


Chapter

4

*ADTs Stack  
and Queue*

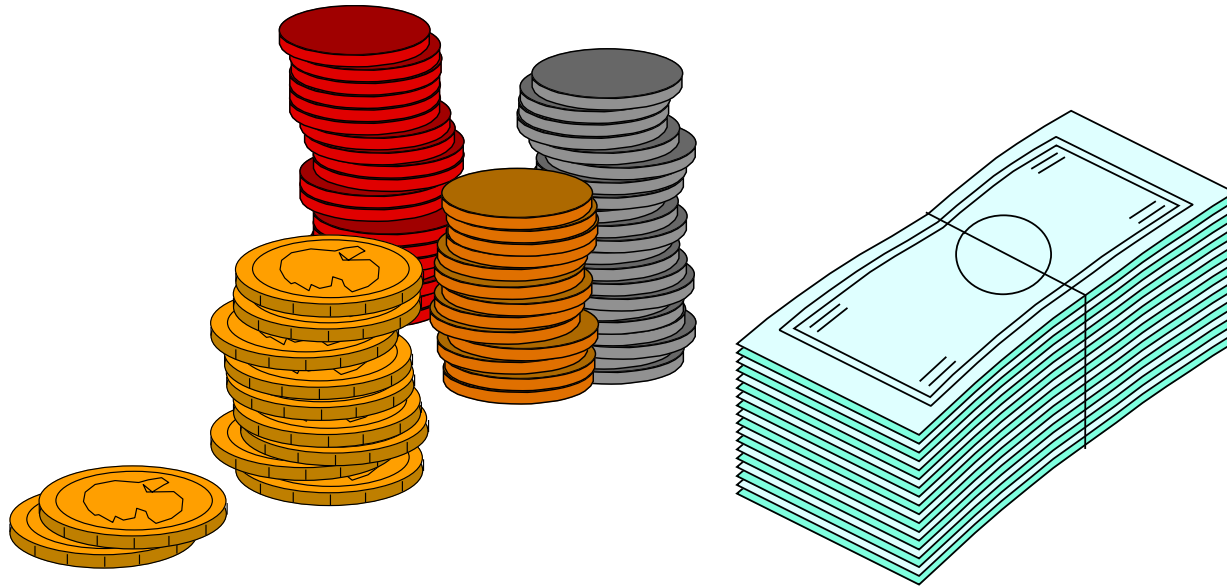


*Third Edition*

# **C<sup>++</sup>** *Plus* Data Structures

*Nell Dale*

# Stacks of Coins and Bills



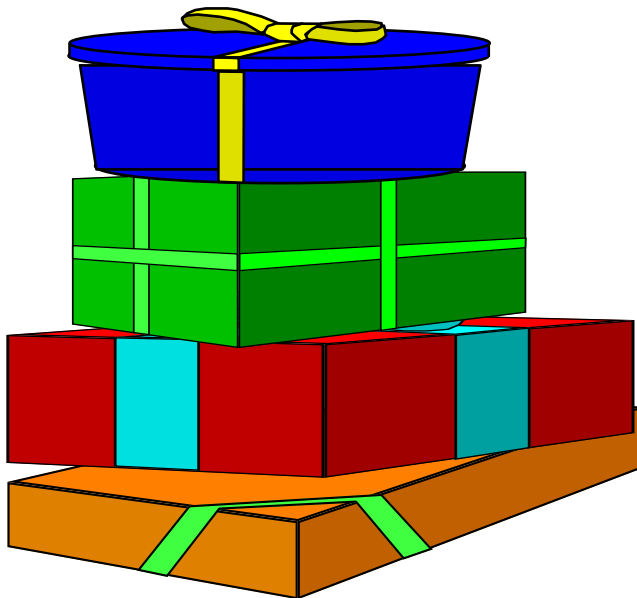


# What is a Stack?

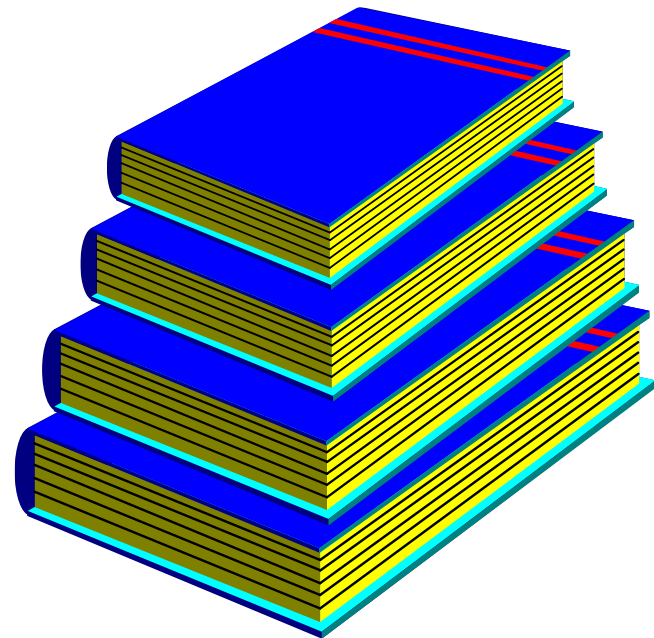
- ***Logical (or ADT) level:*** A stack is an ordered group of **homogeneous items** (elements), in which the removal and addition of stack items can take place only at the top of the stack.
- A stack is a **LIFO** “last in, first out” structure.

# Stacks of Boxes and Books

**TOP OF THE STACK**



**TOP OF THE STACK**





# Stack ADT Operations

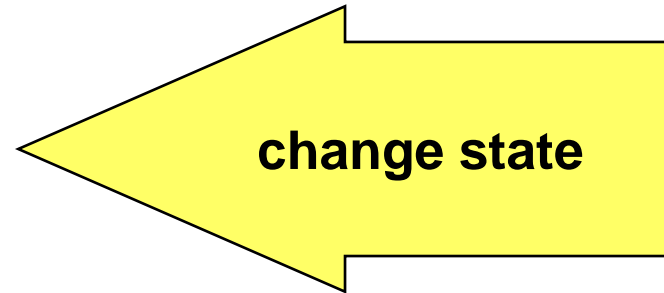
- **MakeEmpty** -- Sets stack to an empty state.
- **IsEmpty** -- Determines whether the stack is currently empty.
- **IsFull** -- Determines whether the stack is currently full.
- **Push (ItemType newItem)** -- Throws exception if stack is full; otherwise adds newItem to the top of the stack.
- **Pop** -- Throws exception if stack is empty; otherwise removes the item at the top of the stack.
- **ItemType Top** -- Throws exception if stack is empty; otherwise returns a copy of the top item



# ADT Stack Operations

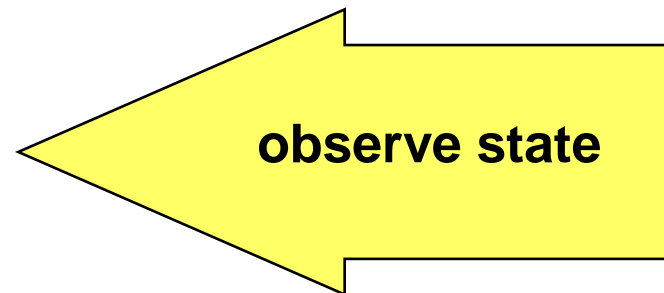
## Transformers


- Push
- Pop



## Observers

- IsEmpty
- IsFull
- IsFull





```
// Class specification for Stack ADT in file StackType.h

class FullStack                // Exception class thrown by
                                // Push when stack is full
{};

class EmptyStack               // Exception class thrown by
                                // Pop and Top when stack is empty
{};

#include "ItemType.h"

class StackType
{
public:

    StackType( );
    // Class constructor.
    bool IsFull ( ) const;
    // Function: Determines whether the stack is full.
    // Pre: Stack has been initialized
    // Post: Function value = (stack is full)
```

```

bool IsEmpty() const;
// Function: Determines whether the stack is empty.
// Pre:    Stack has been initialized.
// Post:   Function value = (stack is empty)
void Push( ItemType item );
// Function: Adds newItem to the top of the stack.
// Pre: Stack has been initialized.
// Post: If (stack is full), FullStack exception is thrown;
//        otherwise, newItem is at the top of the stack.
void Pop();
// Function: Removes top item from the stack.
// Pre: Stack has been initialized.
// Post: If (stack is empty), EmptyStack exception is thrown;
//        otherwise, top element has been removed from stack.
ItemType Top();
// Function: Returns a copy of top item on the stack.
// Pre: Stack has been initialized.
// Post: If (stack is empty), EmptyStack exception is thrown;
//        otherwise, top element has been removed from stack.
private:
    int top;
    ItemType  items[MAX_ITEMS];
};

```





```
// File: StackType.cpp
```

```
#include "StackType.h"
```

```
#include <iostream>
```

```
StackType::StackType( )
```

```
{
```

```
    top = -1;
```

```
}
```

```
bool StackType::IsEmpty() const
```

```
{
```

```
    return(top == -1);
```

```
}
```

```
bool StackType::IsFull() const
```

```
{
```

```
    return (top == MAX_ITEMS-1);
```

```
}
```

```
void StackType::Push(ItemType newItem)
{
    if( IsFull() )
        throw FullStack();
    top++;
    items[top] = newItem;
}
```

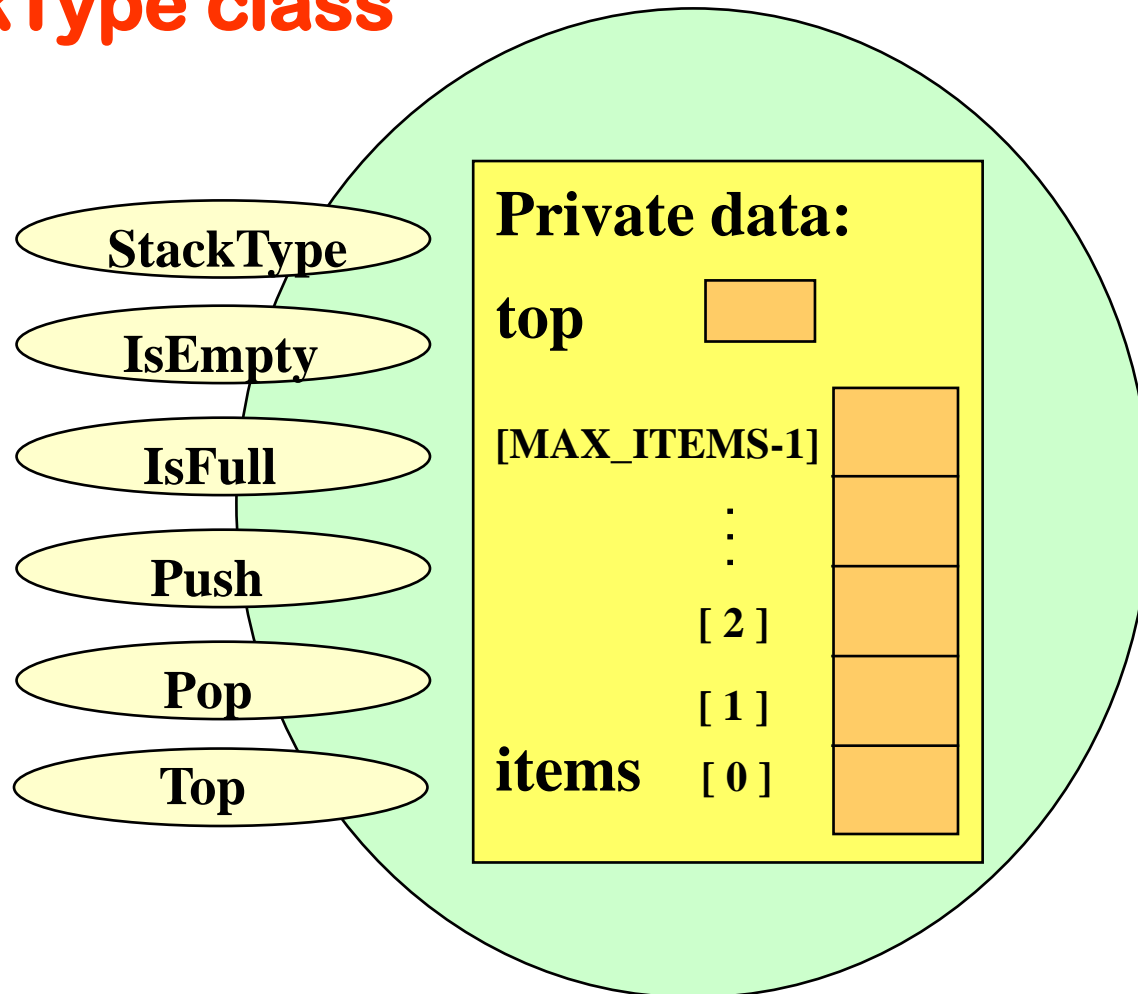
```
void StackType::Pop()
{
    if( IsEmpty() )
        throw EmptyStack();
    top--;
}
```

```
ItemType StackType::Top()
{
    if (IsEmpty())
        throw EmptyStack();
    return items[top];
}
```

# Class Interface Diagram

(Memory reversed to better illustrate concept)

## StackType class





# Tracing Client Code

letter

'V'

Private data:

top



[MAX\_ITEMS-1]

⋮

[ 2 ]

[ 1 ]

items [ 0 ]



```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

'V'

Private data:

top

-1

[MAX\_ITEMS-1]

⋮

[ 2 ]

[ 1 ]

items [ 0 ]

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**0**

[MAX\_ITEMS-1]

⋮

[ 2 ]

[ 1 ]

items [ 0 ]

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( )  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**1**

[MAX\_ITEMS-1]

⋮

[ 2 ]

[ 1 ]

items [ 0 ]

**'C'**

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( )  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**2**

[MAX\_ITEMS-1]

:

[ 2 ]

[ 1 ]

items [ 0 ]

**'S'**

**'C'**

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```





# Tracing Client Code

letter

**'V'**

Private data:

top

**2**

[MAX\_ITEMS-1]

:

[ 2 ]

**'S'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';  
StackType charStack;  
charStack.Push(letter);  
charStack.Push('C');  
charStack.Push('S');  
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );  
charStack.Push('K');  
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**1**

[MAX\_ITEMS-1]

:

[ 2 ]

**'S'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))
```

```
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))
```

```
{ letter = charStack.Top();
```

```
    charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**2**

[MAX\_ITEMS-1]

:

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';  
StackType charStack;  
charStack.Push(letter);  
charStack.Push('C');  
charStack.Push('S');  
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );  
charStack.Push('K');  
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**2**

[MAX\_ITEMS-1]

:

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

'K'

Private data:

top

2

[MAX\_ITEMS-1]

:

[ 2 ]

'K'

[ 1 ]

'C'

items [ 0 ]

'V'

```
char letter = 'V';
StackType charStack;
charStack.Push(letter);
charStack.Push('C');
charStack.Push('S');
if ( !charStack.IsEmpty( ))
    charStack.Pop( );
charStack.Push('K');
while (!charStack.IsEmpty( ))
{ letter = charStack.Top();
  charStack.Pop(0)}
```



# Tracing Client Code

letter

'K'

Private data:

top

1

[MAX\_ITEMS-1]

⋮

[ 2 ]

'K'

[ 1 ]

'C'

items

[ 0 ]

'V'

```
char letter = 'V';
StackType charStack;
charStack.Push(letter);
charStack.Push('C');
charStack.Push('S');
if ( !charStack.IsEmpty( ))
    charStack.Pop( );
charStack.Push('K');
while (!charStack.IsEmpty( ))
{ letter = charStack.Top();
  charStack.Pop(0)}
```



# Tracing Client Code

letter

'K'

Private data:

top

1

[MAX\_ITEMS-1]

:

[ 2 ]

'K'

[ 1 ]

'C'

items [ 0 ]

'V'

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'C'**

**Private data:**

top

**0**

[MAX\_ITEMS-1]

:

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items

[ 0 ]

**'V'**

```
char letter = 'V';  
StackType charStack;  
charStack.Push(letter);  
charStack.Push('C');  
charStack.Push('S');  
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );  
charStack.Push('K');  
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
    charStack.Pop(0)}
```





# Tracing Client Code

letter

**'C'**

Private data:

top

**0**

[MAX\_ITEMS-1]

:

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';  
StackType charStack;  
charStack.Push(letter);  
charStack.Push('C');  
charStack.Push('S');  
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );  
charStack.Push('K');  
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# Tracing Client Code

letter

**'V'**

**Private data:**

top

**-1**

[MAX\_ITEMS-1]

⋮

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';  
StackType charStack;  
charStack.Push(letter);  
charStack.Push('C');  
charStack.Push('S');  
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );  
charStack.Push('K');  
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
    charStack.Pop(0)}
```



# End of Trace

letter

**'V'**

Private data:

top

**-1**

[MAX\_ITEMS-1]

:

[ 2 ]

**'K'**

[ 1 ]

**'C'**

items [ 0 ]

**'V'**

```
char letter = 'V';
```

```
StackType charStack;
```

```
charStack.Push(letter);
```

```
charStack.Push('C');
```

```
charStack.Push('S');
```

```
if ( !charStack.IsEmpty( ))  
    charStack.Pop( );
```

```
charStack.Push('K');
```

```
while (!charStack.IsEmpty( ))  
{ letter = charStack.Top();  
  charStack.Pop(0)}
```



# What is a Class Template?

- A class template allows the compiler to generate **multiple versions of a class type** by using type parameters.
- The formal parameter appears in the class template definition, and the actual parameter appears in the client code. Both are enclosed in pointed brackets, **< >**.



StackType<int> numStack;

ACTUAL PARAMETER

top

3

[MAX\_ITEMS-1]

▪  
▪  
▪

[ 3 ]

789

[ 2 ]

-56

[ 1 ]

132

items [ 0 ]

5670



StackType<float> numStack;

ACTUAL PARAMETER

top

3

[MAX\_ITEMS-1]

▪  
▪  
▪

[ 3 ]

3456.8

[ 2 ]

-90.98

[ 1 ]

98.6

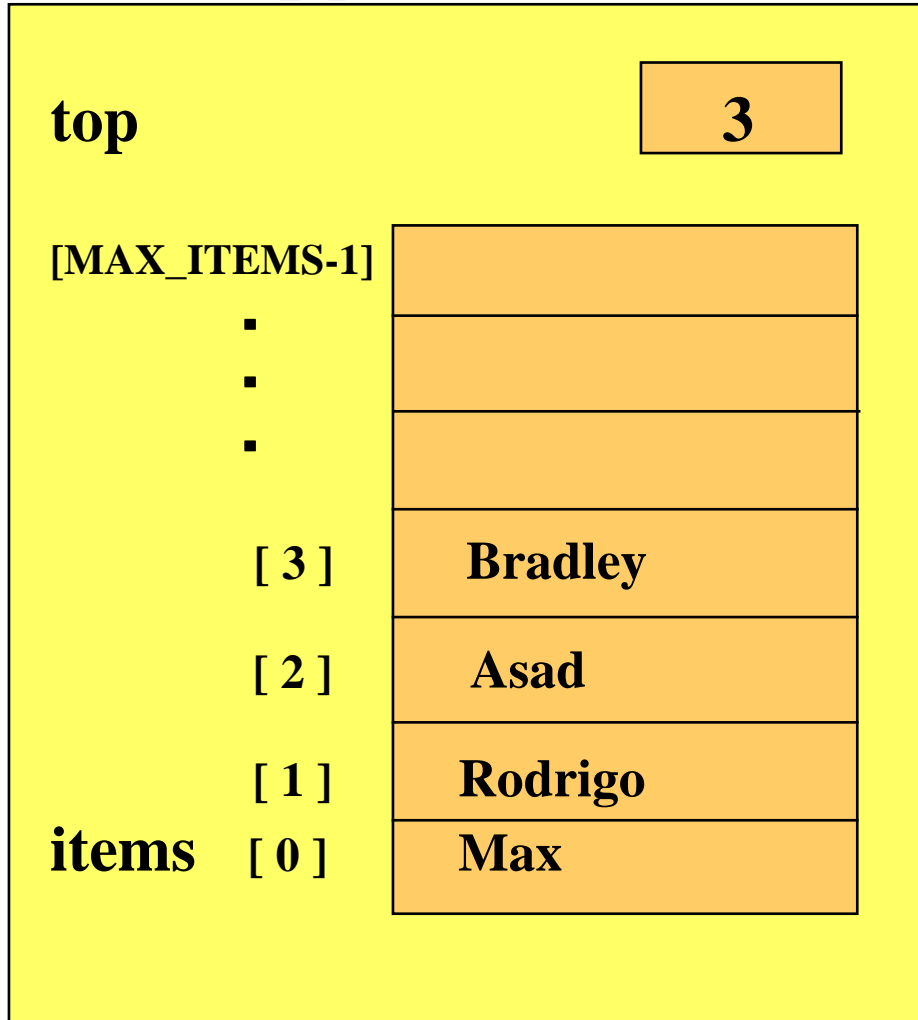
items [ 0 ]

167.87



StackType<StrType> numStack;

ACTUAL PARAMETER





```
//-----  
// CLASS TEMPLATE DEFINITION  
//-----  
#include "ItemType.h"           // for MAX_ITEMS and ItemType  
  
template<class ItemType>        // formal parameter list  
class StackType  
{  
public:  
    StackType( );  
    bool IsEmpty( ) const;  
    bool IsFull( ) const;  
    void Push( ItemType item );  
    void Pop( ItemType& item );  
    ItemType Top( );  
private:  
    int      top;  
    ItemType items[MAX_ITEMS];  
};
```





```
//-----  
//  SAMPLE CLASS MEMBER FUNCTIONS  
//-----  
  
template<class ItemType>    // formal parameter list  
StackType<ItemType>::StackType( )  
{  
    top = -1;                Notice that the class name is StackType<ItemType>  
}  
  
template<class ItemType>    // formal parameter list  
void StackType<ItemType>::Push ( ItemType newItem )  
{  
    if (IsFull())  
        throw FullStack();  
    top++;  
    items[top] = newItem;    // STATIC ARRAY IMPLEMENTATION  
}
```



# Using class templates

- **The actual parameter to the template is a data type.** Any type can be used, either built-in or user-defined.
- **When creating class template**
  - Put .h and .cpp in same file or
  - Have .h include .cpp file



# Recall that . . .

```
char msg [ 8 ];
```

**msg** is the **base address** of the array. We say **msg** is a pointer because its value is an address. It is a pointer constant because the value of **msg** itself cannot be changed by assignment. It “points” to the memory location of a char.

**6000**

'H'	'e'	'l'	'l'	'o'	'\0'		
msg [0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]



# Addresses in Memory

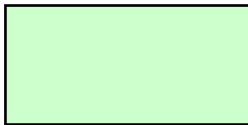
- When a variable is declared, enough memory to hold a value of that type is allocated for it at an unused memory location. This is the address of the variable. For example:

```
int      x;
```

```
float    number;
```

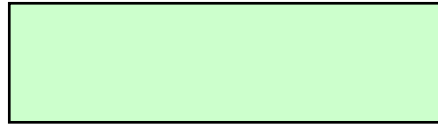
```
char     ch;
```

**2000**



**x**

**2002**



**number**

**2006**



**ch**



# Obtaining Memory Addresses

- The address of a non-array variable can be obtained by using the **address-of operator &**.

```
using namespace std;
```

```
int      x;
```

```
float    number;
```

```
char     ch;
```

```
cout << "Address of x is " << &x << endl;
```

```
cout << "Address of number is " << &number << endl;
```

```
cout << "Address of ch is " << &ch << endl;
```



# What is a pointer variable?

- A pointer variable is a **variable whose value is the address of a location in memory.**
- To declare a pointer variable, you must specify the type of value that the pointer will point to. For example,

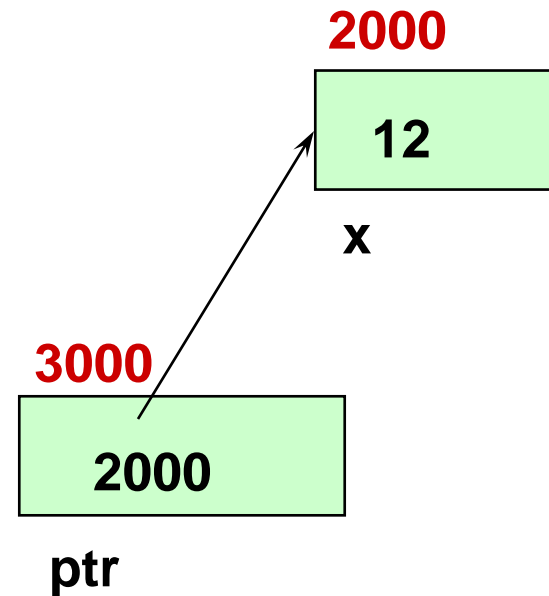
```
int*    ptr; // ptr will hold the address of an int
```

```
char*   q;   // q will hold the address of a char
```

# Using a pointer variable

```
int  x;  
x = 12;
```

```
int* ptr;  
ptr = &x;
```



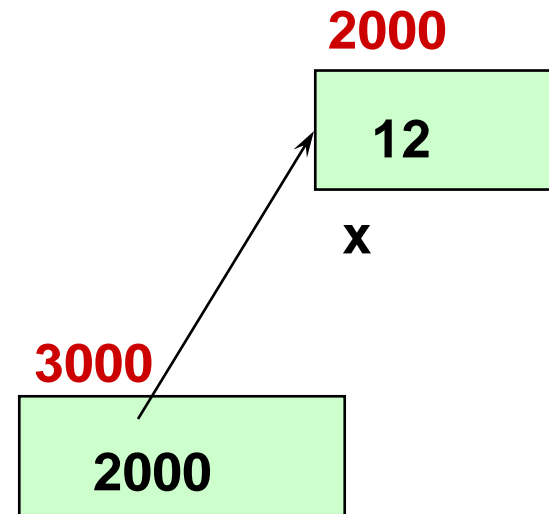
**NOTE:** Because `ptr` holds the address of `x`, we say that `ptr` “points to” `x`

# Unary operator \* is the deference (indirection) operator

```
int x;  
x = 12;
```

```
int* ptr;  
ptr = &x;
```

```
std::cout << *ptr;
```



**NOTE:** The value pointed to by `ptr` is denoted by `*ptr`



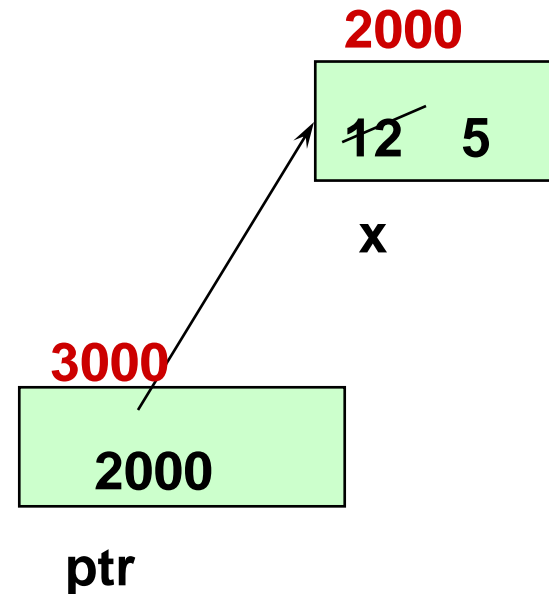
# Using the dereference operator

```
int x;  
x = 12;
```

```
int* ptr;  
ptr = &x;
```

```
*ptr = 5;
```

```
// changes the value  
// at address ptr to 5
```





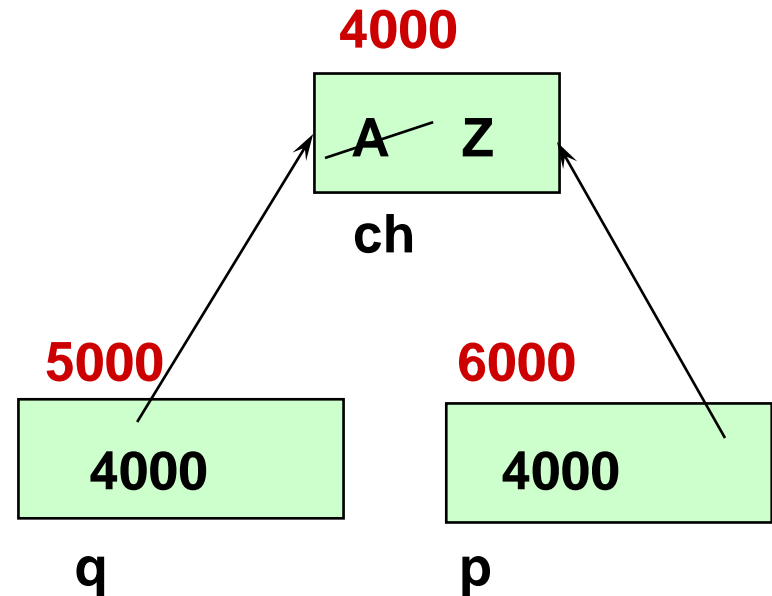
# Another Example

```
char  ch;  
ch =  'A' ;
```

```
char*  q;  
q  =  &ch;
```

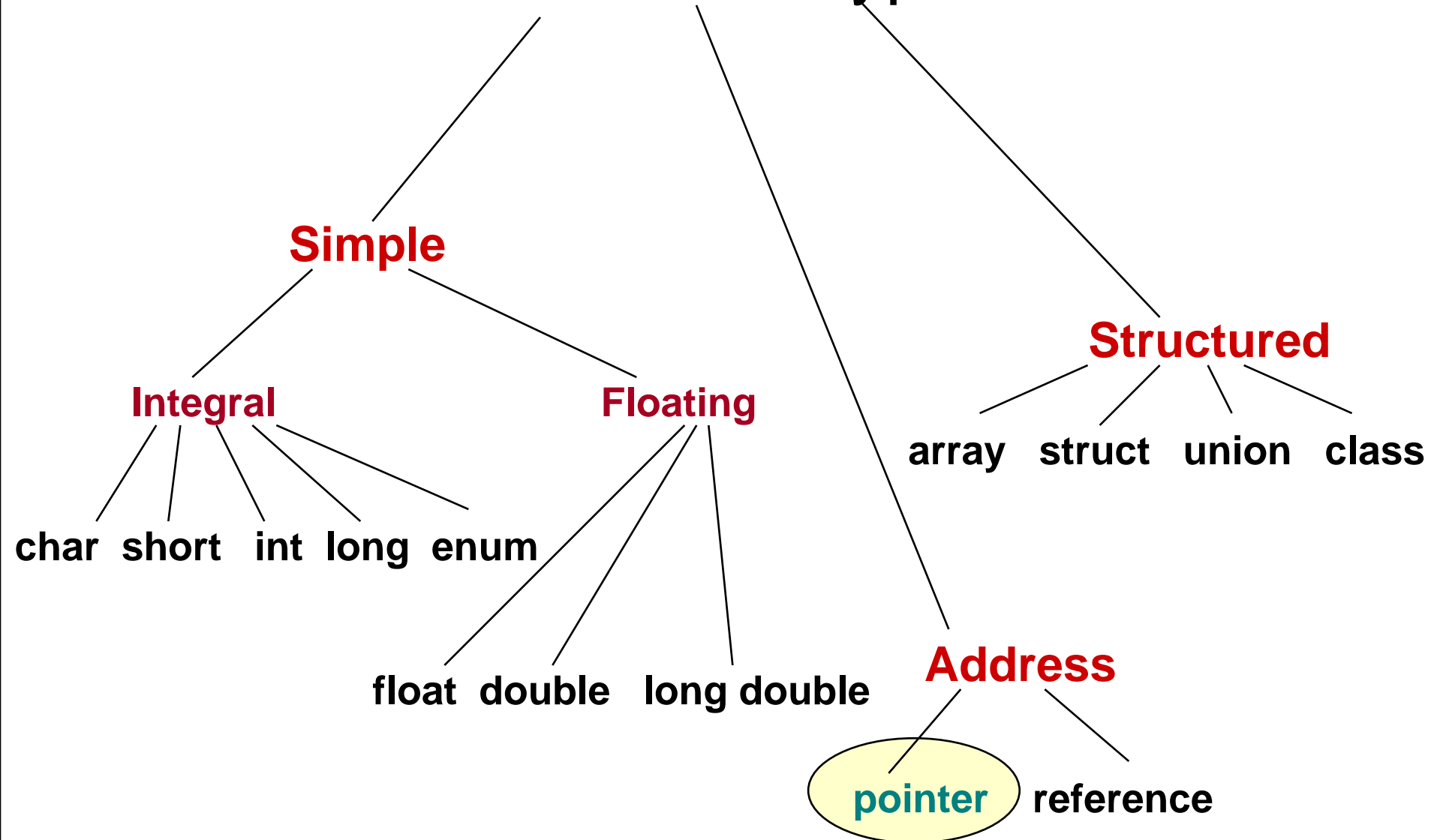
```
*q =  'Z' ;  
char*  p;
```

```
p = q;    // the right side has value 4000  
          // now p and q both point to ch
```





# C++ Data Types





# The NULL Pointer

There is a pointer constant 0 called the “null pointer” denoted by NULL in `cstddef`.

But NULL is not memory address 0.

NULL allows a pointer to point nothing

**NOTE:** It is an error to dereference a pointer whose value is NULL. Such an error may cause your program to crash, or behave erratically. It is the programmer’s job to check for this.

```
while (ptr != NULL)
```

```
{
```

```
    . . .
```

```
}
```

*// ok to use \*ptr here*



# Allocation of memory

## STATIC ALLOCATION

Static allocation is the allocation of memory space at **compile time**.

## DYNAMIC ALLOCATION

Dynamic allocation is the allocation of memory space at **run time** by using operator **new**.



# 3 Kinds of Lifetime for Program Data

- **STATIC DATA:** memory allocation exists throughout execution of program.  
`static long SeedValue;`
- **AUTOMATIC DATA:** automatically created at function entry, resides in activation frame of the function, and is destroyed when returning from function.
- **DYNAMIC DATA:** explicitly allocated and deallocated during program execution by C++ instructions written by programmer using unary operators `new` and `delete`
- \* The *lifetime* of a variable is the time during program execution when the variable has storage assigned to it.



# Using operator new

If memory is available in an area called the free store (or heap), operator new **allocates the requested object or array, and returns a pointer to (address of ) the memory allocated.**

Otherwise, the null pointer 0 is returned.

The dynamically allocated object exists until the delete operator destroys it.



# Dynamically Allocated Data

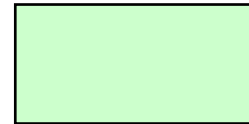
```
char* ptr;
```

```
ptr = new char;
```

```
*ptr = 'B' ;
```

```
std::cout << *ptr;
```

2000



ptr



# Dynamically Allocated Data

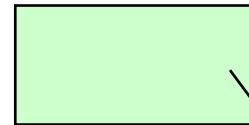
```
char* ptr;
```

```
ptr = new char;
```

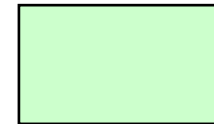
```
*ptr = 'B';
```

```
std::cout << *ptr;
```

2000



ptr



**NOTE: Dynamic data has no variable name**

# Dynamically Allocated Data

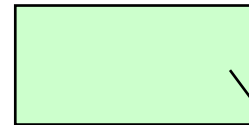
```
char* ptr;
```

```
ptr = new char;
```

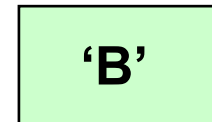
```
*ptr = 'B' ;
```

```
std::cout << *ptr;
```

2000



ptr



**NOTE: Dynamic data has no variable name**



# Dynamically Allocated Data

```
char* ptr;
```

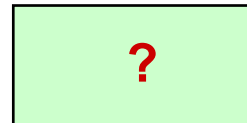
```
ptr = new char;
```

```
*ptr = 'B' ;
```

```
std::cout << *ptr;
```

```
delete ptr;
```

2000



ptr

**NOTE:** Delete deallocates the memory pointed to by ptr.



# Using operator delete

The **object or array currently pointed to by the pointer is deallocated**, and the pointer is considered unassigned. The memory is returned to the free store.

Square brackets are used with delete to deallocate a dynamically allocated array of classes.



# Some C++ pointer operations

```
MoneyType* moneyPtr = new MoneyType;  
moneyPtr->dollars = 3245;  
(*moneyPtr).cents = 33; // NO *moneyPtr.cents = 33;
```

## Precedence

*Higher*

Unary:

->

Select member of class pointed to

++

--

!

\*

new

delete

Increment, Decrement, NOT, Dereference, Allocate, Deallocate

+

-

Add Subtract

<

<=

>

>=

Relational operators

==

!=

Tests for equality, inequality

=

Assignment

*Lower*