

Step 1

1) Laser Point = $\begin{pmatrix} u \\ v \\ 1 \end{pmatrix}$ \leftarrow 2 points from left
1 point from right

$$2) \underbrace{P_w}_{(3 \times 1)} = \underbrace{s \cdot \underbrace{R^{-1}}_{(3 \times 3)} \cdot \underbrace{A^{-1}}_{(3 \times 1)}}_{\vec{b}} \underbrace{\begin{pmatrix} u \\ v \\ 1 \end{pmatrix}}_{(3 \times 1)} - \underbrace{\underbrace{R^{-1}}_{(3 \times 3)} T}_{\vec{a}}_{(3 \times 1)}$$

where $\vec{a} = \begin{pmatrix} a_x \\ a_y \\ a_z \end{pmatrix}$ and $\vec{b} = \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix}$

so $s(\text{scalar}) = a_z / b_z$

Step 2 : Transform right laser point in left coordinate system

$$\underbrace{P_c}_{(3 \times 1)} = \underbrace{R^{-1}}_{(3 \times 3)} \cdot \underbrace{P_k}_{(3 \times 1)} - \underbrace{R^{-1} T}_{(3 \times 1)}$$

where $P_k = \underbrace{[R_2 | T_2]}_{3 \times 4} \cdot \underbrace{P_w}_{4 \times 1}$

Step 3 : Find Laser Plane Equation from 3 points

$$Ax + By + Cz + D = 0$$

where $\vec{N} = \begin{pmatrix} A \\ B \\ C \end{pmatrix}$

Step 4 : find 3D object point \leftarrow object point

$$1) P_w = s \cdot \underbrace{R^{-1}}_{(3 \times 3)} \cdot \underbrace{A^{-1}}_{(3 \times 1)} \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} - \underbrace{R^{-1} T}_{(3 \times 1)}$$

where

$$s = \frac{\vec{N} \cdot \vec{a} - D}{\vec{b} \cdot \vec{N}}$$