

09/06/2020

Logistic Regression

[28M]

Q. what is logistic Regression?

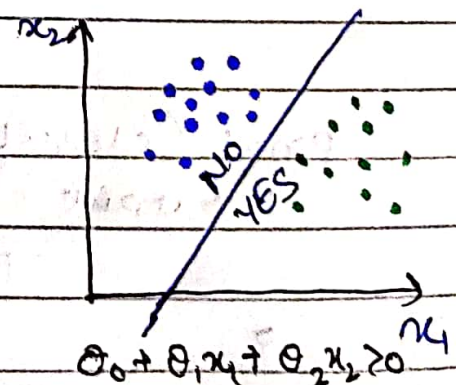
- Logistic Regression is a classification algorithm for categorical variables.

Logistic Regression Applications

- Predicting the probability of a person having heart attack.
- Predicting the mortality in injured patients.
- Predicting a customer's propensity to purchase a product or halt a subscription.
- Predicting the probability of failure of a given process or product.
- Predicting the likelihood of a homeowner defaulting on a mortgage.

when is logistic Regression suitable?

- If your data is binary
→ 0/1, YES/NO, TRUE/FALSE
- If you need Probabilistic results
- When you need a linear Decision Boundary
- If you need to understand the impact of a feature.



- Independent feature, $X \in \mathbb{R}^{m \times n}$
where, $m \rightarrow$ features
 $n \rightarrow$ records

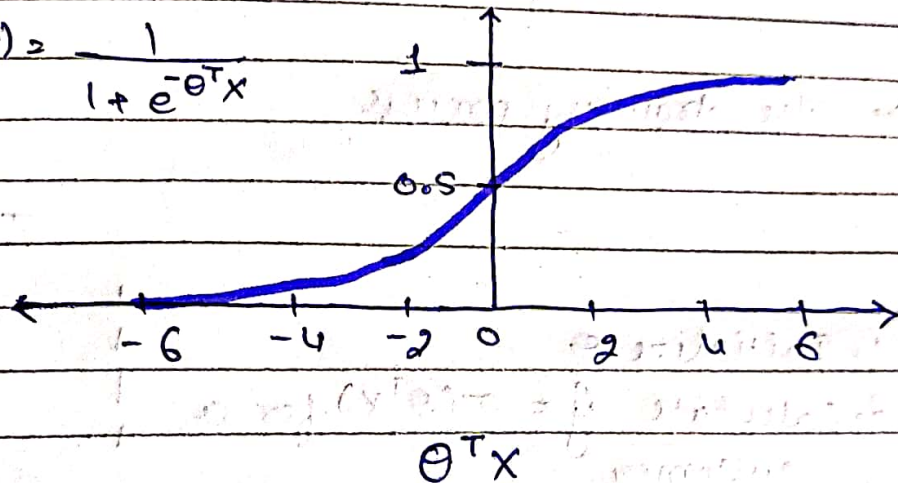
- Dependent variable, $y \in \{0, 1\}$

- $\hat{y} = P(y=1|x)$

2. Sigmoid function in Logistic Regression

- Logistic function

$$\sigma(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$



- If $\theta^T x$ is bigger than $\sigma(\theta^T x)$ will be equivalent to 1.

- If $\theta^T x$ is smaller than $\sigma(\theta^T x)$ will be equivalent to 0.

- So, the value of Sigmoid func.ⁿ will be in b/w $[0, 1]$

2. Classification of the customer churn model

- what is the o/p of our model?

$$\rightarrow P(Y=1|x)$$

$$\rightarrow P(Y=0|x) = 1 - P(Y=1|x)$$

$$\rightarrow P(\text{churn}=1 | \text{income, age}) = 0.8$$

$$\rightarrow P(\text{churn}=0 | \text{income, age}) = 1 - 0.8 = 0.2$$

$$\sigma(\theta^T x) \rightarrow P(Y=1|x)$$

$$1 - \sigma(\theta^T x) \rightarrow P(Y=0|x)$$

2. The training process

	$\sigma(\theta^T x) \rightarrow P(Y=1 x)$
	eg
1. Initialize θ	$\theta = [-1, 2]$
2. Calculate $\hat{y} = \sigma(\theta^T x)$ for a customer	$\hat{y} = \sigma([-1, 2] \times [2, 5])$ ≈ 0.7
3. Compare the output of \hat{y} with the actual o/p of customer, y , and record it as error.	Error $\approx 1 - 0.7 = 0.3$
4. Calculate the Error for all customers.	Cost = $J(\theta)$
5. Change the θ to reduce the cost.	θ_{new}
6. Go back to Step 2.	

* Logistic Regression Training

General Cost Function

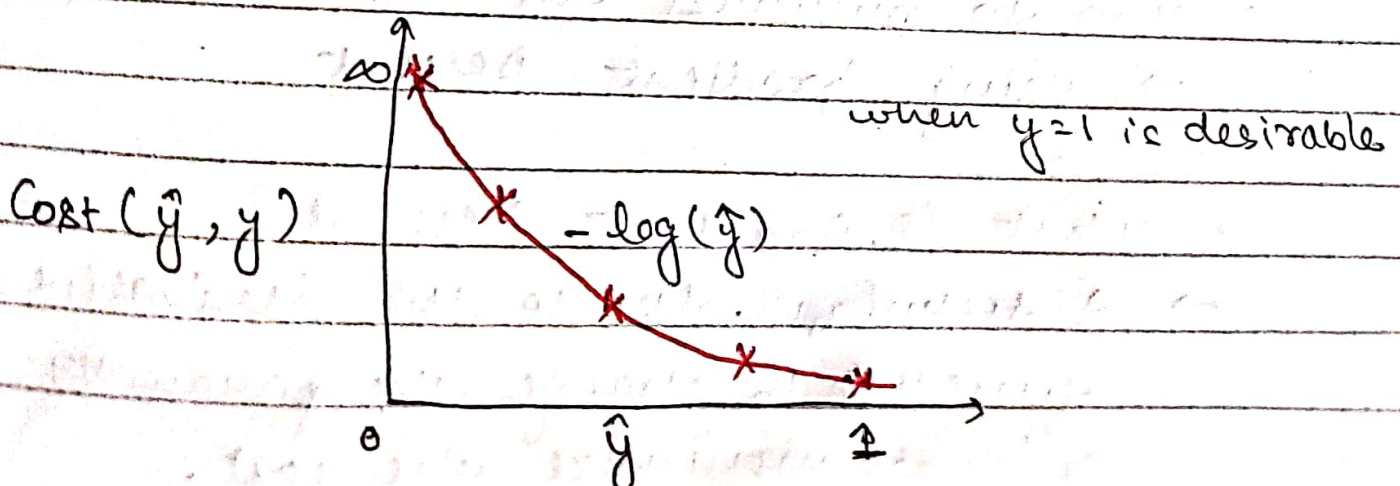
- $\sigma(\theta^T x) \rightarrow P(Y=1|x)$
- change the weight \rightarrow Reduce the cost
- Cost function

$$\text{cost}(\hat{y}, y) = \frac{1}{2} (\overset{\substack{\text{Predicted value} \\ \text{of the target}}}{\sigma(\theta^T x)} - \overset{\substack{\text{Actual value} \\ \text{of the target}}}{y})^2$$

$$J(\theta) = \frac{1}{m} \sum_{i=1}^m \text{cost}(\hat{y}_i, y_i)$$

Plotting the cost function of the model

- Model \hat{y}
- Actual value $y=1$ or 0
- If $y=1$, & $\hat{y}=1 \rightarrow \text{cost}=0$
- If $y=1$, & $\hat{y}=0 \rightarrow \text{cost}=\text{large}$



Logistic Regression Cost function

- So, we will replace cost function with:

$$\rightarrow \text{cost}(\hat{y}, y) = \frac{1}{2} (\sigma(\theta^T x) - y)^2$$

$$\Downarrow$$
$$\text{cost}(\hat{y}, y) = \begin{cases} -\log(\hat{y}) & \text{if } y=1 \\ -\log(1-\hat{y}) & \text{if } y=0 \end{cases}$$

$$\rightarrow J(\theta) = \frac{1}{n} \sum_{i=1}^n \text{cost}(\hat{y}^i, y^i)$$

$$\Downarrow$$
$$J(\theta) = -\frac{1}{n} \sum_{i=1}^n y^i \log(\hat{y}^i) + (1-y^i) \log(1-\hat{y}^i)$$

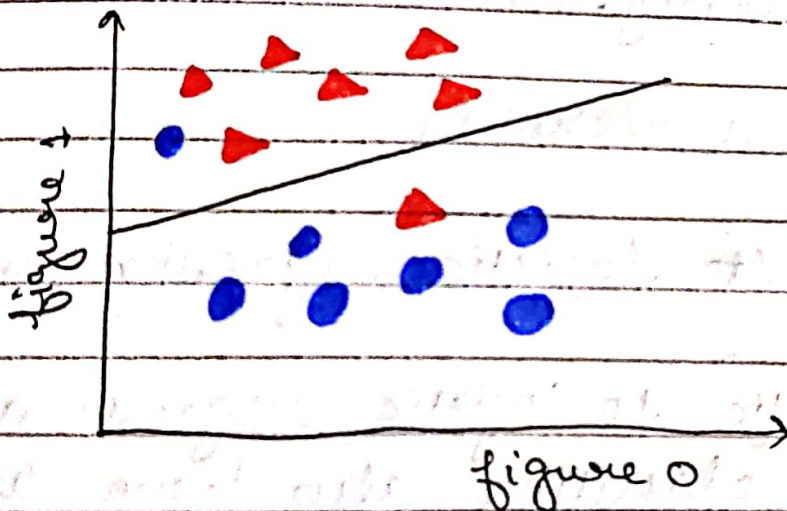
Minimizing the cost function of the model:

- How to minimize the best parameters of our model?
 \rightarrow minimize the cost function
- How to minimize the cost function?
 \rightarrow using Gradient Descent
- what is Gradient Descent?
 \rightarrow A technique to use the derivative of a cost function to change the parameter values, in order to minimize the cost.

Logistic Regression and the ROC curve [DATACAMP]

• Logistic Regression for binary classification

- Logistic Regression outputs probabilities
- If the probability 'p' is greater than 0.5:
→ The data is labelled '1'
- If the probability 'p' is less than 0.5:
→ The data is labelled '0'
- Logistic Regression helps to create Linear Decision Boundary



Logistic Regression

→ Logistic Regression in Scikit-learn

```
from sklearn.linear_model import LogisticRegression
from sklearn.model_selection import train_test_split
```

```
logreg = LogisticRegression()
```

```
X_train, X_test, y_train, y_test =  
train_test_split(X, y, test_size=0.4,  
random_state=42)
```

```
logreg.fit(X_train, y_train)  
y_pred = logreg.predict(X_test)
```

→ Probability thresholds

- By default logistic regression threshold = 0.5
- Not specific to logistic regression
→ KNN classifier also have thresholds

→ what is ROC curve? (TOWARDS DATA SCIENCE)

- Receiver Operating Characteristics curve
- ROC curve is a performance measurement for classification problem at various threshold settings.
- ROC is a probability curve.

- The ROC curve is plotted with TPR against the FPR where TPR is on y-axis & FPR is on x-axis.

where,

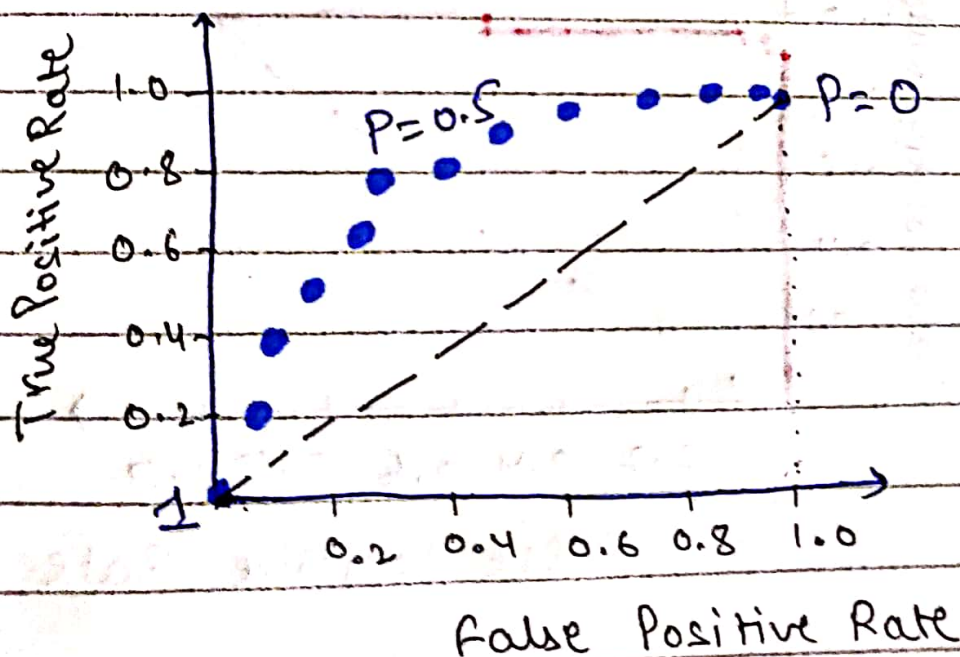
$$\hookrightarrow (\text{TPR: TRUE POSITIVE RATE}) / \text{RECALL} / \text{Sensitivity} = \frac{TP}{TP + FN}$$

$$\hookrightarrow (\text{FPR: False Positive Rate}) = 1 - \text{Specificity} = 1 - \frac{TN}{TN + FP}$$

$$\hookrightarrow \text{Specificity} = \frac{TN}{TN + FP}$$

The ROC curve

[DATACAMP]



Plotting the ROC curve

- from sklearn.metrics import roc_curve
y_pred_prob = logreg.predict_proba(X_test)[0,1]
fpr, tpr, thresholds = roc_curve(y_test,
y_pred_prob)

```
plt.plot([0,1],[0,1], 'k--')
```

```
plt.plot(fpr, tpr, label='Logistic Regression')
```

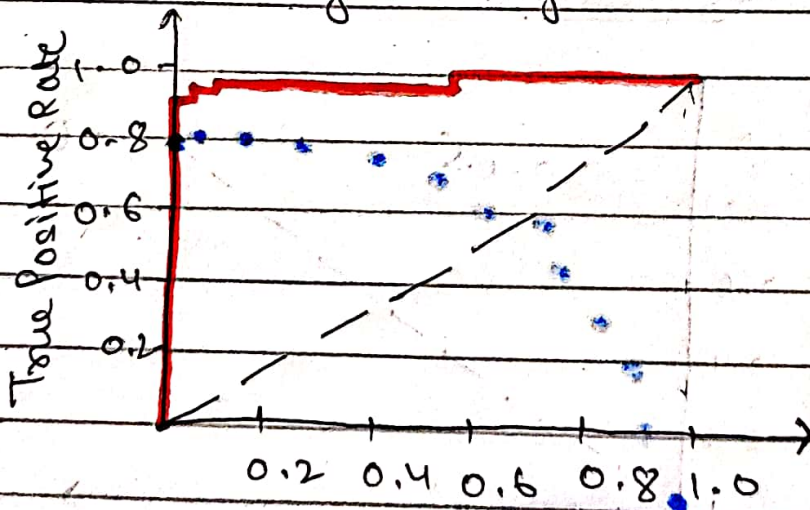
```
plt.xlabel('False Positive Rate')
```

```
plt.ylabel('True Positive Rate')
```

```
plt.title('Logistic Regression ROC curve')
```

```
plt.show()
```

Logistic Regression ROC curve



False Positive Rate