

Deep Learning

Content

- Vanishing Gradient & Activation Functions
- Dropout
- Batch Normalization

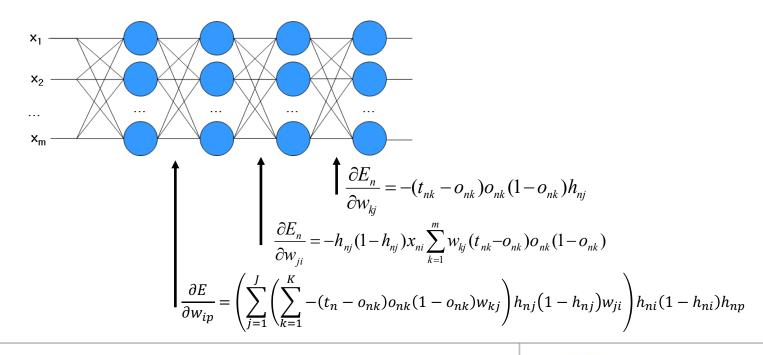


Gradient Vanishing & Activation Functions

Gradient Vanishing & Exploding

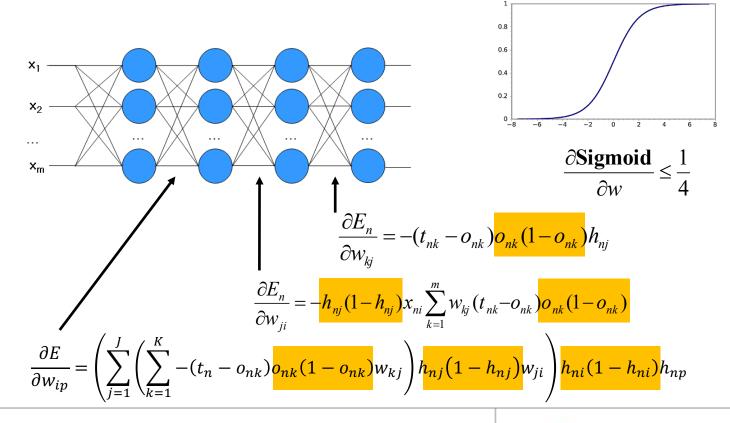
Gradient is easy to vanish or explode

- To many terms are multiplied.
- If some are small numbers, gradient becomes very small.
- If some are large numbers, gradient becomes very large.



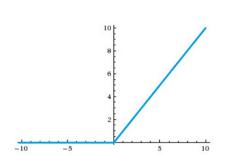
Vanishing Gradient

The major terms are the derivatives of the activation function

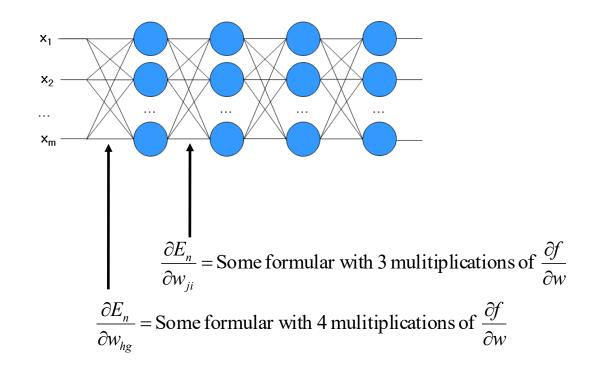


Using another functions instead of sigmoid

Rectified Linear Unit (ReLU)



$$f(x) = \begin{cases} x & \text{if } x > 0\\ 0 & \text{otherwise} \end{cases}$$



Advantage

- No vanishing gradient problems.
 - Deep networks can be trained without pre-training
- Sparse activation
 - In a randomly initialized network, only about 50% of hidden units are activated
- Fast computation:
 - 6 times faster than sigmoid function

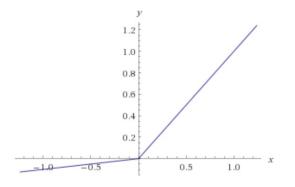
Disadvantage

Knockout Problem

You may use another

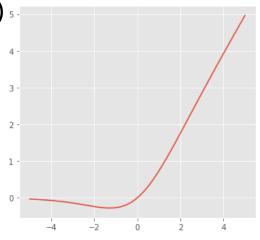
Leaky ReLU

$$f(x) = \begin{cases} x & \text{if } x > 0\\ 0.01x & \text{otherwise} \end{cases}$$

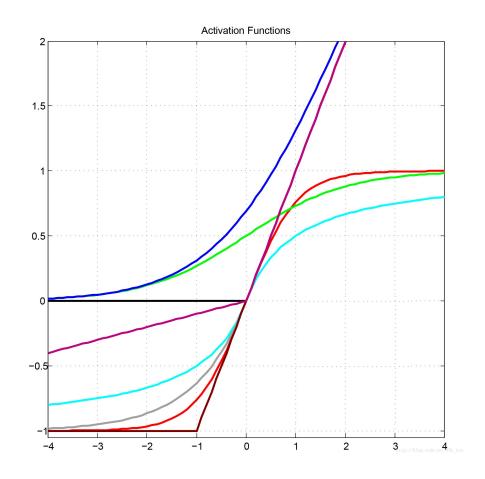


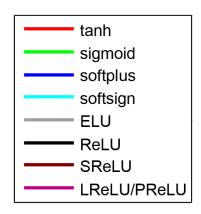
Swish (or SiLU-Sigmoid Linear Unit)

$$f(x) = \frac{x}{1 + e^{-x}}$$



Other Activation Functions



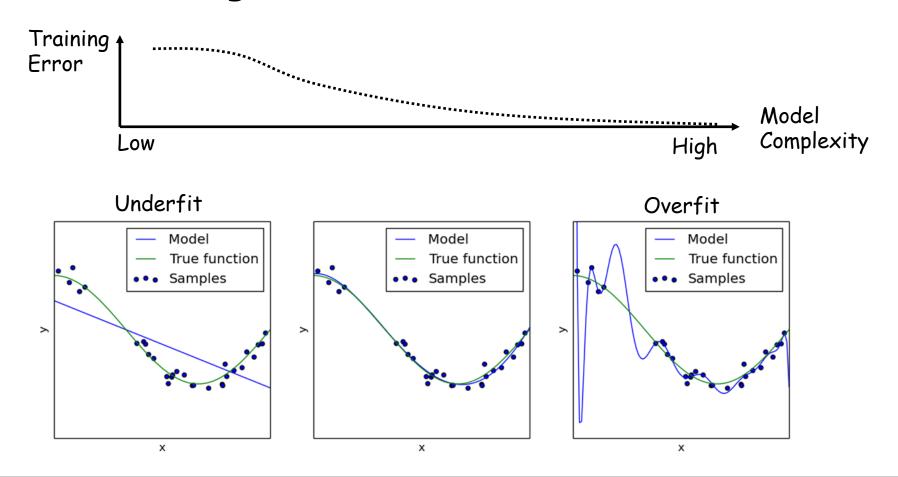




Regularization

Overfitting

Overfitting



Regularization

What is Regularization

Introducing additional information to prevent over-fitting

Approaches

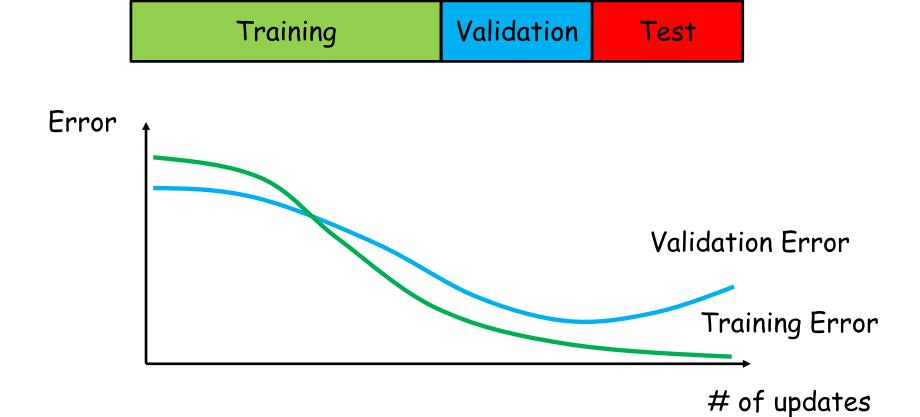
Proper Learning: Early stopping

Proper Structure: Weight decay, Dropout,

DropConnect, Stochastic pooling

Early Stopping

Split data into 3 groups



L1 Regularization

- Leading most weights very close to zero
- Choosing a small subset of most important inputs
- Resistant to noise in the inputs.

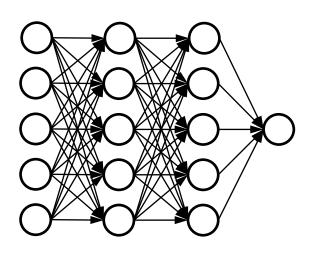
$$\widetilde{E}(\mathbf{w}) = E(\mathbf{w}) + \frac{\lambda}{2} |\mathbf{w}|$$

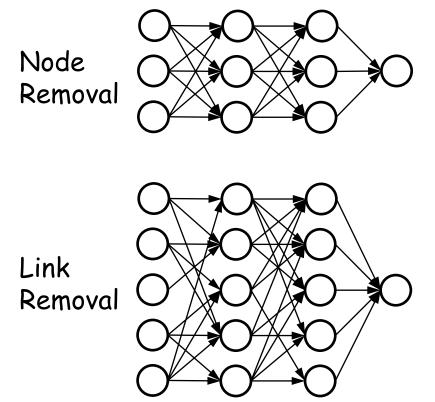
L2 Regularization

- Penalizing peaky weights
- Encouraging to use all of its inputs a little rather than using only some of its inputs a lot.

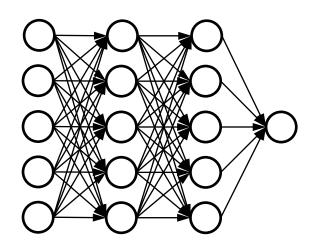
$$\widetilde{E}(\mathbf{w}) = E(\mathbf{w}) + \frac{\lambda}{2} \mathbf{w}^T \mathbf{w}$$

Complex Structure vs Simple Structure

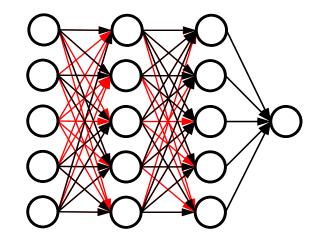




Complex Structure vs Simple Structure



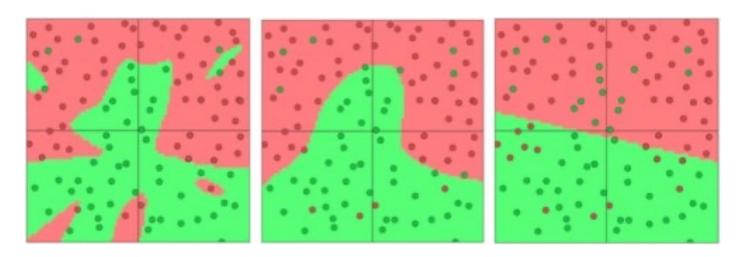
Set many links to zero



|w| is large <-> NN is Complex

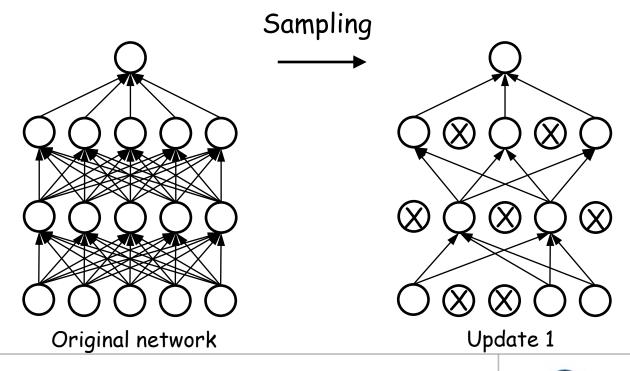
|w| is small \leftarrow NN is Simple

Example: Separating green and red

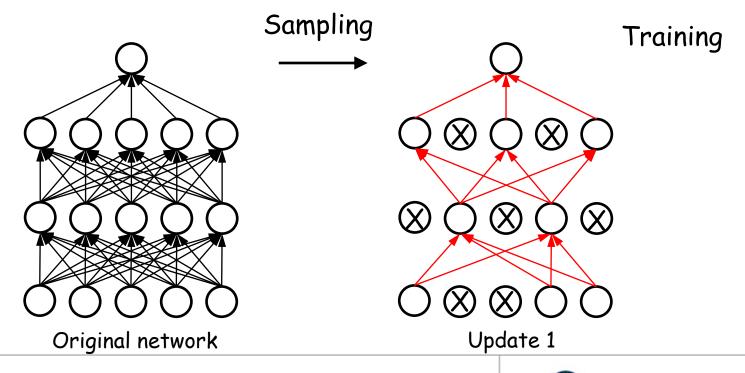


L2 regularization strengths of 0.01, 0.1, and 1

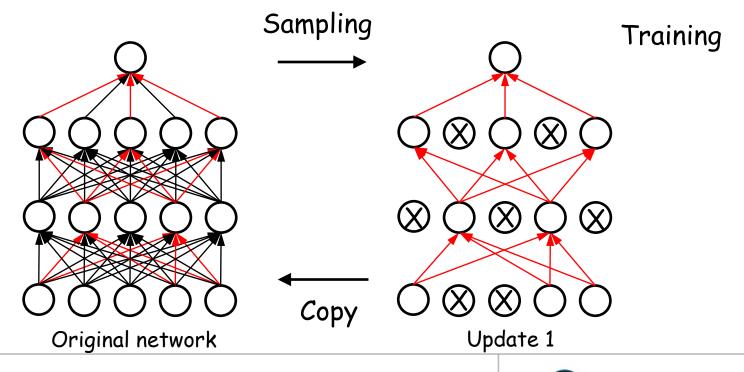
- How can we reduce the structural complexity without removing nodes?
 - Hmm??



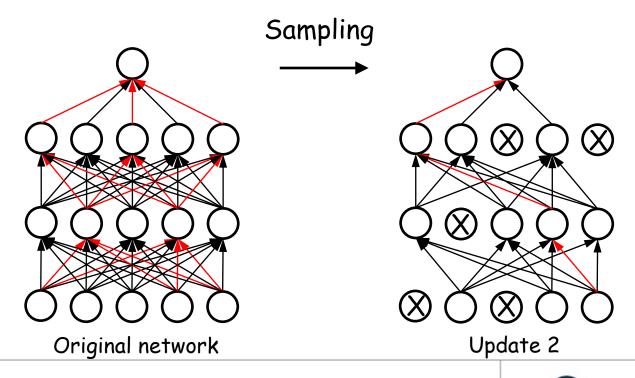
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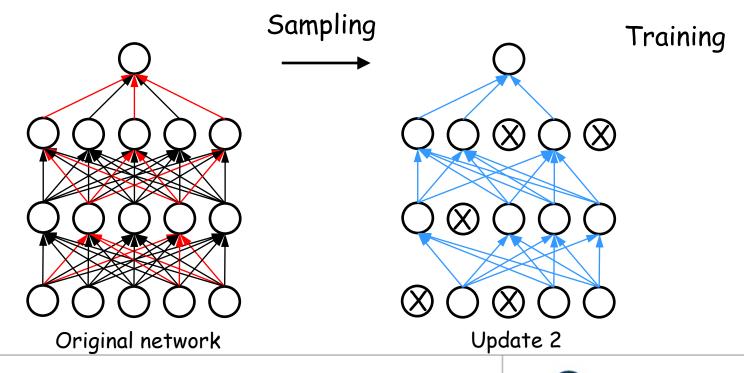
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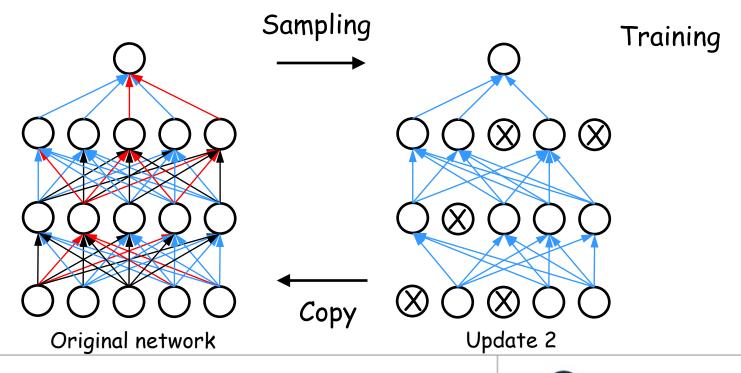
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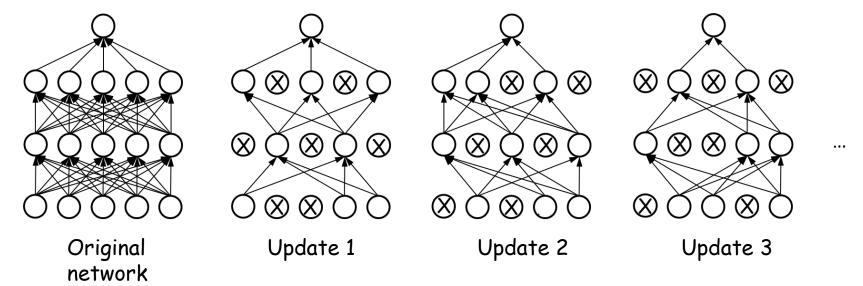


- How can we reduce the structural complexity without removing nodes?
 - Hmm??



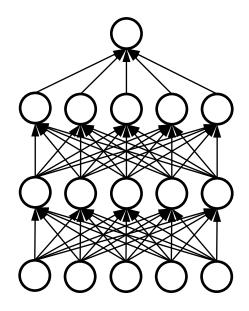
Do this at every epoch

- Randomly choose nodes with a probability of p
 - Usually p = 0.5
- Train the simplified neural network
 - At every epoch, we train different neural network which share connection weight each other



Testing

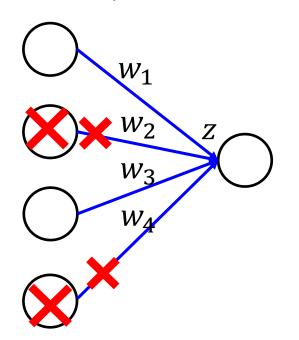
Use all the nodes without dropout



Testing

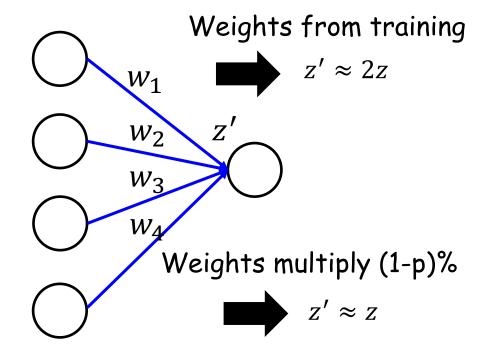
Training of Dropout

Assume dropout rate is 50%



Testing of Dropout

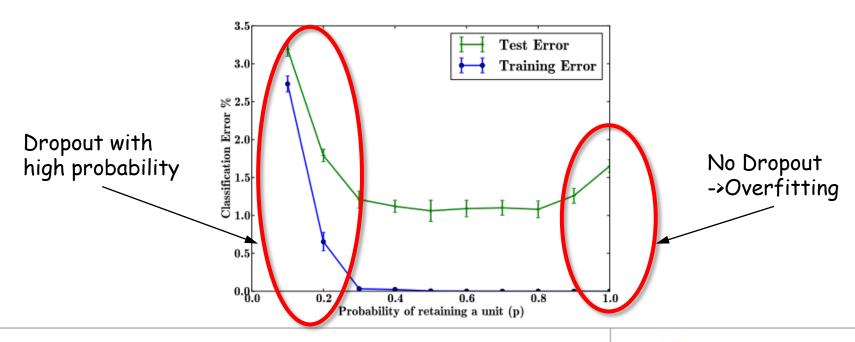
No dropout





The effect of the dropout rate p:

- An architecture of 784-2048-2048-2048-10 is used on the MNIST dataset.
- The dropout rate p is changed from small numbers (most units are dropped out) to 1.0 (no dropout).



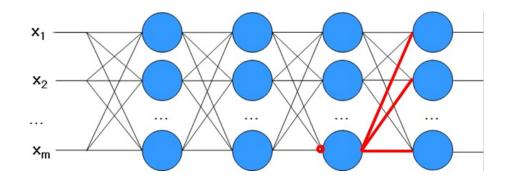
Summary

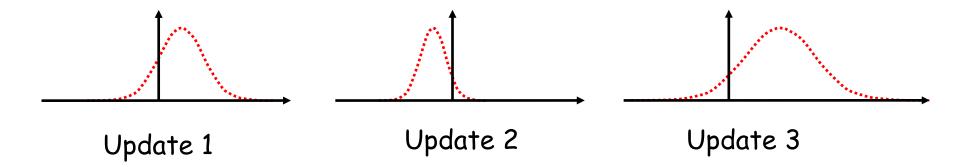
- Dropout is a very good and fast regularization method.
- Dropout is a bit slow to train (2-3 times slower than without dropout).
- If the amount of data is average-large dropout excels.
 When data is big enough, dropout does not help much.
- Dropout achieves better results than former used regularization methods (Weight Decay).



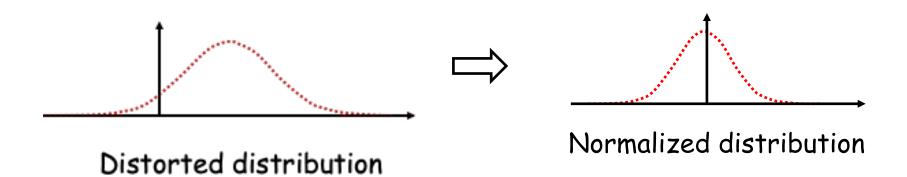
Distribution Shift

Output distribution of the red node

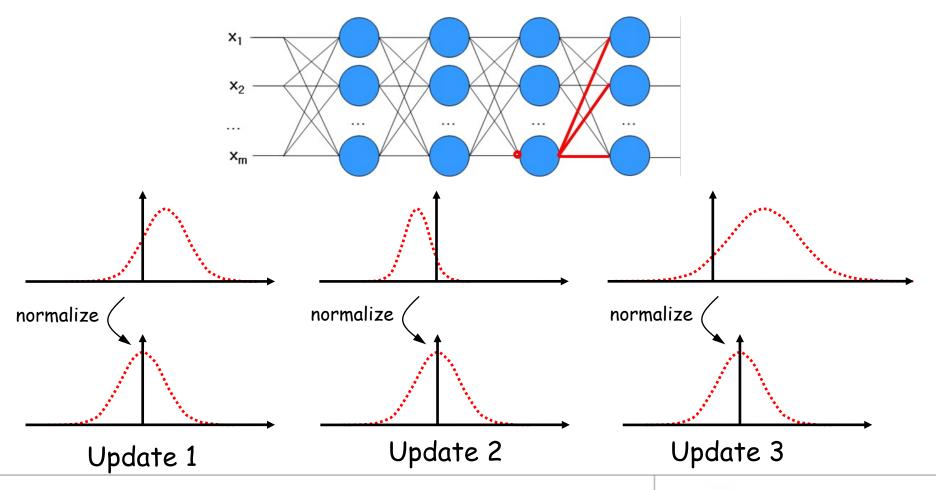


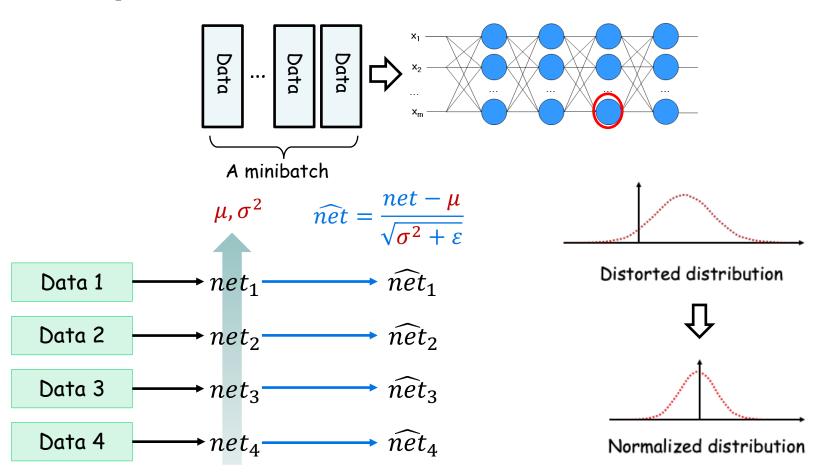


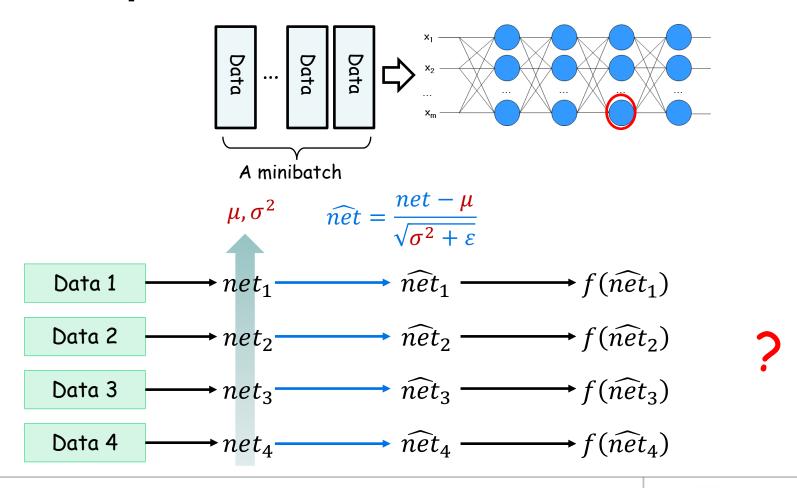
- Distribution Shift
 - It disturbs the learning process,
 - Learning is getting slow down
- Why don't we normalize the distribution of inputs

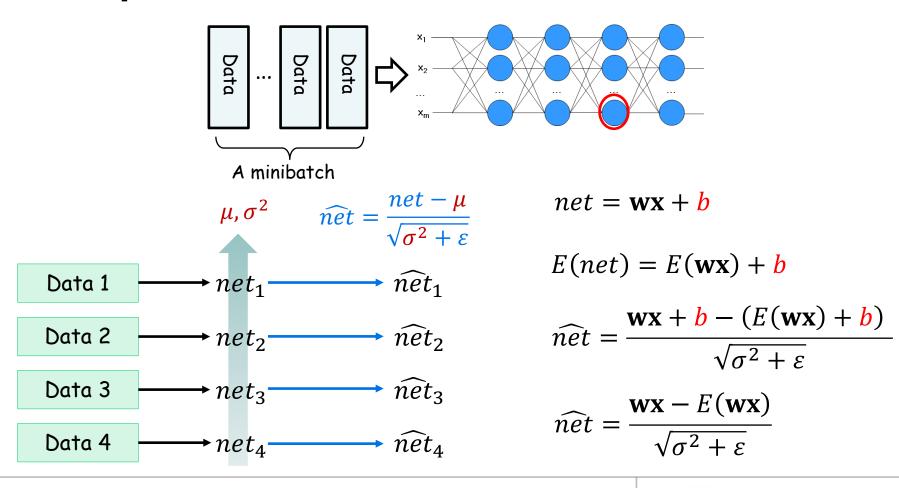


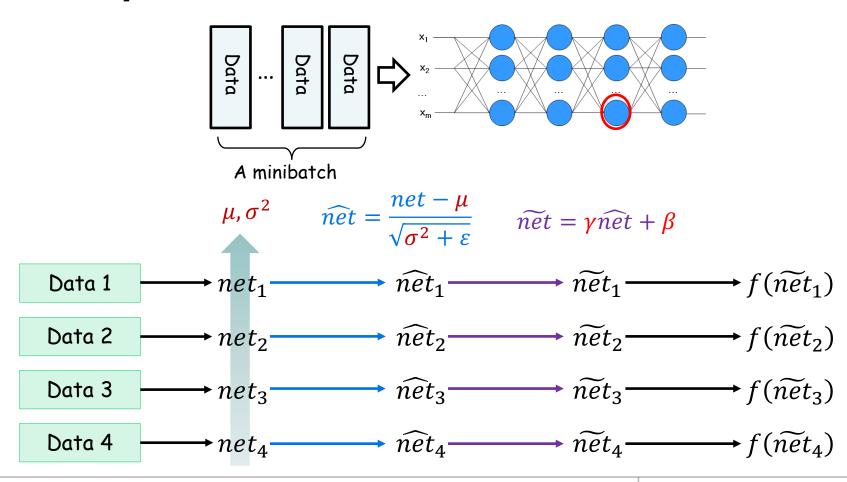
Normalization of outputs



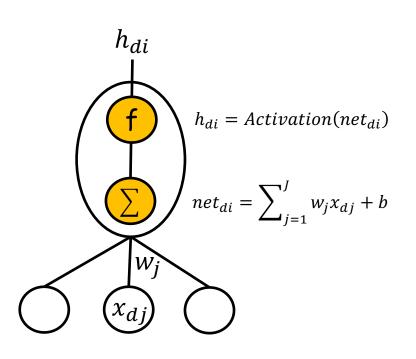


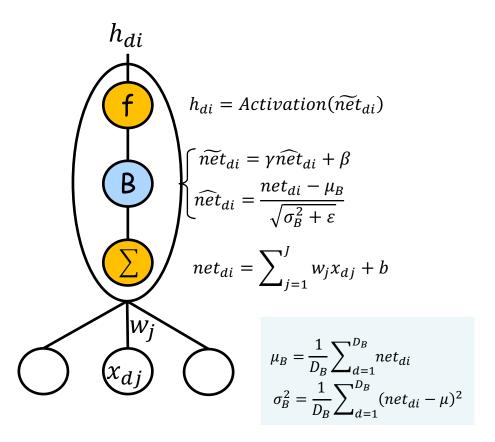






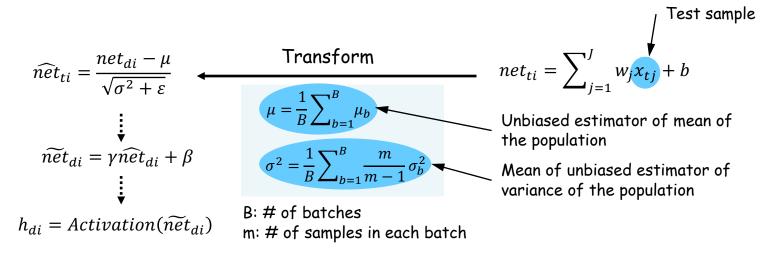
For a Single Node



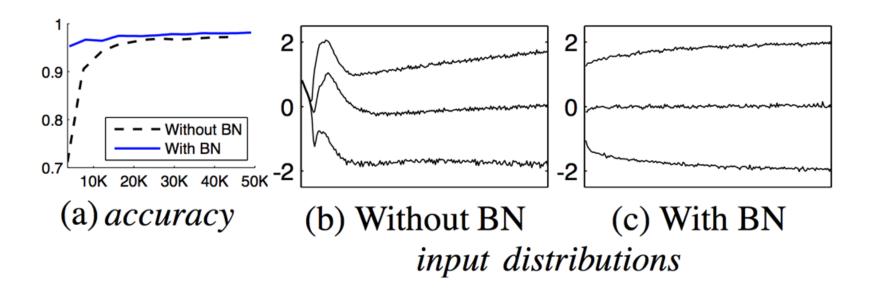


Testing

- For Training, the mean and variance of each batch are used for normalization
- For Testing, of which data the mean and variance will be used?
 - Estimated with those of batches in the training



Performance with BN



Advantage

- Reduces internal covariant shift.
- Reduces the dependence of gradients on the scale of the connection weights.
- Regularizes the model and reduces the need for regularization techniques.
 - It adds some stochastic noise to the activations as a result of using noisy estimates computed on the mini-batches. This has a regularization effect in some applications,

Disadvantage

- Expensive: Memory and time
 - Must keep interim results of all instances in a batch
 - Especially in CNN, usually an image is large
- Hard to apply when the batch size is small
 - If batches are small, the means and variances cannot approximate the global ones.
- Hard to apply to recurrent networks
 - It doesn't match to structure of recurrent networks
 - Hard to implement with recurrent networks