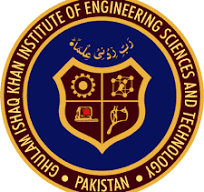
**Ghulam Ishaq Khan Institute of Engineering Sciences and Technology**

**Faculty of Computer Science and Engineering**

**CS342 – Numerical Analysis Project**

**Submitted To: Sir Aamir Shehzad**

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# Bisection Method

## ****Method Overview****

The bisection method is a root-finding algorithm that:

* Requires a continuous function that changes sign over an interval [a, b]
* Repeatedly bisects the interval and selects the subinterval containing the root
* Guarantees convergence to a root if the function is continuous
* Uses a tolerance of 1e-6 and maximum 100 iterations as stopping criteria
* Calculates error as the difference between consecutive approximations

## Explanation of the Code

The implementation consists of three main functions:

**bisectionMethod:**

* Takes function, interval bounds [a, b], tolerance, and max iterations
* Returns root approximation, iteration count, and iteration data
* Checks for sign change at interval endpoints
* Updates interval based on function value at midpoint

**printResults:**

* Shows current interval bounds [a, b] and their function values
* Displays midpoint (x) and its function value
* Calculates error between consecutive approximations
* Formats output in a clear tabular form

**plotResults:**

* Error vs Iterations plot showing convergence
* Function curve plot with root location

## Tables of Results

**Stopping Tolerance: 10-6**

**f(x) = x3- 4x + 1**

**Interval: [0,1]**

| **Iteration** | **a** | **f(a)** | **b** | **f(b)** | **x** | **f(x)** | **Error** |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0.000000 | 1.000000 | 1.000000 | -2.000000 | 0.500000 | -0.875000 | inf |
| 2 | 0.000000 | 1.000000 | 0.500000 | -0.875000 | 0.250000 | 0.015625 | 0.250000 |
| 3 | 0.250000 | 0.015625 | 0.500000 | -0.875000 | 0.375000 | -0.447266 | 0.125000 |
| 4 | 0.250000 | 0.015625 | 0.375000 | -0.447266 | 0.312500 | -0.219482 | 0.062500 |
| 5 | 0.250000 | 0.015625 | 0.312500 | -0.219482 | 0.281250 | -0.102753 | 0.031250 |
| 6 | 0.250000 | 0.015625 | 0.281250 | -0.102753 | 0.265625 | -0.043758 | 0.015625 |
| 7 | 0.250000 | 0.015625 | 0.265625 | -0.043758 | 0.257812 | -0.014114 | 0.007812 |
| 8 | 0.250000 | 0.015625 | 0.257812 | -0.014114 | 0.253906 | 0.000744 | 0.003906 |
| 9 | 0.253906 | 0.000744 | 0.257812 | -0.014114 | 0.255859 | -0.006688 | 0.001953 |
| 10 | 0.253906 | 0.000744 | 0.255859 | -0.006688 | 0.254883 | -0.002973 | 0.000977 |
| 11 | 0.253906 | 0.000744 | 0.254883 | -0.002973 | 0.254395 | -0.001115 | 0.000488 |
| 12 | 0.253906 | 0.000744 | 0.254395 | -0.001115 | 0.254150 | -0.000185 | 0.000244 |
| 13 | 0.253906 | 0.000744 | 0.254150 | -0.000185 | 0.254028 | 0.000279 | 0.000122 |
| 14 | 0.254028 | 0.000279 | 0.254150 | -0.000185 | 0.254089 | 0.000047 | 0.000061 |
| 15 | 0.254089 | 0.000047 | 0.254150 | -0.000185 | 0.254120 | -0.000069 | 0.000031 |
| 16 | 0.254089 | 0.000047 | 0.254120 | -0.000069 | 0.254105 | -0.000011 | 0.000015 |
| 17 | 0.254089 | 0.000047 | 0.254105 | -0.000011 | 0.254097 | 0.000018 | 0.000008 |
| 18 | 0.254097 | 0.000018 | 0.254105 | -0.000011 | 0.254101 | 0.000003 | 0.000004 |
| 19 | 0.254101 | 0.000003 | 0.254105 | -0.000011 | 0.254103 | -0.000004 | 0.000002 |
| 20 | 0.254101 | 0.000003 | 0.254103 | -0.000004 | 0.254102 | -0.000000 | 0.000001 |

**f(x) =**

**Interval: [0,10]**

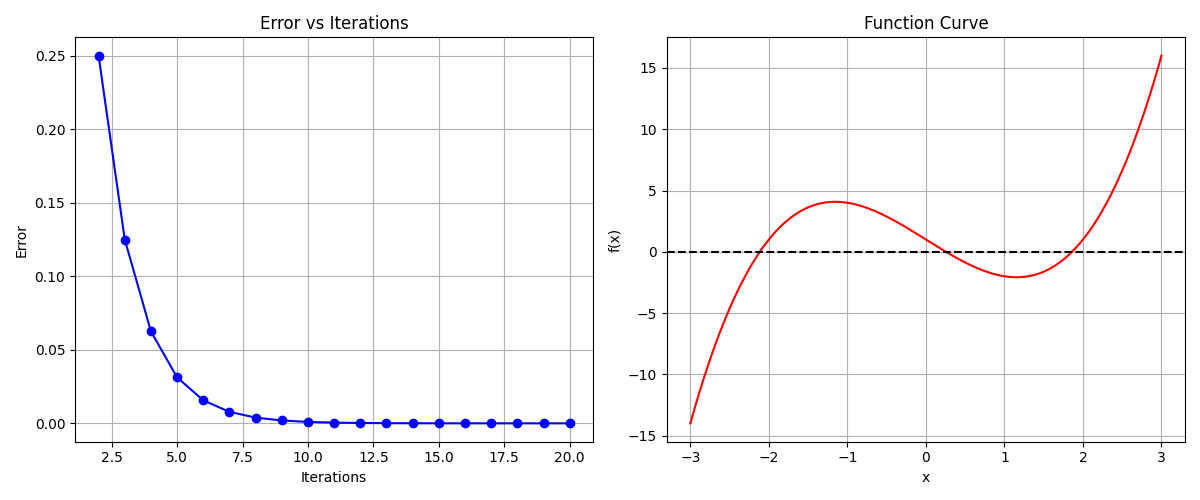
| **Iteration** | **a** | **f(a)** | **b** | **f(b)** | **x** | **f(x)** | **Error** |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0.000000 | -2.000000 | 10.000000 | 1.162278 | 5.000000 | 0.236068 | inf |
| 2 | 0.000000 | -2.000000 | 5.000000 | 0.236068 | 2.500000 | -0.418861 | 2.500000 |
| 3 | 2.500000 | -0.418861 | 5.000000 | 0.236068 | 3.750000 | -0.063508 | 1.250000 |
| 4 | 3.750000 | -0.063508 | 5.000000 | 0.236068 | 4.375000 | 0.091650 | 0.625000 |
| 5 | 3.750000 | -0.063508 | 4.375000 | 0.091650 | 4.062500 | 0.015564 | 0.312500 |
| 6 | 3.750000 | -0.063508 | 4.062500 | 0.015564 | 3.906250 | -0.023576 | 0.156250 |
| 7 | 3.906250 | -0.023576 | 4.062500 | 0.015564 | 3.984375 | -0.003910 | 0.078125 |
| 8 | 3.984375 | -0.003910 | 4.062500 | 0.015564 | 4.023438 | 0.005851 | 0.039062 |
| 9 | 3.984375 | -0.003910 | 4.023438 | 0.005851 | 4.003906 | 0.000976 | 0.019531 |
| 10 | 3.984375 | -0.003910 | 4.003906 | 0.000976 | 3.994141 | -0.001465 | 0.009766 |
| 11 | 3.994141 | -0.001465 | 4.003906 | 0.000976 | 3.999023 | -0.000244 | 0.004883 |
| 12 | 3.999023 | -0.000244 | 4.003906 | 0.000976 | 4.001465 | 0.000366 | 0.002441 |
| 13 | 3.999023 | -0.000244 | 4.001465 | 0.000366 | 4.000244 | 0.000061 | 0.001221 |
| 14 | 3.999023 | -0.000244 | 4.000244 | 0.000061 | 3.999634 | -0.000092 | 0.000610 |
| 15 | 3.999634 | -0.000092 | 4.000244 | 0.000061 | 3.999939 | -0.000015 | 0.000305 |
| 16 | 3.999939 | -0.000015 | 4.000244 | 0.000061 | 4.000092 | 0.000023 | 0.000153 |
| 17 | 3.999939 | -0.000015 | 4.000092 | 0.000023 | 4.000015 | 0.000004 | 0.000076 |
| 18 | 3.999939 | -0.000015 | 4.000015 | 0.000004 | 3.999977 | -0.000006 | 0.000038 |
| 19 | 3.999977 | -0.000006 | 4.000015 | 0.000004 | 3.999996 | -0.000001 | 0.000019 |
| 20 | 3.999996 | -0.000001 | 4.000015 | 0.000004 | 4.000006 | 0.000001 | 0.000010 |
| 21 | 3.999996 | -0.000001 | 4.000006 | 0.000001 | 4.000001 | 0.000000 | 0.000005 |
| 22 | 3.999996 | -0.000001 | 4.000001 | 0.000000 | 3.999999 | -0.000000 | 0.000002 |
| 23 | 3.999999 | -0.000000 | 4.000001 | 0.000000 | 4.000000 | -0.000000 | 0.000001 |
| 24 | 4.000000 | -0.000000 | 4.000001 | 0.000000 | 4.000000 | 0.000000 | 0.000001 |

**f(x) = cos(x) - x**

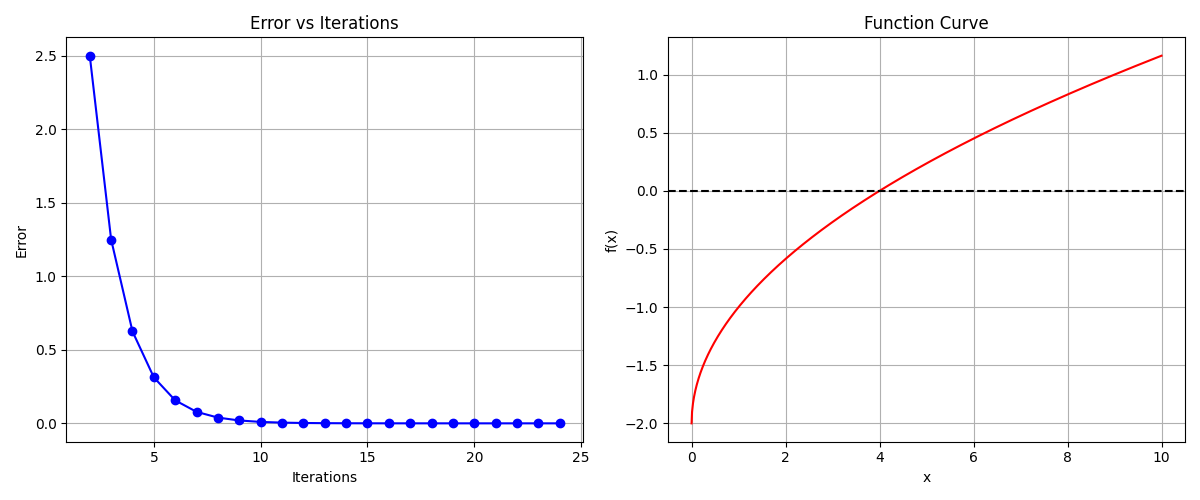
**Interval: [0,1]**

| **Iteration** | **a** | **f(a)** | **b** | **f(b)** | **x** | **f(x)** | **Error** |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 1 | 0.000000 | 1.000000 | 1.000000 | -0.459698 | 0.500000 | 0.377583 | inf |
| 2 | 0.500000 | 0.377583 | 1.000000 | -0.459698 | 0.750000 | -0.018311 | 0.250000 |
| 3 | 0.500000 | 0.377583 | 0.750000 | -0.018311 | 0.625000 | 0.185963 | 0.125000 |
| 4 | 0.625000 | 0.185963 | 0.750000 | -0.018311 | 0.687500 | 0.085335 | 0.062500 |
| 5 | 0.687500 | 0.085335 | 0.750000 | -0.018311 | 0.718750 | 0.033879 | 0.031250 |
| 6 | 0.718750 | 0.033879 | 0.750000 | -0.018311 | 0.734375 | 0.007875 | 0.015625 |
| 7 | 0.734375 | 0.007875 | 0.750000 | -0.018311 | 0.742188 | -0.005196 | 0.007812 |
| 8 | 0.734375 | 0.007875 | 0.742188 | -0.005196 | 0.738281 | 0.001345 | 0.003906 |
| 9 | 0.738281 | 0.001345 | 0.742188 | -0.005196 | 0.740234 | -0.001924 | 0.001953 |
| 10 | 0.738281 | 0.001345 | 0.740234 | -0.001924 | 0.739258 | -0.000289 | 0.000977 |
| 11 | 0.738281 | 0.001345 | 0.739258 | -0.000289 | 0.738770 | 0.000528 | 0.000488 |
| 12 | 0.738770 | 0.000528 | 0.739258 | -0.000289 | 0.739014 | 0.000120 | 0.000244 |
| 13 | 0.739014 | 0.000120 | 0.739258 | -0.000289 | 0.739136 | -0.000085 | 0.000122 |
| 14 | 0.739014 | 0.000120 | 0.739136 | -0.000085 | 0.739075 | 0.000017 | 0.000061 |
| 15 | 0.739075 | 0.000017 | 0.739136 | -0.000085 | 0.739105 | -0.000034 | 0.000031 |
| 16 | 0.739075 | 0.000017 | 0.739105 | -0.000034 | 0.739090 | -0.000008 | 0.000015 |
| 17 | 0.739075 | 0.000017 | 0.739090 | -0.000008 | 0.739082 | 0.000005 | 0.000008 |
| 18 | 0.739082 | 0.000005 | 0.739090 | -0.000008 | 0.739086 | -0.000002 | 0.000004 |
| 19 | 0.739082 | 0.000005 | 0.739086 | -0.000002 | 0.739084 | 0.000001 | 0.000002 |
| 20 | 0.739084 | 0.000001 | 0.739086 | -0.000002 | 0.739085 | -0.000000 | 0.000001 |

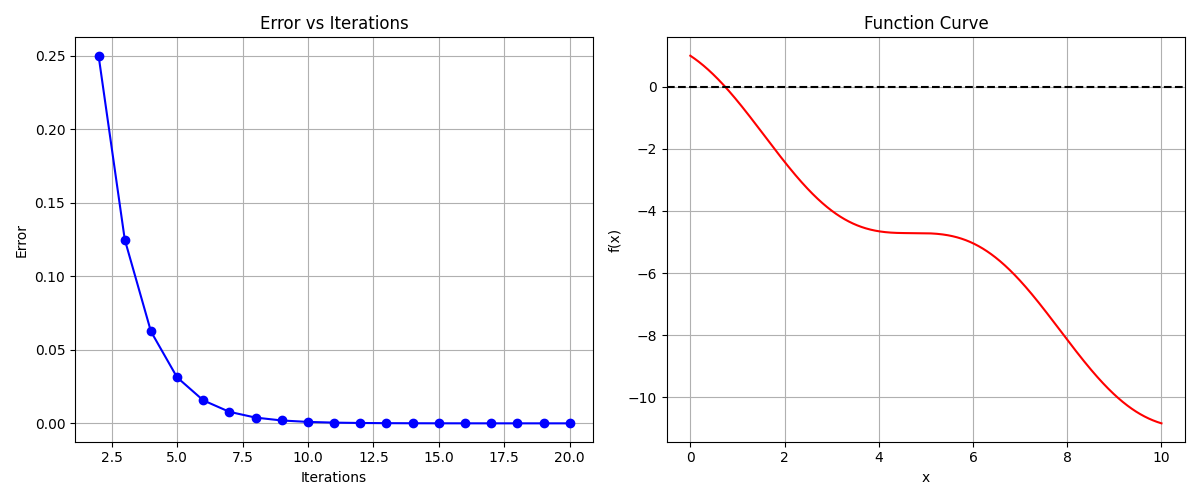
## Graphs

**f(x) = x3- 4x + 1**

**f(x) =**

****

**f(x) = cos(x) - x**

****

## ****Interpretation of Results****

The bisection method was applied to three functions, each with a known sign change in the given interval. In all cases, the method successfully converged to a root within the specified tolerance of 10−6.

### ****Function 1:**** (x) = x3 - 4x + 1 ****on**** [0, 1]

* **Root found:** ≈ 0.254102
* **Iterations:** 20
* **Remarks:** Function changes sign over [0,1]; convergence was steady and accurate.

### ****Function 2:**** f(x)= ****on**** [0, 10]

* **Root found:** ≈ 4.000000
* **Iterations:** 24
* **Remarks:** Root at x=4x = 4 was accurately detected; error halved each step.

### ****Function 3:**** f(x)=cos(x)−x on[0, 1]

* **Root found:** ≈ 0.739085
* **Iterations:** 20
* **Remarks:** Classic fixed-point problem; bisection method converged reliably.

### ****Conclusion****

The method showed consistent convergence in all cases, with clear reduction in error and root approximation through midpoint updates. Tabulated results confirm the method's precision and stability.

# Fixed Point Iteration

## Method Overview

The Fixed Point Iteration method is a numerical technique used to find fixed points of a function, where x = g(x). A fixed point is a value that remains unchanged when the function is applied to it. This implementation provides a robust solution with visualization and detailed iteration tracking.

## Explanation of Code

**Main Function: fixedPointIteration()**

**Input Parameters:**

* g(x): The iteration function
* x0: Initial guess
* tolerance: Convergence criterion (default: 1e-6)
* maxIterations: Maximum allowed iterations (default: 100)
* Returns: (fixed point, iterations count, iteration data)

**Visualization: plotResults()**

Generates two plots:

* Error convergence over iterations
* Iteration function g(x) with y=x line intersection

**Results Display: printResults()**

* Presents iteration data in a formatted table
* Shows convergence progress and final results

## Table of Results

**Tolerance Limit = 10-6**

**g(x)=cos(x)**

**Initial guess: x0=0**

| **Iteration** | **xₙ** | **g(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 1.000000 | 0.540302 | 1.000000 |
| 2 | 0.540302 | 0.857553 | 0.459698 |
| 3 | 0.857553 | 0.654290 | 0.317251 |
| 4 | 0.654290 | 0.793480 | 0.203263 |
| 5 | 0.793480 | 0.701369 | 0.139191 |
| 6 | 0.701369 | 0.763960 | 0.092112 |
| 7 | 0.763960 | 0.722102 | 0.062591 |
| 8 | 0.722102 | 0.750418 | 0.041857 |
| 9 | 0.750418 | 0.731404 | 0.028315 |
| 10 | 0.731404 | 0.744237 | 0.019014 |
| 11 | 0.744237 | 0.735605 | 0.012833 |
| 12 | 0.735605 | 0.741425 | 0.008633 |
| 13 | 0.741425 | 0.737507 | 0.005820 |
| 14 | 0.737507 | 0.740147 | 0.003918 |
| 15 | 0.740147 | 0.738369 | 0.002640 |
| 16 | 0.738369 | 0.739567 | 0.001778 |
| 17 | 0.739567 | 0.738760 | 0.001198 |
| 18 | 0.738760 | 0.739304 | 0.000807 |
| 19 | 0.739304 | 0.738938 | 0.000544 |
| 20 | 0.738938 | 0.739184 | 0.000366 |
| 21 | 0.739184 | 0.739018 | 0.000247 |
| 22 | 0.739018 | 0.739130 | 0.000166 |
| 23 | 0.739130 | 0.739055 | 0.000112 |
| 24 | 0.739055 | 0.739106 | 0.000075 |
| 25 | 0.739106 | 0.739071 | 0.000051 |
| 26 | 0.739071 | 0.739094 | 0.000034 |
| 27 | 0.739094 | 0.739079 | 0.000023 |
| 28 | 0.739079 | 0.739089 | 0.000016 |
| 29 | 0.739089 | 0.739082 | 0.000010 |
| 30 | 0.739082 | 0.739087 | 0.000007 |
| 31 | 0.739087 | 0.739084 | 0.000005 |
| 32 | 0.739084 | 0.739086 | 0.000003 |
| 33 | 0.739086 | 0.739085 | 0.000002 |
| 34 | 0.739085 | 0.739086 | 0.000001 |
| 35 | 0.739086 | 0.739085 | 0.000001 |

**g(x)=**

**Initial guess: x0=0**

| **Iteration** | **xₙ** | **g(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 0.666667 | 0.888889 | 0.666667 |
| 2 | 0.888889 | 0.962963 | 0.222222 |
| 3 | 0.962963 | 0.987654 | 0.074074 |
| 4 | 0.987654 | 0.995885 | 0.024691 |
| 5 | 0.995885 | 0.998628 | 0.008230 |
| 6 | 0.998628 | 0.999543 | 0.002743 |
| 7 | 0.999543 | 0.999848 | 0.000914 |
| 8 | 0.999848 | 0.999949 | 0.000305 |
| 9 | 0.999949 | 0.999983 | 0.000102 |
| 10 | 0.999983 | 0.999994 | 0.000034 |
| 11 | 0.999994 | 0.999998 | 0.000011 |
| 12 | 0.999998 | 0.999999 | 0.000004 |
| 13 | 0.999999 | 1.000000 | 0.000001 |

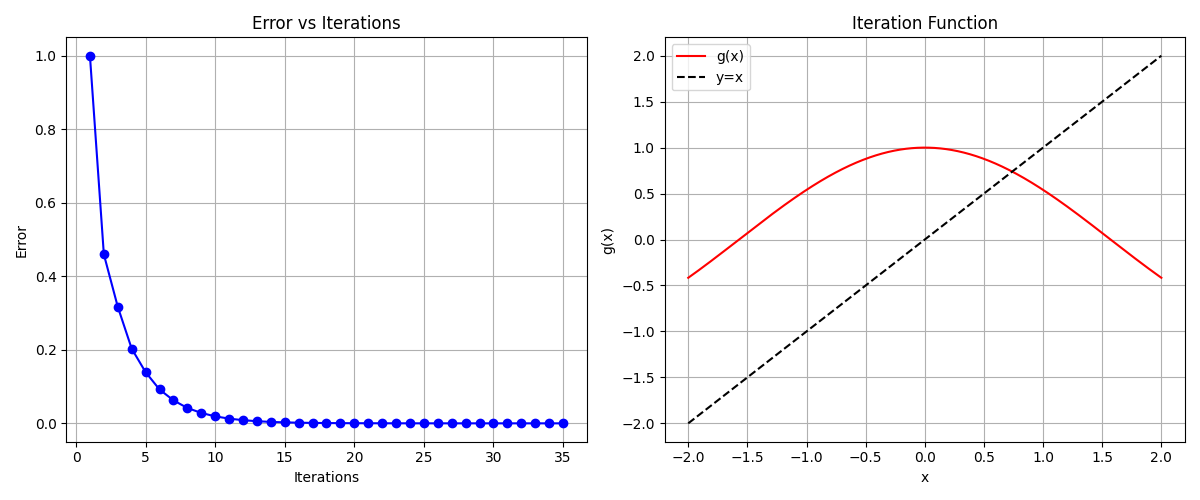
**g(x)=**

**Initial guess: x0=2**

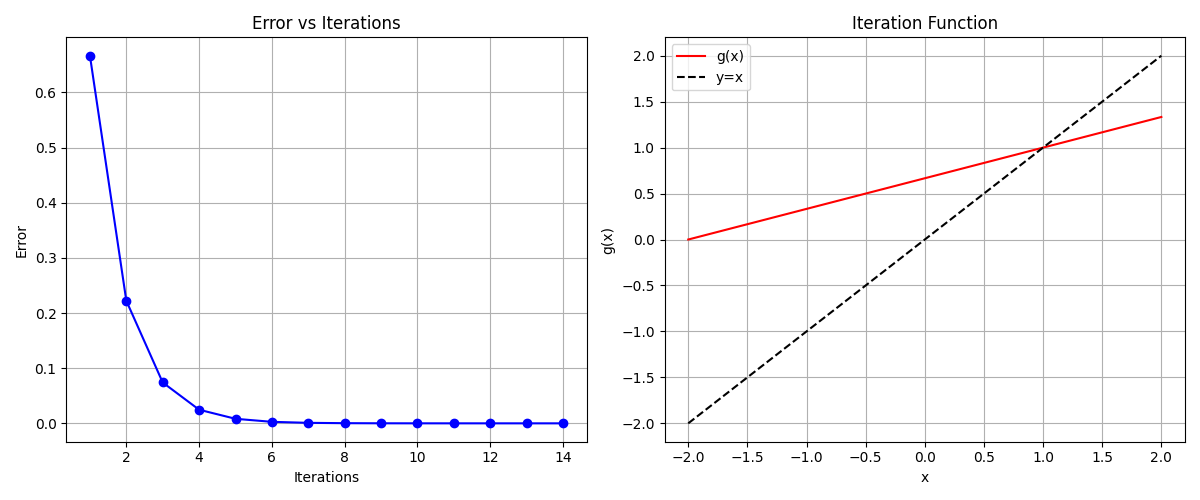
| **Iteration** | **xₙ** | **g(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 1.250000 | 1.025000 | 0.750000 |
| 2 | 1.025000 | 1.000305 | 0.225000 |
| 3 | 1.000305 | 1.000000 | 0.024695 |
| 4 | 1.000000 | 1.000000 | 0.000305 |
| 5 | 1.000000 | 1.000000 | 0.000000 |

## Graphs

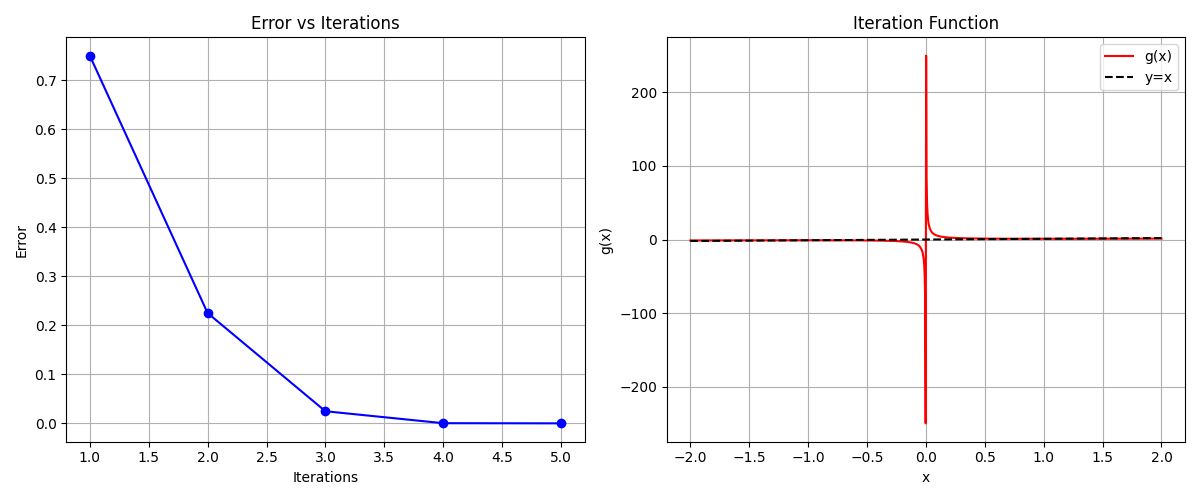
**g(x)=cos(x)**



**g(x)=**



**g(x)=**



## ****Interpretation of Results****

The Fixed Point Iteration method was applied to three functions using an initial guess and a convergence tolerance of 10−6. Results are as follows:

### ****Function 1:**** g(x)=cos(x), x0=0

* **Fixed Point:** ≈ 0.739085
* **Iterations:** 35
* **Remarks:** Convergence was gradual due to the nature of cosine near the root, showing consistent error reduction.

### ****Function 2:**** g(x)= , x0=0

* **Fixed Point:** ≈ 1.000000
* **Iterations:** 13
* **Remarks:** Smooth and steady convergence with fewer iterations, demonstrating strong contractive behavior.

### ****Function 3:**** g(x)= , x0=2

* **Fixed Point:** ≈ 1.000000
* **Iterations:** 5
* **Remarks:** Fast convergence due to the function’s rapid correction of the initial guess.

### ****Conclusion****

The method successfully converged in all cases, with the speed of convergence dependent on the function's nature and constructiveness. Proper choice of g(x)g(x) and initial guess significantly impacts performance.

# Newton-Raphson Method

## Method Overview

The Newton-Raphson method is an iterative technique for finding roots of a differentiable function. It uses the function's derivative to generate successively better approximations to the roots of a real-valued function. The method starts with an initial guess and uses the tangent line at that point to find the next approximation.

## Explanation of the Code

**Main Function: newtonRaphson()**

**Input Parameters:**

* f(x): The function whose root we want to find
* df(x): The derivative of f(x)
* x0: Initial guess
* tolerance: Convergence criterion (default: 1e-6)
* maxIterations: Maximum allowed iterations (default: 100)
* Returns: (root, iterations count, iteration data)

**Visualization: plotResults()**

**Generates three plots:**

* Error convergence over iterations
* Original function f(x)
* Derivative function f'(x)

**Results Display: printResults()**

* Presents iteration data in a formatted table
* Shows convergence progress and final results

## Table of Results

**Tolerance Limit = 10-6**

**f(x)=x3−x−2**

**Initial guess: x0=2**

| **Iteration** | **xₙ** | **f(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 1.636364 | 0.745304 | 0.363636 |
| 2 | 1.530392 | 0.053939 | 0.105972 |
| 3 | 1.521441 | 0.000367 | 0.008951 |
| 4 | 1.521380 | 0.000000 | 0.000062 |
| 5 | 1.521380 | 0.000000 | 0.000000 |

**f(x)=x2 – cos(x)**

**Initial guess: x0=1**

| **Iteration** | **xₙ** | **f(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 0.838218 | 0.033822 | 0.161782 |
| 2 | 0.824242 | 0.000261 | 0.013977 |
| 3 | 0.824132 | 0.000000 | 0.000110 |
| 4 | 0.824132 | 0.000000 | 0.000000 |

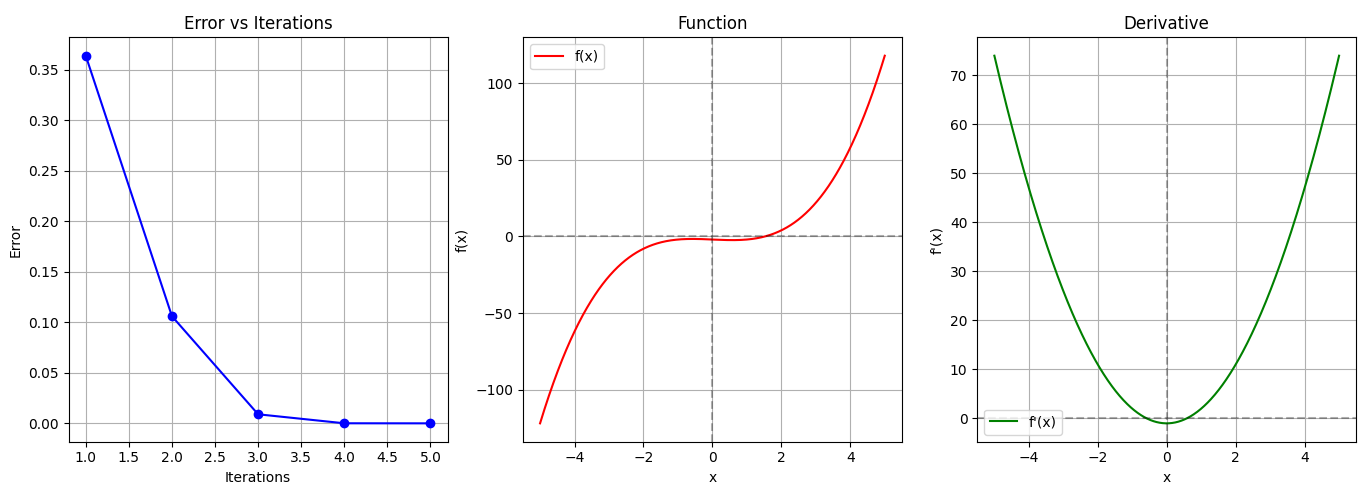
**f(x) = ex – 5x**

**Initial guess: x0=2**

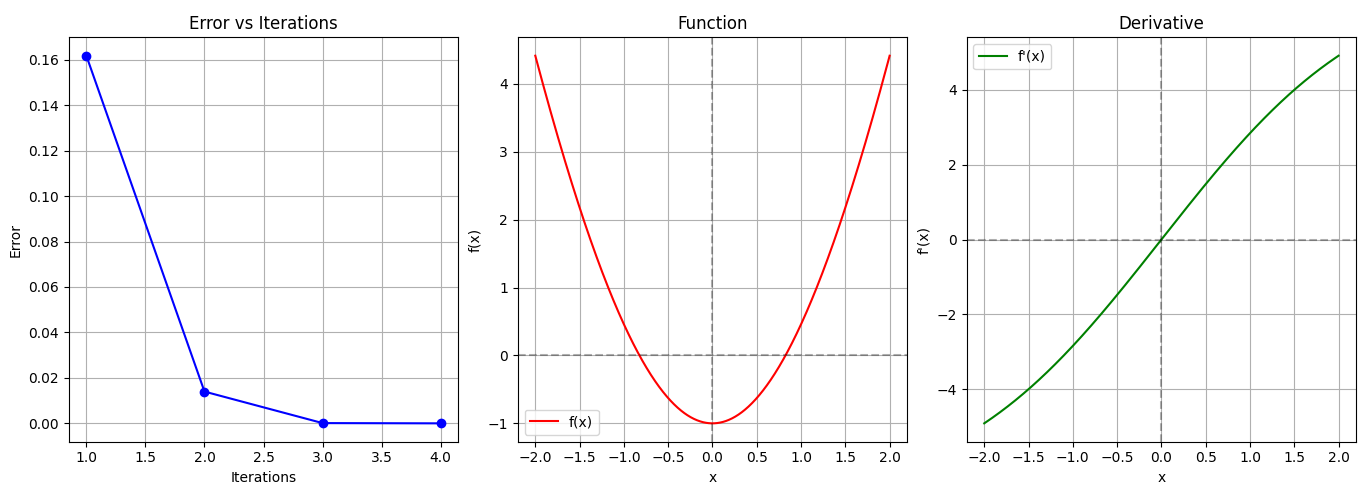
| **Iteration** | **xₙ** | **f(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 3.092877 | 6.576008 | 1.092877 |
| 2 | 2.706970 | 1.448952 | 0.385907 |
| 3 | 2.561839 | 0.150436 | 0.145130 |
| 4 | 2.542939 | 0.002300 | 0.018900 |
| 5 | 2.542641 | 0.000001 | 0.000298 |
| 6 | 2.542641 | 0.000000 | 0.000000 |

## Graphs

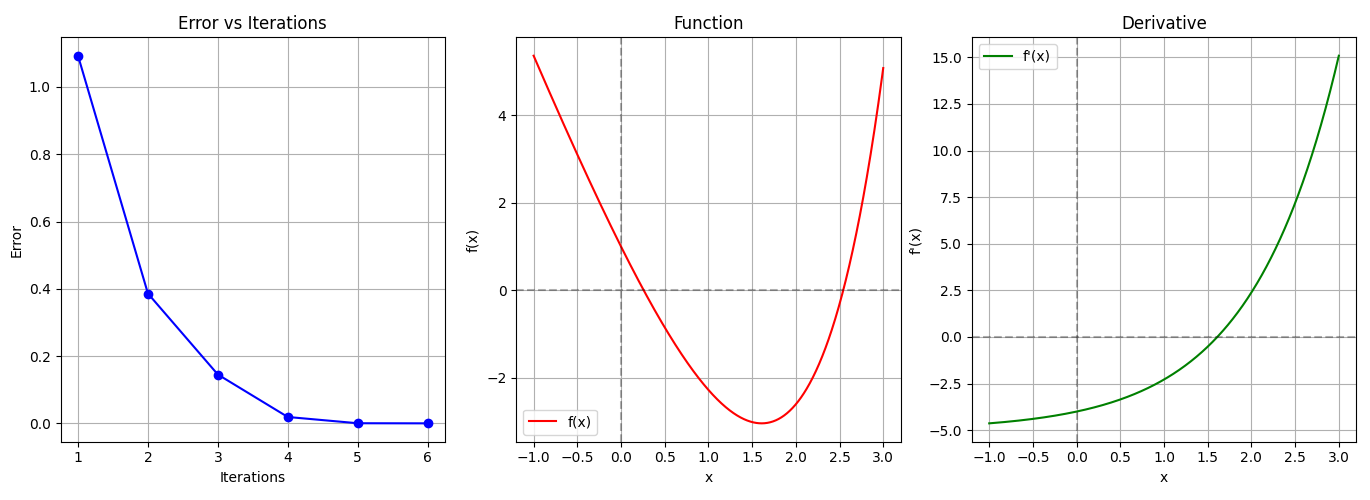
**f(x)=x3−x−2**



**f(x)=****x2 – cos(x)**



**f(x) = ex – 5x**



## ****Interpretation of Results****

The Newton-Raphson method was applied to three functions using an initial guess and a convergence tolerance of 10−6. Results are as follows:

### ****Function 1:**** f(x)=x3−x−2, x0=2

* **Root Found:** ≈ 1.521380
* **Iterations:** 5
* **Remarks:** Fast convergence with quadratic error reduction as expected from the method's nature.

### ****Function 2:**** f(x)=x2 – cos(x), x0=1

* **Root Found:** ≈ 0.824132
* **Iterations:** 4
* **Remarks:** Smooth convergence with rapid stabilization of function values.

### ****Function 3:**** f(x)=ex−5x, x0=2

* **Root Found:** ≈ 2.542641
* **Iterations:** 6
* **Remarks:** Initial large error due to steep slope, followed by steady convergence.

### ****Conclusion****

Newton-Raphson method demonstrated efficient and rapid convergence for all tested functions. Its effectiveness depends on a good initial guess and the behavior of the derivative near the root.

# Secant Method

## Method Overview

The Secant Method is a root-finding algorithm that uses a succession of roots of secant lines to better approximate a root of a function. It's similar to the Newton-Raphson method but doesn't require derivatives, making it particularly useful when derivatives are difficult or expensive to compute.

## Explanation of the Code

**Main Function: secant()**

**Input Parameters:**

* f(x): The function whose root we want to find
* x0: First initial guess
* x1: Second initial guess
* tolerance: Convergence criterion (default: 1e-6)
* maxIterations: Maximum allowed iterations (default: 100)
* Returns: (root, iterations count, iteration data)

**Visualization: plotResults()**

**Generates two plots:**

* Error convergence over iterations
* Function f(x) with root location

**Results Display: printResults()**

* Presents iteration data in a formatted table
* Shows convergence progress and final results

## Table of Results

**Tolerance Limit = 10-6**

**g(x)=x3 – 2x - 5**

**Initial guess: x0=2, x1 = 3**

| **Iteration** | **xₙ** | | **f(xₙ)** | **Error** |
| --- | --- | --- | --- | --- |
| 1 | 2.058824 | -0.390800 | | 0.941176 |
| 2 | 2.081264 | -0.147204 | | 0.022440 |
| 3 | 2.094824 | 0.003044 | | 0.013560 |
| 4 | 2.094549 | -0.000023 | | 0.000275 |
| 5 | 2.094551 | -0.000000 | | 0.000002 |
| 6 | 2.094551 | 0.000000 | | 0.000000 |

**f(x)=sin(x)−x/2**

**Initial guess: x0=1.5, x1 = 2**

| **Iteration** | **xₙ** | **f(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | 1.865903 | 0.023820 | 0.134097 |
| 2 | 1.893794 | 0.001391 | 0.027891 |
| 3 | 1.895524 | -0.000024 | 0.001730 |
| 4 | 1.895494 | 0.000000 | 0.000030 |
| 5 | 1.895494 | 0.000000 | 0.000000 |

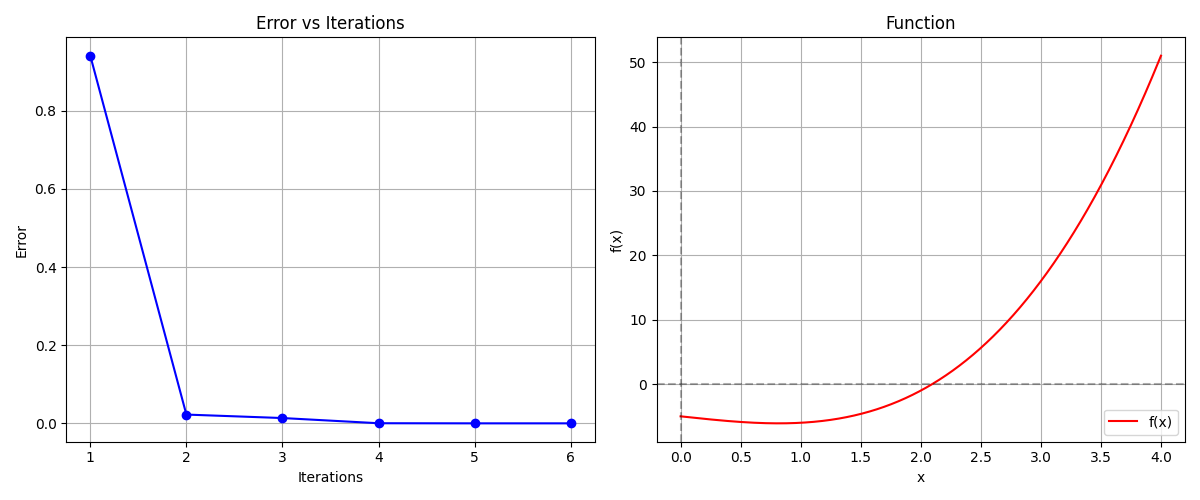
**f(x) = ex – 5x**

**Initial guess: x0=1, x1 = 2**

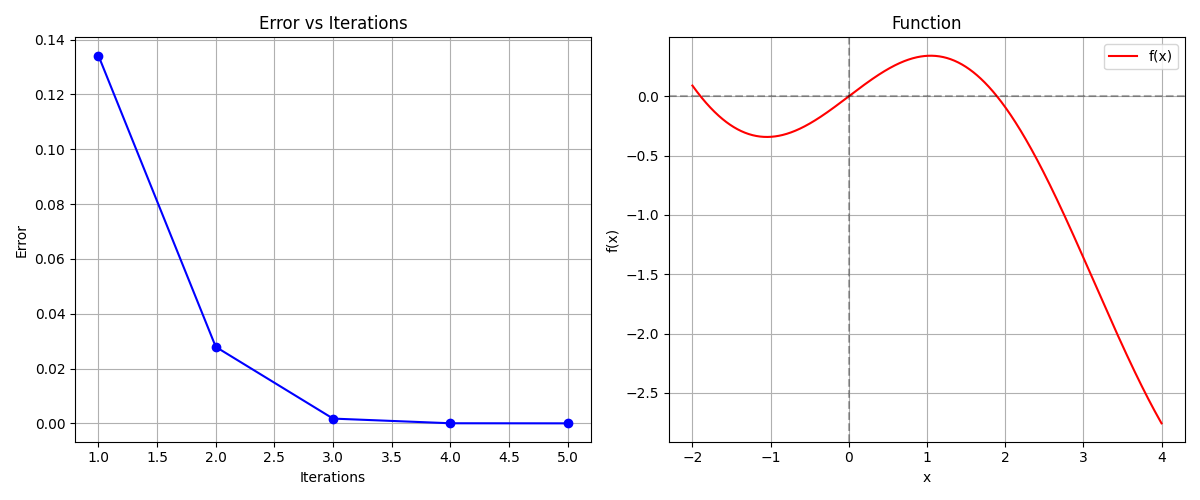
| **Iteration** | **xₙ** | **f(xₙ)** | **Error** |
| --- | --- | --- | --- |
| 1 | -5.930558 | 29.655449 | 7.930558 |
| 2 | 1.358272 | -2.901894 | 7.288831 |
| 3 | 0.708606 | -1.511871 | 0.649666 |
| 4 | 0.001990 | 0.992043 | 0.706616 |
| 5 | 0.281949 | -0.084033 | 0.279959 |
| 6 | 0.260086 | -0.003389 | 0.021863 |
| 7 | 0.259167 | 0.000014 | 0.000919 |
| 8 | 0.259171 | -0.000000 | 0.000004 |
| 9 | 0.259171 | -0.000000 | 0.000000 |

## Graphs

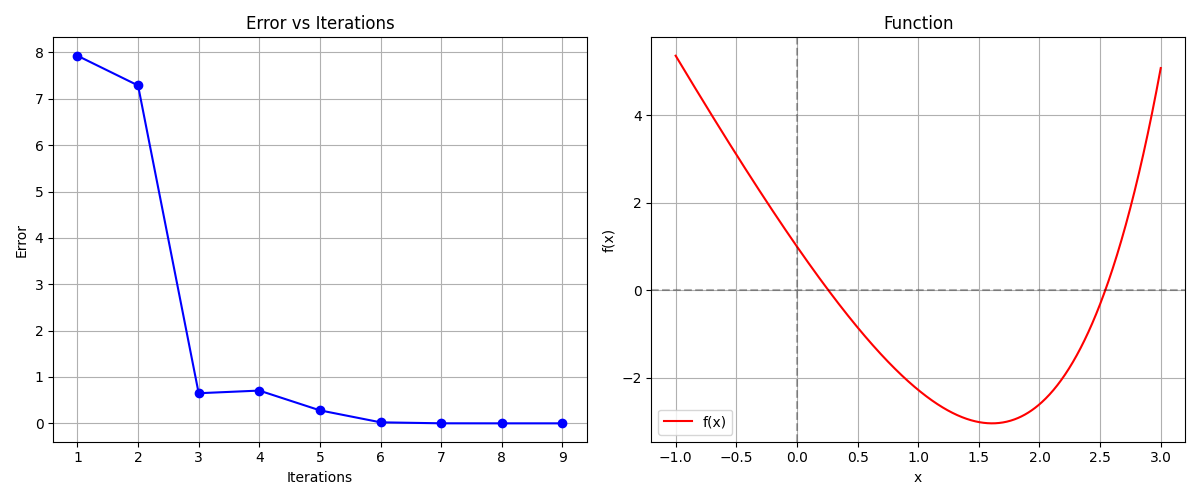
**g(x)=x3 – 2x - 5**



**f(x)=sin(x)−x/2**



**f(x) = ex – 5x**



## ****Interpretation of Results****

The Secant Method was applied to three functions using two initial guesses and a convergence tolerance of 10−6. The outcomes are summarized below:

### ****Function 1:**** f(x)=x3−2x−5, x0=2, x1=3

* **Root Found:** ≈ 2.094551
* **Iterations:** 6
* **Remarks:** Rapid convergence without derivative use, closely matching Newton-Raphson performance.

### ****Function 2:**** f(x)=sin(x)−x/2, x0­=1.5, x1=2

* **Root Found:** ≈ 1.895494
* **Iterations:** 5
* **Remarks:** Smooth and stable convergence, even with initial moderate error.

### ****Function 3:**** f(x)=ex−5x, x0=1, x1=2

* **Root Found:** ≈ 0.259171
* **Iterations:** 9
* **Remarks:** Erratic start due to poor initial guesses, but successfully stabilized and converged.

### ****Conclusion****

The Secant Method effectively finds roots without requiring derivatives, offering good accuracy and convergence for all functions. It is especially advantageous when derivatives are difficult to compute, though careful selection of initial guesses is important for stability.