```
Compilation
FLAGS=-g -Wall -Wextra -Wshadow -Wno-unused-result -D_GLIBCXX_DEBUG -fsanitize=address -fsanitize=undefined
\hookrightarrow -fno-sanitize-recover
run_a run_A: clean
        @g++ A.cpp \$(FLAGS) -DJUNCO_DEBUG && ./a.out < z.in
Template
#include <bits/stdc++.h>
                                                              11 LSB(11 x) {return x & (-x);}
using namespace std;
                                                              void unset_bit(ll &x, ll i) {x = (x | (111<<i)) ^ (111<<i);}</pre>
using ll = long long;
                                                              stringstream ss;
ios::sync_with_stdio(false); cin.tie(nullptr); cout.tie(nullptr); "Hello world";
cout.precision(20); cout << fixed << ans;</pre>
                                                              while(ss >> s) cout << s << endl;</pre>
bool is_set(ll x, ll i) {return (x>>i)&1;}
                                                              ss.clear();
void set_bit(ll &x, ll i) {x |= 111<<i;}</pre>
Bitmask
// Iterate over all submasks of a mask. CONSIDER SUBMASK = 0/APABTb) = (a/b) \hat{} (a8b).
for(submask = mask; submask > 0; submask = (submask-1)&mask)/\frac{1}{4} (a+b) = (a/b) + (a&b).
                                                              //(a+b) = (a^b) + 2*(a8b).
                                                              // Two complement -x = x + 1.
// With OR and AND you can get XOR.
// (a^b) = (a/b) - (a8b).
                                                              // a^b belongs to [a-b, a+b] and [b-a, a+b].
Point
template<typename T>
                                                                      return sqrt(a*a - d*d);
class Point {
                                                                  }
    public:
                                                                  int get_quadrant() {
    static const int LEFT_TURN = 1;
                                                                       if(x > 0 && y >= 0) return 1;
    static const int RIGHT_TURN = −1;
                                                                       if(x \leq 0 && y > 0) return 2;
                                                                      if(x < 0 && y <= 0) return 3;
    T x = 0, y = 0;
    Point() = default;
                                                                      if(x >= 0 && y < 0) return 4;
    Point(T _x, T _y) {
                                                                      return 0; // Point (0, 0).
                                                                  }
        x = x;
        y = y;
                                                                   // Relative quadrant respect the point other, not the orig
                                                                  int get_relative_quadrant(Point<T> other) {
    }
    friend ostream &operator << (ostream &os, Point<T> p) {
                                                                      Point<T> p(other.x - x, other.y - y);
        os << "(" << p.x << ", " << p.y << ")";
                                                                      return p.get_quadrant();
        return os;
    }
                                                                   // Orientation of points *this -> a -> b.
    bool operator == (const Point<T> other) const {
                                                                  int get_orientation(Point<T> a, Point<T> b) {
        return x == other.x && y == other.y;
                                                                      T \text{ prod} = (a.x - x)*(b.y - a.y) - (a.y - y)*(b.x - a.x)
                                                                      if(prod == 0) return 0;
    // Get the (1^{\circ}) bottom (2^{\circ}) left point.
                                                                      return prod > 0? LEFT_TURN : RIGHT_TURN;
    bool operator < (const Point<T> other) const {
        if(y != other.y) return y < other.y;</pre>
                                                                   // True if a have less angle than b, if *this->a->b is a l
        return x < other.x;
                                                                  bool angle_cmp(Point<T> a, Point<T> b) {
    }
                                                                       if(get_relative_quadrant(a) != get_relative_quadrant(b
    T euclidean_distance(Point<T> other) {
                                                                           return get_relative_quadrant(a) < get_relative_qua
        T dx = x - other.x;
                                                                       int ori = get_orientation(a, b);
        T dy = y - other.y;
                                                                       if(ori == 0) return euclidean_distance_squared(a) < eu</pre>
        return sqrt(dx*dx + dy*dy);
                                                                      return ori == LEFT_TURN;
    T euclidean_distance_squared(Point<T> other) {
                                                                   // Anticlockwise sort starting at 1º quadrant, respect to
                                                                  void polar_sort(vector<Point<T>> &v) {
        T dx = x - other.x;
        T dy = y - other.y;
                                                                      sort(v.begin(), v.end(), [&](Point<T> a, Point<T> b)
        return dx*dx + dy*dy;
                                                                       {return angle_cmp(a, b);});
                                                                  // Convert v to its convex hull, Do a Graham Scan. O(n log
    T manhatan_distance(Point<T> other) {
        return abs(other.x - x) + abs(other.y - y);
                                                                  void convert_convex_hull(vector<Point<T>> &v) {
                                                                      if((int)v.size() < 3) return;</pre>
    // Get the height of the triangle with base b1, b2.
                                                                      Point<T> bottom_left = v[0], p2;
    T height_triangle(Point<T> b1, Point<T> b2) {
                                                                      for(auto p : v) bottom_left = min(bottom_left, p);
        if(b1 == b2 || *this == b1 || *this == b2) return 0; // It'sbottom_leftnpolar_sort(v);
        T a = euclidean_distance(b1);
                                                                      vector<Point<T>> v_input = v; v.clear();
```

for(auto p : v\_input) {

while(v.size() >= 2) {

p2 = v.back(); v.pop\_back();

T b = b1.euclidean\_distance(b2);

T c = euclidean\_distance(b2);

T d = (c\*c-b\*b-a\*a)/(2\*b);

 $\operatorname{time}(\operatorname{NULL})$ 

```
if(v.back().get\_orientation(p2, p) == LEFT\_TURN) { m = (p2.y - p1.y)/(p2.x - p1.x);}
                    v.pb(p2);
                                                                     n = m*-p1.x + p1.y;
                    break;
                                                                 friend ostream &operator << (ostream &os, Line<T> 1) {
                                                                     if(l.is_vertical) os << "x = " << l.n;
            }
                                                                     else os << "y = " << 1.m << "x + " << 1.n;
            v.pb(p);
        }
                                                                     return os;
    // Constraint: The points have to be in order p0 -> p1 -> ..PointpT} intersection(Eipe<T> p0.{
    static ld get_area_polygon(vector<Point<T>> &v) {
                                                                     if(is_vertical && l.is_vertical) return Point<T>(-inf,
        if(v.size() < 3) return 0;</pre>
                                                                     if(is_vertical) return Point<T>(n, 1.m*n + 1.n);
        11 i, sum = 0, n = v.size();
                                                                     if(l.is_vertical) return Point<T>(l.n, m*l.n + n);
        for(i = 0; i < n; i++) {
                                                                     T \text{ new_m} = (1.n-n)/(m-1.m);
            sum += v[i].x*v[(i+1)%n].y - v[(i+1)%n].x*v[i].y;
                                                                     return Point<T>(new_m, m*new_m + n);
        }
        return abs(sum)/2.0;
                                                             };
                                                             // Point of intersection of two lines formed by (p1, p2), (p3,
    }
    // Rotate p alpha radians (anti clock wise) respect to tRointold.intersection4points(Point<ld>p1, Point<ld>p2, Point</ld>
    Point<T> rotate(Point<T> p, ld alpha) {
                                                                 Line<ld> 11(p1, p2), 12(p3, p4);
        PointT> q(p.x - x, p.y - y); // p shifted.
                                                                 return 11.intersection(12);
        return Point<T>(x + q.x*cos(alpha) - q.y*sin(alpha),}
                        y + q.x*sin(alpha) + q.y*cos(alpha)) // Return random float in [0, 1].
    }
                                                             ld rand_float() {
};
                                                                 return rand()/(ld)RAND_MAX;
                                                             } // Return a point inside a triangle formed by p1, p2, p3.
template<typename T>
                                                             Point<ld> random_triangle(Point<ld> p1, Point<ld> p2, Point<ld
class Line{
   public:
                                                                 ld u1 = rand_float(), u2 = rand_float();
    bool is_vertical = false; // If vertical, line := x = n.
                                                                 if(u1 + u2 > 1) u1 = 1 - u1, u2 = 1 - u2; // rectangle ->
    T m = 0, n = 0; // y = mx + n.
                                                                 return Point<ld>(p2.x + (p1.x-p2.x)*u1 + (p3.x-p2.x)*u2,
    Line(T _m, T _n) \{m = _m; n = _n; \}
                                                                                  p2.y + (p1.y-p2.y)*u1 + (p3.y-p2.y)*u2);
    Line(Point<T> p1, Point<T> p2) {
                                                             }
        if(p1.x == p2.x) {is_vertical = true; n = p1.x; return;}
Articulation Point
// v is an AP if removing v from graph it split into more than one componentif(parent[u] != -1 && low[v] >= discover[u])
// 1- v is the root and v has > 1 child in the DFS.
                                                                             AP[u] = true;
// 2- v is not the root and has one child u that dont have any back edge.
                                                                             //if(low[v] > discover[u])
vector<vi> graph;
                                                                             // \{\} // edge u->v is a bridge.
class ArticulationPoint{
                                                                         if(v != parent[u]) low[u] =
   int n:
    vi low; // Minimum discover time using a back edge.
                                                                         min(low[u], discover[v]); // Back edge.
    vi discover; // Discover DFS time.
    vi parent;
                                                                 }
    int Time = 0;
                                                                 public:
    void dfs(int u) { // Call dfs(root).
                                                                 vector<bool> AP; // True iff i is an Articulation Point.
        if(discover[u] != -1) return;
                                                                 ArticulationPoint() {
        low[u] = discover[u] = Time++;
                                                                     n = graph.size();
        int children = 0;
                                                                     low.assign(n, -1);
        for(auto v : graph[u]) {
                                                                     discover.assign(n, -1);
            if(discover[v] == -1) {
                                                                     parent.assign(n, -1);
                children++;
                                                                     AP.assign(n, false);
                                                                 }
                parent[v] = u;
                dfs(v);
                                                                 void get_AP() {
                low[u] = min(low[u], low[v]);
                                                                     for(int i = 0; i < n; i++) {
                // Every time you set AP[u] = true, the number of component(discover[i] == -1) dfs(i);
                // removing the nodes u or v from the graph increase}
                if(parent[u] == -1 && children > 1)
                                                                 }
                AP[u] = true;
                                                             };
Cycle detection
```

tortoise = x0;

hare = f(hare);

while(tortoise != hare)

while(tortoise != hare)

hare = f(hare), lambda++;

tortoise = f(tortoise), hare = f(hare), mu++;

ll f(ll x) {

return (x + 1) % 4; // Example.

// lambda is the length of the cycle.

pll floyd\_cycle\_detection(ll x0) {

// mu is the first index of the node in the cycle.

11 tortoise = f(x0), hare = f(f(x0)), mu = 0, lambda = 1; return mp(mu, lambda);

while(tortoise != hare) tortoise = f(tortoise), hare = ff(hare));

## Toposort

if(v == p) continue;

dfs\_lvl(v, u);

```
\mathbf{a}
```

```
vector<vi> graph;
                                                                  public:
class Toposort{
                                                                  vi vSorted;
   vector<bool> visited;
                                                                  Toposort(int n) {
                                                                      visited.assign(n, false);
   void topo_rec(int u) {
        if(visited[u]) return;
                                                                      for(int i = 0; i < n; i++) topo_rec(i);</pre>
        visited[u] = true;
                                                                      reverse(vSorted.begin(), vSorted.end());
        for(auto _v : graph[u]) topo_rec(_v);
                                                                  }
                                                              };
        vSorted.pb(u);
   }
Flow Dinic
class Edge {
                                                                          if(pushed > 0) {
   public:
                                                                              edge[el].flow += pushed;
   int u, v;
                                                                              edge[el^1].flow -= pushed;
   int cap, flow = 0; // Capacity and current flow.
                                                                              return pushed;
   Edge(int _u, int _v, int _cap) : u(_u), v(_v), cap(_cap) { }
                                                                      }
// O(V^2*E). For unit edge capacity O(sqrt(V)*E).
                                                                      return 0;
                                                                  }
class Dinic{
   vector<Edge> edge;
                                                                  public:
   vector<vi> graph;
                                                                  Dinic(int _n, int _source, int _sink) :
                                                                  n(_n), source(_source), sink(_sink) {
   int n, n_edges = 0;
   int source, sink, inf_flow = INT_MAX;
                                                                      graph.assign(_n, vi());
   vi lvl; // lvl of the node to the source.
   vi ptr;
                                                                  void add_edge(int u, int v, int flow) { // Add u->v edge.
    queue<11> q;
                                                                      Edge uv(u, v, flow), vu(v, u, 0); // Not multiedge.
   bool BFS() {
                                                                      edge.pb(uv);
        while(!q.empty()) {
                                                                      edge.pb(vu);
            int u = q.front(); q.pop();
                                                                      graph[u].pb(n_edges);
            for(auto el : graph[u]) {
                                                                      graph[v].pb(n_edges+1);
                if(lvl[edge[el].v] != -1) continue;
                                                                      n_{edges} += 2;
                if(edge[el].cap - edge[el].flow <= 0) continue; }</pre>
                lvl[edge[el].v] = lvl[edge[el].u] + 1;
                                                                  int max_flow() { // It consumes the graph.
                q.push(edge[el].v);
                                                                      int flow = 0, pushed;
                                                                      while(true) {
        }
                                                                          lvl.assign(n, -1);
        return lvl[sink] != -1;
                                                                          lvl[source] = 0;
   }
                                                                          q.push(source);
    int dfs(int u, int min_flow) {
                                                                          if(!BFS()) break;
        if(u == sink) return min_flow;
                                                                          ptr.assign(n, 0);
        int pushed, el;
                                                                          while(true) {
                                                                              pushed = dfs(source, inf_flow);
        for(;ptr[u] < (int)graph[u].size(); ptr[u]++) {</pre>
        //if you can pick ok, else you crop that
                                                                              if(!pushed) break;
            el = graph[u][ptr[u]];
                                                                              flow += pushed;
            if(lvl[edge[el].v] != lvl[edge[el].u] + 1
            || edge[el].cap - edge[el].flow <= 0) {
                                                                      }
                continue;
                                                                      return flow;
                                                                  }
            pushed = dfs(edge[el].v, min(min_flow,
                                                              };
            edge[el].cap - edge[el].flow));
LCA
const int MAX_N = 1e5+5;
                                                                  }
const int MAX_LOG_N = 18;
                                                                  public:
int parent[MAX_N] [MAX_LOG_N]; // Sparse table.
                                                                  int lvl[MAX_N];
class LCA{ // LCA in O(\log n), with O(n \log n) preprocess.
                                                                  LCA() = default;
                                                                  LCA(vector<vi> &_graph) {
    vector<vi> graph;
                                                                      int i, j;
    void dfs_lvl(int u, int p) {
                                                                      graph = _graph;
        parent[u][0] = p;
                                                                      n = graph.size();
                                                                      lvl[0] = 0; // The root is 0.
        lvl[u] = lvl[p] + 1;
                                                                      dfs_lvl(0, 0); // The parent of root is root.
        for(auto v : graph[u]) {
```

for(j = 1; j < MAX\_LOG\_N; j++) {</pre>

 $for(i = 0; i < n; i++) {$ 

```
parent[i][j] = parent[parent[i][j-1]][j-1];
                                                                     }
            }
                                                                     return parent[u][0];
        }
                                                                 }
    }
                                                                 int dist(int u, int v) { // distance from u to v O(\log n).
                                                                     return lvl[u] + lvl[v] - 2*lvl[lca(u, v)];
    int lca(int u, int v) { // O(log n).
        if(lvl[u] > lvl[v]) swap(u, v);
        int i, d = lvl[v] - lvl[u];
                                                                 int get_parent(int u, int dst) { // Calculate the dst pare
        v = get_parent(v, d);
                                                                     dst = max(dst, 0);
                                                                     for(int i = 0; i < MAX_LOG_N; i++) {</pre>
        if(u == v) return u;
                                                                          if(is_set(dst, i)) u = parent[u][i];
        for(i = MAX_LOG_N - 1; i >= 0; i--) {
            if(parent[u][i] != parent[v][i]) {
                                                                     return u;
                u = parent[u][i], v = parent[v][i];
                                                                 }
                                                             };
SCC Kosaraju
                                                                 Kosaraju() {
vector<vi> graph;
class Kosaraju{ // SCC O(n). x2 times slower than Tarjan.
                                                                     int i, n = graph.size();
    vi s; // Stack.
                                                                     visited.assign(n, false);
    vector<vi> graphT;
                                                                     for(i = 0; i < n; i++)
    vector<bool> visited;
                                                                          if(!visited[i]) dfs1(i);
    void dfs1(int u) {
                                                                     graphT.assign(n, vi());
        visited[u] = true;
                                                                     for(i = 0; i < n; i++)
        for(auto v : graph[u])
                                                                         for(auto v : graph[i])
            if(!visited[v]) dfs1(v);
                                                                             graphT[v].pb(i);
                                                                     visited.assign(n, false);
        s.pb(u);
    } // Add to the current component.
                                                                     while(true) {
    void dfs2(int u) {
                                                                          while(!s.empty() && visited[s.back()])
        visited[u] = true;
                                                                          s.pop_back();
        for(auto v : graphT[u])
                                                                          if(s.empty()) break;
           if(!visited[v]) dfs2(v);
                                                                          components.pb(vi());
        components.back().pb(u);
                                                                          dfs2(s.back());
    }
                                                                     }
                                                                 }
    public:
                                                             };
    vector<vi> components;
Mod operations
11 mul(11 a, 11 b) {
    11 ans = 0, neg = (a < 0) \hat{ } (b < 0);
                                                             // ONLY USE WHEN MOD IS PRIME, ELSE USE GCD.
    a = abs(a); b = abs(b);
                                                             // a^{(mod - 1)} = 1, Euler.
                                                             11 inv(11 a) {
    while(b) {
        if(b & 1) ans = (ans + a) \% mod;
                                                                 return elevate(((a%mod) + mod)%mod, mod - 2);
        b >>= 1;
        a = (a + a) \% mod;
                                                             const int MAX = 1e5 + 10;
                                                             //inv_fact is fact^-1
                                                             11 fact[MAX], inv_fact[MAX];
    if(neg) return -ans;
                                                             void init() {
    return ans;
                                                                 int i = 0;
ll elevate(ll a, ll b) { // b >= 0.
                                                                 fact[0] = 1;
                                                                 inv_fact[0] = 1;
   11 \text{ ans} = 1;
    while(b) {
                                                                 for(i = 1; i < MAX; i++) {
                                                                     fact[i] = fact[i-1]*i;
       if (b & 1) ans = ans * a % mod;
        b >>= 1;
                                                                     fact[i] %= mod;
                                                                     inv_fact[i] = inv(fact[i]);
        a = a * a \% mod;
    }
                                                             }
    return ans;
Catalan Numbers // (2nCn)/(n+1).
Chinese Remainder
class ChineseRemainder{
                                                                          a = (a + a) modulo;
    11 mul(11 a, 11 b) {
        ll ans = 0, neg = (a < 0) ^ (b < 0);
                                                                     if(neg) return -ans;
        a = abs(a); b = abs(b);
                                                                     return ans;
```

}

ll gcdEx(ll a, ll b, ll \*x1, ll \*y1) {

while(b) {

b >>= 1;

if(b & 1) ans = (ans + a)%modulo;

```
if(a == 0) {
                                                                        g = gcdEx(m[n-1], m[n-2], &x, &y);
            *x1 = 0;
                                                                        if((c[n-1]-c[n-2])%g != 0) {n = -1; return;}
                                                                        x = c[n-1] + mul(m[n-1], mul(-x, (c[n-1]-c[n-2])/g));
            *y1 = 1;
            return b;
                                                                        c.pop_back(); m.pop_back(); n--;
        }
                                                                        c[n-1] = mod(x); m[n-1] = modulo;
                                                                    }
        11 x0, y0, g;
                                                                    public:
        g = gcdEx(b\%a, a, &x0, &y0);
        *x1 = y0 - (b/a)*x0;
                                                                    ll modulo;
        *y1 = x0;
                                                                    void insert(ll _c, ll _m) { // _m > 0.
        return g;
    }
                                                                        modulo = _m;
                                                                        m.pb(_m);
    11 mod(11 x) {
                                                                        c.pb(mod(_c));
        return ((x%modulo) + modulo)%modulo;
                                                                    }
    }
                                                                    11 solve() {
    11 n = 0:
                                                                        while(n > 1) solve_one();
    vll c, m; //x == c[i] \mod m[i], m[i] \mod m[i] not need to be coprime.
                                                                        return n <= 0? -1 : c[0];
    void solve_one() { // m[i] <= 1e9</pre>
                                                                    }
        11 x, y, g;
                                                                };
        modulo = m[n-2]*(m[n-1]/_gcd(m[n-2], m[n-1]));
Formulas
// a/b is truncate function.
                                                                // Sum_{0, n} i^3 = Sum \ of \ i^3 \ in \ [0, n] = ((n(n+1))/2)^2.
ll floor_div(ll a, ll b) {
                                                                ll formula_6(ll _n) {
    return a/b - ((a^b) < 0 && a\%b);
                                                                    11 ans = formula_1(_n);
                                                                    return ans*ans;
// Sum_{0, n} i = Sum \ of \ i \ in [0, n] = n*(n+1)/2.
ll formula_1(ll _n) {
                                                                // Sum_{0}, inf x^{i} = 1/(1-x) if abs(x) < 1, inf abs(x) >= 1.
    return _n*(_n+1)/2;
                                                                // Sum_{0, inf} i*x^i = x/(1-x)^2 if abs(x) < 1, inf abs(x) >=
                                                                ll elevate(ll a, ll b) { // b >= 0.
// Sum_{a, b} i = Sum \ of \ i \ in [a, b].
                                                                    11 \text{ ans} = 1;
11 formula_2(11 _a, 11 _b) {
                                                                    while(b) {
    return formula_1(_b) - formula_1(_a-1);
                                                                        if(b & 1) ans = ans * a;
                                                                        b >>= 1;
// Sum_{n} i/k = Sum \ of \ i/k \ (floor) \ in \ [0, n]. \ n >= 0.
                                                                        a = a * a;
11 formula_3(11 _n, 11 _k) {
                                                                    }
    ll _ans = 0, r = _n;
                                                                    return ans:
    while((r+1)%_k != 0) {_ans += r/_k; r--;}
                                                                }
    return _ans + _k*formula_1(r/_k);
                                                                // Sum_{0}, n x^{i} = Sum \ of \ x^{i} \ in [0, n] =
                                                                //(Last*Ratio - First)/(Ratio - 1). Geometric sum.
// Sum_{0, n} (x + i*d) Arithmetic sum.
                                                                11 formula_7(11 r, 11 n) {
11 formula_4(11 x, 11 d, 11 _n) {
                                                                    return (elevate(r, n + 1) - 1) / (r - 1);
    return _n*x + d*formula_1(_n);
                                                                }
                                                                // Number of digits of num in base 10.
 /\!/ Sum_{\{0, n\}} i^2 = Sum \ of \ i^2 \ in \ [0, n] = (n(n+1)(2n+1))/6.11 \ formula_8(11 \ num) \ \{ \ /\!/ floor(log10(num)) + 1. \} 
11 formula_5(11 _n) {
                                                                    return log10(num)+1;
                                                                }
    return _n*(_n+1)*(2*_n+1)/6;
Extended GCD
// a*x1 + b*y1 = g;
                                                                    11 x0, y0, g;
ll gcdEx(ll a, ll b, ll *x1, ll *y1) {
                                                                    g = gcdEx(b\%a, a, &x0, &y0);
    if(a == 0) {
                                                                    *x1 = y0 - (b/a)*x0;
        *x1 = 0;
                                                                    *y1 = x0;
                                                                    return g;
        *y1 = 1;
        return b;
```

## All inverses

}

}

```
const 11 \mod = 31;
                                                                 for(11 i = 2; i < mod; i++) {
                                                                      inverse[i] = -(mod/i)*inverse[mod%i];
ll inverse[mod];
                                                                      inverse[i] = (inverse[i]%mod + mod) % mod;
// Calculates inverse for all i < mod.
void init() {
    inverse[1] = 1;
                                                             }
```

## Linear Sieve

```
const int MAX_PRIME = 1e6+5;
                                                              }
bool num[MAX_PRIME]; // If num[i] = false => i is prime.
                                                              vll fact, nfact; // The factors of n and their exponent. n \ge 1
int num_div[MAX_PRIME]; // Number of prime divisors of i.
                                                              void factorize(int n) { // Up to MAX_PRIME*MAX_PRIME.
int min_div[MAX_PRIME]; // The smallest prime that divide i.
                                                                  11 cont, prev_p;
vector<int> prime;
                                                                  fact.clear(); nfact.clear();
void linear_sieve(){
                                                                  for(auto p : prime) {
                                                                      if(n < MAX_PRIME) break;</pre>
                                                                      if(n\%p == 0) {
    int i, j, prime_size = 0;
    min_div[1] = 1;
                                                                          fact.pb(p);
    for(i = 2; i < MAX_PRIME; ++i){</pre>
                                                                          cont = 0:
        if(num[i] == false) {prime.push_back(i); ++prime_size; num_div[i∳h±l¢(nm/pn=div[iի ≠=ip} cont++;
                                                                          nfact.pb(cont);
        for(j = 0; j < prime_size && i * prime[j] < MAX_PRIME; ++j){}</pre>
            num[i * prime[j]] = true;
                                                                  if(n >= MAX_PRIME) {
            num_div[i * prime[j]] = num_div[i] + 1;
                                                                      fact.pb(n);
            min_div[i * prime[j]] = min(min_div[i], prime[j]);
                                                                      nfact.pb(1);
            if(i % prime[j] == 0) break;
                                                                      return:
    }
                                                                  while(n != 1) { // When n < MAX_PRIME, factorization in al
                                                                      prev_p = min_div[n];
bool is_prime(ll n) {
                                                                      cont = 0;
                                                                      while(n\%prev_p == 0) n /= prev_p, cont++;
    for(auto el : prime) {
        if(n == el) return true;
                                                                      fact.pb(prev_p);
        if(n%el == 0) return false;
                                                                      nfact.pb(cont);
                                                                  }
                                                              }
    return true;
Lazy Segment Tree
template<typename T>
                                                                      build(k<<1, 1, mid);
class Node { // Only modify this class.
                                                                      build(k<<1|1, mid+1, r);
                                                                      tree[k] = NodeT>(tree[k<<1], tree[k<<1|1]);
    public:
    int l = -1, r = -1; // Interval [l, r].
                                                                      tree[k].1 = 1; tree[k].r = r;
                                                                  }
    T value = 0;
    static const T lazy_default = -inf; // Don't change.
                                                                  void update(int k, int l, int r, int ql, int qr, T x) {
    T lazy = lazy_default;
                                                                      push_lazy(k, 1, r);
    Node() = default;
                                                                      if(qr < 1 || r < ql) return;
    Node(T _value) {value = _value;}
                                                                      if(ql <= 1 && r <= qr) {
    // Merge nodes.
                                                                          tree[k].actualize_update(x);
    Node(Node<T> a, Node<T> b) {value = max(a.value, b.value);} // MFNELES &UM query.
    void actualize_update(T x) {
                                                                          int mid = (1 + r) >> 1;
        if(x == -inf) return;
                                                                          update(k<<1, 1, mid, q1, qr, x);
        if(lazy == -inf) lazy = 0;
                                                                          update(k<<1|1, mid+1, r, ql, qr, x);
        lazy += x; // (= SET update), (+= SUM update).
        value += x; // MINMAX query + (= SET update), (+= SUM updatepush_lazy(k, 1, r);
        // value = (r-l+1)*x; // SUM query + (= SET update), (+=SUM update).
    }
                                                                  Node<T> query(int k, int l, int r, int ql, int qr) {
};
                                                                      push_lazy(k, 1, r);
                                                                      if(ql <= 1 \&\& r <= qr) return tree[k];
template<typename T>
class LazySegmentTree { // Use lazy propagation.
                                                                      int mid = (1 + r) >> 1;
    vector<Node<T>> tree;
                                                                      if(qr <= mid) return query(k<<1, 1, mid, q1, qr);</pre>
    vector<T> v;
                                                                      if(mid+1 \le ql) return query(k \le 1 | 1, mid+1, r, ql, qr)
                                                                      NodeT a = query(k<<1, 1, mid, q1, qr);
                                                                      Node<T> b = query(k <<1 | 1, mid+1, r, ql, qr);
    // Value is the real value, and lazy is only for its children.
    void push_lazy(int k, int l, int r) {
                                                                      return Node<T>(a, b);
        if(1 != r) {
            tree[k<<1].actualize_update(tree[k].lazy);</pre>
                                                                  public:
            tree[k<<1|1].actualize_update(tree[k].lazy);</pre>
                                                                  LazySegmentTree() = default;
            tree[k] = Node<T>(tree[k<<1], tree[k<<1|1]);
                                                                  LazySegmentTree(vector<T> _v) {
            tree[k].1 = 1; tree[k].r = r;
                                                                      v = v;
                                                                      n = v.size();
        tree[k].lazy = tree[k].lazy_default;
                                                                      tree.assign(4*n, {});
    }
                                                                      build(1, 0, n-1);
    void build(int k, int l, int r) {
                                                                  void update(int ql, int qr, T x) { // [ql, qr].
        if(1 == r) {
            tree[k] = NodeT>(v[1]);
                                                                      if(ql > qr) swap(ql, qr);
            tree[k].1 = 1; tree[k].r = r;
                                                                      ql = max(ql, 0);
                                                                      qr = min(qr, n-1);
            return;
```

int mid = (1 + r) >> 1;

update(1, 0, n-1, ql, qr, x);

}

```
T query(int ql, int qr) { // [ql, qr].
                                                                      Node<T> ans = query(1, 0, n-1, ql, qr);
        if(ql > qr) swap(ql, qr);
                                                                      return ans.value;
                                                                  }
        ql = max(ql, 0);
                                                              };
        qr = min(qr, n-1);
Dates
// Change here and date_to_num.
                                                              // Tiny optimization, binary search the year, month and day.
ll is_leap_year(ll y) {
                                                              void num_to_date(ll num, ll &d, ll &m, ll &y) {
    // if(y\%4 \mid | (y\%100==0) \& y\%400)) return 0; // Complete leapdyeat; m=1; y=0; // The date searched is >= this date.
    if(y\%4 != 0) return 0; // Restricted leap year.
                                                                  while(date_to_num(d, m, y) <= num) y++;</pre>
    return 1;
                                                                  while(date_to_num(d, m, y) <= num) m++;</pre>
11 days_month[12] =
{31, 28, 31, 30, 31, 30, 31, 30, 31, 30, 31};
                                                                  while(date_to_num(d, m, y) <= num) d++;</pre>
11 days_month_accumulate[12] =
{31, 59, 90, 120, 151, 181, 212, 243, 273, 304, 334, 365}; }
// d 1-index, m 1-index.
                                                              void cin_date(ll &d, ll &m, ll &y) {
11 date_to_num(ll d, ll m, ll y) {
                                                                  char c;
    11 sum = d;
                                                                  cin >> d >> c >> m >> c >> y;
                                                              }
    m = 2;
    if(m >= 1) sum += is_leap_year(y);
                                                              void cout_date(ll &d, ll &m, ll &y) {
                                                                      if(d < 10) cout << "0";
    if(m >= 0) sum += days_month_accumulate[m];
                                                                      cout << d << "/";
                                                                      if(m < 10) cout << "0";
    if(y >= 0) {
                                                                      cout << m << "/";
        sum += 365*y;
        // sum += y/4 -y/100 + y/400; // Complete leap year.
                                                                      if(y < 10) cout << "000";
        sum += y/4; // Restricted leap year.
                                                                      else if(y < 100) cout << "00";
                                                                      else if(y < 1000) cout << "0";
    return sum;
                                                                      cout << y;</pre>
                                                              }
Time
// Read the hour. scanf("%d:%d:%d", &h, &m, &s);
                                                                  sec %= 86400; sec += 86400; sec %= 86400;
void cin_hour(ll &h, ll &m, ll &s) {
                                                                  h = sec / (60*60);
    char c; // Dummy for read ':'.
                                                                  sec %= 60*60;
    cin >> h >> c >> m >> c >> s;
                                                                  m = sec / 60;
                                                                  sec %= 60;
// Prints the hour. printf("%02d:%02d:%02d", h, m, s);
                                                                  s = sec;
void cout_hour(ll h, ll m, ll s) {
    h \% = 24; h += 24; h \% = 24;
                                                              // Convert grades of the clock hand to hours and minutes. gh i
    m \% = 60; m += 60; m \% = 60;
                                                              // return mp(-1, -1) if no solution exists.
    s %= 60; s += 60; s %= 60;
                                                              pair<11, 11> grades_to_hour(1d gh, 1d gm) {
   if(h < 10) cout << "0";
                                                                  11 h = gh/30, m = gm/6;
    cout << h << ":";
                                                                  if((1d)30*h + (1d)m/2 != gh || (1d)6*m != gm) return mp(-1)
    if(m < 10) cout << "0";
                                                                  return mp(h, m);
    cout << m << ":";
    if(s < 10) cout << "0";
                                                              // Convert hours and minutes to grades of the clock hand, mp(g
    cout << s;</pre>
                                                              pair<ld, ld> hour_to_grades(ll h, ll m) {
                                                                  return mp((1d)30*h + (1d)m/2, (1d)6*m);
// One day has 60*60*24 = 86400 seconds.
// Converts the hour to number of seconds since 00:00:00.
                                                              // Convert hours and minutes to grades of the clock hand, mp(g
ll hours_to_seconds(ll h, ll m, ll s) {
                                                              // Not tested.
    return 60*60*h + 60*m + s;
                                                              pair<ld, pair<ld, ld>> hour_to_grades(ll h, ll m, ll s) {
                                                                  return mp((1d)30*h + (1d)m/2 + (1d)s/120,
// From sec seconds, get the hour. Just's for one day.
                                                                  mp((1d)6*m + (1d)s/10, (1d)6*s));
void seconds_to_hours(ll &h, ll &m, ll &s, ll sec) {
Knapsack
const int MAX_KNAPSACK = 2000005;
                                                                  for(i = 0; i < n; i++) v[i].se /= g;
11 dp[MAX_KNAPSACK]; // dp[i] is maximum value can get with i wemak\underline{t}knapsack /= g;
vector<pll> v; // (value, weight).
                                                                  for(i = 1; i \le \max_{k=1}^{n} \max_{i \in \mathbb{N}} dp[i] = -\inf;
// Return max value with weight <= max_knapsack. O(n*max_knapsacdp[0] = 0;
```

for(i = 0; i < n; i++) {

for(j = max\_knapsack;  $j \ge 0$ ; j--) {

dp[j + v[i].se] =

if(dp[j] != -inf && j+v[i].se < MAX\_KNAPSACK)</pre>

max(dp[j + v[i].se], dp[j] + v[i].fi);

}

// If can repeat elements, iterate O->max\_knapsack.

for(i = 1; i < n; i++)  $g = \_gcd(g, v[i].se);$ 

11 knapsack(int max\_knapsack) {

int i, j, n = v.size(); 11 ans = 0, g = v[0].se;

```
}
                                                                 return ans;
    }
    for(i = max_knapsack; i >= 0; i--) ans = max(ans, dp[i]);
LIS
vll LIS(vll &v) { // Is >=, but can be transformed to fit >.
                                                                     lis[pos] = v[i];
    int i, t, n = v.size();
                                                                     lis_t[i] = pos+1;
                                                                  }
    if(n == 0) return vll();
    vll lis, lis_t(n), ans;
                                                                 for(i = n-1, t = lis.size(); i >= 0; i--) {
    lis.pb(v[0]); lis_t[0] = 1;
                                                                      if(lis_t[i] == t \&\& (ans.empty() || v[i] <= ans.back()
                                                                          ans.pb(v[i]), t--; //v[i] < ans.back() for >.
    for(i = 1; i < n; i++) {
        // if(v[i] == lis.back()) continue; // For >.
                                                                 }
        if(v[i] >= lis.back())
                                                                 reverse(ans.begin(), ans.end());
            {lis.pb(v[i]); lis_t[i] = lis.size(); continue;}
                                                                 return ans:
        int pos = upper_bound(lis.begin(), lis.end(), v[i]) } lis.begin();
        // if(pos > 0) & lis[pos - 1] == v[i]) continue; // For >.
DSU
class DSU {
                                                                     for(int i = 0; i < n; ++i) parent[i] = i;</pre>
                                                                 }
    int n;
                                                                 bool is_connected(int a, int b){
    vi parent;
                                                                     return find_parent(a) == find_parent(b);
    vi rank;
    vi sz; // Size of the component.
    int find_parent(int a){
                                                                  void merge(int a, int b){
        if(parent[a] == a) return a;
                                                                     a = find_parent(a);
                                                                     b = find_parent(b);
        return parent[a] = find_parent(parent[a]);
    }
                                                                     if(a == b) return;
    public:
                                                                     number_components--;
    int number_components;
                                                                      if(rank[a] > rank[b]) parent[b] = a, sz[a] += sz[b];
    DSU() = default;
                                                                     else if(rank[a] < rank[b]) parent[a] = b,</pre>
    DSU(int _n) {
                                                                     sz[b] += sz[a];
                                                                     else {parent[a] = b; rank[b]++, sz[b] += sz[a];}
        n = _n;
        number_components = n;
                                                                  int size(int a) {return sz[find_parent(a)];}
        parent.assign(n, 0);
                                                             };
        rank.assign(n, 0);
        sz.assign(n, 1);
Unordered Set
// Use unordered_set<pii, pair_hash> us or unordered_map<pii, int, pair_hash> um;
struct pair_hash
    template <class T1, class T2>
    size_t operator () (pair<T1, T2> const &pair) const
        size_t h1 = hash<T1>()(pair.first);
        size_t h2 = hash<T2>()(pair.second);
        return (h1 ^ 0b11001001011001101) + (0b011001010011100111 ^ h2);
};
HashString
// https://www.browserling.com/tools/prime-numbers.
                                                                     while(_b){
// s = a[i], hash = a[0] + b*a[1] + b^2*a[2] + b^n*a[n].
                                                                          if(_b & 1) ans = ans*a % mod;
class HashString {
                                                                          _b >>= 1;
    char initial = '0'; // change initial for range. 'a', 'A', '0'.
                                                                          a = a*a \% mod;
    public:
    string s;
                                                                     return ans;
    int n, n_p;
                                                                 }
    vector<vll> v; // contain the hash for [0..i].
                                                                  // a^{(mod - 1)} = 1, Euler.
    vll p = \{16532849, 91638611, 83157709\};
                                                                 11 inv(int i, int j){
    // prime numbers. // 15635513 77781229
                                                                      if(b_inv[i][j] != -1) return b_inv[i][j];
    vll base = {37, 47, 53}; // base numbers: primes that > alphabetreturn b/infs[&B[j] = elevate(b[i][j], p[i] - 2, p[i]);
    vector<vll> b; // b[i][j] = (b_i \hat{j}) \% p_i.
    vector<vll> b_inv; // b_inv[i][j] = (b_i^j)^{-1} \% p_i.
                                                                 HashString() = default;
```

11 elevate(11 a, 11 \_b, 11 mod){

ll ans = 1;

 ${\tt HashString(string \&\_s) ~\{~//~Not~empty~strings.}$ 

if(1 > 0) ans -= v[i][1-1];

```
n_p = (int)p.size();
                                                                       ans *= inv(i, 1);
       v.assign(n_p, vll(n, 0));
                                                                       ans = ((ans\%p[i])+p[i])\%p[i];
       b.assign(n_p, vll(n, 0));
                                                                       vans.pb(ans);
                                                                   }
       b_inv.assign(n_p, vll(n, -1));
       int i, j;
                                                                   return vans;
       for(i = 0; i < n_p; i++) {
                                                               }
           b[i][0] = 1;
                                                               // 0(1).
           for(j = 1; j < n; j++) {
                                                               bool operator == (HashString other) {
               b[i][j] = (b[i][j-1]*base[i]) % p[i];
                                                                   if(n != other.n) return false;
                                                                   return getHash(0, n-1) == other.getHash(0, n-1);
           v[i][0] = s[0]-initial+1;
                                                               }
           for(j = 1; j < n; j++) {
                                                               // return the index of the Longest Comon Prefix, -1 if no
               v[i][j]
                                                               // O(\log n).
                (b[i][j]*(s[j]-initial+1) + v[i][j-1]) % p[i]; int LCP(HashString other) {
           }
                                                                   int l = 0, r = min(n, other.n), mid;
       }
                                                                   if(s[0]!= other.s[0]) return -1;
   }
                                                                   if(*this == other) return n-1;
   void add(char c) { // Need something previously added.
                                                                   while(1 + 1 < r) {
                                                                       mid = (1 + r) >> 1;
       int i;
                                                                       if(getHash(0, mid) == other.getHash(0, mid)) 1 = m
       s += c;
       n++;
                                                                   }
       for(i = 0; i < n_p; i++) {
           b[i].pb((b[i][n-2]*base[i]) % p[i]);
                                                                   return 1;
           b_{inv}[i].pb(-1);
           }
                                                                   int id = LCP(other);
   }
                                                                   if(id == -1) return s[0] < other.s[0];</pre>
   void add(string &_s) {
                                                                   if(*this == other) return false;
       for(auto c : _s) add(c);
                                                                   if(id == n) return true; // "ho" < "hol"</pre>
                                                                   if(id == other.n) return false;
   vll getHash(int 1, int r) {
       ll i, ans;
                                                                   return s[id+1] < other.s[id+1];</pre>
                                                               }
       vll vans;
                                                           };
       for(i = 0; i < n_p; i++) {
           ans = v[i][r];
Z algorithm
// Search the ocurrences of t (pattern to search) in s (the text).
// \mathcal{O}(n+m). It increases R at most 2n times and decreases at most n times.
// z[i] is the longest string s[i..i+z[i]-1] that is a prefix = s[0..z[i]-1].
void z_algorithm(string &s, string &t) {
   s = t + "$" + s; // "£" is a char not present in s nor t.
   int n = s.length(), m = t.length(), i, L = 0, R = 0;
   vi z(n, 0);
   // s[L..R] = s[0..R-L], [L, R] is the current window.
   for(i = 1; i < n; i++) {
       if(i > R) { // Old window, recalculate.
           L = R = i;
           while (R < n \&\& s[R] == s[R-L]) R++;
           z[i] = R - L + 1;
       } else {
           if(z[i-L] < R - i) z[i] = z[i-L]; // z[i] will fall in the window.
           else { // z[i] can fall outside the window, try to increase the window.
               while (R < n \&\& s[R] == s[R-L]) R++;
               z[i] = R - L + 1;
           }
       }
       if(z[i] == m) { // Match found.}
           //echo("Pattern found at: ", i-m-1);
```

## Longest Palindromic Substring

}

}

n = \_s.length();

```
// LPS Longest Palindromic Substring, O(n).
void Manacher(string &str) {
```

```
char ch = '#'; // '#' a char not contained in str.
   string s(1, ch), ans;
   for(auto c : str) \{s += c; s += ch;\}
   int i, n = s.length(), c = 0, r = 0;
   vi lps(n, 0);
    for(i = 1; i < n; i++) {
        // lps[i] >= it's mirror, but falling in the interval [L..R]. L = c - (R - c).
        if(i < r) lps[i] = min(r - i, lps[c - (i - c)]);
        // Try to increase.
        while(i-lps[i]-1) >= 0 \&\& i+lps[i]+1 < n \&\& s[i-lps[i]-1] == s[i+lps[i]+1]) lps[i]++;
        // Update the interval [L..R].
        if(i + lps[i] > r) c = i, r = i + lps[i];
   }
    // Get the longest palindrome in ans.
   int pos = max_element(lps.begin(), lps.end()) - lps.begin();
   for(i = pos - lps[pos]; i <= pos + lps[pos]; i++) {</pre>
        if(s[i] != ch) ans += s[i];
    //cout << ans.size() << "\n";
2 SAT
vector<vi> graph;
                                                                          for(auto u : kosaraju.components[i])
                                                                          el2component[u] = i;
class SAT{ // 2SAT, (xi \ or \ xj) and () \dots \ O(n).
   public:
                                                                      for(i = 0; i < n; i += 2)
   SAT(int n) {
                                                                          if(el2component[i] == el2component[i + 1])
        graph.assign(2*n, vi());
                                                                          return false;
                                                                      vector<vi> graph2 = graph;
    int get_pos(int i) {return 2*i;}
                                                                      graph.assign(n_component, vi());
    int get_neg(int i) {return 2*i + 1;}
                                                                      for(i = 0; i < n; i++)
    void add_or(int i, int j) { // Use it with get_pos.
                                                                          for(auto u : graph2[i])
                                                                          if(el2component[i] != el2component[u])
        graph[i^1].pb(j);
        graph[j^1].pb(i);
                                                                              graph[el2component[i]].pb(el2component[u]);
   }
                                                                      Toposort toposort(n_component);
   void add_value(int i, int val) { // x[i] = val;
                                                                      x.assign(n/2, false);
        if(val) add_or(get_pos(i), get_pos(i));
                                                                      vi component_order(n_component, 0);
        else add_or(get_neg(i), get_neg(i));
                                                                      for(i = 0; i < n_component; i++)</pre>
   }
                                                                          component_order[toposort.vSorted[i]] = i;
    vector<bool> x; // Can add (xi or xi) if you know xi = true.
                                                                      for(i = 0; i < n; i += 2)
   bool solve() {
                                                                          x[i/2] = component_order[el2component[i]]
        Kosaraju kosaraju;
                                                                          > component_order[el2component[i + 1]];
        int i, n = graph.size(), n_component = kosaraju.components.size()n true;
        vi el2component(n, 0);
        for(i = 0; i < n_component; i++)</pre>
                                                              }:
Python Template
from decimal import Decimal, getcontext
                                                                   x = input() # until EOF.
import math, sys
                                                              #
                                                                   if len(x) == 0:
input = sys.stdin.readline
                                                              #
                                                                       exit(0)
# getcontext().prec = 3 # 3 de precision, trunca el resto. # except:
\# n = Decimal(1) / Decimal(3)
                                                                  exit(0)
                                                              \# v = [k \text{ for } k \text{ in } map(int, s.split(' '))]
# try:
vector<vector<pll>>> graph; // Dijkstra
                                                                      if(dist[u.se] != inf) continue;
// Return the vector of minimum distance between s to all other n nodist[unse] eanu.fiirecheable.
//u = (cost, next node), graph[u] = vector of (next node, cost). for(auto el : graph[u.se]) {
vll dijkstra(ll s) {
                                                                          if(dist[el.fi] != inf) continue;
   priority_queue<pll, vector<pll>, greater<pll>> p;
                                                                          p.push(mp(u.fi + el.se, el.fi));
                                                                      }
   vll dist(graph.size(), inf);
   pll u;
                                                                  }
   p.push(mp(0, s));
                                                                  return dist;
    while(p.empty() == false) {
                                                             }
```

u = p.top(); p.pop();