# **Assignment 1: Tabular Reinforcement Learning**

CS260R 2023Fall: Reinforcement Learning. Department of Computer Science at University of California, Los Angeles. Course Instructor: Professor Bolei ZHOU. Assignment author: Zhenghao PENG, Yiran WANG.

Student Name	Student ID
Jun Kang	406182577

Welcome to the assignment 1 of our reinforcement learning course. The objective of this assignment is for you to understand the classic methods used in tabular RL.

This assignment has the following sections:

- Section 1: Warm-up on the RL environment (35 points)
- Section 2: Implementation of the model-based family of algorithms: policy iteration and value iteration. (65 points)

You need to go through this self-contained notebook, with dozens of **TODO**s are scattered in the cells. You need to finish all TODOs.

You are encouraged to add more code on extra cells at the end of each section to investigate the problems you think interesting. At the end of the file, we leave a place for you to write comments optionally (Yes, please give us either negative or positive rewards so that we can keep improving the assignment!).

Please report any code bugs to us via <u>GitHub issues (https://github.com/ucla-rlcourse/assignment-2022fall)</u>.

Before you get start, remember to follow the instruction at <a href="https://github.com/ucla-rlcourse/assignment-2022fall/tree/main/assignment0">https://github.com/ucla-rlcourse/assignment-2022fall/tree/main/assignment0</a>) to set up your python environment.

# **Dependencies**

This assignment requires the following dependencies:

- 1. gymnasium==0.29.1
- 2. numpy
- 3. scipy

You can install all of them through the following cell:

In [1]: # If you already installed everything, you don't need to run this cell. # Install dependencies to your current python environment.

> !pip install -U pip !pip install mediapy numpy scipy "gymnasium==0.29.1" "gymnasium[toy-text]==

kequirement aiready satistied: pygments>=2.4.0 in c:\users\i8o46\anacon da3\envs\cs260r1\lib\site-packages (from ipython->mediapy) (2.15.1) Requirement already satisfied: stack-data in c:\users\18646\anaconda3\e nvs\cs260r1\lib\site-packages (from ipython->mediapy) (0.2.0) Requirement already satisfied: traitlets>=5 in c:\users\18646\anaconda3 \envs\cs260r1\lib\site-packages (from ipython->mediapy) (5.11.2) Requirement already satisfied: colorama in c:\users\18646\anaconda3\env s\cs260r1\lib\site-packages (from ipython->mediapy) (0.4.6) Requirement already satisfied: contourpy>=1.0.1 in c:\users\18646\anaco nda3\envs\cs260r1\lib\site-packages (from matplotlib->mediapy) (1.1.1) Requirement already satisfied: cycler>=0.10 in c:\users\18646\anaconda3 \envs\cs260r1\lib\site-packages (from matplotlib->mediapy) (0.12.1) Requirement already satisfied: fonttools>=4.22.0 in c:\users\18646\anac onda3\envs\cs260r1\lib\site-packages (from matplotlib->mediapy) (4.43.

Requirement already satisfied: kiwisolver>=1.0.1 in c:\users\18646\anac onda3\envs\cs260r1\lib\site-packages (from matplotlib->mediapy) (1.4.5) Requirement already satisfied: packaging>=20.0 in c:\users\18646\anacon da3\envs\cs260r1\lib\site-packages (from matplotlib->mediapy) (23.1) Requirement already satisfied: pyparsing>=2.3.1 in c:\users\18646\anaco

Now start running the cells sequentially (by ctrl + enter or shift + enter ) to avoid unnecessary errors by skipping some cells.

# Section 1: Warm-up on the RL environment

(35/100 points)

In this section, we will go through the basic concepts of RL environments using OpenAI Gym. Besides, you will get the first sense of the toy environment we will use in the rest of the assignment.

Every Gym environment should contain the following attributes:

- 1. env.step(action) To advance the environment by one time step through applying action. Will return four things: observation, reward, done, info, wherein done is a boolean value indicating whether this episode is finished. info is a dict containing some information the user is interested in.
- 2. env.reset() To reset the environment, back to the initial state. Will return the initial observation of the new episode.
- 3. env.render() To render the current state of the environment for human-being
- 4. env.action space The allowed action format. In our case, it is Discrete(4) which means the action is an integer in the range [0, 1, 2, 3]. Therefore, the action for step(action) should obey the limit of the action space.
- 5. env.observation\_space The observation space.

Note that the word episode means the process that an agent interacts with the environment from the initial state to the terminal state. Within one episode, the agent will only receive one done=True, when it goes to the terminal state (the agent is dead or the game is over).

We will use FrozenLake8x8-v1 as our environment. In this environment, the agent controls the movement of a *character* in a grid world. Some tiles of the grid are walkable, and others are not, making to the agent falling into the water. Additionally, the movement direction of the agent is uncertain and only partially depends on the chosen direction. The agent is rewarded for finding a walkable path to a goal tile. The meaning of each character:

S: starting point, safe
 F: frozen surface, safe
 H: hole, fall to your doom

4. G: goal, where the frisbee is located

```
In [2]: # Run this cell without modification
       import time
       from typing import List, Callable
       # Import some packages that we need to use
       import gymnasium as gym
       import numpy as np
       # Prepare some useful functions
       from IPython.display import clear_output
       import mediapy as media
       import matplotlib.pyplot as plt
       %matplotlib inline
       def wait(sleep=0.2):
          clear_output(wait=True)
          time.sleep(sleep)
       def print table(data):
          if data.ndim == 2:
             for i in range(data.shape[1]):
                print("\n=== The state value for action {} ===".format(i))
                print_table(data[:, i])
             return
          assert data.ndim == 1, data
          if data.shape[0] == 16: # FrozenLake-v0
             text = "+----+\n" \
                   "| 0 | 1 | 2 | 3 |\n" \
                   "|----+\n"
             for row in range(4):
                tmp = "| {} |{:.3f}|{:.3f}|{:.3f}|{n" }
                     "+----+\n" \
                    row, *[data[row * 4 + col] for col in range(4)]
                text = text + tmp
          else:
             text = "+----+\n"
                   "| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |\n"
                   "|----+----|\n"
             for row in range(8):
                tmp = "| {} | {:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|
                     ":.3f}|\n" \
                     "".format(
                   row, *[data[row * 8 + col] for col in range(8)]
                text = text + tmp
          print(text)
       def test random policy(policy, env):
          _acts = set()
          for i in range(1000):
             act = policy(0)
             _acts.add(act)
             assert env.action space.contains(act), "Out of the bound!"
```

```
if len(_acts) != 1:
    print(
        "[HINT] Though we call self.policy 'random policy', "
        "we find that generating action randomly at the beginning "
        "and then fixing it during updating values period lead to bette
        "performance. Using a stochastic policy is not even work! "
)
```

#### Section 1.1: Make the environment

You need to know

- 1. How to make an environment
- 2. How to set the random seed of environment
- 3. What is observation space and action space

```
In [3]: # Solve the TODOs and remove `pass`

# TODO: Just a reminder. Do you add your name and student
# ID in the table at top of the notebook?

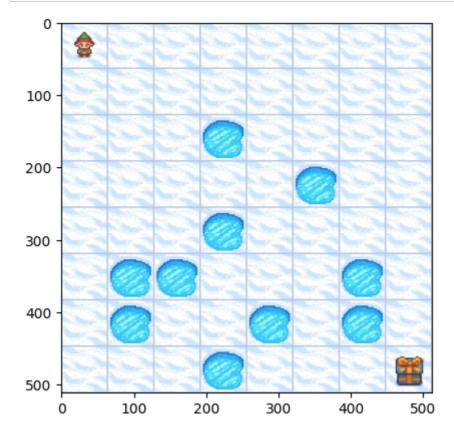
# Create the environment
env = gym.make('FrozenLake8x8-v1', render_mode="ansi")

# You need to reset the environment immediately after instantiating env.
env.reset(seed=0) # TODO: uncomment this line

print("Current observation space: {}".format(env.observation_space))
print("Current action space: {}".format(env.action_space))
print("0 in action space? {}".format(env.action_space.contains(0)))
print("5 in action space? {}".format(env.action_space.contains(5)))
```

Current observation space: Discrete(64)
Current action space: Discrete(4)
0 in action space? True
5 in action space? False

```
In [4]: # Run this cell without modification to get a sense of the environment.
    tmp_env = gym.make('FrozenLake8x8-v1', render_mode="rgb_array")
    tmp_env.reset()
    _ = plt.imshow(tmp_env.render())
```



# Section 1.2: Play the environment with random actions

You need to know

- 1. How to step the environment;
- 2. How to rollout a complete episode.

```
In [5]: # Solve the TODOs and remove `pass`
        # Run 1000 steps for test, terminate if done.
        # You can run this cell multiples times.
        env.reset(seed=0)
        while True:
            # Take random action
            # TODO: Uncomment next two lines
            observation, reward, terminated, truncated, info = env.step(env.action
            done = terminated or truncated
            # Render the environment.
            # You will see a pop-up window visualizing the behaviors of the agent
            # if you are using local machine to run this notebook.
            print(env.render())
            print("Current observation: {}\nCurrent reward: {}\n"
                  "Whether we are done: {}\ninfo: {}".format(
                observation, reward, done, info
            ))
            wait(sleep=0.1)
            # TODO: Terminate the Loop if done
            if done:
                break
          (Left)
        SFFFFFF
        FFFFFFF
        FFFHFFF
        FFFFFHFF
        FFFHFFF
        FHHFFFHF
        FHFFHFHF
```

# FHHFFHF FHFFHFFFG Current observation: 41 Current reward: 0.0 Whether we are done: True info: {'prob': 0.33333333333333333333

# Section 1.3: Define the evaluation function to value the random baseline

Now we need to define an evaluation function to evaluate a given policy.

As a reminder, you should create a FrozenLake8x8-v1 environment instance by default, reset it after each episode (and at the beginning), step the environment, and terminate the episode if done. According to Gym v26 update,

After implementing the evaluate function, run the next cell to check whether the function is working.

```
In [6]: # Solve the TODOs and remove `pass`
        def _render_helper(env):
            print(env.render())
            wait(sleep=0.05)
        def evaluate(
            policy: Callable,
            num_episodes: int,
            seed: int = 0,
            env_name: str = 'FrozenLake8x8-v1',
            render: bool = False,
            render mode: str = 'ansi',
        ) -> float:
            """This function evaluates the given policy and returns the
            average episodic return across #num_episodes episodes.
            We use `seed` argument for testing purpose.
            You should pass the tests in the next cell.
            :param policy: a function whose input is an integer (observation)
            :param num_episodes: number of episodes you wish to run
            :param seed: an integer, used for testing.
            :param env_name: the name of the environment
            :param render: a boolean flag. If true, please call render helper
            function.
            :param render_mode: a string specifies the render mode if render=True.
            :return: the averaged episode reward of the given policy.
            # Create environment (according to env_name, we will use env other than
            env = gym.make(env name, render mode=render mode if render else None)
            # Build inner loop to run.
            # For each episode, do not set the limit.
            # Only terminate episode (reset environment) when done = True.
            # The episode reward is the sum of all rewards happen within one episod
            # Call the helper function `render(env)` to render
            rewards = []
            for i in range(num_episodes):
                # reset the environment
                obs, info = env.reset(seed=seed + i)
                action = policy(obs)
                ep reward = 0
                while True:
                    # TODO: run the environment and terminate it if done, collect t
                    # reward at each step and sum them to the episode reward.
                    observation, reward, terminated, truncated, info = env.step(act
                    done = terminated or truncated
                    obs = observation
                    action = policy(obs)
                    ep reward += reward
                    if render:
                         render helper(env)
                    if done:
                        break
                rewards.append(ep_reward)
```

```
return float(np.mean(rewards))
# TODO: Run next cell to test your implementation!
```

```
In [7]: # Run this cell without modification
        # Run this cell to test the correctness of your implementation of `evaluate
        LEFT = 0
        DOWN = 1
        RIGHT = 2
        UP = 3
        def expert(obs):
            """Go down if agent at the right edge, otherwise go right."""
            return DOWN if (obs + 1) % 8 == 0 else RIGHT
        def assert_equal(seed, value, env_name):
            ret = evaluate(expert, 1000, seed, env_name=env_name)
            assert ret == value, \
                "When evaluate on seed {}~{} in {} environment, the " \
                "averaged reward should be {}. But you get {}." \
                "".format(seed, seed + 1000, env_name, value, ret)
        assert_equal(0, 0.046, 'FrozenLake8x8-v1')
        assert_equal(1000, 0.047, 'FrozenLake8x8-v1')
        assert equal(2000, 0.065, 'FrozenLake8x8-v1')
        assert_equal(0, 0.024, 'FrozenLake-v1')
        assert_equal(1000, 0.034, 'FrozenLake-v1')
        assert_equal(2000, 0.035, 'FrozenLake-v1')
        print("Test Passed!")
        print("\nAs a baseline, the mean episode reward of a hand-craft "
               "agent is: ", evaluate(expert, 1000))
```

Test Passed!

As a baseline, the mean episode reward of a hand-craft agent is: 0.046

Congratulation! You have finished section 1 (if and only if not error happens above).

## Section 2: Model-based Tabular RL

(65/100 points)

We have learned how to use the Gym environment to run an episode, as well as how to interact between the agent (policy) and environment via env.step(action) to collect observation, reward, done, and possible extra information.

Now we need to build the basic tabular RL algorithm to solve this environment. **Note that** compared to the model-free methods in the Sec.3, the algorithms in this section needs to access the internal information of the environment, namely the transition

#### dynamics.

In our case, given a state and an action, we need to know which state current environment will jump to, the probability of this transition, and the reward of the transition. You will find that we provide you a helper function <code>self.\_get\_transitions(state, action)</code> that takes state and action as input and return you a list of possible transitions.

First, we will implement an abstract class to represent a Trainer. Though this seems to be over-complex for tabular RL, we will use the same framework in the future assignments. So it would be helpful for you to get familiar with how to implement an RL algorithm in the classoriented programming style.

```
In [8]: # Run this cell without modification
        class TabularRLTrainerAbstract:
            """This is an abstract class for tabular RL trainer. We will subclass t
             to implement specific algorithm, so that we can reuse the codes like
            getting the dynamic of the environment (self._get_transitions()) or ren
            learned policy (self.render())."""
            def __init__(self, env_name='FrozenLake8x8-v1', model_based=True):
                self.env name = env name
                self.env = gym.make(self.env_name)
                self.action_dim = self.env.action_space.n
                self.obs_dim = self.env.observation_space.n
                self.model_based = model_based
                # Define the policy as a numpy array that has shape (self.obs_dim,
                # It's a lookup table that return the selected action given a state
                self.policy = None
                # Define the value table as a numpy array.
                self.value_table = None
            def _get_transitions(self, state: int, act: int) -> List:
                """Query the environment to get the transition probability,
                reward, the next state, and done given a pair of state and action.
                We implement this function for you. But you need to know the
                return format of this function.
                self._check_env_name()
                assert self.model_based, "You should not use _get_transitions in "
                                          "model-free algorithm!"
                # call the internal attribute of the environments.
                # `transitions` is a list contain all possible next states and the
                # probability, reward, and termination indicator corresponding to i
                transitions = self.env.unwrapped.P[state][act]
                # Given a state-action pair, it is possible
                # to have multiple transitions, since the
                # environment is not deterministic.
                # The return of this function: a list of dicts
                for prob, next state, reward, done in transitions:
                    ret.append({
                        "prob": prob,
                        "next_state": next_state,
                        "reward": reward,
                        "done": done
                    })
                return ret
            def _check_env_name(self):
                assert self.env_name.startswith('FrozenLake')
            def print table(self):
                """print beautiful table, only work for FrozenLake8X8-v1 env. We
                write this function for you."""
                self._check_env_name()
                print_table(self.value_table)
```

```
In [9]: # Run this cell without modification

# Run trainer._get_transitions and give you a sense of how it works.
test_trainer = TabularRLTrainerAbstract()
transitions = test_trainer._get_transitions(state=0, act=0)
print(f"The return transitions is a {type(transitions)}.\n\n{transitions}")
```

The return transitions is a <class 'list'>.

### **Section 2.1: Policy Iteration**

Recall the process of policy iteration:

- 1. Update the state value function, given all possible transitions at current state of the environment.
- 2. Find the best policy that earns the highest value under current state value function.
- 3. If the best policy is identical to the previous one then stop the training. Otherwise, return to step 1.

In step 1, update the state value function by

$$v_{k+1} = E_{s'}[r(s, a) + \gamma v_k(s')]$$

wherein the a is given by current policy, s' is next state, r is the reward,  $v_k(s')$  is the next state value given by the old (not updated yet) value function. The expectation is computed among all possible transitions given a state and action pair (As the environment is not deterministic, it's possible to transit to different next states even given the same state-action pair). Note that the new value  $v_{k+1}$  should be temporarily stored at some places, instead of

In step 2, the best policy is the one that takes the action with maximal expected return given a state:

```
a = argmax_a E_{s'}[r(s, a) + \gamma v_k(s')]
```

Policy iteration algorithm has an outer loop (update policy, step 1 to 3) and an inner loop (fit the value function, within step 1).

In each outer loop, we call once trainer.train(), where we call trainer.update\_value\_function() once to update the value function (the state value table).

After that we call trainer.update\_policy() to update the current policy.

trainer object has a trainer.policy attribute, which is a function that takes observation as input and returns an action.

You should implement the trainer following the framework we already wrote for you. Please carefully go through the codes and finish all TODO in it.

```
In [10]: # Solve the TODOs and remove `pass`
         class PolicyIterationTrainer(TabularRLTrainerAbstract):
             def __init__(self, gamma=1.0, eps=1e-10, env_name='FrozenLake8x8-v1'):
                 super(PolicyIterationTrainer, self).__init__(env_name)
                 # Discount factor
                 self.gamma = gamma
                 # Value function convergence criterion
                 self.eps = eps
                 # The **value table** for each possible observation
                 self.value_table: np.ndarray = np.zeros((self.obs_dim,))
                 # TODO: you need to implement a uniform random policy at the beginn
                 # self.policy is a python function that takes an integer (the obser
                 # as input and return an integer (action).
                 # You can use self.action dim to get the dimension (range)
                 # of the action. An action is an integer in range
                 # [0, ..., self.action_dim - 1]
                 # Note: policy should be a deterministic function. That is, given a
                 # it should also return the same action.
                 def init_policy(obs):
                     np.random.seed(obs)
                     return np.random.randint(0, self.action_dim - 1)
                 self.policy: Callable = init_policy
                 # test your random policy
                 test_random_policy(self.policy, self.env)
             def train(self):
                 """Conduct one iteration of learning."""
                 # TODO: self.value_table may be need to be reset to zeros.
                 # If you think it should, than do it. If not, then go ahead.
                 # self.value_table = np.zeros((self.obs_dim,))
                 self.update value function()
                 self.update_policy()
             def update_value_function(self):
                 count = 0 # count the steps of value updates
                 while True:
                     old_table = self.value_table.copy()
                     for state in range(self.obs_dim):
                         action = self.policy(state)
                         transition_list = self._get_transitions(state, action)
                         state value = 0
                         # Iterate over all possible next states given a state-actio
                         for transition in transition list:
                             prob = transition['prob']
                             reward = transition['reward']
                             next state = transition['next state']
                             done = transition['done']
                             # TODO: compute state value
                             # hint: you should use reward, self.gamma, old_table, p
                             # and next_state to compute the state value
                             state value += prob * (reward + self.gamma * old table[
```

```
# update the state value
            self.value_table[state] = state_value
        # TODO: Compare the old_table and current table to
        # decide whether to break the value update process.
        # hint: you should use self.eps, old_table and self.value_table
        should_break: bool = np.sum(np.fabs(old_table - self.value_tabl)
        if should break:
            print("[DEBUG]\tThe value table was updated for {} steps. "
                  "Difference between new and old table is: {:.4f}".for
                count, np.sum(np.abs(old_table - self.value_table))
            ))
            break
        count += 1
        if count > 6000:
            raise ValueError("Clearly your code has problem. Check it!"
def update_policy(self):
    """You need to define a new policy function, given current
    value function. The best action for a given state is the one that
    has the highest expected return.
    To optimize computing efficiency, we introduce a policy table,
    which is a numpy array taking state as index and return the action
    policy_table: np.ndarray = np.zeros([self.obs_dim, ], dtype=int)
    for state in range(self.obs_dim):
        state_action_values = [0] * self.action_dim
        # TODO: assign the action with greatest state-action value
        # to policy_table[state].
        # Hint:
        # You should use the value table, gamma, reward, as well as
        # the return from self._get_transitions() to compute the
        # state-action value first before getting the action.
        # Bellman equation may help.
        best_action = np.argmax([sum(t['prob'] * (t['reward'] + self.ga
                                for t in self._get_transitions(state, a
                                for action in range(self.action_dim)])
        policy_table[state] = best_action
    self.policy = lambda obs: policy table[obs]
```

Now we have built the Trainer class for policy iteration algorithm. In the following few cells, we will train the agent to solve the problem and evaluate its performance.

```
In [11]: # Solve the TODOs and remove `pass`
         # Managing configurations of your experiments is important for your researc
         default_pi_config = dict(
             max_iteration=1000,
             evaluate_interval=1,
             gamma=1.0,
             eps=1e-10
         def policy_iteration(train_config=None):
             # Prepare a config dict
             config = default_pi_config.copy()
             if train_config is not None:
                 config.update(train_config)
             # Initialize the trainer
             trainer = PolicyIterationTrainer(gamma=config['gamma'], eps=config['eps
             # Initialize an array as the policy mapping obs to action.
             old_policy = np.zeros(trainer.obs_dim, dtype=int)
             old_policy.fill(-1)
             for i in range(config['max_iteration']):
                 # train the agent
                 trainer.train()
                 # TODO: compare the new policy with old policy to check whether
                 # we should stop. If new and old policy have same output given any
                 # observation, then we consider the algorithm is converged and
                 # should be stopped.
                 new_policy = np.array([trainer.policy(obs) for obs in range(trainer
                 should_stop: bool = np.all(old_policy == new_policy)
                 old_policy = new_policy.copy()
                 if should stop:
                     print("We found policy is not changed anymore at "
                           "iteration {}. Current mean episode reward "
                           "is {}. Stop training.".format(i, trainer.evaluate()))
                     break
                 old policy = new policy
                 # evaluate the result
                 if i % config['evaluate_interval'] == 0:
                     print(
                          "[INFO]\tAfter {} iterations, current policy has mean episo
                         "".format(i, trainer.evaluate()))
                     if i > 20:
                         print("You sure your codes is OK? It shouldn't take so many
                                "({}) iterations to train a policy iteration "
                               "agent.".format(i))
             assert trainer.evaluate() > 0.8, \
                 "We expect to get the mean episode reward greater than 0.8. " \
                 "But you get: {}. Please check your codes.".format(trainer.evaluate
             return trainer
```

#### In [12]: # Run this cell without modification

# It may be confusing to call a trainer agent. But that's what we normally
pi\_agent = policy\_iteration()

[DEBUG] The value table was updated for 314 steps. Difference between new and old table is: 0.0000

[INFO] After 0 iterations, current policy has mean episode reward 0.767.

[DEBUG] The value table was updated for 1540 steps. Difference between new and old table is: 0.0000

[INFO] After 1 iterations, current policy has mean episode reward 0.86.

[DEBUG] The value table was updated for 567 steps. Difference between new and old table is: 0.0000

[INFO] After 2 iterations, current policy has mean episode reward 0.788.

[DEBUG] The value table was updated for 973 steps. Difference between new and old table is: 0.0000

[INFO] After 3 iterations, current policy has mean episode reward 0.705.

[DEBUG] The value table was updated for 1199 steps. Difference between new and old table is: 0.0000

[INFO] After 4 iterations, current policy has mean episode reward 0.884.

[DEBUG] The value table was updated for 89 steps. Difference between new a nd old table is: 0.0000

[INFO] After 5 iterations, current policy has mean episode reward 0.882.

[DEBUG] The value table was updated for 0 steps. Difference between new an d old table is: 0.0000

We found policy is not changed anymore at iteration 6. Current mean episod e reward is 0.882. Stop training.

#### In [13]: # Run this cell without modification

Your policy iteration agent achieve 0.882 mean episode reward. The optimal score should be > 0.8.

#### In [14]: # Run this cell without modification

pi agent.render()

(Right)

SFFFFFF

**FFFFFFF** 

FFFHFFF

**FFFFFHFF** 

**FFFHFFF** 

**FHHFFFHF** 

**FHFFHFHF** 

FFFHFFG

```
In [15]: # Run this cell without modification
    pi_agent.print_table()
```

+	++State Value Mapping+								
		0	1	2	3	4	5	6	7
	0	1.000 	1.000	1.000	1.000	1.000	1.000	1.000	1.000
	1	1.000 	1.000	1.000	1.000	1.000	1.000	1.000	1.000
	2	1.000	0.978	0.926	0.000	0.857	0.946	0.982	1.000
	3	1.000	0.935	  0.801 	0.475	0.624	0.000	0.945	1.000
	4	1.000	0.826	  0.542 	0.000	0.539 	0.611	0.852	1.000
	5	1.000 	0.000	0.000 	0.168	0.383	0.442	0.000	1.000
	6	1.000	0.000	0.195	0.121	0.000	0.332	0.000	1.000
	7	1.000	0.732	0.463	0.000	0.277	0.555	0.777	0.000  
-									

Congratulations! You have successfully implemented the policy iteration trainer (if and only if no error happens at the above cells).

Here are few further problems for you to investigate:

- 1. What is the impact of the discount factor gamma?
- 2. What is the impact of the value function convergence criterion epsilon?

If you are interested in doing more investigation (not limited to these two), feel free to open new cells at the end of this notebook and left a clear trace of your thinking and coding, which leads to extra credit if you do a good job. It's an optional job, and you can ignore it.

Now let's continue our journey!

#### **Section 2.2: Value Iteration**

Recall the idea of value iteration. We update the state value:

$$v_{k+1}(s) = \max_{a} E_{s'}[r(s, a) + \gamma v_k(s')]$$

wherein the s' is next state, r is the reward,  $v_k(s')$  is the next state value given by the old (not updated yet) value function. The expectation is computed among all possible transitions (given a state and action pair, it is possible to have many next states, since the environment is not deterministic).

The value iteration algorithm does not require an inner loop. It computes the expected return of all possible actions at a given state and uses the maximum of them as the state value. You can imagine it "pretends" we already have the optimal policy and run policy iteration based on it. Therefore, we do not need to maintain a policy object in a trainer. We only need to retrieve the optimal policy using the same rule as policy iteration, given current value function.

You should implement the trainer following the framework we already wrote for you. Please carefully go through the code and finish all TODO in it.

```
In [16]: # Solve the TODOs and remove `pass`
         class ValueIterationTrainer(PolicyIterationTrainer):
             """Note that we inherit Policy Iteration Trainer, to reuse the
             code of update_policy(). It's same since it get optimal policy from
             current state-value table (self.table).
             def __init__(self, gamma=1.0, env_name='FrozenLake8x8-v1'):
                 super(ValueIterationTrainer, self).__init__(gamma, None, env_name)
             def train(self):
                 """Conduct one iteration of learning."""
                 # TODO: self.value_table may be need to be reset to zeros.
                 # If you think it should, than do it. If not, then move on.
                 # Should not be reset to zero, you update new policy with previous
                 # In value iteration, we do not explicit require a
                 # policy instance to run. We update value function
                 # directly based on the transitions. Therefore, we
                 # don't need to run self.update_policy() in each step.
                 self.update_value_function()
             def update_value_function(self):
                 old_table = self.value_table.copy()
                 for state in range(self.obs_dim):
                     state_value = 0
                     # TODO: Compute the new state value.
                     # Hint: try to compute the state-action value first
                     best_action = np.argmax([sum(t['prob'] * (t['reward'] + self.ga
                                              for t in self._get_transitions(state, a
                                              for action in range(self.action_dim)])
                     state_value = sum(t['prob'] * (t['reward'] + self.gamma * old_t
                                              for t in self. get transitions(state, b
                     self.value_table[state] = state_value
                 # Till now the one-step value update is finished.
                 # You can see that we do not use an inner loop to update
                 # the value function like what we did in the policy iteration.
                 # This is because to compute the state value, which is
                 # an expectation among all possible action given by a
                 # specified policy, we **pretend** we already have the optimal
                 # policy (the max operation). Therefore we don't need to
                 # compute the state-action values for those actions that will not
                 # be selected by the policy.
             def evaluate(self):
                 """Since in value iteration we do not maintain a policy function,
                 so we need to retrieve it when we need it."""
                 self.update policy()
                 return super().evaluate()
             def render(self):
                  """Since in value iteration we do not maintain a policy function,
```

so we need to retrieve it when we need it."""
self.update\_policy()
return super().render()

```
In [17]: # Solve the TODOs and remove `pass`
         # Managing configurations of your experiments is important for your researc
         default_vi_config = dict(
             max_iteration=10000,
             evaluate_interval=100, # don't need to update policy each iteration
             gamma=1.0,
             eps=1e-10
         def value_iteration(train_config=None):
             config = default_vi_config.copy()
             if train config is not None:
                 config.update(train_config)
             # TODO: initialize Value Iteration Trainer. Remember to pass
             # config['gamma'] to it.
             trainer: TabularRLTrainerAbstract = ValueIterationTrainer(gamma=config[
             old_policy = np.zeros(trainer.obs_dim, dtype=int)
             old_policy.fill(-1)
             old_state_value_table = trainer.value_table.copy()
             for i in range(config['max_iteration']):
                 # train the agent
                 trainer.train()
                 # evaluate the result
                 if i % config['evaluate_interval'] == 0:
                     print("[INFO]\tIn {} iteration, current "
                            "mean episode reward is {}.".format(
                          i, trainer.evaluate()
                     ))
                     # TODO: Compare the new policy with old policy to check should
                     # we stop.
                     # Hint: If new and old policy have same output given any
                     # observation, them we consider the algorithm is converged and
                     # should be stopped.
                     # should_stop = np.sum(np.fabs(old_state_value_table - trainer.
                     new policy = np.array([trainer.policy(obs) for obs in range(tra
                     should stop = all(new policy[state] == old policy[state] for st
                     old_policy = new_policy.copy()
                     old_state_value_table = trainer.value_table.copy()
                     if should_stop:
                          print("We found policy is not changed anymore at "
                                "iteration {}. Current mean episode reward "
                                "is {}. Stop training.".format(i, trainer.evaluate())
                         break
                     if i > 3000:
                          print("You sure your codes is OK? It shouldn't take so many
                                 '({}) iterations to train a policy iteration "
                                "agent.".format(
                              i))
             assert trainer.evaluate() > 0.8, \
                  "We expect to get the mean episode reward greater than 0.8. " \setminus
```

```
"But you get: {}. Please check your codes.".format(trainer.evaluate return trainer
```

# In [18]: # Run this cell without modification vi\_agent = value\_iteration()

[INFO] In 0 iteration, current mean episode reward is 0.0.
[INFO] In 100 iteration, current mean episode reward is 0.89.
[INFO] In 200 iteration, current mean episode reward is 0.882.
[INFO] In 300 iteration, current mean episode reward is 0.882.
[INFO] In 400 iteration, current mean episode reward is 0.882.
[INFO] In 500 iteration, current mean episode reward is 0.882.
We found policy is not changed anymore at iteration 500. Current mean episode reward is 0.882. Stop training.

# 

Your value iteration agent achieve 0.882 mean episode reward. The optimal score should be > 0.8.

```
In [20]: # Run this cell without modification
    vi_agent.render()
```

```
In [21]: # Run this cell without modification
    vi_agent.print_table()
```

+		<b></b>	9	State \	/alue N	1appine	Z	<b></b>	+
		0	1	2	3	4	5	6	7
	0	0.999 	0.999 	  0.999 	0.999 	0.999 	0.999	0.999	0.999
	1	0.999 	0.999	0.999	0.999 	0.999	0.999	0.999	0.999  
	2	0.998 	0.976 	  0.925 	0.000 	0.856	0.945	0.981	0.999  
	3	0.997 	0.932	  0.799 	0.474	0.623	0.000	0.944	1.000
	4	0.997 	0.823	  0.541 	0.000 	0.539	0.611	0.851	1.000
	5	0.996 	0.000	0.000 	0.168 	0.383	0.442	0.000	1.000
	6	0.996 	0.000	0.194 	0.121 	0.000	0.332	0.000	1.000
	7	0.996 	0.728	0.461	0.000 	0.277	0.555	0.777	0.000  
_		r - <b></b>		r - <b></b>	r				<del>-</del> -

Congratulation! You have successfully implemented the value iteration trainer (if and only if no error happens at the above cells). Few further problems for you to investigate:

- 1. Do you see that some iteration during training yields better rewards than the final one? Why does that happen?
- 2. What is the impact of the discount factor gamma?
- 3. What is the impact of the value function convergence criterion epsilon?

If you are interested in doing more investigation (not limited to these two), feel free to open new cells at the end of this notebook and left a clear trace of your thinking and coding, which leads to extra credit if you do a good job. It's an optional job, and you can ignore it.

Now let's continue our journey!

### Section 2.3: Compare two model-based agents

Now we have two agents: pi\_agent and vi\_agent . They are believed to be the optimal policies in this environment.

```
In [22]: # Solve the TODO and remove `pass`

# TODO: Print the value tables of these two policies and see if they match
print("Value Table for pi_agent:")
pi_agent.print_table()

print("\nValue Table for vi_agent:")
vi_agent.print_table()

if np.allclose(pi_agent.value_table, vi_agent.value_table):
    print("pi_agent and vi_agent have matching value tables.")
else:
    print("pi_agent and vi_agent have different value tables.")
```

<pre>Value Table for pi_agent: ++State Value Mapping+</pre>								
+					. ''			⊦+   <del>-</del>
	0	'	2 +	3	4	5	6	/
0	İ	  1.000 	  1.000 	  1.000 		j	j	1.000
1   1	1.000 		  1.000 	1.000 	1.000	1.000	1.000	1.000  
2	1.000 	İ	0.926 	0.000 	  0.857 	0.946 		1.000
3		+  0.935 					0.945 	1.000
4	1.000 	0.826 	0.542 	0.000 	0.539 	0.611 	0.852	1.000
+   5 	+  1.000 	0.000 	0.000 	0.168 	0.383 	0.442 	0.000	1.000
6   	1.000 	0.000 	0.195 	İ		İ	0.000	1.000
7 	+  1.000 	0.732   	0.463 	•	  0.277 		0.777	0.000  
•	•	•	•	•	•	•	•	

Value Table for vi_agent: ++State Value Mapping++									
į	0	1					6	7     7	
0	0.999 	0.999 	0.999	0.999 	0.999	0.999	0.999	0.999	
1	0.999 	0.999 	0.999 	0.999 	0.999	0.999	0.999	0.999	
2	+  0.998 	0.976 	0.925 	0.000 	0.856	0.945	0.981	0.999	
3	0.997 	0.932 	0.799 	0.474 	0.623	0.000	0.944	1.000	
4	0.997 	0.823 	0.541 	0.000 	0.539	0.611	0.851	1.000	
5   	0.996 	0.000 	0.000 	0.168 	0.383	0.442	0.000	1.000	
6 	0.996 	0.000 	0.194 	0.121 	0.000	0.332	0.000	1.000	
7   	0.996   	0.728   	0.461   	0.000   	0.277	0.555	0.777   	  0.000    +	

pi\_agent and vi\_agent have different value tables.

- 1. The impact of the discount factor gamma is to help better train the agent. A discounted reward would let agent know it's better to win the game as early as possible.
- 2. The epsilon let us know when the value table converges. Without the epsilon, the value tables are very less likely to match exactly.

What if I compare the value table in value iteration instead of comparing the old & new policies?

The following codes are from section 2.2, I just changed from policy convergence to value function convergence

```
In [23]: # What if I compare the value table in value iteration instead of comparing
         # The following codes are from section 2.2, I just changed from policy conv
         # Managing configurations of your experiments is important for your researc
         default_vi_config = dict(
             max_iteration=10000,
             evaluate interval=100, # don't need to update policy each iteration
             gamma=1.0,
             eps=1e-10
         )
         def value iteration(train config=None):
             config = default_vi_config.copy()
             if train_config is not None:
                 config.update(train_config)
             # TODO: initialize Value Iteration Trainer. Remember to pass
             # config['gamma'] to it.
             trainer: TabularRLTrainerAbstract = ValueIterationTrainer(gamma=config[
             old_policy = np.zeros(trainer.obs_dim, dtype=int)
             old_policy.fill(-1)
             old_state_value_table = trainer.value_table.copy()
             for i in range(config['max_iteration']):
                 # train the agent
                 trainer.train()
                 # evaluate the result
                 if i % config['evaluate_interval'] == 0:
                     print("[INFO]\tIn {} iteration, current "
                            "mean episode reward is {}.".format(
                         i, trainer.evaluate()
                     ))
                     # TODO: Compare the new policy with old policy to check should
                     # we stop.
                     # Hint: If new and old policy have same output given any
                     # observation, them we consider the algorithm is converged and
                     # should be stopped.
                     should stop = np.sum(np.fabs(old state value table - trainer.va
                     # new_policy = np.array([trainer.policy(obs) for obs in range(t
                     # should_stop = all(new_policy[state] == old_policy[state] for
                     # old_policy = new_policy.copy()
                     old_state_value_table = trainer.value_table.copy()
                     if should stop:
                         print("We found policy is not changed anymore at "
                                "iteration {}. Current mean episode reward "
                               "is {}. Stop training.".format(i, trainer.evaluate())
                         break
                     if i > 3000:
                         print("You sure your codes is OK? It shouldn't take so many
                                "({}) iterations to train a policy iteration "
                                "agent.".format(
                             i))
```

```
assert trainer.evaluate() > 0.8, \
    "We expect to get the mean episode reward greater than 0.8. " \
    "But you get: {}. Please check your codes.".format(trainer.evaluate
    return trainer
```

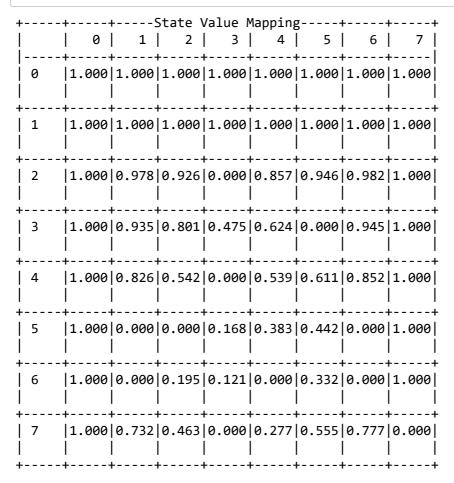
# In [24]: vi\_agent = value\_iteration()

```
[INFO] In 0 iteration, current mean episode reward is 0.0.
       In 100 iteration, current mean episode reward is 0.89.
[INFO]
       In 200 iteration, current mean episode reward is 0.882.
       In 300 iteration, current mean episode reward is 0.882.
[INFO]
       In 400 iteration, current mean episode reward is 0.882.
[INFO]
       In 500 iteration, current mean episode reward is 0.882.
[INFO]
[INFO] In 600 iteration, current mean episode reward is 0.882.
[INFO]
       In 700 iteration, current mean episode reward is 0.882.
[INFO] In 800 iteration, current mean episode reward is 0.882.
[INFO] In 900 iteration, current mean episode reward is 0.882.
[INFO] In 1000 iteration, current mean episode reward is 0.882.
[INFO] In 1100 iteration, current mean episode reward is 0.882.
[INFO] In 1200 iteration, current mean episode reward is 0.882.
[INFO] In 1300 iteration, current mean episode reward is 0.882.
[INFO] In 1400 iteration, current mean episode reward is 0.882.
[INFO] In 1500 iteration, current mean episode reward is 0.882.
[INFO] In 1600 iteration, current mean episode reward is 0.882.
[INFO] In 1700 iteration, current mean episode reward is 0.882.
[INFO] In 1800 iteration, current mean episode reward is 0.882.
[INFO] In 1900 iteration, current mean episode reward is 0.882.
[INFO] In 2000 iteration, current mean episode reward is 0.882.
We found policy is not changed anymore at iteration 2000. Current mean epi
sode reward is 0.882. Stop training.
```

If we check the avg reward, it's the same, maybe not exactly the same, but the 3figs are 0.882. So now let's render the game env and check out the value table.

```
In [25]: vi_agent.render()
```

In [26]: vi\_agent.print\_table()



This is differenet with the value table in section 2.2. But if we compare this with the value table from policy iteration, the values match. Why?

As I concerned, you can use both policy convergence and value table convergence for both policy and value iterations to find the optimal policy. However, they generate slightly different results, overall they are almost the same, both optimal. Value iteration mostly use value table convergence because we update the value function in each state, and it's also straightforward to compare the value tables. On top of that, comparing the value function can be computationally efficient because it only requires comparing real numbers. You don't need to store and compare policies for each state, which can be more complex and computationally intensive.

In contrast, policy iteration aims to find the optimal policy, and it alternates between policy evaluation and policy improvement. While you can use policy convergence as a stopping criterion in policy iteration, it involves maintaining and comparing policies at each iteration, which can be more complex and computationally demanding.

# **Conclusion and Discussion**

In this assignment, we learn how to use the gym (now Gymnasium) library, how to use Object Oriented Programming to build a basic tabular RL algorithm.

Follow the submission instruction in the README to submit your assignment. Thank you!