Primal feasibility: $\forall i \in \mathcal{I}$, $\arg \max \Phi_c(x_i; \theta^*) = y_i$ Dual feasibility: $\forall i \in \mathcal{I}, \quad \lambda_i > 0$, $\theta^* = -\sum_i \lambda_i \nabla_{\theta} \mathcal{L}(\Phi(x_i; \theta^*), y_i),$ Stationarity: Manifold: $\forall i \in \mathcal{I}, \quad x_i \in \mathcal{M}.$