

14/05/2020

LESSON 8: Python Probability Practice1. Simulating coin flips

```
→ import numpy as np
import matplotlib.pyplot as plt
% matplotlib inline
```

```
→ # outcome of one coin flip
np.random.randint(2)
↳ 0
```

```
→ # outcomes of ten thousand coin flips
np.random.randint(2, size=10000)
↳ array([0, 1, ..., 0, 0])
    0 x 10000
```

```
→ # mean outcome of ten thousand coin flips
np.random.randint(2, size=10000).mean()
↳ 0.5000
```

```
→ # outcome of one coin flip
np.random.choice([0, 1])
↳ 0
```

```
→ # outcome outcome of ten thousand coin flips
np.random.choice([0, 1], size=10000)
↳ array([1, 1, 0, 1, ..., 1, 0, 1])
    10000 x 1
```

```
→ # mean outcome of ten thousand coin flips
np.random.choice([0, 1], size=10000).mean()
↳ 0.4924
```

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→ # outcomes of ten thousand biased coin flips
np.random.choice([0,1], size=10000, p=[0.8,0.2])
→ array([0,0,...,1,0,0])

→ # mean outcomes of ten thousand biased coin flips
np.random.choice([0,1], size=10000, p=[0.8,0.2]).mean()
↳ 0.8053

→ Conditional Probability & Bayes' rule Quiz

$$P(\text{cancer}) = 0.105$$

$$P(\neg \text{cancer}) = 0.895$$

$$P(\text{Positive} | \text{cancer}) = 0.905$$

$$P(\text{Negative} | \text{cancer}) = 0.095$$

$$P(\text{Positive} | \neg \text{cancer}) = 0.204$$

$$P(\text{Negative} | \neg \text{cancer}) = 0.796$$

a) $P(\text{cancer} | \text{positive})$

$$P(\text{cancer} | \text{positive}) = \frac{P(\text{Positive} | \text{cancer}) P(\text{cancer})}{P(\text{Positive})}$$

$$P(\text{Positive}) = P(\text{cancer}) \cdot P(\text{Positive} | \text{cancer}) + P(\neg \text{cancer}) \cdot P(\text{Positive} | \neg \text{cancer})$$

$$= 0.105 \times 0.905 + 0.895 \times 0.204$$

$$= 0.277605$$

$$P(\text{cancer} | \text{positive}) = \frac{0.905 \times 0.105}{0.277605}$$

$$= 0.3422$$

b) $P(\neg \text{cancer} | \text{Positive})$

$$P(\neg \text{cancer} | \text{Positive}) = \frac{P(\neg \text{cancer}) P(\text{Positive} | \neg \text{cancer})}{P(\text{Positive})}$$

$$= \frac{0.895 \times 0.204}{0.277605}$$

$$= 0.658$$

c) $P(\text{cancer} | \text{Negative})$

$$P(\text{Negative}) = P(\text{cancer}) \times P(\text{Negative} | \text{cancer}) + P(\neg \text{cancer}) \times P(\text{Negative} | \neg \text{cancer})$$

$$= 0.105 \times 0.095 + 0.895 \times 0.796$$

$$= 0.741$$

$$P(\text{cancer} | \text{Negative}) = \frac{P(\text{Negative} | \text{cancer}) P(\text{cancer})}{P(\text{Negative})}$$

$$= \frac{0.095 \times 0.105}{0.741}$$

d) $P(\neg \text{cancer} | \text{Negative})$

$$P(\neg \text{cancer} | \text{Negative}) = \frac{P(\text{Negative} | \neg \text{cancer}) \cdot P(\neg \text{cancer})}{P(\text{Negative})}$$

$$= \frac{0.796 \times 0.895}{0.741}$$

$$= 0.961$$