

A Mouse on a Checkerboard (150 points)

Introduction

A mouse is on a checkerboard of size $M \times N$ (The North West corner is $(0,0)$). With every step, the mouse can move **North**, **East**, **South**, **West** or **Stay** at the same place with probabilities P_n , P_e , P_s , P_w and P_{stay} respectively.

The mouse starts on position (X_0, Y_0) .

What is the probability of finding the mouse at position (X_f, Y_f) after K steps?

Note that if the mouse is on the border, the probabilities are **renormalized** to take into account the impossibility of moving in one or more directions.

Input Specifications

M , N , X_0 , Y_0 , X_f , Y_f , K are integers P_n , P_e , P_s , P_w , P_{stay} are floats.

Your program will take a single line in the following format as input:

- $M \ N \ P_n \ P_e \ P_s \ P_w \ P_{stay} \ X_0 \ Y_0 \ X_f \ Y_f \ K$

Output Specifications

The probability of finding the mouse on $X_f \ Y_f$ after K steps, **truncated** at 3rd decimal e.g:

- $0.02398754245 \Rightarrow 0.023$

Sample Input/Output

Input

3 3 0.25 0.25 0.25 0.25 0 1 1 0 1 1

Output

0.25

Explanation

After one step the mouse has a probability of 25% to be North of the starting position.

Input

9 9 0.25 0.25 0.125 0.125 0.25 4 4 4 4 3

Output

0.109

Explanation

The probability of finding the mouse in the initial position after 3 steps is $\sim 10.9\%$.

Input

3 3 0.25 0.25 0.125 0.125 0.25 1 1 1 1 10

Output

0.121

Explanation

On the border, the mouse cannot move in certain directions. The remaining options need to have their probability re-normalized.