# **ANLY590 HW0**

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Regularization. Using the accompanying Hitters dataset, we will explore regression models to predict a player's Salary from other variables. You can use any programming languages or frameworks that you wish.

https://gist.github.com/keeganhines/59974f1ebef97bbaa44fb19143f90bad

(https://gist.github.com/keeganhines/59974f1ebef97bbaa44fb19143f90bad) (Links to an external site.)Links to an external site.

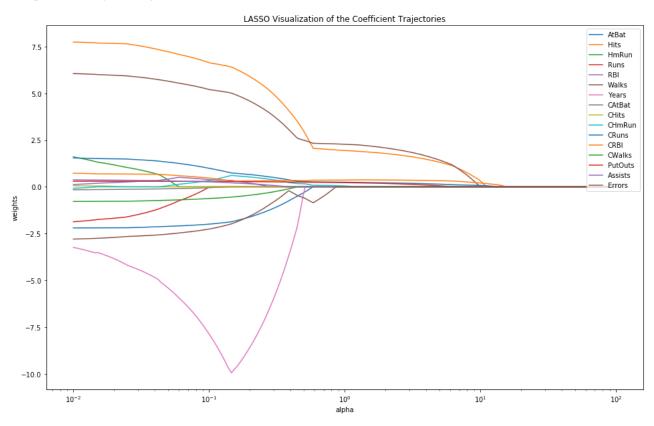
### **Problem 1**

# 1.1 Use LASSO regression to predict Salary from the other numeric predictors (you should omit the categorical predictors).

```
In [1]:
        import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        from sklearn.linear_model import Ridge, RidgeCV, Lasso, LassoCV
        from sklearn.metrics import mean_squared_error
        Hitters = pd.read csv('Hitters.csv')
        #print(Hitters.head())
        # remove dummy variables and NA
        num_idx = []
        for i, t in enumerate(Hitters.dtypes):
            if str(t) in ["int64", "float64"]:
                num idx.append(i)
            df = Hitters.iloc[:,num idx]
        df = df.dropna()
        print(df.head())
        X = df.iloc[:,:-1]
        Y = df.iloc[:,-1]
           AtBat Hits HmRun Runs RBI
                                          Walks Years CAtBat CHits CHmRun CRuns
        1
             315
                   81
                           7
                                 24
                                     38
                                             39
                                                    14
                                                          3449
                                                                  835
                                                                           69
                                                                                 321
        2
             479
                   130
                           18
                                 66
                                     72
                                             76
                                                    3
                                                          1624
                                                                  457
                                                                           63
                                                                                 224
             496
                  141
                           20
                                 65
                                     78
                                                          5628
                                                                 1575
                                                                                 828
        3
                                             37
                                                    11
                                                                          225
                                                    2
             321
                   87
                           10
                                 39
                                      42
                                             30
                                                          396
                                                                 101
                                                                                 48
        4
                                                                          12
             594
                   169
                            4
                                 74
                                      51
                                             35
                                                    11
                                                          4408
                                                                 1133
                                                                           19
                                                                                 501
           CRBI CWalks PutOuts Assists Errors Salary
            414
                    375
                             632
                                                    475.0
                                       43
                                               10
        2
            266
                    263
                             880
                                       82
                                               14
                                                    480.0
                             200
                                                    500.0
        3
            838
                    354
                                       11
                                               3
                             805
                                                    91.5
            46
                    33
                                       40
                                               4
            336
                    194
                             282
                                      421
                                               25
                                                    750.0
```

```
In [2]:
        #Create a visualization of the coefficient trajectories.
        alphas = np.logspace(-2,2,200)
        alphas
        lasso = Lasso(max_iter = 10000, normalize = True)
        coefs = []
        for a in alphas:
            lasso.set_params(alpha=a)
            lasso.fit(X, Y)
            coefs.append(lasso.coef_)
        plt.figure(figsize=(16, 10))
        ax = plt.gca()
        ax.plot(alphas, coefs)
        ax.set_xscale('log')
        plt.xlabel('alpha')
        plt.ylabel('weights')
        plt.axis('tight')
        plt.title('LASSO Visualization of the Coefficient Trajectories')
        plt.legend(list(X), loc=1)
```

Out[2]: <matplotlib.legend.Legend at 0x10f05d4e0>



```
In [3]: #Comment on which are the final three predictors that remain in the model.
    lasso = Lasso(max_iter = 10000, normalize = True)
    #Based on the graph above, there are three non-zero predictor around alpha = 10.5
    #Then try the lasso model with that alpha and print out the coefs.
    lasso.set_params(alpha=10.5)
    lasso.fit(X, Y)
    table = pd.DataFrame()
    table['Predictor']=X.columns
    table['Coefs']=list(lasso.coef_)
    table
```

#### Out[3]:

	Predictor	Coefs
0	AtBat	0.000000
1	Hits	0.183459
2	HmRun	0.000000
3	Runs	0.000000
4	RBI	0.000000
5	Walks	0.000000
6	Years	0.000000
7	CAtBat	0.000000
8	CHits	0.000000
9	CHmRun	0.000000
10	CRuns	0.069606
11	CRBI	0.190326
12	CWalks	0.000000
13	PutOuts	0.000000
14	Assists	0.000000
15	Errors	0.000000

Based on the result table above, the final three predictors that remain in the model are Hits, CRuns, and CRBI.

```
In [4]: #Use cross-validation to find the optimal value of the regularization penality.
lassocv = LassoCV(alphas = None, cv = 10, max_iter = 100000, normalize = True)
lassocv.fit(X, Y)
opitmal_alpha = lassocv.alpha_
print(lassocv.alpha_)
```

0.0635481759986

```
In [5]: #How many predictors are left in that model?
lasso = Lasso(max_iter = 10000, normalize = True)
lasso.set_params(alpha=lassocv.alpha_)
lasso.fit(X, Y)
opt_table = pd.DataFrame()
opt_table['Predictor']=X.columns
opt_table['Coefs']=list(lasso.coef_)
opt_table
```

### Out[5]:

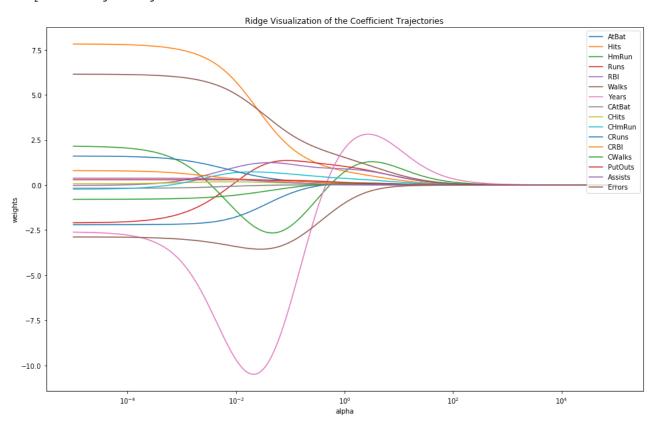
	Predictor	Coefs
0	AtBat	-2.082954
1	Hits	7.041011
2	HmRun	0.000000
3	Runs	-0.682615
4	RBI	0.496552
5	Walks	5.511781
6	Years	-6.107625
7	CAtBat	-0.087066
8	CHits	0.000000
9	CHmRun	0.156468
10	CRuns	1.228061
11	CRBI	0.583821
12	CWalks	-0.690601
13	PutOuts	0.292694
14	Assists	0.304372
15	Errors	-2.450795

With the optimal alpha, there are 14 predictors left in the model (except HmRum and CHits, the rest are all remained).

# 1.2 Repeat with Ridge Regression.

```
In [6]:
        #Create a visualization of the coefficient trajectories.
        alphas = np.logspace(-5,5,200)
        alphas
        ridge = Ridge(normalize=True)
        coefs = []
        for a in alphas:
            ridge.set_params(alpha=a)
            ridge.fit(X, Y)
            coefs.append(ridge.coef_)
        # Plot alpha-coefficient relation# Plot
        plt.figure(figsize=(16, 10))
        ax = plt.gca()
        ax.plot(alphas, coefs)
        ax.set_xscale('log')
        plt.xlabel('alpha')
        plt.ylabel('weights')
        plt.axis('tight')
        plt.title('Ridge Visualization of the Coefficient Trajectories')
        plt.legend(list(X), loc=1)
```

Out[6]: <matplotlib.legend.Legend at 0x1153f8588>



## Comment on which are the final three predictors that remain in the model.

By the definition of Ridge Model, there is no last three predictors, since all coefs are approach to zero but not exactly zero, therefore, all the predictors are still remain in the model.

```
In [7]: ridgecv = RidgeCV(alphas=alphas, cv=10, normalize=True)
    ridgecv.fit(X, Y)
    opitmal_alpha = ridgecv.alpha_
    print(opitmal_alpha)
```

0.943787827778

### Explain in your own words the bias-variance tradeoff.

Bias discribes how well a model is able to predict the value given a specific data set. High bias indicates that the model (is too simple) does not fit the data set well, while low bias means the model (is complex enough) does fit the data set well.

Variance is the sensitivity to small changes in data set, it discribes how well a model is able to fit with different data sets. High variance indicateds that the difference between the errors from different sets are large, i.e. the model is not that good, while low variance means the difference between the errors are small, i.e. the model is good.

For instance, given a training set, if the model has low bias, then the model fit the training set well. Given the training set and test set, if the difference between the training error and the test error is small, then the model has small variance and is a good model to use.

The Bias-Variance Tradeoff is property which indicates that if the model has a lower bias for estimating the parameters, it would has a higer variance across different sets. It is hard to obtain a model with very a low bias as well as a low variance. Since when the bias getting smaller, the model become more complex, it would more likely be overfitting the data set, and the difference between the sample errors would most likely be large.

#### What role does regularization play in this tradeoff?

Regularization helps to indicate which predictors are more significant and which are not that important. It leads the increase on bias and decrease on variance when we dropping off the not important predictors i.e. making the model less flexible.

### Make reference to your findings in number (1) to describe models of high/low bias and variance.

On order to show this, I split the data set into training set and test set, and compute the MSE under different alphas for both Lasso and Ridge Regression.

```
In [8]: #With Lasso
        from sklearn.model selection import train test split
        X_train, X_test , Y_train, Y_test = train_test_split(X, Y, test_size=0.7, random_state=1)
        alphas = [0.01, 0.1, 0.5, 1, 5, 15, 50, 100]
        lasso_train_MSE=[]
        lasso_test_MSE=[]
        lasso = Lasso(max iter = 10000, normalize = True)
        for a in alphas:
            lasso.set params(alpha=a)
            lasso.fit(X train, Y train)
            lasso train MSE.append(mean squared error(Y train, lasso.predict(X train)))
            lasso_test_MSE.append(mean_squared_error(Y_test, lasso.predict(X_test)))
        lasso_table = pd.DataFrame()
        lasso_table['Alpha'] = alphas
        lasso_table['Training MSE'] = lasso_train_MSE
        lasso_table['Test MSE'] = lasso_test_MSE
        lasso_table
```

### Out[8]:

	Alpha	Training MSE	Test MSE
0	0.01	66877.365168	123130.857886
1	0.10	67595.871902	119273.218688
2	0.50	74812.022447	120318.142136
3	1.00	79718.386357	120477.902358
4	5.00	94595.209731	121616.343007
5	15.00	125756.414794	122833.378231
6	50.00	263192.251623	178776.733180
7	100.00	263192.251623	178776.733180

```
In [9]: #With Ridge
    ridge_train_MSE=[]
    ridge = Ridge(normalize=True)
    for a in alphas:
        ridge.set_params(alpha=a)
            ridge.fit(X_train, Y_train)
        ridge_train_MSE.append(mean_squared_error(Y_train, ridge.predict(X_train)))
        ridge_test_MSE.append(mean_squared_error(Y_test, ridge.predict(X_test)))

ridge_table = pd.DataFrame()
    ridge_table['Alpha'] = alphas
    ridge_table['Training MSE'] = ridge_train_MSE
    ridge_table['Test_MSE'] = ridge_test_MSE
    ridge_table['Test_MSE'] = ridge_test_MSE
    ridge_table['Test_MSE'] = ridge_test_MSE
```

#### Out[9]:

	Alpha	Training MSE	Test MSE
0	0.01	71150.169800	116882.263571
1	0.10	83931.147426	122482.489442
2	0.50	95434.229498	120550.805510
3	1.00	102595.459542	117998.502735
4	5.00	135651.335159	118879.865607
5	15.00	180126.430265	135709.126133
6	50.00	226707.300045	158906.404145
7	100.00	243013.612782	167654.410543

From the above tables, when alpha increases, the training MSE increase, i.e. the bias of the model increases, and the test MSE and training MSE are first getting closer i.e. the model is getting less overfitting (variance decreases) until reach the optimal alpha. However, after the optimal alpha, as alpha keep increasing, the training MSE still increases, i.e. the bias of the model getting bigger and bigger; the test MSE and training MSE are getting further away from each other and the model is getting worse.