

Lesson 10: Sampling Distributions & the Central Limit Theorem:2. Probability to Statistics

→ This begins a set of lessons that will be more data oriented in the way that you are applying ideas, & less probability oriented.

→ Often we use statistics to verify conclusions of probability through simulation.

2. Sampling Distribution

→ The distribution of a statistic.

2. Notation for parameters vs statistics

Parameters

Statistic

Mean

 μ $\bar{x}, \hat{\mu}$

Standard deviation

 σ $s, \hat{\sigma}$

variance

 σ^2 $s^2, \hat{\sigma}^2$

Proportion

 π $p, \hat{\pi}$

Regression coefficient

 β $b, \hat{\beta}$

2. Two important mathematical theorems for working with sample distributions include:
1. Law of large numbers
 2. Central limit theorem.

1. Law of large numbers

→ It says that as our sample size increases, the sample mean gets closer to the population mean.

→ But how did we determine that the sample mean would estimate a population mean in the first place? How would we identify another relationship b/w parameter & statistic like this in future?

Three of the most common ways are with the following estimation techniques:

1. Maximum likelihood estimation.
2. Method of moments estimation.
3. Bayesian Estimation.

2. Central Limit Theorem

→ The central limit theorem states that with a large ~~same~~ enough samples size the sampling distribution of the mean will be normally distributed.

→ The central limit theorem actually applies for these well known statistics:

1. Sample means (\bar{x})
2. Sample proportions (p)
3. Difference in sample means ($\bar{x}_1 - \bar{x}_2$)
4. Difference in sample proportions ($p_1 - p_2$)

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2. Bootstrapping

- Bootstrapping is sampling with replacement.
- using random.choice in python actually samples in this way, where the probability of any number in our set stays the same regardless of how many times it has been chosen.

→ Flipping a coin & rolling a die are kind of like bootstrap sampling as well, as rolling a 6 in one scenario doesn't mean that 6 is less likely later.

→ Bootstrapping is used in leading machine learning algorithms:

- ↳ Random forest
- ↳ Stochastic gradient boosting

2. How to take boot sample?

bootsamp = coffee.sed.sample(200, replace=True)