# Attribute-Based Encryption With Verifiable Outsourced Decryption

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*Abstract*—Attribute-based encryption (ABE) is a public-key-based one-to-many encryption that allows users to encrypt and decrypt data based on user attributes. A promising application of ABE is flexible access control of encrypted data stored in the cloud, using access polices and ascribed attributes associated with private keys and ciphertexts. One of the main efficiency drawbacks of the existing ABE schemes is that decryption involves expensive pairing operations and the number of such operations grows with the complexity of the access policy. Recently, Green *et al.* proposed an ABE system with outsourced decryption that largely eliminates the decryption overhead for users. In such a system, a user provides an untrusted server, say a cloud service provider, with a transformation key that allows the cloud to translate any ABE ciphertext satisfied by that user's attributes or access policy into a simple ciphertext, and it only incurs a small computational overhead for the user to recover the plaintext from the transformed ciphertext. Security of an ABE system with outsourced decryption ensures that an adversary (including a malicious cloud) will not be able to learn anything about the encrypted message; however, it does not guarantee the correctness of the transformation done by the cloud. In this paper, we consider a new requirement of ABE with outsourced decryption: verifiability. Informally, verifiability guarantees that a user can efficiently check if the transformation is done correctly. We give the formal model of ABE with verifiable outsourced decryption and propose a concrete scheme. We prove that our new scheme is both secure and verifiable, without relying on random oracles. Finally, we show an implementation of our scheme and result of performance measurements, which indicates a significant reduction on computing resources imposed on users.

*Index Terms*—Attribute-based encryption, outsourced decryption, verifiability.

## I. INTRODUCTION

IN distributed settings with untrusted servers, such as the cloud, many applications need mechanisms for complex access-control over encrypted data. Sahai and Waters [1] addressed this issue by introducing the notion of attribute-based encryption (ABE). ABE is a new public key based one-to-many encryption that enables access control over encrypted data using access policies and ascribed attributes associated with private keys and ciphertexts. There are two kinds of ABE schemes: key-policy ABE (KP-ABE) [2]–[7] and ciphertext-policy ABE (CP-ABE) [8], [9], [5], [6]. In a CP-ABE scheme, every ciphertext is associated with an access policy on attributes, and every user's private key is associated with a set of attributes. A user is able to decrypt a ciphertext only if the set of attributes associated with the user's private key satisfies the access policy associated with the ciphertext. In a KP-ABE scheme, the roles of an attribute set and an access policy are swapped from what we described for CP-ABE: attributes sets are used to annotate the ciphertexts and access polices over these attributes are associated with users' private keys. In the following, we will use the terms access policy, access structure and access formula interchangeably.

One of the main efficiency drawbacks of the most existing ABE schemes is that decryption is expensive for resource-limited devices due to pairing operations, and the number of pairing operations required to decrypt a ciphertext grows with the complexity of the access policy. At the cost of security, only proven in a weak model (i.e., selective security), there exist several expressive ABE schemes [10], [11] where the decryption algorithm only requires a constant number of pairing computations. Recently, Green *et al.* [12] proposed a remedy to this problem by introducing the notion of ABE with outsourced decryption, which largely eliminates the decryption overhead for users. Based on the existing ABE schemes, Green *et al.* [12] also presented concrete ABE schemes with outsourced decryption. In these schemes (refer to Fig. 1 below), a user provides an untrusted server, say a proxy operated by a cloud service provider, with a transformation key TK that allows the latter to translate any ABE ciphertext CT satisfied by that user's attributes or access policy into a simple ciphertext CT', and it only incurs a small overhead for the user to recover the plaintext from the
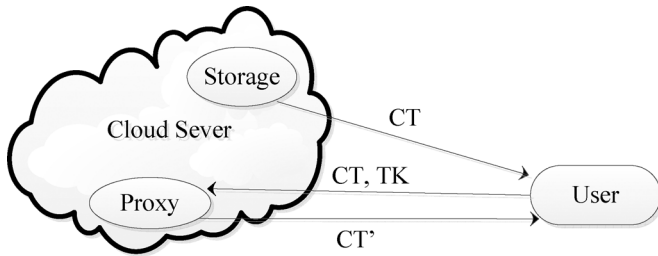
Fig. 1.   ABE system with outsourced decryption.

transformed ciphertext CT'. The security property of the ABE scheme with outsourced decryption guarantees that an adversary (including the malicious cloud server) be not able to learn anything about the encrypted message; however, the scheme provides no guarantee on the correctness of the transformation done by the cloud server. In the cloud computing setting, cloud service providers may have strong financial incentives to return incorrect answers, if such answers require less work and are unlikely to be detected by users.

Consider a cloud based electronic medical record system in which patients' medical records are protected using ABE schemes with outsourced decryption (e.g., [12]) and are stored in the cloud. In order to efficiently access patients' medical records on her mobile phone, a doctor generates and delegates a transformation key to a proxy in the cloud for outsourced decryption; Given a transformed ciphertext from the proxy, the doctor can read a patient's medical record by just performing a simple step of computation. If no verification of the correctness of the transformation is guaranteed, however, the system might run into the following two problems: 1) for the purpose of saving computing cost, the proxy could return a medical record transformed previously for the same doctor; 2) due to system malfunction or malicious attack, the proxy could send the medical record of another patient or a file of the correct form but carrying wrong information. The consequence of treating the patient based on incorrect information could be very serious or even catastrophic.

The above observation motivates us to study ABE with verifiable outsourced decryption in this paper. We emphasize that an ABE scheme with secure outsourced decryption does not necessarily guarantee verifiability (i.e., correctness of the transformation done by the cloud server). For example, the secure ABE schemes with outsourced decryption proposed by Green *et al.* in [12] are not verifiable, as we will show in Section III.

### A.  Our Contributions

In [12], Green *et al.* also considered the verifiability of the cloud's transformation and provided a method to check the correctness of the transformation. However, the authors did not formally define verifiability. In fact, as we will demonstrate in Section III, it is not feasible to construct ABE schemes with verifiable outsourced decryption following the model defined in [12]. Moreover, the method proposed in [12] relies on random oracles (RO) [13]. Unfortunately, the RO model is heuristic, and a proof of security in the RO model does not directly imply anything about the security of an ABE scheme in the real world. It is well known that there exist cryptographic schemes which are

secure in the RO model but are inherently insecure when the RO is instantiated with any real hash function [14]–[17].

In this paper, we first modify the original model of ABE with outsourced decryption in [12] to allow for verifiability of the transformations. After describing the formal definition of verifiability, we propose a new ABE model and based on this new model construct a concrete ABE scheme with verifiable outsourced decryption. Our scheme does not rely on random oracles.

During the rest of the paper, we only focus on CP-ABE with verifiable outsourced decryption. The same approach applies to KP-ABE with verifiable outsourced decryption, which we will omit here in order to keep the paper compact.

To assess the performance of our ABE scheme with verifiable outsourced decryption, we implement the CP-ABE scheme with verifiable outsourced decryption and conduct experiments on both an ARM-based mobile device and an Intel-core personal computer to model a mobile user and a proxy, respectively. Our software is based on the CP-ABE implementation in the libfenc [18] library. Through the experiments, we find that it takes almost 50 seconds for the mobile device to execute a standard decryption on ABE ciphertext with policy consisting of 100 attributes. On the other hand, the Intel processor takes less than 5 seconds to decrypt the same ABE ciphertext. With the outsourced decryption, we shift this burdensome task from the mobile device to the proxy, which results in a significant reduction on computing cost for the mobile device. As a consequence, decrypting the ciphertext took approximately 180 milliseconds on the ARM-based device.

### B.  Related Work

In this subsection, we review some closely related works, including noninteractive verifiable computation, pairing delegation and proxy reencryption.

*Noninteractive Verifiable Computation:*  Noninteractive verifiable computation [19], [20] enables a computationally weak client to outsource the computation of a function to one or more workers. The workers return the result of the function evaluation as well as a noninteractive proof that the computation of the function was carried out correctly. Since these schemes [19], [20] deal with outsourcing of general computation problems and preserve the privacy of input data, they can be used to outsource decryption in ABE systems. However, the schemes proposed in [19], [20] use Gentry's fully homomorphic encryption system [21] as a building block, and thus the overhead in these schemes is currently too large to be practical [22]. Recently, Parno *et al.* [23] establish an important connection between verifiable computation and ABE. They show how to construct a verifiable computation scheme with public delegation and public verifiability from any ABE scheme and how to construct a multifunction verifiable computation scheme from the ABE scheme with outsourced decryption presented in [12]. Goldwasser *et al.* [24] propose a succinct functional encryption scheme for general functions, and show that, by replacing the ABE scheme used in [23] with their succinct functional encryption scheme, one can obtain a delegation scheme with is both publicly verifiable and secret, in the sense that the prover does not learn anything about the input or output of the function being delegated. All

these schemes [19], [20], [23], [24] focus on delegating general functions, and are not sufficiently efficient for the problem at hand.

*Pairing Delegation:* Pairing delegation [25], [26] enables a client to outsource the computation of parings to another entity. However, the schemes proposed in [25], [26] still require the client to compute multiple exponentiations in the target group for every pairing it outsources. Most importantly, when using paring delegation in the decryption of ABE ciphertexts, the amount of computation of the client is still proportional to the size of the access policy. Tsang *et al.* [27] consider batch pairing delegation. However, the scheme proposed in [27] can only handle batch delegation for pairings in which one of the points is a constant and it still requires the client to compute a pairing.

*Proxy Reencryption:* In ABE with outsourced decryption, a user provides the cloud with a transformation key that allows the cloud to translate an ABE ciphertext on message $m$ into a simple ciphertext on the same $m$, without learning anything about $m$. This is reminiscent of the concept of proxy reencryption [28], [29]. Proxy reencryption allows a proxy, using a reencryption key, to transform an encryption of $m$ under Alice's public key into an encryption of the same $m$ under Bob's public key without the proxy learning anything about the encrypted message $m$. We emphasize that in the model of proxy reencryption, verifiability of the proxy's transformation cannot be achieved. This can be briefly explained as follows. A proxy could replace the encryption of $m$ under Alice's public key with the encryption of another message $m'$ under Alice's public key and then use its reencryption key to transform the latter into an encryption of $m'$ under Bob's public key. Obviously, without interaction with Alice, Bob cannot detect this malicious behavior of the proxy.

### C. Organization

The rest of the paper is organized as follows. In Section II, we review some standard notations and cryptographic definitions. In Section III, we describe our new model of CP-ABE with verifiable outsourced decryption. We present a new CP-ABE scheme with verifiable outsourced decryption and its security analysis in Section IV. Section V shows the experimental results on the performance of our proposed scheme. Finally, we state our conclusion in Section VI.

## II. PRELIMINARIES

If $S$ is a set, then $s \xleftarrow{\$} S$ denotes the operation of picking an element $s$ uniformly at random from $S$. Let $\mathbb{N}$ denote the set of natural numbers. If $\lambda \in \mathbb{N}$ then $1^\lambda$ denotes the string of $\lambda$ ones. Let $z \leftarrow \mathsf{A}(x, y, \ldots)$ denote the operation of running an algorithm $\mathsf{A}$ with inputs $(x, y, \ldots)$ and output $z$. A function $f(\lambda)$ is *negligible* if for every $c > 0$ there exists a $\lambda_c$ such that $f(\lambda) < 1/\lambda^c$ for all $\lambda > \lambda_c$.

### A. Bilinear Groups

Let $\mathcal{G}$ be an algorithm that takes as input a security parameter $\lambda$ and outputs a tuple $(p, \mathbb{G}, \mathbb{G}_T, e)$, where $\mathbb{G}$ and $\mathbb{G}_T$ are multiplicative cyclic groups of prime order $p$, and $e : \mathbb{G} \times \mathbb{G} \to \mathbb{G}_T$ is a map such that:

1) **Bilinearity:** $e(g^a, h^b) = e(g, h)^{ab}$ for all $g, h \in \mathbb{G}$ and $a, b \in \mathbb{Z}_p^*$.
2) **Nondegeneracy:** $e(g, h) \neq 1$ whenever $g, h \neq 1_{\mathbb{G}}$.
3) **Computable:** efficient computability for any input pair.

We refer to the tuple $(p, \mathbb{G}, \mathbb{G}_T, e)$ as a *bilinear group*.

### B. Complexity Assumptions

We state below the complexity assumption to be used in the paper.

*a) Discrete Logarithm (DL) Assumption:* Let $(p, \mathbb{G}, \mathbb{G}_T, e)$ be a prime order bilinear group system. Given $(p, \mathbb{G}, \mathbb{G}_T, e, \ g, g^x)$, where $g \in \mathbb{G}$ and $x \in \mathbb{Z}_p^*$ are chosen uniformly at random, the DL problem in $(p, \mathbb{G}, \mathbb{G}_T, e)$ is to compute $x$. The DL assumption in the prime order bilinear group system $(p, \mathbb{G}, \mathbb{G}_T, e)$ is that no probabilistic polynomial-time (PPT) algorithm $\mathcal{A}$ can solve the DL problem with nonnegligible advantage. The advantage of $\mathcal{A}$ is defined as

$$\Pr[\mathcal{A}(p, \mathbb{G}, \mathbb{G}_T, e, \ g, g^x) = x]$$

where the probability is over the randomly chosen $g, x$ and the random bits consumed by $\mathcal{A}$.

### C. Access Structures

*Definition 1 (Access Structure [30]):* Let $\{P_1, \ldots, P_n\}$ be a set of parties. A collection $\mathbb{A} \subseteq 2^{\{P_1, \ldots, P_n\}}$ is monotone for $\forall B$ and $C$, if $B \in \mathbb{A}, B \subseteq C$, then $C \in \mathbb{A}$. An access structure (respectively, monotone access structure) is a collection (respectively, monotone collection) $\mathbb{A}$ of nonempty subsets of $\{P_1, \ldots, P_n\}$, i.e., $\mathbb{A} \subseteq 2^{\{P_1, \ldots, P_n\}} \setminus \{\emptyset\}$. The sets in $\mathbb{A}$ are called authorized sets, and the sets not in $\mathbb{A}$ are called unauthorized sets.

In our context, attributes play the role of parties and we restrict our attention to monotone access structures. It is possible to (inefficiently) realize general access structures using our techniques by treating the negation of an attribute as a separate attribute.

### D. Linear Secret Sharing Schemes

Our construction will employ linear secret-sharing schemes. We use the definition adapted from [30].

*Definition 2 (Linear Secret-Sharing Schemes (LSSS)):* A secret sharing scheme $\Pi$ over a set of parties $\mathcal{P}$ is called linear (over $\mathbb{Z}_p$) if

1) The shares for each party form a vector over $\mathbb{Z}_p$.
2) There exists a matrix $\mathbf{A}$ with $\ell$ rows and $n$ columns called the share-generating matrix for $\Pi$. For all $i = 1, \ldots, \ell$, the $i$th row of $\mathbf{A}$ is labeled by a party $\rho(i)$ ($\rho$ is a function from $\{1, \ldots, \ell\}$ to $\mathcal{P}$). When we consider the column vector $v = (s, r_2, \ldots, r_n)$, where $s \in \mathbb{Z}_p$ is the secret to be shared, and $r_2, \ldots, r_n \in \mathbb{Z}_p$ are randomly chosen, then $\mathbf{A}v$ is the vector of $\ell$ shares of the secret $s$ according to $\Pi$. The share $(\mathbf{A}v)_i$ belongs to party $\rho(i)$.

It is shown in [30] that every linear secret-sharing scheme according to the above definition also enjoys the linear reconstruction property, defined as follows. Suppose that $\Pi$ is an LSSS for the access structure $\mathbb{A}$. Let $S \in \mathbb{A}$ be any authorized set, and let $I \subset \{1, \ldots, \ell\}$ be defined as $I = \{i \mid \rho(i) \in S\}$. Then there

exist constants $\{\omega_i \in \mathbb{Z}_p\}_{i \in I}$ such that, if $\{\lambda_i\}$ are valid shares of any secret $s$ according to $\Pi$, then $\sum_{i \in I} \omega_i \lambda_i = s$. Let $A_i$ denotes the $i$th row of $\mathbb{A}$, we have $\sum_{i \in I} \omega_i A_i = (1, 0, \ldots, 0)$. These constants $\{\omega_i\}$ can be found in time polynomial in the size of the share-generation matrix $\mathbf{A}$ [30]. Note that, for unauthorized sets, no such constants $\{\omega_i\}$ exist.

**Boolean Formulas** Access structures might also be described in terms of monotonic boolean formulas. Using standard techniques one can convert any monotonic boolean formula into an LSSS representation. We can represent the boolean formula as an access tree. An access tree of $\ell$ nodes will result in an LSSS matrix of $\ell$ rows. We refer the reader to the Appendix of [31] for a discussion on how to perform this conversion.

### E. CP-ABE

A CP-ABE scheme consists of the following four algorithms:
- Setup$(\lambda, U)$ takes as input a security parameter $\lambda$ and an attribute universe description $U$. It outputs the public parameters PK and a master secret key MSK.
- KeyGen$(\text{PK}, \text{MSK}, \mathcal{S})$ takes as input the public parameters PK, the master secret key MSK and a set of attributes $\mathcal{S}$. It outputs a private key $\text{SK}_{\mathcal{S}}$.
- Encrypt$(\text{PK}, M, \mathbb{A})$ takes as input the public parameters PK, a message $M$ and an access structure $\mathbb{A}$. It outputs a ciphertext $CT$.
- Decrypt$(\text{PK}, \text{SK}_{\mathcal{S}}, CT)$ takes as input the public parameters PK, a private key $\text{SK}_{\mathcal{S}}$ for $\mathcal{S}$ and a ciphertext $CT$. It outputs a message $M$.

Let $(\text{PK}, \text{MSK}) \leftarrow \text{Setup}(1^\lambda)$, $\text{SK}_{\mathcal{S}} \leftarrow \text{KeyGen}(\text{PK}, \text{MSK}, \mathcal{S})$, $CT \leftarrow \text{Encrypt}(\text{PK}, M, \mathbb{A})$. For correctness, we require the following to hold:
1) If the set $\mathcal{S}$ of attributes satisfies the access structure $\mathbb{A}$, then $M \leftarrow \text{Decrypt}(\text{PK}, \text{SK}_{\mathcal{S}}, CT)$;
2) Otherwise, $\text{Decrypt}(\text{PK}, \text{SK}_{\mathcal{S}}, CT)$ outputs the error symbol $\perp$.

We now give the definition of indistinguishability under chosen-ciphertext attack (CCA security) for CP-ABE scheme. This is described by a game between a challenger and an adversary $\mathcal{A}$. The game proceeds as follows:
- Setup The challenger runs Setup algorithm to obtain the public parameters PK and a master secret key MSK. It gives the public parameters PK to the adversary $\mathcal{A}$ and keeps MSK to itself.
- Query phase 1 The challenger initializes an empty set $D$. The adversary $\mathcal{A}$ adaptively issues queries:
  1) *Private key* query, on input a set of attributes $\mathcal{S}$: The challenger runs $\text{SK}_{\mathcal{S}} \leftarrow \text{KeyGen}(\text{PK}, \text{MSK}, \mathcal{S})$ and sets $D = D \cup \{\mathcal{S}\}$. It then returns to the adversary the private key $\text{SK}_{\mathcal{S}}$.
  2) *Decryption* query, on a set of attributes $\mathcal{S}$ and a ciphertext $CT$: The challenger runs $\text{SK}_{\mathcal{S}} \leftarrow \text{KeyGen}(\text{PK}, \text{MSK}, \mathcal{S})$ and $M \leftarrow \text{Decrypt}(\text{PK}, \text{SK}_{\mathcal{S}}, CT)$. It then returns $M$ to the adversary.
- Challenge The adversary $\mathcal{A}$ submits two (equal length) messages $M_0, M_1$ and an access structure $\mathbb{A}^*$, subject to the restriction that, for all $\mathcal{S} \in D$, $\mathbb{A}^*$ cannot be satisfied by $\mathcal{S}$. The challenger selects a random bit $\beta \in \{0, 1\}$, sets

$CT^* = \text{Encrypt}(\text{PK}, M_\beta, \mathbb{A}^*)$ and sends $CT^*$ to the adversary as its challenge ciphertext.
- Query phase 2 The adversary continues to adaptively issue *Private key* and *Decryption* queries, as in Query phase 1, but with the restrictions that the adversary cannot
  1) issue a *Private key* query that would result in a set of attributes $\mathcal{S}$ which satisfies the access structure $\mathbb{A}^*$ being added to $D$.
  2) issue a *Decryption* query on a set of attributes $\mathcal{S}$ and a ciphertext $CT$ such that $\mathcal{S}$ satisfies $\mathbb{A}^*$ and $CT = CT^*$.
- Guess The adversary $\mathcal{A}$ outputs its guess $\beta' \in \{0, 1\}$ for $\beta$ and wins the game if $\beta = \beta'$.

The advantage of the adversary in this game is defined as $|\text{Pr}[\beta = \beta'] - \frac{1}{2}|$ where the probability is taken over the random bits used by the challenger and the adversary.

*Definition 3:* A CP-ABE scheme is CCA-secure if all polynomial time adversaries have at most a negligible advantage in this security game.

*CPA Security:* We say that a CP-ABE scheme is *CPA-secure* (or secure against chosen-plaintext attacks) if the adversary cannot make decryption queries.

*Selective Security:* We say that a CP-ABE scheme is *selectively secure* if we add an **Init** stage before **Setup** where the adversary commits to the challenge access structure $\mathbb{A}^*$.

## III. NEW MODEL OF CP-ABE WITH OUTSOURCED DECRYPTION

In the original model defined in [12], a CP-ABE scheme with outsourced decryption consists of five algorithms: Setup, Encrypt, KeyGen$_{out}$, Transform and Decrypt$_{out}$. A trusted party uses the algorithm Setup to generate the public parameters and a master secret key, and uses KeyGen$_{out}$ to generate a private key and a transformation key for a user. Taking as input the transformation key given by a user and a ciphertext, the cloud can use the algorithm Transform to transform the ciphertext into a simple ciphertext if the user's attribute satisfies the access structure associated with the ciphertext; then the user uses the algorithm Decrypt$_{out}$ to recover the plaintext from the transformed ciphertext. Note that in the definition of Green *et al.* [12], the input to the algorithm Decrypt$_{out}$ includes only the private key of the user and the transformed ciphertext, but does not include the original ciphertext. Because of this omission of the original ciphertext, it is not possible to construct a CP-ABE scheme with verifiable outsourced decryption under the definition of [12]. This can be explained as follows. A malicious cloud could replace the ciphertext it supposes to transform with a ciphertext of a different message, and then transform the latter into a simple ciphertext using its transformation key. Obviously, the user cannot detect this malicious behavior of the cloud since the input to the algorithm Decrypt$_{out}$ does not include the original ciphertext required to be transformed. In order to achieve verifiability, we need to modify the model of CP-ABE with outsourced decryption defined in [12]. We now formally describe our new model.

A CP-ABE scheme with outsourced decryption consists of the following seven algorithms:

- Setup$(\lambda, U)$ takes as input a security parameter $\lambda$ and attribute universe description $U$. It outputs the public parameters PK and a master secret key MSK.
- KeyGen(PK, MSK, $\mathcal{S}$) takes as input the public parameters PK, the master secret key MSK and a set of attributes $\mathcal{S}$. It outputs a private key $\mathsf{SK}_{\mathcal{S}}$.
- Encrypt(PK, $M$, $\mathbb{A}$) takes as input the public parameters PK, a message $M$ and an access structure $\mathbb{A}$. It outputs a ciphertext $CT$.
- Decrypt(PK, $\mathsf{SK}_{\mathcal{S}}$, $CT$) takes as input the public parameters PK, a private key $\mathsf{SK}_{\mathcal{S}}$ for $\mathcal{S}$ and a ciphertext $CT$. It outputs a message $M$.
- GenTK$_{out}$(PK, $\mathsf{SK}_{\mathcal{S}}$) takes as input the public parameters PK and a private key $\mathsf{SK}_{\mathcal{S}}$ for $\mathcal{S}$. It outputs a transformation key $\mathsf{TK}_{\mathcal{S}}$ and the corresponding retrieving key $\mathsf{RK}_{\mathcal{S}}$.
- Transform$_{out}$(PK, $CT$, $\mathsf{TK}_{\mathcal{S}}$) takes as input the public parameters PK, a ciphertext $CT$ and a transformation key $\mathsf{TK}_{\mathcal{S}}$ for $\mathcal{S}$. It outputs a partially decrypted ciphertext $CT'$.
- Decrypt$_{out}$(PK, $CT$, $CT'$, $\mathsf{RK}_{\mathcal{S}}$) takes as input the public parameters PK, a ciphertext $CT$, a partially decrypted ciphertext $CT'$ and a retrieving key $\mathsf{RK}_{\mathcal{S}}$ for $\mathcal{S}$. It outputs a message $M$.

Let (PK, MSK) $\leftarrow$ Setup$(1^\lambda)$, $\mathsf{SK}_{\mathcal{S}} \leftarrow$ KeyGen(PK, MSK, $\mathcal{S}$), $CT \leftarrow$ Encrypt(PK, $M$, $\mathbb{A}$), $(\mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}}) \leftarrow$ GenTK$_{out}$(PK, $\mathsf{SK}_{\mathcal{S}}$) and $CT' \leftarrow$ Transform$_{out}$(PK, $CT$, $\mathsf{TK}_{\mathcal{S}}$). For correctness, we require the following to hold:

1) If the set $\mathcal{S}$ of attributes satisfies the access structure $\mathbb{A}$, then $M \leftarrow$ Decrypt(PK, $\mathsf{SK}_{\mathcal{S}}$, $CT$) and $M \leftarrow$ Decrypt$_{out}$(PK, $CT$, $CT'$, $\mathsf{RK}_{\mathcal{S}}$);
2) Otherwise, Decrypt(PK, $\mathsf{SK}_{\mathcal{S}}$, $CT$) and Decrypt$_{out}$(PK, $CT$, $CT'$, $\mathsf{RK}_{\mathcal{S}}$) output the error symbol $\perp$.

In our new model, the algorithms Setup, KeyGen, Encrypt and Decrypt constitute a traditional CP-ABE scheme. The input to the algorithm Decrypt$_{out}$ includes the original ciphertext and the transformed ciphertext. In fact, in our concrete scheme, a user only needs to know a small part of the original ciphertext to verify the correctness of the transformation done by the cloud in the algorithm Decrypt$_{out}$. In addition, in our model, using the algorithm GenTK$_{out}$ and his private key, the user generates the transformation key by himself, not by the trusted party as in [12]. Having either the trusted party or the user generate the transformation key does not have an effect on the security of the scheme. However, it is more flexible if we let the user himself generate the transformation key. Imagine that a user doesn't know whether he will outsource decryption of his stored files or not in the future. At the setup stage of our proposed ABE with verifiable outsourced decryption system, the user can just initialize an ordinary ABE system without outsourced decryption. Then, the user can generate the transformation key himself whenever he wants to outsource decryption, without having to resetup of the whole system. On the other hand, if the trusted party is responsible for the generation of transformation keys, the user is required to reinitialize the system for outsourced decryption.

Now, we formally describe the security and verifiability requirements of a CP-ABE scheme with outsourced decryption.

Informally, security ensures that an adversary (including a malicious cloud) not be able to learn anything about the encrypted message and verifiability allows a user to check on the correctness of the transformation done by the cloud.

**Security.** Since the traditional notion of security against adaptive chosen-ciphertext attacks (CCA) does not allow any bit of the ciphertext to be altered, similar to [12], we adopt a relaxation due to Canetti *et al.* [32] called replayable CCA (RCCA) security, which allows modifications to the ciphertext provided they cannot change the underlying message in a meaningful way. The RCCA security for CP-ABE with outsourced decryption is described as a game between a challenger and an adversary. The RCCA security game proceeds as follows:

- Setup The challenger runs Setup algorithm to obtain the public parameters PK and a master secret key MSK. It gives the public parameters PK to the adversary $\mathcal{A}$ and keeps MSK to itself.
- Query phase 1 The challenger initializes an empty table $T$ and an empty set $D$. The adversary $\mathcal{A}$ adaptively issues queries:
  1) *Private key* query, on input a set of attributes $\mathcal{S}$: The challenger runs $\mathsf{SK}_{\mathcal{S}} \leftarrow$ KeyGen(PK, MSK, $\mathcal{S}$) and sets $D = D \cup \{\mathcal{S}\}$. It then returns to the adversary the private key $\mathsf{SK}_{\mathcal{S}}$.
  2) *Transformation key* query, on input a set of attributes $\mathcal{S}$: The challenger searches the entry $(\mathcal{S}, \mathsf{SK}_{\mathcal{S}}, \mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}})$ in table $T$. If such entry exists, it returns the transformation key $\mathsf{TK}_{\mathcal{S}}$. Otherwise, it runs $\mathsf{SK}_{\mathcal{S}} \leftarrow$ KeyGen(PK, MSK, $\mathcal{S}$), $(\mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}}) \leftarrow$ GenTK$_{out}$(PK, $\mathsf{SK}_{\mathcal{S}}$) and stores in table $T$ the entry $(\mathcal{S}, \mathsf{SK}_{\mathcal{S}}, \mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}})$. It then returns to the adversary the transformation key $\mathsf{TK}_{\mathcal{S}}$.
  Without of loss of generality, we assume that an adversary do not issue *Transformation key* query on a set of attributes $\mathcal{S}$, if it has already issued a *Private key* query on the same set of attributes $\mathcal{S}$. Since anyone can by himself generate a transformation key for a user using the algorithm GenTK$_{out}$ and the user's private key, our assumption is reasonable.
  3) *Decryption* query, on input a set of attributes $\mathcal{S}$ and a ciphertext $CT$: The challenger runs $\mathsf{SK}_{\mathcal{S}} \leftarrow$ KeyGen(PK, MSK, $\mathcal{S}$) and $M \leftarrow$ Decrypt(PK, $\mathsf{SK}_{\mathcal{S}}$, $CT$). It then returns $M$ to the adversary.
  4) *Decryption$_{out}$* query, on input a set of attributes $\mathcal{S}$ and a pair of ciphertexts $(CT, CT')$: The challenger searches the entry $(\mathcal{S}, \mathsf{SK}_{\mathcal{S}}, \mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}})$ in table $T$. If such entry exists, it runs $M \leftarrow$ Decrypt$_{out}$(PK, $CT$, $CT'$, $\mathsf{RK}_{\mathcal{S}}$) and returns to the adversary $M$; otherwise, it returns $\perp$.
- Challenge The adversary $\mathcal{A}$ submits two (equal length) messages $M_0, M_1$ and an access structure $\mathbb{A}$, subject to the restriction that, for all $\mathcal{S} \in D$, $\mathbb{A}$ cannot be satisfied by $\mathcal{S}$. The challenger selects a random bit $\beta \in \{0, 1\}$, sets $CT^* =$ Encrypt(PK, $M_\beta$, $\mathbb{A}$) and sends $CT^*$ to the adversary as its challenge ciphertext.
- Query phase 2 The adversary continues to adaptively issue *Private key, Transformation key, Decryption* and

$Decryption_{out}$ queries, as in Query phase 1, but with the restrictions that the adversary cannot

1) issue a *Private key* query that would result in a set of attributes $\mathcal{S}$ which satisfies the access structure $\mathbb{A}$ being added to $D$.

2) issue a trivial decryption query. That is, *Decryption* and $Decryption_{out}$ queries will be answered as in Query phase 1, except that if the response would be either $M_0$ or $M_1$, then the challenger responds with the error symbol $\perp$.

- Guess The adversary $\mathcal{A}$ outputs its guess $\beta' \in \{0, 1\}$ for $\beta$ and wins the game if $\beta = \beta'$.

The advantage of the adversary in this game is defined as $|\Pr[\beta = \beta'] - \frac{1}{2}|$ where the probability is taken over the random bits used by the challenger and the adversary.

*Definition 4:* A CP-ABE scheme with outsourced decryption is RCCA-secure if all polynomial time adversaries have at most a negligible advantage in this security game.

*CPA Security:* We say that a CP-ABE scheme with outsourced decryption is *CPA-secure* (or secure against chosen-plaintext attacks) if the adversary cannot make decryption queries.

*Selective Security:* We say that a CP-ABE scheme with outsourced decryption is *selectively secure* if we add an **Init** stage before **Setup** where the adversary commits to the challenge access structure $\mathbb{A}^*$.

**Verifiability.** Verifiability of CP-ABE with outsourced decryption is also described by a game between a challenger and an adversary. The game proceeds as follows:

- Setup The challenger runs Setup algorithm to obtain the public parameters PK and a master secret key MSK. It gives the public parameters PK to the adversary $\mathcal{A}$ and keeps MSK to itself.

- Query phase 1 The challenger initializes an empty table $T$. The adversary $\mathcal{A}$ adaptively issues queries:

1) *Private key* query, on input a set of attributes $\mathcal{S}$: The challenger runs $\mathsf{SK}_{\mathcal{S}} \leftarrow \mathsf{KeyGen}(\mathsf{PK}, \mathsf{MSK}, \mathcal{S})$ and returns to the adversary the private key $\mathsf{SK}_{\mathcal{S}}$.

2) *Transformation key* query, on input a set of attributes $\mathcal{S}$: The challenger runs $\mathsf{SK}_{\mathcal{S}} \leftarrow \mathsf{KeyGen}(\mathsf{PK}, \mathsf{MSK}, \mathcal{S})$, $(\mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}}) \leftarrow \mathsf{GenTK}_{out}(\mathsf{PK}, \mathsf{SK}_{\mathcal{S}})$ and stores in table $T$ the entry $(\mathcal{S}, \mathsf{SK}_{\mathcal{S}}, \mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}})$. It then returns to the adversary the transformation key $\mathsf{TK}_{\mathcal{S}}$.
   Without of loss of generality, we assume that an adversary does not issue *Transformation key* query on a set of attributes $\mathcal{S}$, if it has already issued a *Private key* query on the same set of attributes $\mathcal{S}$. Since anyone can by himself generate a transformation key for a user using the algorithm $\mathsf{GenTK}_{out}$ and the user's private key, our assumption is reasonable.

3) *Decryption* query, on input a set of attributes $\mathcal{S}$ and a ciphertext $CT$: The challenger runs $\mathsf{SK}_{\mathcal{S}} \leftarrow \mathsf{KeyGen}(\mathsf{PK}, \mathsf{MSK}, \mathcal{S})$ and $M \leftarrow \mathsf{Decrypt}(\mathsf{PK}, \mathsf{SK}_{\mathcal{S}}, CT)$. It then returns to the adversary $M$.

4) $Decryption_{out}$ query, on input a set of attributes $\mathcal{S}$ and a pair of ciphertexts $(CT, CT')$: The challenger

searches the entry $(\mathcal{S}, \mathsf{SK}_{\mathcal{S}}, \mathsf{TK}_{\mathcal{S}}, \mathsf{RK}_{\mathcal{S}})$ in table $T$. If such entry exists, it runs $M \leftarrow \mathsf{Decrypt}_{out}(\mathsf{PK}, CT, CT', \mathsf{RK}_{\mathcal{S}})$ and returns $M$ to the adversary; otherwise, it returns $\perp$.

- Challenge The adversary $\mathcal{A}$ submits a message $M^*$ and an access structure $\mathbb{A}$. The challenger sets $CT^* = \mathsf{Encrypt}(\mathsf{PK}, M^*, \mathbb{A})$ and sends $CT^*$ to the adversary.

- Query phase 2 The adversary continues to adaptively issue *Private key, Transformation key, Decryption* and $Decryption_{out}$ queries, as in Query phase 1.

- Output The adversary $\mathcal{A}$ outputs a set of attributes $\mathcal{S}^*$ and a transformed ciphertext $CT^{*\prime}$. We assume that entry $(\mathcal{S}^*, \mathsf{SK}_{\mathcal{S}^*}, \mathsf{TK}_{\mathcal{S}^*}, \mathsf{RK}_{\mathcal{S}^*})$ exists in table $T$ (If not, the challenger can generate the entry as in the response of *Transformation key* query). The adversary wins the game if $\mathsf{Decrypt}_{out}(\mathsf{PK}, CT^*, CT^{*\prime}, \mathsf{RK}_{\mathcal{S}^*}) \notin \{M^*, \perp\}$.

The advantage of the adversary in this game is defined as $\Pr[\mathcal{A} \; wins]$ where the probability is taken over the random bits used by the challenger and the adversary.

*Definition 5:* A CP-ABE scheme with outsourced decryption is verifiable if all polynomial time adversaries have at most a negligible advantage in the above game.

One stronger notion of verifiability is that, even if the trusted party who setups the system is malicious, a user still can check on the correctness of the transformation done by the cloud. That is, the adversary generates the system's public parameters and master secret key by himself in the above game. Nevertheless, it is difficult to construct a CP-ABE scheme with outsourced decryption which is verifiable in such stronger model, since most existing techniques of provable security need to generate the system's public parameters *elaborately* by the challenger. This challenging problem will be left as one of our future research topics.

## IV. PROPOSED CP-ABE SCHEME WITH VERIFIABLE OUTSOURCED DECRYPTION

In this section, we first propose a new CP-ABE scheme utilizing Waters' CP-ABE scheme [4], which is proven to be selectively CPA-secure. Then, based on the scheme, we propose a CP-ABE scheme with outsourced decryption and prove that it is selectively CPA-secure and verifiable in the standard model. Recently, the first CP-ABE scheme that achieved full security was proposed by Lewko *et al.* [5]. Since the underlying structure of the CP-ABE scheme presented by Lewko *et al.* [5] is almost identical to the underlying Waters' CP-ABE scheme [4] we use, one can adapt our construction techniques to the CP-ABE scheme proposed in [5] to achieve fully secure (i.e., RCCA secure) CP-ABE scheme with verifiable outsourced decryption in the standard model.

### A. New CP-ABE Scheme

Before presenting our new CP-ABE scheme, we give some intuitions of our construction. Based on Waters' CP-ABE scheme [4], we add to the ciphertext the encryption of an extra random message and a checksum value, which is computed with this random message and the actual plaintext. We regard this checksum value as a commitment of the actual plaintext, which can be used to check if the transformation is done

correctly in our CP-ABE Scheme with verifiable outsourced decryption. In fact, using our techniques, we can modify unbounded ABE schemes [7], [33] to unbounded ABE scheme with verifiable outsourced decryption.

Our new CP-ABE scheme consists of the following algorithms:

- Setup($\lambda, U$) The setup algorithm takes as input a security parameter $\lambda$ and a small universe description $U = \{1, 2, \ldots, \ell\}$. It first runs $\mathcal{G}(\lambda)$ to obtain $(p, \mathbb{G}, \mathbb{G}_T, e)$, where $\mathbb{G}$ and $\mathbb{G}_T$ are cyclic groups of prime order $p$. It then chooses $g, u, v, d \in \mathbb{G}$, and $\alpha, a \in \mathbb{Z}_p^*$ uniformly at random. For each attribute $i \in U$, it chooses a random value $s_i \in \mathbb{Z}_p^*$. Finally, it chooses a collision-resistant hash function $H : \mathbb{G} \to \mathbb{Z}_p^*$. The public parameters are published as $\mathsf{PK} = (\mathbb{G}, \mathbb{G}_T, e, g, u, v, d, g^a, e(g, g)^\alpha, T_i = g^{s_i} \forall i, H)$. The master secret key is $\mathsf{MSK} = \alpha$.

- KeyGen($\mathsf{PK}, \mathsf{MSK}, \mathcal{S}$) The key generation algorithm randomly picks $t \in \mathbb{Z}_p^*$. The secret key $\mathsf{SK}_\mathcal{S} = (\mathcal{S}, K, K_0, K_i)$ is computed as $K = g^\alpha g^{at}$, $K_0 = g^t$, $K_i = T_i^t \ \forall i \in \mathcal{S}$.

- Encrypt($\mathsf{PK}, M, \mathbb{A}$) The encryption algorithm takes as input the public parameters $\mathsf{PK}$, a message $M \in \mathbb{G}_T$ to encrypt and an LSSS access structure $\mathbb{A} = (\mathbf{A}, \rho)$, where $\mathbf{A}$ is an $\ell \times n$ matrix and $\rho$ is a map from each row $A_i$ of $\mathbf{A}$ to an attribute $\rho(i)$. It chooses two random vectors $\vec{v}, \vec{v}' \in \mathbb{Z}_p^{*n}$, denoted $\vec{v} = (s, v_2, \ldots, v_n)$ and $\vec{v}' = (s', v_2', \ldots, v_n')$. For each row $A_i$ of $\mathbf{A}$, it chooses $r_{1,i}, r_{2,i} \in \mathbb{Z}_p^*$ uniformly at random. Finally, it chooses a random message $\tilde{M} \in \mathbb{G}_T$. The ciphertext is $CT = ((\mathbf{A}, \rho), \hat{C}, C_1, C_1', C_{1,i}, D_{1,i}, C_2, C_2', C_{2,i}, D_{2,i})$, where

$$\hat{C} = u^{H(M)} v^{H(\tilde{M})} d,$$

$$C_1 = M \cdot e(g, g)^{\alpha s}, \ C_1' = g^s,$$

$$C_{1,i} = g^{a A_i \cdot v} T_{\rho(i)}^{-r_{1,i}}, \ D_{1,i} = g^{r_{1,i}} \ \forall i \in \{1, 2, \ldots, \ell\},$$

$$C_2 = \tilde{M} \cdot e(g, g)^{\alpha s'}, \ C_2' = g^{s'},$$

$$C_{2,i} = g^{a A_i \cdot v'} T_{\rho(i)}^{-r_{2,i}}, \ D_{2,i} = g^{r_{2,i}} \ \forall i \in \{1, 2, \ldots, \ell\}.$$

- Decrypt($\mathsf{PK}, \mathsf{SK}_\mathcal{S}, CT$) The decryption algorithm takes as input the public parameters $\mathsf{PK}$, a private key $\mathsf{SK}_\mathcal{S} = (\mathcal{S}, K, K_0, K_i)$ for a set of attributes $\mathcal{S}$ and a ciphertext $CT = ((\mathbf{A}, \rho), \hat{C}, C_1, C_1', C_{1,i}, D_{1,i}, C_2, C_2', C_{2,i}, D_{2,i})$ for an access structure $\mathbb{A} = (\mathbf{A}, \rho)$. If $\mathcal{S}$ does not satisfy the access structure $\mathbb{A}$, it outputs $\perp$. Suppose that $\mathcal{S}$ satisfies the access structure and let $I \subset \{1, 2, \ldots, \ell\}$ be defined as $I = \{i : \rho(i) \in \mathcal{S}\}$. It computes constant $\omega_i \in \mathbb{Z}_p^*$ such that $\sum_{i \in I} \omega_i A_i = (1, 0, \ldots, 0)$. The decryption algorithm then computes:

$$C_1 \cdot \frac{\left( \prod_{i \in I} (e(C_{1,i}, K_0) \cdot e(K_{\rho(i)}, D_{1,i}))^{\omega_i} \right)}{e(C_1', K)}$$

$$= M \cdot e(g, g)^{\alpha s} \cdot \frac{\left( \prod_{i \in I} e(g, g)^{at A_i \cdot v \cdot \omega_i} \right)}{(e(g, g)^{\alpha s} e(g, g)^{ats})} = M,$$

$$C_2 \cdot \frac{\left( \prod_{i \in I} (e(C_{2,i}, K_0) \cdot e(K_{\rho(i)}, D_{2,i}))^{\omega_i} \right)}{e(C_2', K)}$$

$$= \tilde{M} \cdot e(g, g)^{\alpha s'} \cdot \frac{\left( \prod_{i \in I} e(g, g)^{at A_i \cdot v' \cdot \omega_i} \right)}{(e(g, g)^{\alpha s'} e(g, g)^{ats'})} = \tilde{M}.$$

If $\hat{C} = u^{H(M)} v^{H(\tilde{M})} d$, it outputs the message $M$; otherwise, it outputs $\perp$.

Obviously, the above CP-ABE scheme satisfies correctness. Observe that, in our construction, a ciphertext includes three parts: $(C_1, C_1', C_{1,i}, D_{1,i})$, $(C_2, C_2', C_{2,i}, D_{2,i})$ and $\hat{C}$. The first and second parts are encryptions of message $M$ and a random message $\tilde{M}$, respectively, using the encryption algorithm of Waters' CP-ABE scheme [4]. In fact, the second and third parts are redundant. However, the redundant parts are the point that we can construct a CP-ABE with verifiable outsourced decryption from the above CP-ABE scheme.

*Theorem 1:* Suppose that the construction of Waters [4] is a selectively CPA-secure CP-ABE scheme, then the above construction of CP-ABE scheme is also selectively CPA-secure.

*Proof:* To prove the selective CPA security of our CP-ABE scheme, we consider the following two games.

- Game$_0$ The original selectively CPA-secure game of CP-ABE.
- Game$_1$ Same as Game$_0$ except for the way that the challenger generates the challenge ciphertext $CT^* = ((\mathbf{A}, \rho), \hat{C}, C_1, C_1', C_{1,i}, D_{1,i}, C_2, C_2', C_{2,i}, D_{2,i})$, where the challenger picks $\hat{C} \in \mathbb{G}$ randomly and the rest parts of the challenge ciphertext are generated properly as in Game$_0$.

We prove this theorem by the following two lemmas. Lemma 1 states that Game$_0$ and Game$_1$ are indistinguishable; and Lemma 2 states that the advantage of the adversary in Game$_1$ is negligible. Therefore, we conclude that the advantage of the adversary in Game$_0$ (i.e., the original selectively CPA-secure game) is negligible. This completes the proof of Theorem 1. ∎

*Lemma 1:* Suppose that the construction of Waters [4] is a selectively CPA-secure CP-ABE scheme, Game$_0$ and Game$_1$ are computationally indistinguishable.

*Proof:* Suppose there exists an adversary $\mathcal{A}$ that can distinguish Game$_0$ and Game$_1$ with nonnegligible advantage. We build an algorithm $\mathcal{B}$ that can attack the Waters' CP-ABE scheme [4] in the selectively CPA-secure model with nonnegligible advantage.

Let $\mathcal{C}$ be the challenger corresponding to $\mathcal{B}$ in the selectively CPA-secure game of Waters' CP-ABE scheme. $\mathcal{B}$ runs $\mathcal{A}$ executing the following steps.

- Init The adversary $\mathcal{A}$ gives $\mathcal{B}$ its challenge access structure $\mathbb{A}^*$. $\mathcal{B}$ sends $\mathbb{A}^*$ to $\mathcal{C}$ as its challenge access structure and is given the public parameters $\mathsf{PK}' = (p, \mathbb{G}, \mathbb{G}_T, e, g, g^a, e(g, g)^\alpha, T_i = g^{s_i} \forall i)$ of the Waters' CP-ABE scheme.

- Setup $\mathcal{B}$ chooses random exponents $x, y, z \in \mathbb{Z}_p^*$ and sets $u = g^x$, $v = g^y$, and $d = g^z$. $\mathcal{B}$ also chooses a collision-resistant hash function $H : \mathbb{G} \to \mathbb{Z}_p^*$. Then, $\mathcal{B}$ sends the public parameters $\mathsf{PK} = (p, \mathbb{G}, \mathbb{G}_T, e, g, u, v, d, g^a, e(g, g)^\alpha, T_i = g^{s_i} \forall i, H)$ to the adversary $\mathcal{A}$.

- Query phase 1 When the adversary $\mathcal{A}$ adaptively issues a private key query for a set of attributes $\mathcal{S}_i$, $\mathcal{B}$ calls the key generation oracle of $\mathcal{C}$ on $\mathcal{S}_i$ to obtain the private key $\mathsf{SK}_{\mathcal{S}_i}$. Then, $\mathcal{B}$ returns to $\mathcal{A}$ the private key $\mathsf{SK}_{\mathcal{S}_i}$.

- Challenge The adversary $\mathcal{A}$ submits two (equal length) messages $M_0, M_1$. $\mathcal{B}$ chooses a random bit $\beta \in \{0, 1\}$ and two random messages $\tilde{M}_0, \tilde{M}_1 \in \mathbb{G}_T$. Then, $\mathcal{B}$ sends $\tilde{M}_0, \tilde{M}_1$ and $\mathbb{A}^*$ to $\mathcal{C}$. $\mathcal{C}$ selects a random bit $\gamma \in \{0, 1\}$, encrypts the message $\tilde{M}_\gamma$ under $\mathsf{PK}'$ and $\mathbb{A}^*$ using the

encryption algorithm of Waters' CP-ABE scheme, and sends the resulting ciphertext $CT^{*\prime}$ to $\mathcal{B}$. $\mathcal{B}$ parses $CT^{*\prime}$ as $(\mathbb{A}^* = (\mathbf{A}, \rho), \ C_2, C_2', C_{2,i}, D_{2,i})$. Then, $\mathcal{B}$ chooses a random vector $\vec{v} \in \mathbb{Z}_p^{*n}$, denoted $\vec{v} = (s, v_2, \ldots, v_n)$. For each row $A_i$ of $\mathbf{A}$, $\mathcal{B}$ chooses $r_{1,i} \in \mathbb{Z}_p^*$ uniformly at random. Finally, $\mathcal{B}$ sets

$$\hat{C} = u^{H(M_\beta)} v^{H(\tilde{M}_\beta)} d, \ C_1 = M_\beta \cdot e(g,g)^{\alpha s}, \ C_1' = g^s,$$

$$C_{1,i} = g^{a A_i \cdot v} T_{\rho(i)}^{-r_{1,i}}, \ D_{1,i} = g^{r_{1,i}} \ \forall i \in \{1, 2, \ldots, \ell\},$$

and sends $CT^* = ((\mathbf{A}, \rho), \ \hat{C}, \ C_1, C_1', C_{1,i}, D_{1,i}, C_2, C_2', C_{2,i}, D_{2,i})$ to $\mathcal{A}$ as its challenge ciphertext.

- Query phase 2 $\mathcal{A}$ continues to adaptively issue private key queries as in Query phase 1, and $\mathcal{B}$ responds the queries as in Query phase 1.
- Guess $\mathcal{A}$ outputs its guess $\beta' \in \{0, 1\}$ for $\beta$. $\mathcal{B}$ also outputs $\beta'$ as its guess for $\gamma$.

Observe that, if $\beta = \gamma$, then $\mathcal{B}$ has properly simulated $\mathsf{Game}_0$; otherwise, $\mathcal{B}$ properly simulated $\mathsf{Game}_1$. Thus, if $\mathcal{A}$ can distinguish $\mathsf{Game}_0$ and $\mathsf{Game}_1$ with nonnegligible advantage, we can build an algorithm $\mathcal{B}$ that attacks the selectively CPA-secure Waters' CP-ABE scheme [4] with nonnegligible advantage. ∎

*Lemma 2:* Suppose that the construction of Waters [4] is a selectively CPA-secure CP-ABE scheme, the advantage of the adversary in $\mathsf{Game}_1$ is negligible.

*Proof:* Suppose there exists an adversary $\mathcal{A}$ that has a non-negligible advantage in $\mathsf{Game}_1$. We build an algorithm $\mathcal{B}$ that can attack the Waters' CP-ABE scheme [4] in the selectively CPA-secure model with a nonnegligible advantage.

Let $\mathcal{C}$ be the challenger corresponding to $\mathcal{B}$ in the selectively CPA-secure game of Waters' CP-ABE scheme. $\mathcal{B}$ runs $\mathcal{A}$ executing the following steps.

- Init The adversary $\mathcal{A}$ gives $\mathcal{B}$ its challenge access structure $\mathbb{A}^*$. $\mathcal{B}$ sends $\mathbb{A}^*$ to $\mathcal{C}$ as its challenge access structure and is given the public parameters $\mathsf{PK}' = (p, \mathbb{G}, \mathbb{G}_T, e, g, g^a, e(g,g)^\alpha, T_i = g^{s_i} \forall i)$ of the Waters' CP-ABE scheme.
- Setup $\mathcal{B}$ chooses random exponents $x, y, z \in \mathbb{Z}_p^*$ and sets $u = g^x$, $v = g^y$, and $d = g^z$. $\mathcal{B}$ also chooses a collision-resistant hash function $H : \mathbb{G} \to \mathbb{Z}_p^*$. Then, $\mathcal{B}$ sends the public parameters $\mathsf{PK} = (p, \mathbb{G}, \mathbb{G}_T, e, \ g, u, v, d, g^a, e(g,g)^\alpha, T_i = g^{s_i} \forall i, \ H)$ to the adversary $\mathcal{A}$.
- Query phase 1 When the adversary $\mathcal{A}$ adaptively issues a private key query for a set of attributes $\mathcal{S}_i$, $\mathcal{B}$ calls the key generation oracle of $\mathcal{C}$ on $\mathcal{S}_i$ to obtain the private key $\mathsf{SK}_{\mathcal{S}_i}$. Then, $\mathcal{B}$ returns to $\mathcal{A}$ the private key $\mathsf{SK}_{\mathcal{S}_i}$.
- Challenge The adversary $\mathcal{A}$ submits two (equal length) messages $M_0, M_1$. $\mathcal{B}$ sends $M_0, M_1$ and $\mathbb{A}^*$ to $\mathcal{C}$. $\mathcal{C}$ selects a random bit $\gamma \in \{0, 1\}$, encrypts the message $M_\gamma$ under $\mathsf{PK}'$ and $\mathbb{A}^*$ using the encryption algorithm of Waters' CP-ABE scheme, and sends the resulting ciphertext $CT^{*\prime}$ to $\mathcal{B}$. $\mathcal{B}$ parses $CT^{*\prime}$ as $(\mathbb{A}^* = (\mathbf{A}, \rho), \ C_1, C_1', C_{1,i}, D_{1,i})$. Then, $\mathcal{B}$ chooses a random message $\tilde{M} \in \mathbb{G}_T$ and a random vector $\vec{v}' \in \mathbb{Z}_p^{*n}$, denoted $\vec{v}' = (s', v_2', \ldots, v_n')$. For each row $A_i$ of $\mathbf{A}$, $\mathcal{B}$ chooses $r_{2,i} \in \mathbb{Z}_p^*$ uniformly at random. Finally, $\mathcal{B}$ chooses a random element $\hat{C}$ in $\mathbb{G}_{p_1}$ and sets

$$C_2 = \tilde{M} \cdot e(g,g)^{\alpha s'}, \ C_2' = g^{s'},$$

$$C_{2,i} = g^{a A_i \cdot v'} T_{\rho(i)}^{-r_{2,i}}, \ D_{2,i} = g^{r_{2,i}} \ \forall i \in \{1, 2, \ldots, \ell\},$$

and sends $CT^* = ((\mathbf{A}, \rho), \ \hat{C}, \ C_1, C_1', C_{1,i}, D_{1,i}, C_2, C_2', C_{2,i}, D_{2,i})$ to $\mathcal{A}$ as its challenge ciphertext.

- Query phase 2 $\mathcal{A}$ continues to adaptively issue private key queries as in Query phase 1, and $\mathcal{B}$ responds the queries as in Query phase 1.
- Guess $\mathcal{A}$ outputs a bit $\beta'$. $\mathcal{B}$ also takes $\beta'$ as its output.

Obviously, $\mathcal{B}$ has properly simulated in $\mathsf{Game}_1$. Thus, if $\mathcal{A}$ has a nonnegligible advantage in $\mathsf{Game}_1$, then $\mathcal{B}$ attacks the selectively CPA-secure Waters' CP-ABE scheme [4] with a nonnegligible advantage. ∎

### B. Our CP-ABE Scheme With Verifiable Outsourced Decryption

For notational purposes in the below, we denote the above CP-ABE scheme as $\mathsf{BasicCP-ABE}$. Based on $\mathsf{BasicCP-ABE}$, we present a CP-ABE scheme with verifiable outsourced decryption. The Setup, KeyGen, Encrypt and Decrypt algorithms operate exactly as in $\mathsf{BasicCP-ABE}$. We now describe the remaining algorithms:

- $\mathsf{GenTK}_{out}(\mathsf{PK}, \mathsf{SK}_\mathcal{S})$ This algorithm takes as input the public parameters $\mathsf{PK}$ and a private key $\mathsf{SK}_\mathcal{S} = (\mathcal{S}, \ K, \ K_0, K_i)$ for a set of attributes $\mathcal{S}$. It chooses a random value $z \in \mathbb{Z}_p^*$. Then, it sets the transformation key as $\mathsf{TK}_\mathcal{S} = (\mathcal{S}, \ K' = K^{1/z}, K_0' = K_0^{1/z}, K_i' = K_i^{1/z})$ and the retrieving key as $\mathsf{RK}_\mathcal{S} = z$. Note that, with overwhelming probability, $z$ has multiplicative inverse.
- $\mathsf{Transform}_{out}(\mathsf{PK}, CT, \mathsf{TK}_\mathcal{S})$ This algorithm takes as input the public parameters $\mathsf{PK}$, a ciphertext $CT = (\mathbb{A} = (\mathbf{A}, \rho), \ \hat{C}, \ C_1, C_1', C_{1,i}, D_{1,i}, \ C_2, C_2', C_{2,i}, D_{2,i})$ for an access structure $\mathbb{A} = (\mathbf{A}, \rho)$, and a transformation key $\mathsf{TK}_\mathcal{S} = (\mathcal{S}, \ K', \ K_0', K_i')$ for a set of attributes $\mathcal{S}$. It then computes:

$$T_1' = \frac{e(C_1', K')}{\left( \prod_{i \in I} \left( e(C_{1,i}, K_0') \cdot e\left(K_{\rho(i)}', D_{1,i}\right) \right)^{\omega_i} \right)}$$

$$= \frac{e(g,g)^{\alpha s/z} e(g,g)^{ats/z}}{\left( \prod_{i \in I} e(g,g)^{at A_i \cdot v \cdot \omega_i / z} \right)} = e(g,g)^{\alpha s/z},$$

and

$$T_2' = \frac{e(C_2', K')}{\left( \prod_{i \in I} \left( e(C_{2,i}, K_0') \cdot e\left(K_{\rho(i)}', D_{2,i}\right) \right)^{\omega_i} \right)}$$

$$= \frac{e(g,g)^{\alpha s'/z} e(g,g)^{ats'/z}}{\left( \prod_{i \in I} e(g,g)^{at A_i \cdot v' \cdot \omega_i / z} \right)}$$

$$= e(g,g)^{\alpha s'/z},$$

and outputs the transformed ciphertext as $CT' = (\hat{T} = \hat{C}, T_1 = C_1, T_1', T_2 = C_2, T_2')$.

- $\mathsf{Decrypt}_{out}(\mathsf{PK}, CT, CT', \mathsf{RK}_\mathcal{S})$ This algorithm takes as input the public parameters $\mathsf{PK}$, a ciphertext $CT = (\mathbb{A} = (\mathbf{A}, \rho), \ \hat{C}, \ C_1, C_1', C_{1,i}, D_{1,i}, \ C_2, C_2', C_{2,i}, D_{2,i})$, a transformed ciphertext $CT' = (\hat{T}, T_1, T_1', T_2, T_2')$ and a retrieving key $\mathsf{RK}_\mathcal{S} = z$ for a set of attributes $\mathcal{S}$. If $\hat{T} \neq \hat{C}$ or $T_1 \neq C_1$ or $T_2 \neq C_2$, it outputs $\perp$. Then, it computes $M = T_1/T_1'^z$ and $\tilde{M} = T_2/T_2'^z$. If $\hat{T} = u^{H(M)} v^{H(\tilde{M})} d$, it outputs the message $M$; otherwise, it outputs $\perp$.

Obviously, the above CP-ABE scheme with outsourced decryption satisfies correctness. In the above construction, a user runs

the algorithm $\text{Decrypt}_{out}$ to recover the plaintext from the transformed ciphertext and computation cost incurred by the user is about three exponentiations, which is far less than the cost of running the algorithm Decrypt to recover the plaintext from the original ciphertext directly. The input of algorithm $\text{Decrypt}_{out}$ includes the original ciphertext $CT = (\mathbb{A}' = (\mathbf{A}, \rho), \; vk, \; \tilde{C} = (\hat{C}, \; C_1, C_1', C_{1,i}, D_{1,i}, \; C_2, C_2', C_{2,i}, \; D_{2,i}), \; \sigma)$ and the transformed ciphertext. In fact, the user only needs to know $\hat{C}$ to verify the correctness of the transformation done by the cloud.

*Theorem 2:* Assume that $\mathsf{BasicCP\!-\!ABE}$ is selectively CPA-secure. Then the above construction of CP-ABE scheme with outsourced decryption is selectively CPA-secure.

*Proof:* Suppose there exists an adversary $\mathcal{A}$ that can attack the above CP-ABE scheme with outsourced decryption in the selectively CPA-secure model with nonnegligible advantage. We build an algorithm $\mathcal{B}$ that can attack the CP-ABE scheme $\mathsf{BasicCP\!-\!ABE}$ in the selectively CPA-secure model with nonnegligible advantage.

Let $\mathcal{C}$ be the challenger corresponding to $\mathcal{B}$ in the selectively CPA-secure game of the CP-ABE scheme $\mathsf{BasicCP\!-\!ABE}$. $\mathcal{B}$ runs $\mathcal{A}$ to execute the following steps.

- Init The adversary $\mathcal{A}$ gives $\mathcal{B}$ its challenge access structure $\mathbb{A}^*$. $\mathcal{B}$ sends $\mathbb{A}^*$ to $\mathcal{C}$ as its challenge access structure and is given the public parameters $\mathsf{PK} = (N, \mathbb{G}, \mathbb{G}_T, e, g, u, v, d, g^a, e(g,g)^\alpha, T_i = g^{s_i} \forall i, \; H)$ of $\mathsf{BasicCP\!-\!ABE}$.
- Setup $\mathcal{B}$ sends the public parameters $\mathsf{PK}$ to the adversary $\mathcal{A}$.
- Query phase 1 $\mathcal{B}$ initializes an empty table $T$ and an empty set $D$. The adversary $\mathcal{A}$ adaptively issues queries:
  1) *Private key* query for a set of attributes $\mathcal{S}$: $\mathcal{B}$ calls the key generation oracle of $\mathcal{C}$ on $\mathcal{S}$ to obtain the private key $\mathsf{SK}_\mathcal{S}$. Then, $\mathcal{B}$ sets $D = D \cup \{\mathcal{S}\}$ and returns to $\mathcal{A}$ the private key $\mathsf{SK}_\mathcal{S}$.
  2) *Transformation key* query for a set of attributes $\mathcal{S}$: $\mathcal{B}$ searches the entry $(\mathcal{S}, \mathsf{SK}_\mathcal{S}, \mathsf{TK}_\mathcal{S}, \mathsf{RK}_\mathcal{S})$ in table $T$. If such entry exists, it returns the transformation key $\mathsf{TK}_\mathcal{S}$. Otherwise, $\mathcal{B}$ chooses random exponents $z, t \in \mathbb{Z}_p^*$. Then, $\mathcal{B}$ sets

$$K' = g^z g^{at}, \; K_0' = g^t, \; K_i' = T_i^t \; \forall i \in \mathcal{S}.$$

  Finally, $\mathcal{B}$ stores in table $T$ the entry $(\mathcal{S}, *, \mathsf{TK}_\mathcal{S} = (\mathcal{S}, \; K', K_0', K_i'), z)$ and returns to $\mathcal{A}$ the transformation key $\mathsf{TK}_\mathcal{S}$. Note that, $\mathcal{B}$ does not know the actual retrieving key $\mathsf{RK}_\mathcal{S} = \alpha/z$.
- Challenge The adversary $\mathcal{A}$ submits two (equal length) messages $M_0, M_1$ and an access structure $\mathbb{A}$. $\mathcal{B}$ sends $M_0, M_1$ and $\mathbb{A}$ to $\mathcal{C}$ to obtain the challenge ciphertext $CT^*$. Then, $\mathcal{B}$ sends $CT^*$ to the adversary $\mathcal{A}$ as its challenge ciphertext.
- Query phase 2 $\mathcal{A}$ continues to adaptively issue private key queries as in Query phase 1, and $\mathcal{B}$ responds the queries as in Query phase 1.
- Guess The adversary $\mathcal{A}$ outputs a bit $\beta'$. $\mathcal{B}$ also outputs $\beta'$.

So, we build an algorithm $\mathcal{B}$ that can attack $\mathsf{BasicCP\!-\!ABE}$ in the selectively CPA-secure model with nonnegligible advantage, if $\mathcal{A}$ can attack the above CP-ABE scheme with outsourced decryption in the selectively CPA-secure model with nonnegligible advantage. ∎

*Theorem 3:* Suppose that the DL assumption holds in the prime order bilinear group system. Then the above construction of CP-ABE scheme with outsourced decryption is verifiable.

*Proof:* Suppose there exists an adversary $\mathcal{A}$ that can attack the verifiability of the above CP-ABE scheme with outsourced decryption with nonnegligible advantage. We build an algorithm $\mathcal{B}$ that can solve the DL problem in the prime order bilinear group system with nonnegligible advantage.

$\mathcal{B}$ is given $(p, \mathbb{G}, \mathbb{G}_T, e, \; g, g^x)$ and runs $\mathcal{A}$ executing the following steps.

- Setup $\mathcal{B}$ chooses $\alpha, a, y, z \in \mathbb{Z}_p^*$ uniformly at random. For each attribute $i \in U$, $\mathcal{B}$ chooses a random value $s_i \in \mathbb{Z}_p^*$. $\mathcal{B}$ also chooses a collision-resistant hash function $H : \mathbb{G} \to \mathbb{Z}_p^*$. Then, $\mathcal{B}$ sets the public parameters as $\mathsf{PK} = (p, \mathbb{G}, \mathbb{G}_T, e, g, u = g^x, v = g^y, d = g^z, g^a, e(g,g)^\alpha, T_i = g^{s_i} \forall i, \; H)$. The master secret key is $\mathsf{MSK} = \alpha$. Finally, $\mathcal{B}$ sends the public parameters $\mathsf{PK}$ to the adversary $\mathcal{A}$.
- Query phase 1 The adversary $\mathcal{A}$ adaptively issues *Private key*, *Transformation Key*, *Decryption* and $Decryption_{out}$ queries. Since $\mathcal{B}$ knows the master secret key $\mathsf{MSK}$, it can answers the adversary's queries properly.
- Challenge The adversary $\mathcal{A}$ submits a messages $M^*$ and an access structure $\mathbb{A}$. $\mathcal{B}$ sets $CT^* = \text{Encrypt}(\mathsf{PK}, M^*, \mathbb{A})$ and sends $CT^*$ to $\mathcal{A}$. Let $CT^* = (\mathbb{A}' = (\mathbf{A}, \rho), \; vk, \; \tilde{C} = (\hat{C}, \; C_1, C_1', C_{1,i}, D_{1,i}, \; C_2, C_2', C_{2,i}, \; D_{2,i}), \; \sigma)$, where $\hat{C} = u^{H(\tilde{M}^*)} v^{H(\bar{M}^*)} d$ and $\tilde{M}^* \in \mathbb{G}_T$ is chosen by $\mathcal{B}$ randomly.
- Query phase 2 $\mathcal{A}$ continues to adaptively issue private key queries as in Query phase 1, and $\mathcal{B}$ responds the queries as in Query phase 1.
- Output The adversary $\mathcal{A}$ outputs a set of attributes $\mathcal{S}^*$ and a transformed ciphertext $CT^{*\prime} = (\hat{T}, T_1, T_1', T_2, T_2')$.

$\mathcal{B}$ computes $T_1/T_1'^{z_{\mathcal{S}^*}} = M$ and $T_2/T_2'^{z_{\mathcal{S}^*}} = \tilde{M}$, where $z_{\mathcal{S}^*}$, known by $\mathcal{B}$, is the retrieving key for the attributes set $\mathcal{S}^*$. If the adversary $\mathcal{A}$ wins the above game, then $\mathcal{B}$ can obtain

$$g^{xH(M^*)+yH(\tilde{M}^*)+z}$$
$$= u^{H(M^*)} v^{H(\tilde{M}^*)} d = \hat{C} = \hat{T} = u^{H(M)} v^{H(\bar{M})} d$$
$$= g^{xH(M)+yH(\tilde{M})+z},$$

where $M \neq M^*$ and $M^*, \tilde{M}^*, M, \tilde{M}, y, z$ are known by $\mathcal{B}$. Since $H$ is a collision-resistant hash function, with overwhelming probability, $H(M^*)$ is not equal to $H(M)$. Then, $\mathcal{B}$ outputs $x = \frac{y(H(\tilde{M})-H(\tilde{M}^*))}{H(M^*)-H(M)}$ as the solution of the DL problem $(p, \mathbb{G}, \mathbb{G}_T, p_1, p_2, p_3, g, g^x)$. ∎

## V. PERFORMANCE

In order to evaluate the performance of our CP-ABE scheme with verifiable outsourced decryption presented in Section IV, we implement our scheme in software based on the libfenc library [18] and using a 224-bit MNT elliptic curve from the Stanford Pairing-Based Crypto library [34]. Although our implementation based the MNT curve implies the use of asymmetric pairing, only a small change need to be made on our scheme of symmetric setting in the implementation. Specifically, suppose that an asymmetric pairing $e$ takes elements from $\mathbb{G}_1$ and $\mathbb{G}_2$ as inputs. Then, according to the description of our scheme in Section IV, we generate two $g$'s, one from
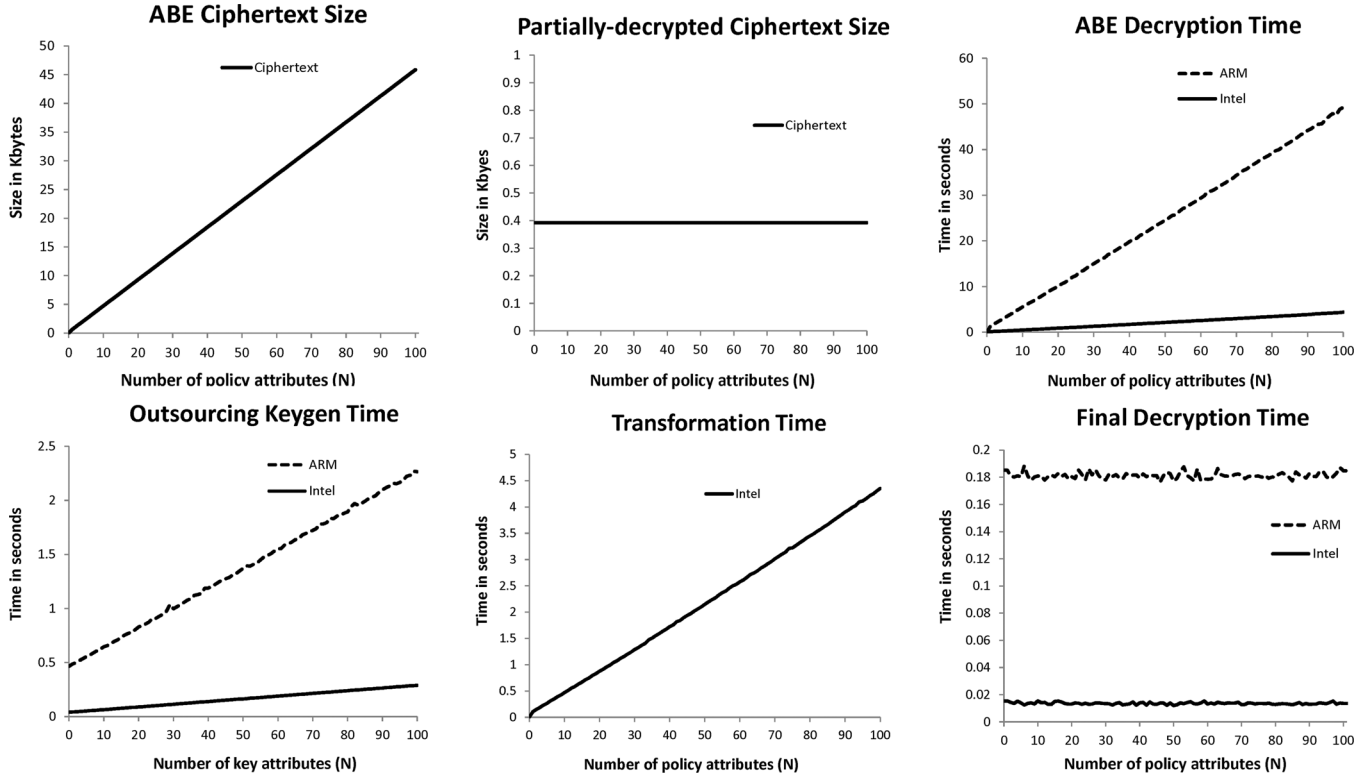
Fig. 2. Performance of our CP-ABE scheme with verifiable outsourced decryption.

$\mathbb{G}_1$ and another from $\mathbb{G}_2$, and compute two corresponding $g^a$'s. We further set $u, v, d, T_i$ as group elements in $\mathbb{G}_1$. As a consequence, among the ciphertext and private key components, $\hat{C}, C'_1, C'_2, C_{1,i}, C_{2,i}, K_i$ are group elements in $\mathbb{G}_1$ while $D_{1,i}, D_{2,i}, K, K_0$ are group elements in $\mathbb{G}_2$. The reason why we implement our proposed scheme using asymmetric pairing is that: compared to symmetric pairings, asymmetric pairings are much faster and more compact to implement [35]–[37]. We compile our code on two dedicated hardware platforms: a 2.53 GHz Intel Core CPU with 4 GB of RAM running 32-bit Linux Kernel version 2.6.32, and a 800 MHz ARM-based Samsung GT-S5830 with 278 MB of RAM running Android OS.

As in [18], our implementation adopts the key encapsulation mechanism, where the ABE ciphertext is the encryption of a symmetric key $k$ and the message is encrypted separately using a symmetric encryption scheme under this $k$. The symmetric key is computed as $k = e(g, g)^{\alpha s}$, and we omit the components $C_1 = M \cdot e(g, g)^{\alpha s}$ and $C_2 = \hat{M} e(g, g)^{\alpha s'}$ in the ABE ciphertext. Note that in our scheme presented in Section IV, the verification step involves $M$ and $\hat{M}$, while in our implementation, we use the two hash values of $e(g, g)^{\alpha s}$ and $e(g, g)^{\alpha s'}$, instead. These modifications reduce the sizes of the ABE ciphertext and the partially-decrypted ciphertext by two elements in $\mathbb{G}_T$, respectively, without sacrificing security and verifiability.

*Experimental Setup:* In a CP-ABE scheme, the complexity of ciphertext policy impacts both the decryption time and the ciphertext size. To illustrate this, we generate ciphertext policies in the form of $(A_1 \text{ and } A_2 \text{ and } \dots \text{ and } A_N)$ (i.e., the worst situation over the policy), where each $A_i$ is an attribute. This approach ensures that all the ciphertext components are involved

the decryption computation. We generate 100 distinct policies in this form with $N$ increasing from 1 to 100. In each case, we construct a corresponding standard decryption key that contains exact $N$ attributes.

In our experiments, we do not consider the effect of symmetric encryption. Thus, all the datum on decryption time and ciphertext size presented in Fig. 2 are only associated with the key encapsulation variant of our ABE scheme. For each ciphertext policy, we repeat our experiment 100 times on the PC and 30 times on the ARM device and we take the average values as the experimental results. In Fig. 2, we show the size of standard ABE ciphertext and partially-decrypted ciphertext, the standard ABE decryption time on the Intel and the ARM platforms, the time of generating an outsourcing key, the time of transforming the ABE ciphertext, and the time of decrypting the transformed ciphertext on the Intel and the ARM platforms.

*Discussion:* The ABE ciphertext size and decryption/transformation time increase linearly as the ciphertext policy's complexity grows. An encryption under a ciphertext policy with 100 attributes results in an ABE ciphertext of nearly 46 KB and it takes about 5 seconds for the Intel platform to decrypt this ciphertext. On the other hand, decryption time degrades considerably on the ARM platform: it requires more than 1 second to decrypt a ciphertext under a policy with one attribute, 5 seconds under a policy with ten attributes and almost 50 seconds under a policy with one hundred attributes.

As expected, outsourcing substantially reduces the computation time required for devices with limited computing resource to recover the plaintext. The bulk of the decryption operation is now handled by the proxy. The transformed ciphertext is not

only much efficient to decrypt but also much smaller in size. In our implementation, each partially-decrypted ciphertext has a constant size of 392 bytes, regardless the complexity of its corresponding ciphertext policy. The final decryption and verification of the transformed ciphertext requires only 13 milliseconds on the Intel platform and approximately 180 milliseconds on the ARM platform.

## VI. CONCLUSION

In this paper, we considered a new requirement of ABE with outsourced decryption: verifiability. We modified the original model of ABE with outsourced decryption proposed by Green *et al.* [12] to include verifiability. We also proposed a concrete ABE scheme with verifiable outsourced decryption and proved that it is secure and verifiable. Our scheme does not rely on random oracles. To assess the practicability of our scheme, we implemented it and conducted experiments in a simulated outsourcing environment. As expected, the scheme substantially reduced the computation time required for resource-limited devices to recover plaintexts.

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