

## 5<sup>th</sup> Practical Class – Graphs: Shortest path

### Instructions

- Download the **cal\_fp05.zip** file from the course webpage and decompress it (contains the **Test.cpp** and **Graph.h** files, based on the code from the two previous classes)
- Open eclipse and create a new C++ C++ Project (File/New/C++ Project/Cute Project) named **CalFp05** and configured to use MinGW GCC.
- Include the Boost library
- Import the extracted files into the project's src folder (Import/General/File System)
  - Answer yes when question about overwriting Test.cpp
  - Compile the project.
  - Run the project as a CUTE Test (Run As/CUTE Test). If questioned about which compiler to use, choose MinGW gdb.
- ***You should solve the exercises in order.*** You can run the project as a CUTE Test whenever you wish to know if your current implementation is sufficient to pass the tests.

### Exercises

#### 1. Shortest path in unweighted graphs

- a) Implement the following public method in the **Graph** class:

```
void unweightedShortestPath(const T &origin)
```

This method implements an algorithm to find the shortest paths from  $v$  (vertex which contains element *origin*) to all other vertices, ignoring edge weights.

- b) Implement the following public member function in class **Graph**:

```
vector<T> getPath(const T &origin, const T &dest)
```

Considering that the *path* property of the graph's vertices has been updated by invoking a shortest path algorithm from one vertex *origin* to all others, this function returns a vector with the sequence of the vertices of the path, from the *origin* to *dest*, inclusively (*dest* is the attribute *info* of the destination vertex of the path). It is assumed that a path calculation function, such as `unweightedShortestPath`, was previously called with the *origin* argument, which is the origin vertex.

#### 2. Dijkstra algorithm

Consider the **Graph** class you used in previous classes, which is defined in the *Graph.h* file. You should edit the classes in *Graph.h* in order to complete the exercises below. Look at the *Test.cpp* file in order to identify auxiliary functions which are required but are not explicitly asked for.

- a) Implement the following public member function in class **Graph**:

```
void dijkstraShortestPath(const T &origin)
```

This method implements the Dijkstra algorithm to find the shortest paths from  $s$  (vertex which contains element *origin*) to all other vertices, in a given weighted graph (see theoretical class slides). Update the **Vertex** class with member variables `int dist` and `Vertex* path`, representing the distance to the start vertex and the previous vertex in the shortest path, respectively. Since the STL doesn't support mutable priority queues, you can use the class provided *MutablePriorityQueue*, as follows:

- To create a queue: `MutablePriorityQueue<Vertex<T> > q;`
- To insert vertex pointer  $v$ : `q.insert(v);`
- To extract the element with minimum value (*dist*): `v = q.extractMin();`
- To notify that the key (*dist*) of  $v$  was decreased: `q.decreaseKey(v);`

- b) Based on the performance data of the Dijkstra algorithm produced by the tests provided, create a chart to show that the average execution time is proportional to  $(|V| + |E|) \log_2 |V|$ . The performance tests generate random graphs in the form of a grid of size  $N \times N$ , in which the number of vertices is  $|V| = N^2$  and the number of edges is  $4N(N-1)$ .

### FOR NEXT CLASS

## 2. Other single source shortest path algorithms

- a) Implement the following public method in **Graph** class:

```
void bellmanFordShortestPath(const T &origin)
```

This method implements the Bellman-Ford algorithm to find the shortest paths from  $v$  (vertex which contains element *origin*) to all other vertices, in a given weighted graph.

## 3. All pairs shortest paths

- a) Implement the following public method in the **Graph** class:

```
void floydWarshallShortestPath()
```

This method implements the Floyd-Warshall algorithm to find the shortest paths between all pairs of vertices in the graph.

Additionally, you will also have to implement the following public method of the **Graph** class:

```
vector<T> getfloydWarshallPath(const T &origin, const T &dest)
```

This method returns a vector with the sequence of elements in the graph in the path from *origin* to *dest* (where *origin* and *dest* are the values of the *info* member of the origin and destination vertices, respectively).