- Given Z= -14MPa, Zy = 6MPa, Zxy=-17MPa

11) Solution: Methos A =

The principal stresses:

$$\begin{cases}
\overline{b_{\text{min}}} = \frac{\overline{b_{x}} + \overline{b_{y}}}{2} + \sqrt{(\underline{b_{x}} - \underline{b_{y}})^{2} + \overline{b_{xy}}} = 15.72 \text{ MPa} \\
\overline{b_{\text{min}}} = \frac{\overline{b_{x}} + \overline{b_{y}}}{2} - \sqrt{(\underline{b_{x}} - \underline{b_{y}})^{2} + \overline{b_{xy}}} = -23.72 \text{ MPa}
\end{cases}$$

The directions:

$$-\tan 2d = \frac{27xy}{5x-7y} \Rightarrow 2d = 1.04 \text{ rad} = 59.59$$

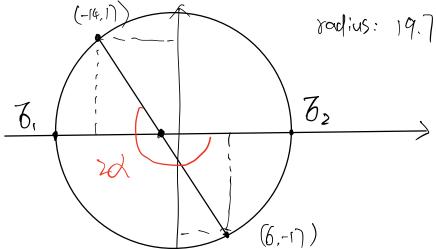
$$\Rightarrow d_1 = 29.79$$

$$\Rightarrow d_2 = 119.79$$

Methos B:

(enter: (-4 0)

radius: 19.72



The directions: As shown in the picture

(2) Solution:

$$tom > 0 = -\frac{3x - 3y}{27xy} \implies 0 = -3x - 3y$$

$$7x'y' = \pm \sqrt{\frac{3x - 3y}{2} + 7xy} = \pm \sqrt{\frac{3}{2}} =$$

$$\frac{3}{3} = \frac{3x + 3y}{2} + \frac{3x - 3y}{2} \cos 2x + \frac{3x - 3y}{2} \cos 2x + \frac{3x - 3y}{2} \cos 2x - \frac{3x - 3y}{2} \cos 2x - \frac{3x - 3y}{2} \cos 2x - \frac{3x - 3y}{2} \cos 2x + \frac$$

method B of (2) (3)?-4

=. Given a three-dimensional stress state with
$$B_x = 10 \, \text{MPa}$$
, $B_y = 20 \, \text{MPa}$, $B_z = -10 \, \text{MPa}$ $B_z = -10 \, \text{MPa}$ $B_z = -10 \, \text{MPa}$ $B_z = -10 \, \text{MPa}$

(a) Solution:

$$(05^{2}(x',x) + (05^{2}(x',y) + (05^{2}(x',z) =)$$

.. As we know cos(x', 2) is positive

$$\therefore (0)(x', 2) = \frac{1}{2}$$

$$P_{x} = \delta_{x} \cdot (o_{S}(x', x) + Zyx \cdot (o_{S}(x', y) + Z_{2x} \cdot co_{S}(x', z)) = \frac{512}{2} MP_{\alpha}$$

$$=(\frac{5/2}{2}, 10/2-5, -\frac{15/2}{2}-10)$$

(b) Solution:

$$\begin{cases} 6 = P_{x} \cdot \cos(x', x) + P_{y} \cdot \cos(x', y) + P_{z} \cdot \cos(x', z) \\ Z = P^{z} - Z^{z} \end{cases}$$

$$5 = -2.07 MPa$$

$$roso = \frac{6}{p}$$
 $|p| = \int p_x^2 + p_y^2 + p_z^2 = 22.82$

$$2. (0.50 = \frac{-2.07}{22.82} = 0.09$$

(d) Solution:

>olution:
if
$$(-\infty, (x, y')) = \frac{1}{2}$$
 and $(-\infty, (x, y'))$ is negative. We can get

$$\begin{cases} \cos^2(x,y') + \cos^2(y,y') + \cos^2(z,y') = 1 \\ \cos(x',x) \cdot \cos(x,y') + \cos(y,y') \cdot \cos(x',y) + \cos(z,y') \cdot \cos(x',z) = 0 \end{cases}$$

Express

vector form -1

x' and

(1)

So we can get
$$COS(2,y') = -\frac{5}{b}$$
 and $COS(y,y') = \frac{\sqrt{2}}{b}$

And according to the relationship between these direction cosines, then we can get $(os(x,z')=\frac{1}{2})$, $(os(y,z')=\frac{1}{2})$, $(os(y,z')=\frac{1}{2})$

then we can get
$$(0S(X,Z')=\frac{1}{2})$$
, $(0S(Y,Z')=\frac{2}{2})$, $(0S(X,Z')=-\frac{1}{6})$

$$Z_{x'y'=P_{x}}(S(x,y')+P_{y}(S(y,y')+P_{z}(OS(z,y'))=21.09 MP_{a}$$

(e) Solution:

As we know the transformational matrix

$$R = \begin{bmatrix} \cos(x,x') & \cos(x,y') & \cos(x,z') \\ \cos(x,x') & \cos(y,y') & \cos(z,y') \\ \cos(x,z') & \cos(y,z') & \cos(z,z') \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & \frac{1}{12} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{6} & -\frac{1}{6} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & -\frac{1}{6} \end{bmatrix}$$

All of the stress components acting on the x', y', 2' plane are shown as bellow:

$$R \cdot S \cdot R^T =$$

$$\begin{bmatrix} -\frac{1}{2} & \frac{1}{2} & \frac$$

$$= \begin{bmatrix} -2.07 & 21.09 & 8.46 \\ 21.09 & 12.06 & 2.93 \\ 8.44 & 2.94 & 10 \end{bmatrix}$$

(f) Solution:

We ran get the

Vie can get The
$$\begin{cases}
\lambda_1 = 30 \\
\lambda_2 = 8.25
\end{cases}$$

$$\lambda_3 = -18.25
\end{cases}$$

$$\begin{cases}
\lambda_1 = 30 \\
\lambda_2 = (-0.8)36, 0.4)92, 0.0849
\end{cases}$$

$$\begin{cases}
\lambda_1 = 30 \\
\lambda_2 = (-0.8)36, 0.4)92, 0.0849
\end{cases}$$

$$\begin{cases}
\lambda_1 = 30 \\
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\end{cases}$$

$$\begin{cases}
\lambda_1 = 30 \\
\lambda_2 = (-0.8)36, 0.4)92, 0.0849
\end{cases}$$

$$\begin{cases}
\lambda_2 = 8.25
\end{cases}$$
MPa
$$\begin{cases}
\lambda_1 = 30 \\
\lambda_2 = -18.23
\end{cases}$$
MPa
$$\begin{cases}
\lambda_2 = 8.23
\end{cases}$$
MPa

$$S_0$$
, $g_1 = 30 MPa$
 $g_2 = 8.23 MPa$
 $g_3 = -18.23 MPa$

$$\begin{cases} (0)(X_{p}, X) = 0.408) \\ (0)(X_{p}, Y) = 0.8115 \\ (0)(X_{p}, Z) = -0.4082 \\ (0)(Y_{p}, X) = -0.8131 \\ (0)(Y_{p}, Y) = 0.4792 \\ (0)(Y_{p}, Z) = 0.0849 \\ (0)(Z_{p}, X) = -0.3650 \\ (0)(Z_{p}, Z) = -0.3220 \\ (0)(Z_{p}, Z) = -0.7089 \end{cases}$$

三、(1) Solution:

$$\begin{cases} \frac{\partial \delta_{x}}{\partial x} + \frac{\partial \mathcal{I}_{yx}}{\partial y} + \frac{\partial \mathcal{I}_{zx}}{\partial z} + f_{x} = 0 \\ \frac{\partial \mathcal{I}_{xy}}{\partial x} + \frac{\partial \mathcal{I}_{y}}{\partial y} + \frac{\partial \mathcal{I}_{zy}}{\partial z} + f_{y} = 0 \\ \frac{\partial \mathcal{I}_{xz}}{\partial x} + \frac{\partial \mathcal{I}_{yz}}{\partial y} + \frac{\partial \mathcal{I}_{zz}}{\partial z} + f_{z} = 0 \end{cases}$$

we can get $\begin{cases}
6x - 6x + 0 = 0 \\
6y - 6y + 0 = 0
\end{cases}$ $\begin{vmatrix}
1 + 0 - 1 & = 0
\end{vmatrix}$

So, he can know this stress state is in equilibrium.

At point
$$(\frac{1}{2}, 1, \frac{2}{4})$$
:

we ran get
$$\begin{cases} 5x = 5 \\ 5y = 3 \\ 7x = 3 \\ 7xy = -3 \\ 7xz = 7yz = 0 \end{cases}$$

$$I_1 = 6_x + 6_y + 6_z = 7_1 + 6_s + 6_s = 9$$

$$\int_{2} = 6x \delta_{y} + 3y \delta_{z} + 3x \delta_{z} - 7x \delta_{y} - 7y \delta_{z} - 7x \delta_{z$$

$$I_{3} = 3x by b_{2} + 2xy ly_{2} l_{2}x + 2x_{2} ly_{x} l_{2}y$$

$$- 3y 2x_{2}^{2} - 3x 2y - 3z 2xy = 3i 32b_{3} = 0$$

$$S_0: \begin{cases} \overline{6}, = 3 \\ \overline{6}, = 6 \end{cases}$$

1> 2> 3-1