/3-
s.XYZ = CIE1931_XYZ(s);
% This is a common pattern: Compute information from a spectrum, and then
% add this information to the same spectrum as an additional field
s

s = struct with fields:
    lam: [360 830]
    val: [1 1]
    XYZ: [1×1 struct]
```

s.XYZ

```
ans = struct with fields:

X: 106.8654

Y: 106.8569

Z: 106.8919

x: 0.3333

y: 0.3333

z: 0.3334
```

CIE_Illuminant

Returns CIE standard illuminants.

Available spectra are:

```
'A';'D65';'C';'E','D50';'D55';'D75';'FL1';'FL2';'FL3';'FL4';'FL5';'FL6';'FL7';'FL8';'FL9';'FL10';'FL11';'FL12';
```

'FL3_1';'FL3_2';'FL3_3';'FL3_4';'FL3_5';'FL3_6';'FL3_7';'FL3_8';'FL3_9';'FL3_10';'FL3_11';'FL3_12'; 'FL3_13';'FL3_14';'FL3_15'; 'HP1';'HP2';'HP3';'HP4';'HP5'

```
% function rv = CIE_Illuminant(name, varargin)
```

Input: name is the desired name, one of the available names listed above

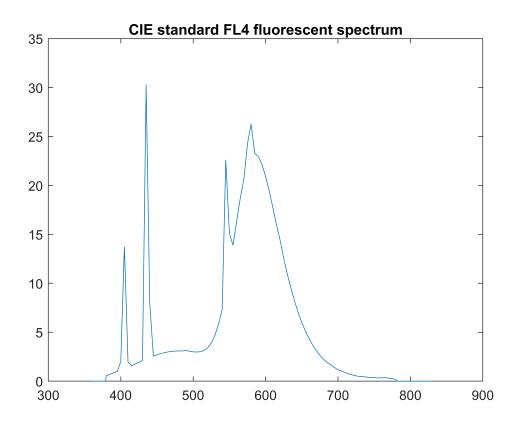
varargin: Name/Value pair 'lam',lam to define the desired wavelength table to which the illuminant spectrum will be interpolated. Default is 360:830 nm in 1 nm steps

Output: spectrum struct with fields lam (copy of input, or default 360:830), val and name (copy of input name)

```
FL4 = CIE_Illuminant('FL4')

FL4 = struct with fields:
    lam: [1×471 double]
    val: [1×471 double]
    name: 'CIE standard illuminant FL4'

clf;plot(FL4.lam,FL4.val);
title('CIE standard FL4 fluorescent spectrum')
```



CIE_Illuminant_D

Returns CIE standard daylight illuminant D as function of CCT.

```
% function rv = CIE_Illuminant_D(CCT, varargin)
```

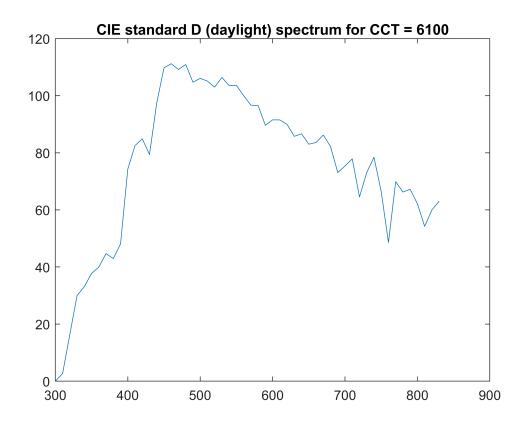
Input: CCT is the desired color temperature. Must be in [4000, 25000].

varargin: Name/Value pair 'lam',lam to define the desired wavelength table to which the illuminant spectrum will be interpolated. Default is 360:830 nm in 1 nm steps

Output: spectrum struct with fields lam (copy of input, or default 360:830), val and name (copy of input name)

Usage Example:

```
D6100 = CIE_Illuminant_D(6100, 'lam', 300:5:830);
clf;plot(D6100.lam, D6100.val);
title('CIE standard D (daylight) spectrum for CCT = 6100');
```



CODATA2018

A struct with the most relevant physical constants for optics, as defined by CODATA

```
% function cd = CODATA2018()
```

Input: None

Output: Struct with fields:

b: Wien's wavelength displacement law constant

bprime: Wien frequency displacement law constant

c: speed of light in vacuum

e: elementary charge

h: Planck constant

k: Boltzmann constant

me: electron mass

mn: neutron mass

mp: proton mass

NA: Avogadro constant

R: molar gas constant

Vm: molar volume of ideal gas

sigma: Stefan-Boltzmann constant

c1: first radiation constant (2 pi h c^2)

c1L: first radiation constant for spectral radiance (2 h c^2)

c2: second radiation constant (h c / k)

Each field is a struct with fields name, value, reluncertainty, absuncertainty, unit. Most uncertainties are zero, since 2018.

Usage Example:

```
clear cd lambda freq pe c
cd = CODATA2018();
lambda = 500e-9; % in meters
c = cd.c.value % speed of light
```

```
c = 299792458
```

```
freq = c/lambda% frequency of 500 nm light about 600 THz
```

```
freq = 5.9958e + 14
```

```
pe = freq * cd.h.value % energy of a 500 nm photon, in Joule
```

```
pe = 3.9729e-19
```

ComputeSpectrumColorimetry

convenience function to compute XYZ, CCT and color rendering values in one call

```
% function rv = ComputeSpectrumColorimetry(s, varargin)
```

Takes the spectrum struct and adds fields with computed colorimetric values:

XYZ: struct with fields x, y, z, X, Y, Z as returned from CIE1931_XYZ(s)

CCT, dist_uv_Planck: color temperature and distance to Planck locus (may be NaN if out of CCT range)

CRI_all: struct with all 16 Ri and Ra as returned from CRI.FullCRI(s) (may be NaN if out of CCT range)

Ra: number, general CRI value

Also performs optional normalization to peak = 1

Input:

s: spectrum, struct with fields lam and val.

varargin: Name/Value pair: 'Normalize', 'peak' | 'off' (default)

Normalize -> 'peak' scales spectrum .val to have peak = 1

Normalize -> 'off' leaves .val unchanged

Output:

rv: the spectrum, with added fields and possibly scaled .val field. Other fields in s, like e.g. .name, remain unchanged

Usage Example:

```
test = MakeSpectrum([400 700],[1 1],'hopp',42); % hopp is just some field to show it remains
ComputeSpectrumColorimetry(test)
```

CRI

A class to compute color rendering indices. See https://en.wikipedia.org/wiki/Color_rendering_index, and CIE 13.3-1995 Technical Report

```
% classdef CRI < handle
```

Constructor:

```
% function this = CRI()
cri = CRI()

cri =
    CRI with properties:
    CRISpectra_: [1×16 struct]
    strict_5nm_: 0
```

loads the CRI reflectivity spectra into the read-only variable CRISpectra_

SetStrict_5nm

```
% function prev = SetStrict_5nm(this, yesno)
prev = cri.SetStrict_5nm(true)

prev = logical
0

% do something
cri.SetStrict_5nm(prev); % restore previous state
```

sets the internal wavelength interval to 5 nm or 1 nm

Input: yesno: logical (true -> 5nm, false -> 1nm)

Output: prev: logical, the value before the call

SingleRi

computes a special Ri value

```
% function rv = SingleRi(this, spectrum, i)
FL4 = CIE_Illuminant('FL4');
D65 = CIE_Illuminant('D65');
cri.SingleRi(FL4,9) % Really really bad R9, fluorescent and saturated red don't work well
ans = -110.6599
cri.SingleRi(D65,9) % By definition, CIE D should work perfectly for CCT > 5000
ans = 99.9511
```

Ra

ans = 99.9866

computes the general Ra, the by far most used value

```
% function [rv, Ri_1_8] = Ra(this, spectrum)
cri.Ra(FL4) % CRI is designed to give 51

ans = 51.5163

cri.Ra(D65) % by definition, 100
```

15

Input: a spectrum

Output: rv: double, the Ra value.

Ri_1_8: array of eight doubles, the individual Ri values of which Ra is the mean

FullCRI

computes the CRI for all sixteen reflectivity spectra. R1..R14 are defined in the standard, R15 is Asian skin, and R16 (my personal addition) is perfect white

```
% function rv = FullCRI(this, spectrum)
cri.FullCRI(FL4)
```

ans = struct with fields:
 Ri: [16×1 double]
 Ra: 51.5163

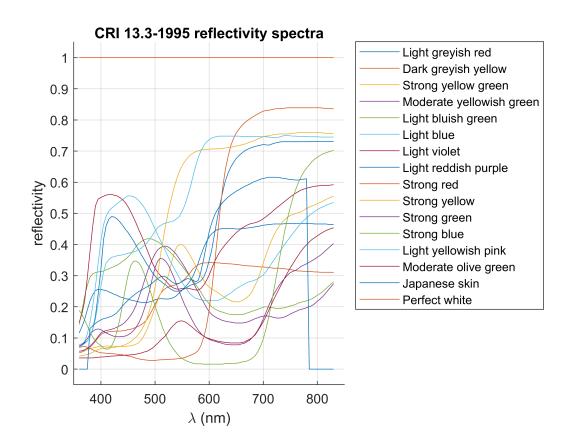
Input: a spectrum

Output: rv: a struct with fields Ri (array of 16 doubles, the individual Ri values), and Ra (the general index)

PlotCRISpectra

plots the 16 reflectivity spectra

```
% function PlotCRISpectra(this)
cri.PlotCRISpectra();
```



CRISpectra_

a read-only property. An array of 16 structs with fields describing the individual spectra:

cri.CRISpectra_

ans = 1×16 struct

Fields	lam	val	name	description	munsell
1	1×471 double	1×471 double	'TCS01'	'Light grey	'7.5 R 6/4'
2	1×471 double	1×471 double	'TCS02'	'Dark greyi	'5 Y6/4'
3	1×471 double	1×471 double	'TCS03'	'Strong yel	'5 GY 6/8'
4	1×471 double	1×471 double	'TCS04'	'Moderate y	'2.5 G 6/6'
5	1×471 double	1×471 double	'TCS05'	'Light blui	'10 BG 6/4'
6	1×471 double	1×471 double	'TCS06'	'Light blue'	'5 PB 6/8'
7	1×471 double	1×471 double	'TCS07'	'Light violet'	'2.5 P 6/8'
8	1×471 double	1×471 double	'TCS08'	'Light redd	'10 P 6/8'
9	1×471 double	1×471 double	'TCS09'	'Strong red'	'4.5 R 4/13'
10	1×471 double	1×471 double	'TCS10'	'Strong yellow'	'5 Y 8/10'
11	1×471 double	1×471 double	'TCS11'	'Strong green'	'4.5 G 5/8'
12	1×471 double	1×471 double	'TCS12'	'Strong blue'	'3 PB 3/11'
13	1×471 double	1×471 double	'TCS13'	'Light yell	'5 YR 8/4'
14	1×471 double	1×471 double	'TCS14'	'Moderate o	'5 GY 4/4'
15	1×471 double	1×471 double	'TCS15'	'Japanese skin	''unknown'
16	1×471 double	1×471 double	'TCS16'	'Perfect white'	'unknown'

Example_WhiteLED.m

example script composing a white LED from blue and yellow, with supporting spectra blue.sre and yellow.sre. Run from Matlab environment and look at variables and figures.

% ExampleWhiteLED()

GaussSpectrum

Creates a normalized Gaussian spectrum with given mean and standard deviation

% function rv = GaussSpectrum(lam_vec,mean,sdev,varargin)

Input:

lam_vec: A vector of positive reals, strictly ascending

mean: Scalar positive number. Mean value of the distribution. May or may not be in the lam_vec range.

sdev: Scalar positive number. Standard deviation

varargin: Optional string argument 'val_only'.

Output:

rv: Spectrum struct, with additional name field. Except if optional argument 'val_only' is present: Then, rv is a column vector of the values.

Usage Example:

see also example for AddWeightedSpectra.

GaussSpectrum(400:500,450,10)

```
ans = struct with fields:
   val: [101×1 double]
   lam: [101×1 double]
   name: 'Gauss spectrum for mean 450 nm and sdev 10 nm, normalized to peak = 1'
```

IntegrateSpectrum

Compute weighted integral of spectrum. If weight omitted, compute just the integral.

```
% function rv = IntegrateSpectrum(spectrum, weight)
```

Spectra in this library are always continuous, and assumed to be linear between the data points. First, spectrum and weight are multiplied. The result will have the wavelengths interweaved, and the multiplication result will be the product of the linearly interpolated individual values. The multiplication result is assumed to be linear between these interweaved points, just like every spectrum in this library. Accordingly, we integrate the multiplication result by simple trapezoidal rule.

This means, however, that even for simple linear spectra and weights, the integral depends on the wavelength resolution.

Input:

spectrum: A valid spectrum

weight: Optional argument, also a valid spectrum

Output:

rv: The integral ov .val over .lam of the multiplied spectrum (see MultiplySpectra for more info about details). If eight is omitted, just integrate the spectrum as-is.

Usage Example:

```
sunlight = PlanckSpectrum(200:10*1000, 5800); % approximate extraterrestrial solar spectrum, fr
visible = MakeSpectrum([360 780],[1 1]);
P_full = IntegrateSpectrum(sunlight);
P_visible = IntegrateSpectrum(sunlight, visible);
fprintf('the visible fraction is %.1f %%', P_visible / P_full * 100);
```

the visible fraction is 48.8 %

IsOctave

Determines if code is running under GNU Octave (or Matlab)

```
% function rv = IsOctave()
```

Output: Returns logical 1 when running under GNU Octave, else returns logical 0

Usage Example:

```
IsOctave()
ans = logical
0
```

IsSpectrum

Checks if a spectrum is valid

```
% function yesno = IsSpectrum(s)
```

Checks if s is a struct with fields 1am and va1, which are both finite real 1D vectors, have same length, and that 1am is strictly ascending and positive

Input:

s: Anything

Output:

yesno: logical, true if s meets the requirements

Usage Example:

```
s = PlanckSpectrum(200:2000,5600);
IsSpectrum(s)

ans = logical
    1

IsSpectrum(0)
```

LDomPurity

ans = logical

Compute dominant wavelength and purity of a spectrum using E = [1/3, 1/3] as white point

```
% function [ldom, purity] = LDomPurity(rhs)
```

Input:

rhs: may be spectrum (struct with lam and val), or XYZ (struct with x and y), or array with length 2

Output:

1dom: dominant wavelength in nm, i.e. the wavelength where the E -> x/y line intersects the monochromatic border. Negative if E -> x/y intersects magenta line, not the monochromatic border. 555 if x/y == E within circle of eps = 2.2e-16.

purity: purity, i.e. the E->x/y distance relative to E->border. 0 if x/y == E, 1 if x/y on border. Negative if E -> x/y intersects magenta line, not the monochromatic border.

Usage Example:

```
blue = GaussSpectrum(360:830,460,20);
[ldom,purity] = LDomPurity(blue) %#ok<ASGLU> % yes, LDom > LPeak for blue
1dom = 465.7497
purity = 0.9694
red = GaussSpectrum(360:830,630,20);
[ldom,purity] = LDomPurity(red) %#ok<ASGLU> % yes, LDom < LPeak for red</pre>
1dom = 614.0548
purity = 0.9999
magenta = AddSpectra(blue, red);
m XYZ = CIE1931 XYZ(magenta);
[ldom,purity] = LDomPurity(m_XYZ) %#ok<ASGLU> % both values are negative
1dom = -554.0733
purity = -0.5550
green xy = [0.16, 0.80];
[ldom,purity] = LDomPurity(green_xy) %#ok<ASGLU> % x/y near border for about 530 nm
1dom = 530.5086
purity = 0.9925
[ldom,purity] = LDomPurity([1/3,1/3]) % ldom is arbitrary
1dom = 555
purity = 0
```

LinInterpol

Computes linearly interpolated values of scalar tabulated function. Very similar to built in interp1, but uses faster C++ DLL under Matlab (on my machine, a factor of five faster).

Used internally as a helper function for higher level library functions, but exposed as a proper library function because it may well be useful to speed up computation in another context.

```
% function yq = LinInterpol(xx,yy,xq)
```

Input:

xx is a 1D vector of numeric values which are not complex, and strictly ascending

yy is a 1D vector of numeric values which are not complex.

xx and yy are of same length and have at least two elements

xq is a 1D vector of numeric values which are not complex, and strictly ascending (the latter is NOT a requirement for interp1)

These preconditions are not checked.

Output:

yq is a vector of same length as xq, with linearly interpolated values. Zero if outside the xx range.

Usage Example:

```
LinInterpol([1 2],[3 4],[-100,1,2,1.7])

ans = 1×4

0  3.0000  4.0000  3.7000
```

LinInterpolAdd4Async

Computes linearly interpolated values of the sum of four input functions. Uses C++ DLL with multithreading under Matlab. On my machine, a factor of five faster than summing the result of interp1 calls, but not faster than summing the results of four LinInterpol calls. I still leave the function in place, there may be a difference for other input values and/or on another machine.

```
% function yq = LinInterpolAdd4Async(xx0,yy0,xx1,yy1,xx2,yy2,xx3,yy3,xq)
```

Input:

xx0 is a 1D vector of numeric values which are not complex, and strictly ascending

yy0 is a 1D vector of numeric values which are not complex.

xx0 and yy0 are of same length and have at least two elements.

Same applies to the xx1/yy1, xx2/yy2, xx3/yy3 pairs, but the xx_ arrays may all be different.

xq is a 1D vector of numeric values which are not complex, and strictly ascending (the latter is NOT a requirement for interp1!!)

Output: yq is a vector of same length as xq, with the sum of the four linearly interpolated values.

Usage Example:

```
LinInterpolAdd4Async([0 1],[1 1.1], [0 1],[2 2], [0 1],[3 3], [0 2],[4 4], [0, 1, 0.5])

ans = 1×3
10.0000 10.1000 10.0500
```

MakeSpectrum

Creates a spectrum struct out of arrays lam and val and checks if they meet the requirements

```
% function rv = MakeSpectrum(lam, val, varargin)
```

Input:

lam is a 1D vector of numeric values which are not complex, > 0, and strictly ascending

val is a 1D vector of numeric values which are not complex.

lam and val are of same length and have at least two elements.

The requirements are checked, an error thrown if violated

varargin: Name/Value pairs for additional fields

Output:

rv is a spectrum struct with column vector fields lam and val.

Usage Example:

```
clear s
s = MakeSpectrum([400 700], [1 1], 'name', 'flat spectrum') %#ok<NASGU>

s = struct with fields:
    lam: [2×1 double]
    val: [2×1 double]
    name: 'flat spectrum'
```

MultiplySpectra

Multiply two spectra, e.g. an LED spectrum with a transmission spectrum

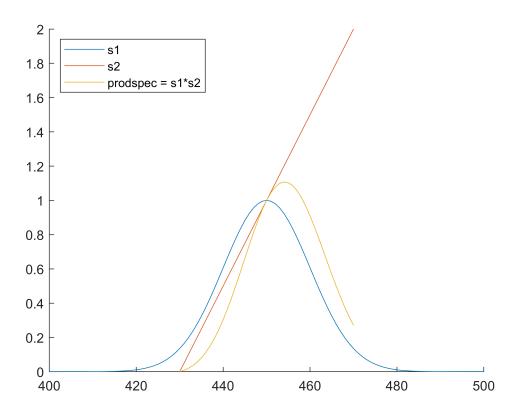
```
% function rv = MultiplySpectra(lhs, rhs)
```

Input: 1hs, rhs: Valid spectrum structs. May or may not overlap.

Output: rv: Spectrum struct, modeling the product of *lhs(lambda)* * *rhs(lambda)*. The rv.lam field covers the overlap region, if any, where it contains all wavelengths from both inputs. The rv.val field contains the product of the respective interpolated values. There is no need to have zero values outside the overlap range, as zero is always assumed outside anyway. When there is no overlap, rv contains a single interval as the overall min/max wavelength range, with zero value.

```
clear s1 s2 prodspec;
s1 = GaussSpectrum(400:500, 450,10);
s2 = MakeSpectrum([430 470],[0 2]);
prodspec = MultiplySpectra(s1, s2);
nfig = nfig + 1;
figure(nfig);
clf;
hold on;
plot(s1.lam, s1.val);
```

```
plot(s2.lam, s2.val);
plot(prodspec.lam, prodspec.val);
legend({'s1','s2','prodspec = s1*s2'},'Location','northwest');
```



PlanckLocus

Compute the x/y, u/v, u'/v' coordinates of the Planck locus, as well as interpolation function objects for x/y, u/v, and the Judd lines (lines of equal correlated color temperature) in u/v.

```
% function rv = PlanckLocus()
```

Input: None

Output: Struct with fields:

nT: Number of temperature points (1001)

invT: Inverse absolute temperature values, from near zero (1e-11) to 0.002 (1/K), in equidistant steps. (The Planck locus points are approximately equidistant in 1/T, and not at all equidistant in T)

T: Absolute temperature values, from 1e11 K down to 500 K

x: CIE 1931 x color coordinate values of the Planck locus curve

y: CIE 1931 y color coordinate values of the Planck locus curve

u: CIE u color coordinate values of the Planck locus curve (to be used only for CCT computation purposes)

v: CIE v color coordinate values of the Planck locus curve (to be used only for CCT computation purposes)

up: CIE u' (u_prime) color coordinate values of the Planck locus curve

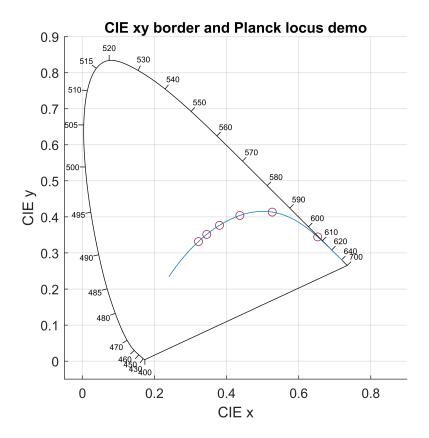
vp: CIE v' (v_prime) color coordinate values of the Planck locus curve

 xy_func : A function object to compute interpolated values of the x/y color coordinates of the Planck locus. To be called like $xy = rv.xy_func(T)$ where T is a scalar of vector of absolute temperatures, and returns an array of size [2, length(T)] with the interpolated x values as first column and the interpolated y values as second column. Returns NaN when T is out of range 500 .. 1e11

uv_func: Same as xy_func, except it returns u/v values.

JuddLine_func: A function object to compute interpolated values of the Judd line parameters. To be called like j1 = rv.JuddLine_func(T) where T is a scalar, absolute temperature. Returns a struct with fields u, v, du, dv where [u,v] are the u/v coordinates of the Planck locus point for T, and [du,dv] is the Judd line direction, normalized to length 1. By definition, the Judd line is perpendicular to the Planck locus in u/v color space, and all color points on a Judd line are deemed to have same CCT (correlated color temperature). Note that the "allowed" meaningful range is +/- 0.05 u/v length units away from the Planck locus.

```
clear pl xb yb T xy
pl = PlanckLocus();
fh = figure();clf;
PlotCIExyBorder('Figure',fh);
hold on;
T = [1000 2000 3000 4000 5000 6000];
xy = pl.xy_func(T);
scatter(xy(:,1),xy(:,2));
plot(pl.x,pl.y);
axis equal;
grid on;
axis([-0.05 0.9 -0.05 0.9]);
xlabel('CIE x');
ylabel('CIE xy border and Planck locus demo')
```



PlanckSpectrum

Generate blackbody spectrum for some absolute temperature.

```
% function rv = PlanckSpectrum(lam_vec, T, varargin)
```

Input:

lam_vec: A wavelength vector, numeric, non-complex, positive, strictly ascending

T: Scalar real number, absolute temperature in K. May be inf, then returns lam_vec.^(-4), scaled to localpeak1 (this is the high temperature limit of the shape of the long wavelength tail).

varargin: Name/Value pairs.

'normalize' -> string, default 'globalpeak1'. Allowed values:

'globalpeak1': scaled such that global peak would be 1.0 even if outside lambda range

'localpeak1': scaled such that the peak value is 1.0 for the given lam_vec. Not exactly identical if global peak is in range, due to discretization

'localflux1': scaled such that integral over lam vec is 1.0

'radiance': scaled such that rv is blackbody spectral radiance, W/(wlu m²sr). wlu is wavelengthUnit, see below

'basic_radiance': scaled such that rv is blackbody spectral basic radiance, differing from radiance by a factor of n^2 . Same units as radiance.

'exitance': scaled such that rv is blackbody spectral exitance, W/(wlu m²). wlu is wavelengthUnit, see below

The following Name/Value pairs define the refractive index of the medium in which the blackbody spectrum is measured. Default is air, with an index of 1.000277.

For details of the physics, see the file BlackbodySpectrumWithRefractiveIndex.pdf or BlackbodySpectrumWithRefractiveIndex.mlx in this library.

For dispersive cases, the wavelengths are given the same units as lam vec.

'n_refr_const' -> positive real scalar, default 1.000277. To obtain the spectrum in vacuum, set to 1.0

'n_refr_func' -> function handle to dispersion function n(lambda), default not used (returning NaN).

Must have signature: [n, dn_dlambda] = n_refr_func(lambda) where dn_dlambda is the derivative, $\frac{dn}{d\lambda}$

'n_refr_table' -> a valid spectrum, i.e. struct with appropriate fields lam and val. Default: unused

'n_refr_func' has precedence over 'n_refr_table', which has precedence over 'n_refr_const'

'wavelengthUnit' -> positive real, wavelength unit in meters, default 1e-9 (nanometers). Examples:

1e-9: lam_vec given in nm, returned spectrum is W / (nm m² sr) or W / (nm m²) for radiance/exitance scaling. rv.XYZ will be CIE XYZ values X, Y, Z, x, y

1e-6: lam_vec given in μm, returned spectrum is W / (μm m² sr) or W / (μm m²) for radiance/exitance scaling.

Output: Spectrum struct with fields

lam: Same as lam_vec, but column vector.

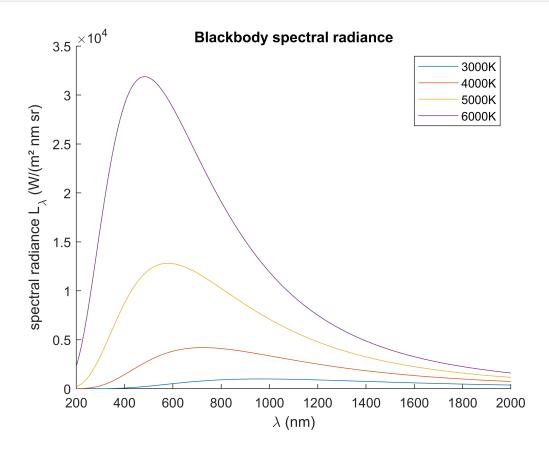
val: The spectral values, column vector of same length, normalized according to 'normalize' (default: global peak 1.0).

name: string, an appropriate name

XYZ: (only for nanometer wavelength units): Struct with X,Y,Z tristrimulus values, and x,y,z CIE 1931 color coordinates.

```
clear bb T
nfig = nfig + 1;
figure(nfig);
clf;
hold on;
for T = [3000 4000 5000 6000]
    bb = PlanckSpectrum(200:2000,T,'normalize','radiance');
    plot(bb.lam,bb.val);
end
```

```
xlabel('\lambda (nm)');
ylabel('spectral radiance L_\lambda (W/(m² nm sr)')
legend({'3000K','4000K','5000K','6000K'})
title('Blackbody spectral radiance')
```



PlotCIExyBorder

plotting the CIE x/y "color horseshoe", with optional ticks and other options

```
% function [ah, fh] = PlotCIExyBorder(varargin)
```

Plot the CIE x/y "color horseshoe" into a new figure or a given figure or axes handle. Various options are available to control the look. Re-use the figure and/or axes handle for further plotting into the same figure

Input:

varargin: Name/Value pairs:

'Handle': valid figure handle to use for the plot. Current hold state will be restored

'Axes' : valid axes handle to use for the plot. Current hold state will be restored. Overrides 'Handle'

'LineSpec': valid LineSpec string (see plot documentation), e.g. '--b' for dashed blue lines, see 'plot' documentation.

'PlotOptions': cell array of valid plot options, e.g. {'Color', [0.5 0.5 0.5], 'LineWidth', 2}

'Ticks': array of wavelength values where ticks and labels are plotted. Reasonable default. Say ..., 'Ticks',[],... to suppress

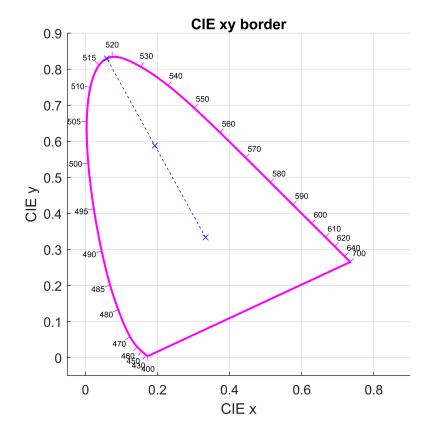
'TickFontSize': number, obvious meaning. Default: 6

Output:

ah: the axis handlefh: the figure handle

Usage Example: (see also the example for PlanckLocus)

```
[ah, fh] = PlotCIExyBorder('LineSpec','m','PlotOptions',{'LineWidth',1.5});
green = ComputeSpectrumColorimetry(GaussSpectrum(450:600,520,30));
% find the point on the monochromatic border corresponding to lDom
load('CIE1931_lam_x_y_z.mat','CIE1931XYZ');
xPure = LinInterpol(CIE1931XYZ.lam, CIE1931XYZ.xBorder, green.Ldom);
yPure = LinInterpol(CIE1931XYZ.lam, CIE1931XYZ.yBorder, green.Ldom);
% plot line from white point, to x/y of green, to border at green.lDom
plot([1/3,green.XYZ.x,xPure], [1/3,green.XYZ.y,yPure],'--bx');
```



ReadLightToolsSpectrumFile

Read LightTools .sre files, as supplied by many LED vendors. Reads also simple ASCII 2-column tables with any text header

```
% function rv = ReadLightToolsSpectrumFile( fn )
```

LightTools .sre files are simple ASCII 2 column text files, with a text header. The files blue.sre and yellow.sre are examples.

LightTools .sre files have the option to be photometric, i.e. values are luminous flux, whereas all spectra in this library are radiometric. If it is photometric, ReadLightToolsSpectrumFile rescales the values properly to radiometric. There is also an option to be discrete, i.e. a spectrum of narrow lines. ReadLightToolsSpectrumFile converts such files to a continuous spectrum with very narrow triangular peaks.

ReadLightToolsSpectrumFile can also be used to read a spectrum from an ASCII file which starts with any number of text header lines, i.e. lines whose first non-whitespace character is not a '0'..'9' digit, followed by lines with two numbers each.

The last line may or may not be terminated with a newline, i.e. the last line may be empty.

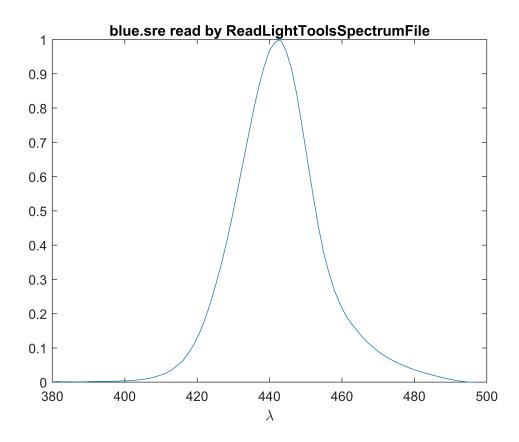
Input:

fn: File name. Extension must be supplied, is not automatically added.

Output:

rv: The spectrum

```
blue = ReadLightToolsSpectrumFile( 'blue.sre' );
figure; clf;
plot(blue.lam, blue.val);
xlabel('\lambda'); title('blue.sre read by ReadLightToolsSpectrumFile');
```



RGBLEDSpectrum

A class that models R,G,B LED spectra at operating conditions, based only on information from data sheets (and spectra as part of ray files, where available).

For the purposes of this class, a red, green or blue LED has a spectrum whose shape is invariant, like the typical spectrum shown on a data sheet. (The actual shape varies a little from LED to LED, and with operating temperature and current, but this effect is neglected here). For some LEDs, the spectra are available as text files as part of the ray file package.

For a given LED, the data sheet shows how, typically, current varies with voltage, relative flux and dominant wavelength vary with current, and flux, wavelength and voltage vary with temperature. Those curves need to be sampled by the user from the data sheet (there is "digitizer" software available to ease that chore, e.g. as part of the LightTools utilities).

LEDs are binned by measuring flux, dominant wavelength and voltage at grouping conditions. The variations just described show how an LED's properties vary from these binning values according to operating conditions.

The use case of this class is to

- characterize an LED model by its typical spectrum, and its typical parameter variation (change of voltage, wavelength and flux vs. current and temperature)
- characterize an invidual LED from this model by its binning parameters (voltage, wavelength and flux at grouping current and temperature)
- apply arbitrary operating parameters (current and junction temperature) to that specific LED
- obtain the estimated spectrum of that specific LED at that specific operating parameters

An additional refinement would be to specify operating solder point temperature instead of junction temperature, using the LED's thermal resistance and the waste heat at operating conditions to estimate actual junction temperature. This, however, requires iteration and is planned for a future revision.

Input:

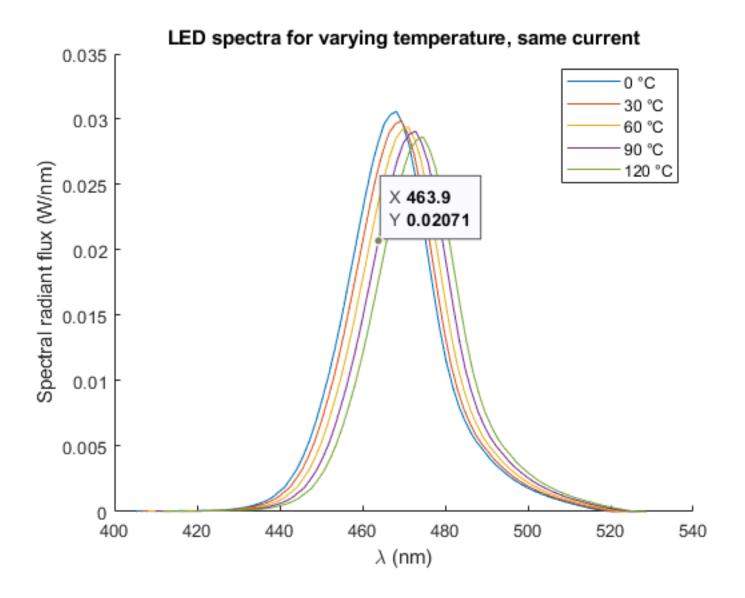
rhs: the right hand side

Output:

1hs: the left hand side

Usage Example:

See script file TestRGBLED.mlx on how to obtain this figure for a certain blue LED:



ShiftToLdom

Shifts the wavelength of a spectrum such that the result has a desired dominant wavelength

```
% function [spec_out, delta_lam] = ShiftToLdom(spec_in, ldom)
```

Given an input spectrum, iteratively adds/subtracts a constant wavelength to the wavelength range, until the resulting spectrum has the desired dominant wavelength

Input:

spec_in: A valid spectrum, at least partially in the visible range

1dom: The desired dominant wavelength in nanometes, within [400,695].

Output:

spec_out: The shifted spectrum

delta_lam: The applied shift

Usage Example:

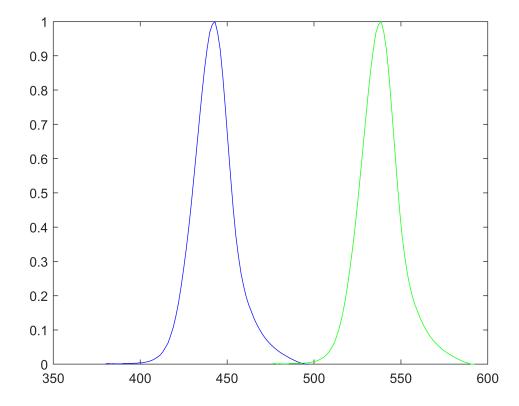
```
clear;
blue = ReadLightToolsSpectrumFile('blue.sre');
dl0 = LDomPurity(blue)

dl0 = 447.3515

green = ShiftToLdom(blue, 540);
LDomPurity(green)

ans = 540.0000

figure();
clf;
plot(blue.lam, blue.val,'b');
hold on;
plot(green.lam, green.val,'g');
```



SpectrumSanityCheck

Checks requirements for a spectrum variable, and returns a sanitized version of the variable, with column vectors lam and val.

```
% function [ok, msg, rv] = SpectrumSanityCheck(spec, varargin)
```

Input:

spec is a spectrum which should adhere to the requirements above.

varargin are optional name/value pairs:

'doThrow', logical, default: true. If there is an error: If flag is true, throws error exception, else returns false in ok and an error message in *msg*.

'doStrip', logical, default: false: If true returns rv with only the lam and val fields, else returns rv with all fields of input spec

Output:

ok: Logical. True if there are no requirement violations, else false

msg: Character string. Empty string if there are no requirement violations, else diagnostic message.

rv: A spectrum struct where lam and val are same as in spec except that both are always column vectors. When the doStrip flag is false, also has all other fields of spec. At requirement violation, is empty array.

Usage Example:

```
clear good bad ok1 msg1 rv1 ok2 msg2 rv2
good = MakeSpectrum([400 700], [1 1]);
[ok1, msg1, rv1] = SpectrumSanityCheck(good)
ok1 = logical
msg1 =
    []
rv1 = struct with fields:
   lam: [2×1 double]
   val: [2×1 double]
bad = struct('lam', [1, 2, 1], 'val', [0 0 0]);
[ok2, msg2, rv2] = SpectrumSanityCheck(bad, 'doThrow', false)
ok2 = logical
  0
msg2 =
'lam must be strictly ascending'
rv2 =
    []
```

TestLinInterpol

A script to test the LinInterpol and LinInterpolAdd4Async functions, also measuring run times.

Input: none

Output: diagnostic text

Usage Example:

TestLinInterpol

```
LinInterpol elapsed time: 1.2692e-05
```

```
interp1 elapsed time: 5.5405e-05, diffnorm = 0
LinInterpolAdd4Async elapsed time: 8.9158e-05
4 x LinInterpol elapsed time: 5.1531e-05, diffnorm = 0
4 x interp1 elapsed time: 0.00021199, diffnorm = 0
```

Vlambda

Returns V(lambda), CIE 1924 as a spectrum

```
% function rv = Vlambda()
```

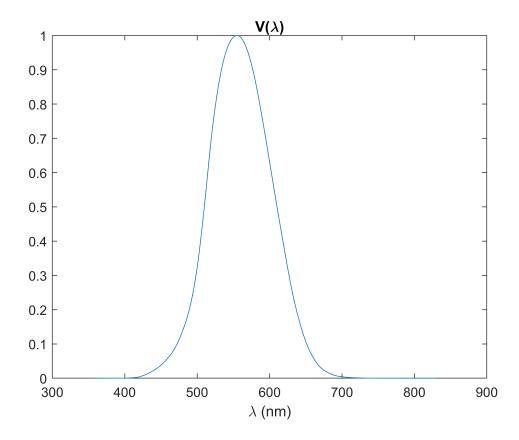
In steps of 1 nm from 360 nm to 830 nm

Input: none

Output:

rv: V(lambda) as spectrum in steps of 1 nm from 360 nm to 830 nm

```
vl = Vlambda();
figure(); clf;
plot(vl.lam, vl.val);
xlabel('\lambda (nm)');
title('V(\lambda)')
```



WriteLightToolsSpectrumFile

Write LightTools .sre spectrum file, to assign to a source

```
% function WriteLightToolsSptrumFile(spectrum, filename, varargin)
```

Input:

spectrum: A valid spectrum with .lam and .val fields. See Spectrum requirements.

If spectrum has other fields which are simple strings or numeric values, they will be written as named comments. E.g. if spectrum.name == 'My LED' then '# name: My LED' will be written.

filename: name of the spectrum file. '.sre' is appended if necessary

optional arguments: Name-Value pairs

'mode': string, only allowed value is 'discrete'. Default spectrum mode is continuous.

Output: none

Usage Example:

```
s = PlanckSpectrum(400:700,5600);
WriteLightToolsSpectrumFile(s,'Planck5600.sre');
will write Planck5600.sre, with the first lines being
# LightTools spectrum file, created 13-Oct-2019 15:16:16
```

```
# name: Planck blackbody spectrum for T = 5600 K, normalized to global peak = 1

dfat 1.0

dataname: Planck blackbody spectrum for T = 5600 K, normalized to global peak = 1
```

continuous

radiometric
400 0.838583

401 0.841573

template for copy paste

short

```
%
```

long

^{&#}x27;comment': string or cell array of strings, will be written as comment(s)

Input:

rhs: the right hand side

Output:

1hs: the left hand side