

# Assignment 4

Junaid Ahmad Bhat

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## Question

$\triangle ABC$  is right angled at B. If  $a = 12$  and  $b+c = 18$ , find  $b$ ,  $c$  and draw the triangle.

## Solution

Given  $a=12$ ,

and  $b+c=18$ ;

$$\Rightarrow c=18-b \quad (1)$$

Therefore,  
we have 3 sides of given right triangle as  $BC=12, AC=b, AB=18-b$ .

By Pythagoras theorem, we have

$$\text{Hypotenuse}^2 = \text{Base}^2 + \text{Altitude}^2$$

As given triangle is right angled at B, side opposite to angle B is AC i.e  $b$  is hypotenuse, therefore,

$$b^2 = 12^2 + (18-b)^2$$

$$b^2 = 144 + 324 + b^2 - 36b$$

$$b = 13 \quad (2)$$

$$\Rightarrow \begin{aligned} c &= 18 - b \\ &= 18 - 13 = 5 \end{aligned} \quad (\text{putting value of } b \text{ from (2) in (1)})$$

So, the sides of triangle are: **a=12, b=13, c=5.**

### Steps of Construction:-

1. Draw a line AC of length =13(i.e b) .
2. Taking A as centre draw an arc of radius =5(i.e c).
3. Taking C as centre draw an arc of radius=12(i.e a).
4. Name the point, where the two arcs meet(step 2 and step 3), as B.
5. Join BA and BC.

Required triangle is given below.

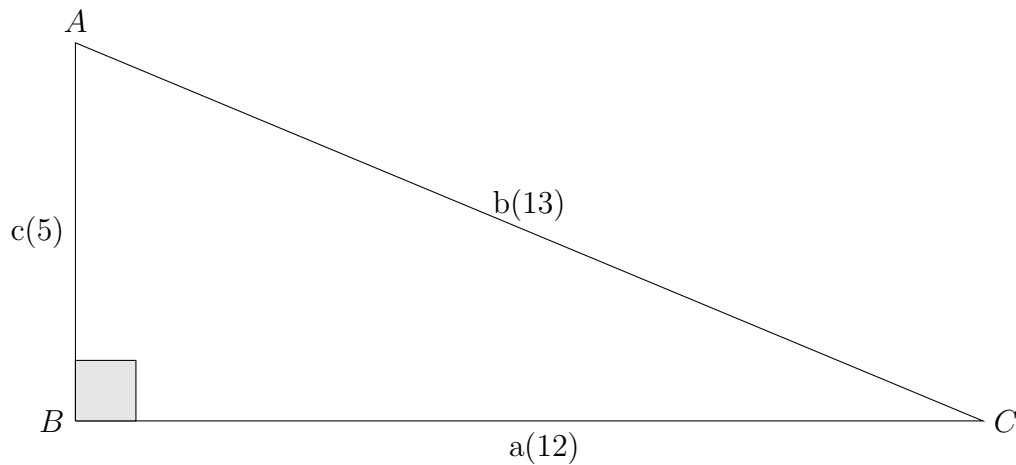


Figure of given triangle(using tikz command)