

Assignment 6

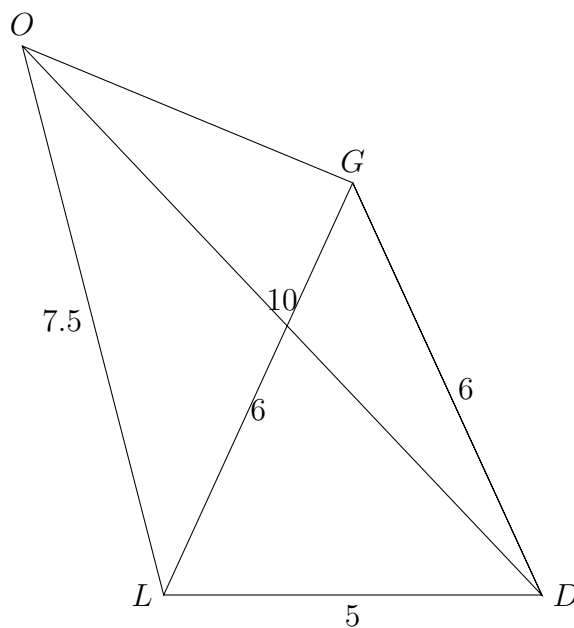
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Question

Draw GOLD such that $OL = 7.5$, $GL = 6$, $GD = 6$, $LD = 5$, $OD = 10$.

Solution



Rough Sketch

TO draw the figure we need to find coordinates of all vertices

Assuming L as origin i.e $L(0,0)$

Therefore coordinates of D are (5,0) (as LD = 5)

Now, let's find coordinates of vertices G and O.

Coordinates of G

G is the intersection point of line LG and DG.

Line LG: $y = mx + c$

$$y = \tan(\angle GLD)x + c \quad (1)$$

$$\angle GLD = \cos^{-1}((6^2 + 5^2 - 6^2)/(2 \cdot 6 \cdot 5)) \quad (\text{cosine rule})$$

$$\text{Therefore, } \angle GLD = 65.37^\circ \quad (2)$$

Putting eqn(2) in eqn(1), we get

$$y = 2.18x + c$$

$$\text{Also } c = 0 \quad (\text{as it passes through } (0,0))$$

$$\text{Therefore LG: } y = 2.18x \quad (A)$$

Similarly

Line DG: $y = mx + c$

$$y = \tan((180^\circ - \angle GDL)x + c \quad (3) (\text{angles measured anti-clockwise})$$

$$\angle GLD = \cos^{-1}((6^2 + 5^2 - 6^2)/(2 \cdot 6 \cdot 5)) \quad (\text{cosine rule})$$

$$\text{Therefore, } \angle GDL = 65.37^\circ \quad (4)$$

Putting eqn(4) in eqn(3), we get

$$y = -2.18x + c$$

$$\text{Also } c = 10.9 \quad (\text{as it passes through } (5,0))$$

$$\text{Line DG: } y = -2.18x + 10.9 \quad (\text{B})$$

solving eqn(A) and eqn(B), we get

$$x = 2.5; y = 5.45$$

Therefore coordinates of G are (2.5, 5.45)

Coordinates of O

G is the intersection point of line LO and DO.

$$\text{Line LO: } y = mx + c$$

$$y = \tan(\angle OLD)x + c \quad (5)$$

$$\angle OLD = \cos^{-1}((7.5^2 + 5^2 - 10^2)/(2 \cdot 7.5 \cdot 5)) \quad (\text{cosine rule})$$

$$\text{Therefore, } \angle OLD = 104.47^\circ \quad (6)$$

Putting eqn(6) in eqn(5), we get

$$y = -3.87x + c$$

$$\text{Also } c = 0 \quad (\text{as it passes through } (0,0))$$

$$\text{Therefore LO: } y = -3.87x \quad (\text{C})$$

Similarly

$$\text{Line DO: } y = mx + c$$

$$y = \tan((180^\circ - \angle ODL)x + c \quad (7) \quad (\text{angles measured anti-clockwise})$$

$$\angle OLD = \cos^{-1}((10^2 + 5^2 - 7.5^2)/(2 \cdot 10 \cdot 5)) \quad (\text{cosine rule})$$

$$\text{Therefore, } \angle ODL = 46.56^\circ \quad (8)$$

Putting eqn(8) in eqn(7), we get

$$y = -1.056x + c$$

Also $c=5.28$ (as it passes through $(5,0)$)

Line DO: $y = -2.18x + 5.28$ (D)

solving eqn(C) and eqn(D), we get

$$x = -1.87; y = 7.26$$

Therefore coordinates of O are $(-1.87, 7.26)$

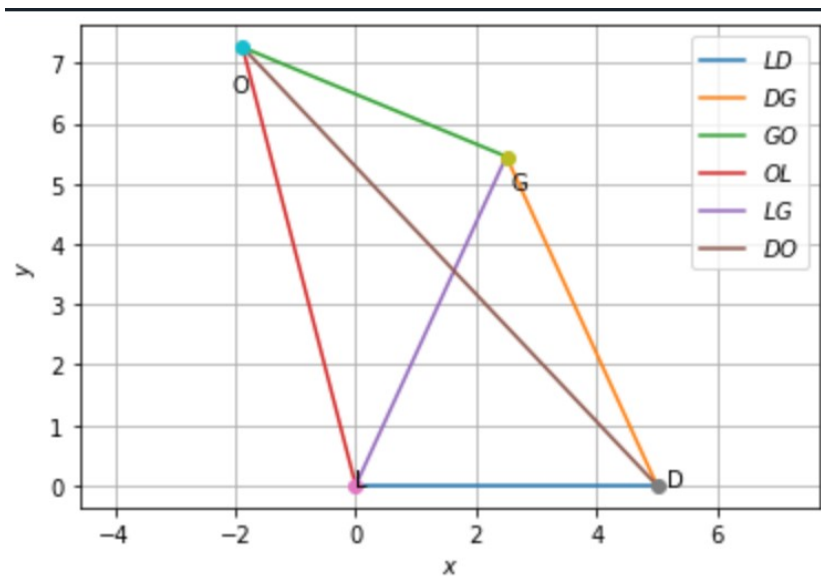


Figure 1: Figure using python

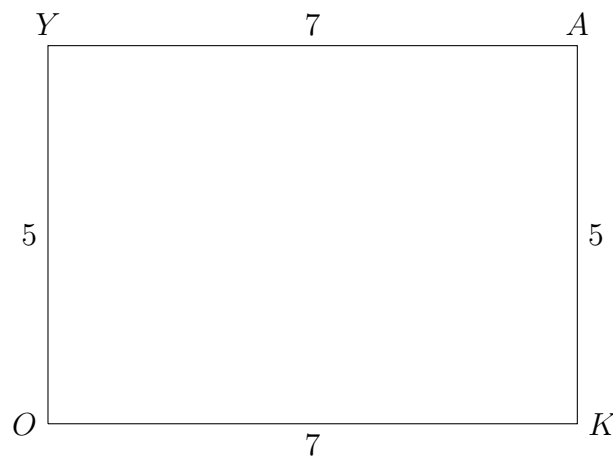
Question

Draw rectangle OKAY with $OK = 7$ and $KA = 5$.

Solution

As given figure is rectangle, therefore

$YO = 5$; $AY = 7$ (opposite sides are equal)



Rough Sketch

To draw triangle, we need coordinates of all vertices

Assuming O as origin i.e $O(0,0)$

Therefore K has coordinates as $(7,0)$ (as $OK=7$)

Also it is clear;y mentioned that given figure rectangle

Therefore A has coordinates as $(7,5)$ (as $KA=5$)

also Y has coordinates as $(0,5)$ (Figure is rectangle)

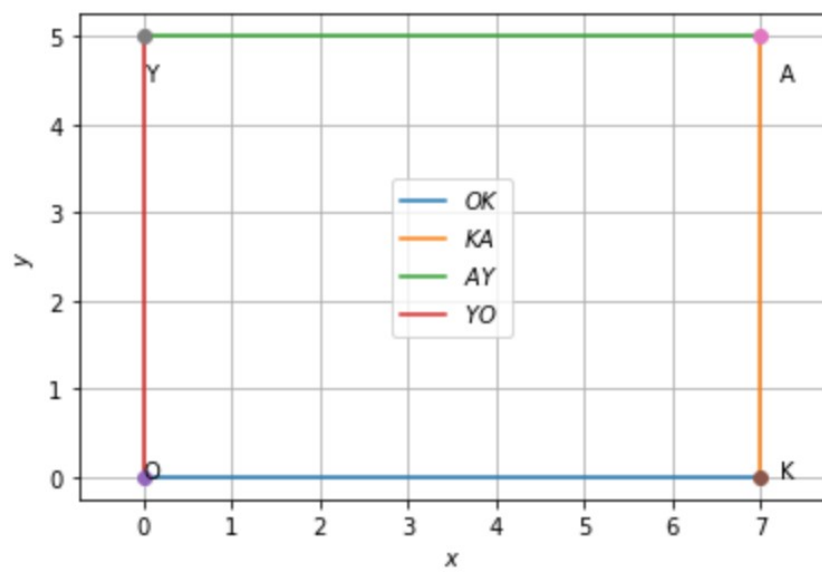


Figure 2: Figure using python