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Computer Science



CS32: Introduction to Computer Science

Discussion Week 4

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Announcement (Week 4)



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- Homework 2 is due on next Tuesday, February 5.
 - Make sure you understand the requirements and also read the FAQ.
- About midterm this Wednesday (Part 1)
 - Grades will be released soon by Prof. David Smallberg.

- **Linked List**
 - Properties of linked list: Review
 - Doubly linked list
 - Sorted linked list
 - Reverse a linked list
- **Stack and Queues**
 - Implementation and applications
- **Inheritance and Polymorphism (Probably not this time)**
 - Examples and applications
- **Group Exercises**

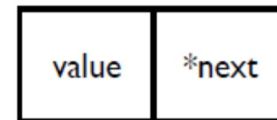
Linked List: Review

Basis



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- Minimum Requirement
 - Key component as unit: Node (with `value` and `pointer` to next node)
 - Head pointer → points to the first term
 - Loop-free (except in some special case: circular linked list)
- Regular operations
 - Insertion
 - Search
 - Removal
- Pros and cons
 - Efficient insertion, flexible memory allocation, simple implementation
 - High complexity of search



```
typedef int ItemType;  
Struct Node  
{  
    ItemType value;  
    Node *next;  
};
```

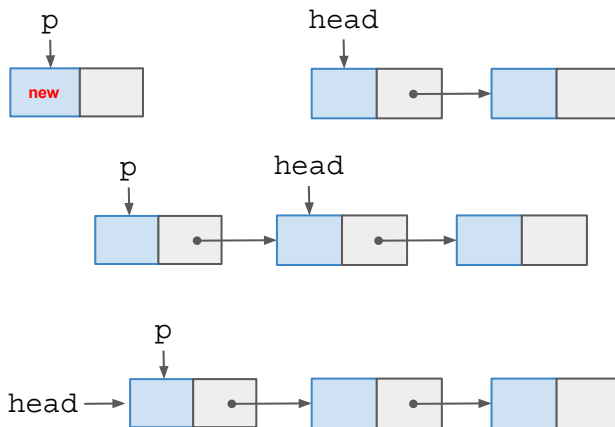


Linked List

Insertion: Add a new node to a list



- Example: Insert as head in a list
- Steps
 - a) Create a new node and call the pointer p
 - b) Make its `next` pointer point to the first item
 - c) Make the head pointer to the new node



```
//Skeleton: Linked list insertion  
//=====
```

```
//insert as head
```

```
p->next = head;
```

```
Head = p;
```

```
//insert after end: End node: q
```

```
q->next = p;
```

```
p->next = nullptr;
```

```
//insert in the middle: node q
```

```
p->next = q->next;
```

```
q->next = p;
```

Linked List

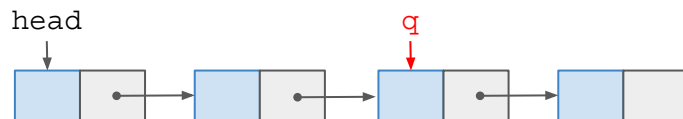
Search



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- **Steps**

- Find matched node and return
- If no match, return NULL



```
// Skeleton Code: Linked list search  
// =====
```

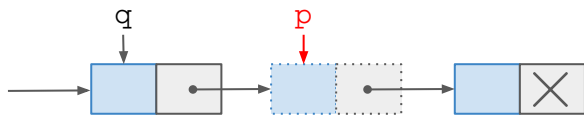
```
Node* Search(int key, Node* head){  
    Node *q = head;  
    while(q != NULL)  
    {  
        if(q -> value != key) q = q -> next;  
        else return q;  
    }  
    return NULL;  
}
```

Linked List

Removal



- Remember to set the previous node q 's next pointer to point the next node of p
 $q \rightarrow \text{next} = p \rightarrow \text{next};$
Delete p
- What if $p == \text{head}$? What if p points to the last node in the linked list?

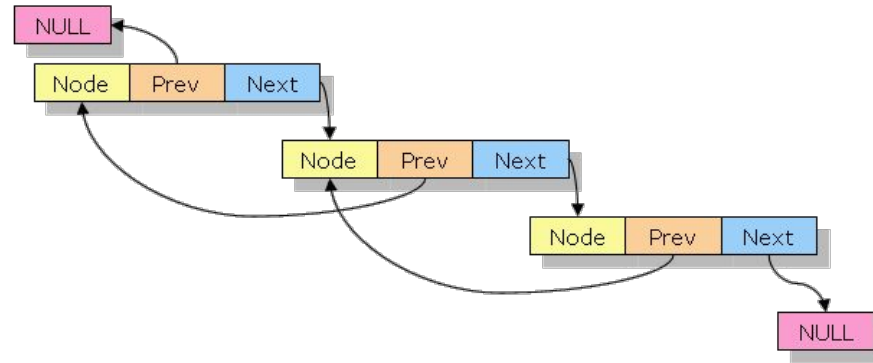


```
// Skeleton Code: Linked list removal
// =====
void remove(int valToRemove, Node* head) {
    Node *p = head, *q = NULL;
    while (p != NULL) {
        if (p->value == valToRemove)
            break;
        q = p;
        p = p->next;
    }
    if (p == NULL) return;
    if (p == head) //special case
        head = p->next;
    else
        q->next = p->next;
    delete p;
}
```

- Pros:
 - Efficient insertion (add new data items)
 - Flexible memory allocation
- Cons:
 - Slow search (search is more important than insertion and removal in real situations)
- Many variations
 - Doubly linked lists
 - Sorted linked lists
 - Circularly linked lists

Double Linked List

Data structures and properties



- A linked list where each node has two pointers:
 - Next – pointing to the next node
 - Prev – pointing to the previous node
- Features
 - head, tail pointers
 - head->prev = NULL; tail->next = NULL;
 - head == tail == NULL when doubly linked list is empty

```
typedef int ItemType;  
Struct Node  
{  
    ItemType value;  
    Node *next;  
    Node *prev; ←  
};
```



Double Linked List

Insertion: How many cases to consider?



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- Four cases:
 - Insert before the head
 - Insert after the tail
 - Insert somewhere in the middle
 - When list is empty ←

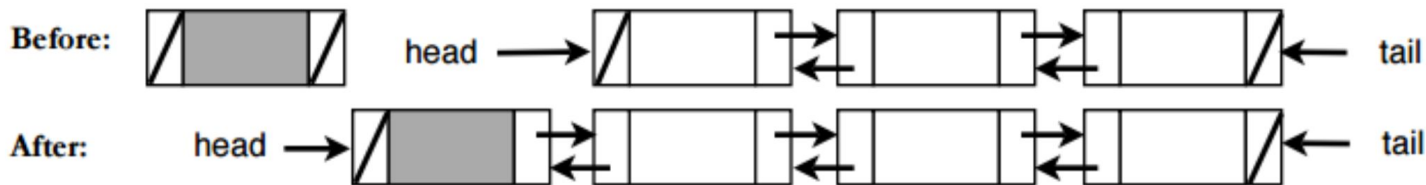
Double Linked List

Insertion: Before head / After tail



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- Steps for insertion before head:
 - Set the `prev` of head to the new node `p`
 - Set the `next` of `p` to head
 - `p` becomes the new head
 - `head->prev = NULL;`
- Steps for insertion after tail:
 - Similar to insertion before head (try it yourself!)



Double Linked List

Insertion: In the middle of the list



- Steps for insertion in the middle (after node q):
 - Fix the next node of q first: `Node *r = q->next;`
 - Point both next of q and prev of r to p: `q->next = r->prev = p;`
 - Point both sides of p to q and r respectively: `p->prev = q; p->next = r;`
- You can do that without the help of pointer r

```
p->prev = q;  
p->next = q->next;  
q->next = q->next->prev = p;
```

Double Linked List

Insertion to empty list / Search



- Insertion to an empty list

```
head = tail = p;  
p->next = p->prev = NULL;
```

- Search in doubly linked list
 - Similar to standard linked list
 - Can be done either from head or tail

Double Linked List

Removal



- Removal is more complex!
- Consider the following cases:
 - Check if the node `p` is the head (`p == head`). Let this boolean be `A`.
 - Check if the node is the tail (`p == tail`). Let this boolean be `B`.
- Different cases:
 - Case 1 (`A`, but not `B`): `P` is the head of the list and there is more than one node.
 - Case 2 (`B`, but not `A`): `P` is the tail of the list, and there is more than one node.
 - Case 3 (`A` and `B`): `P` is the only node.
 - Case 4 (not `A` and not `B`): `P` is in the middle of the list.

Double Linked List

Removal



```
void removeNodeInDLL(Node *p, Node& *head, Node& *tail)
{
    if (p == head && p == tail) //case 3
        head = tail = NULL;
    else if (p == head) {
        //case 1
        head = head -> next;
        head -> prev = NULL; }
    else if (p == tail) {
        //case 2
        tail = tail -> prev;
        tail -> next = NULL; }
    else {
        //case 4
        p -> prev -> next = p -> next;
        p -> next -> prev = p -> prev; }
    delete p;
}
```

Double Linked List

Copy a doubly linked list (and more)



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- Steps
 - Create head and tail for the new list
 - Iterate through the old list. For each node, copy its value to a new node.
 - Insert the new node to the tail of the new list.
 - Repeat until we have iterated the entire old list.
 - Set `NULL` before head and next of tail.
- Tips for linked list problems
 - To draw diagrams of nodes and pointers will be extremely helpful.
 - When copying a linked list, only copy stored values to new nodes. Do not copy pointers.

Sorted Linked List

Motivation and properties



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- Do we need to search the entire linked list?
- What if we store all values in an ascending sorted (or descending order)?



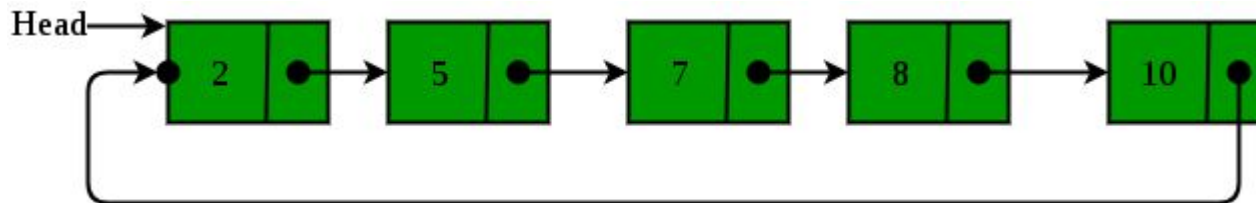
- How do you change insertion function?
 - Find the node q whose value is the greatest lower bound to the new node p .
- How do you change search function?
 - Early stop when we see a node which stores a value that is larger than key for ascending sorted linked list.
- How do you update removal functions?

Circular Linked List

Motivation and properties



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- Linked list where all nodes are connected to form a circle.
 - There is no NULL at the end.
 - Can be a singly circular linked list or doubly circular linked list.
- Pros:
 - Any points can be head (starting point).
 - Implementation for queue or [Fibonacci Heap](#).
 - Fit to repeatedly go around the list.
- It is also very tricky though.

Problem: Reverse Linked List

Leetcode questions #206



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Question: How to reverse a (single) linked list?

Example:

Input: 1->2->3->4->5->NULL

Output: 5->4->3->2->1->NULL

```
// One possible solution
Node* reverseList(struct ListNode* head)
{
    Node *prev=NULL, *cur=head, *next;
    while(cur) {
        next = cur->next;
        cur->next = prev; prev = cur;
        cur = next;
    }
    return prev;
}
```

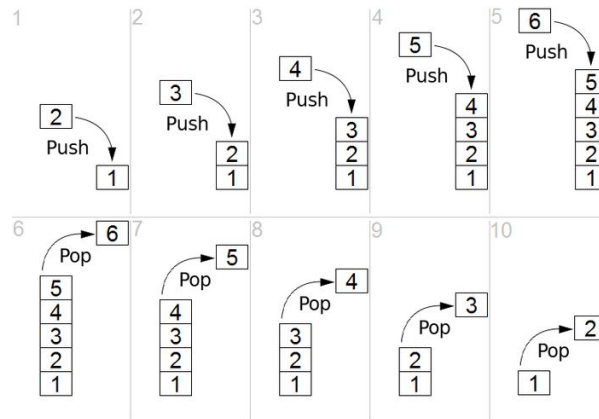
Stack: FILO

Review: Basics



- **FILO: First In, Last Out**
- A standard stack implementation
 - `Push()` and `pop()`
 - Other methods: `top()`, `count()`
- Applications:
 - Stack memory: function call
 - Check expressions: matching brackets
 - Depth-first graph search
- Question: How do you implement stack with linked list / (dynamic) arrays?

```
class Stack
{
public:
    bool push(const ItemType& item);
    ItemType pop();
    bool empty() const;
    int count() const;
private:
    // some features
};
```



- Container: linked list
- Functions:
 - `push()` : Insert node before head.
 - `pop()` : Remove head and return the head value.
 - `top()` : Read head node.
 - `count()` : Maintain a private `int` member.
- Question: How about using arrays?

- Given a math expression or text sequence:
 - $6+((5+2)*3-(7+11)*5)*6$ → Consider calculation of [Reverse Polish Notation](#)
 - Latex: $f^{\text{DNN}}(X, \mathbf{W}) = \sigma(\mathbf{W} \cdot X + \mathbf{b})$

$$f^{\text{DNN}}(X, \mathbf{W}) = \sigma(\mathbf{W} \cdot X + \mathbf{b})$$

- How to check the brackets of all types are valid in the sequence? How to calculate expression in Reverse Polish Notation (RPN)?

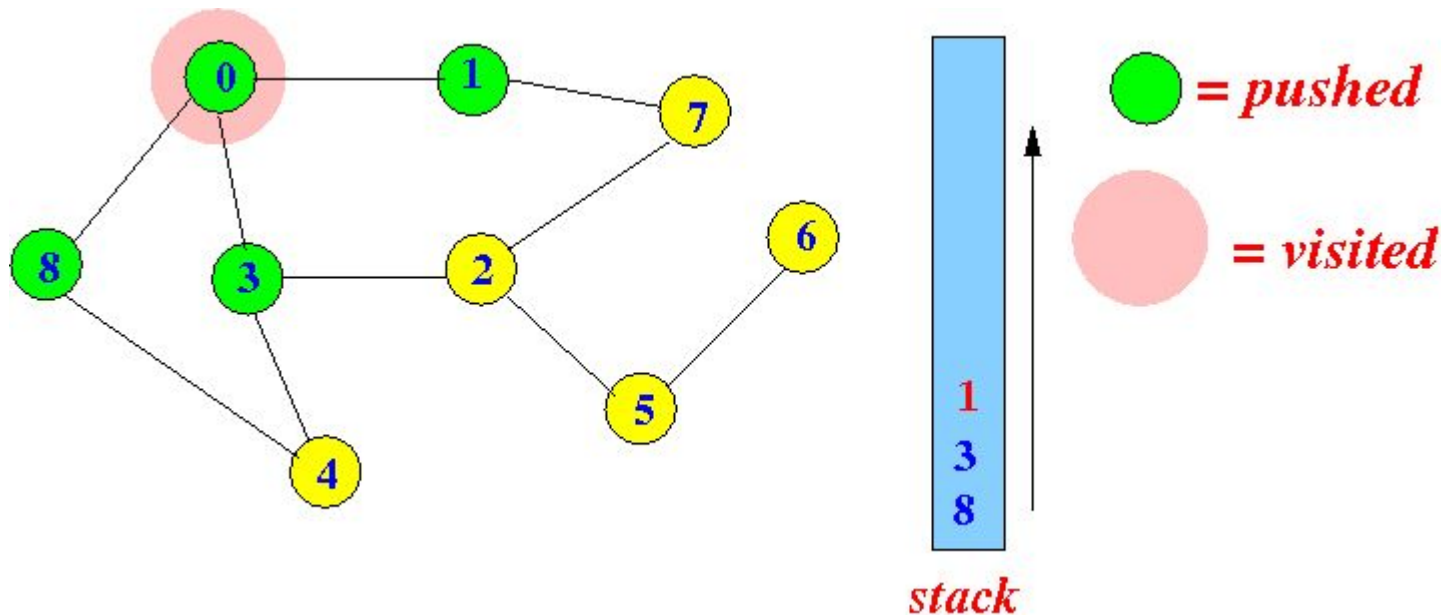
Regular Expression: `2 + 3 * (5 - 1)`

Reverse Polish Notation (RPN): `[2] [3] [5] [1] [-] [*] [+]`

Stack*

Example: Use stack to implement DFS

- Depth-first Search (DFS) on graph (will be later lectures)



```
void Graph::DFS(int s)
{
    vector<bool> visited(V, false);    // Initially mark all vertices as not visited
    stack<int> stack;    // Create a stack for DFS
    stack.push(s);    // Push the current source node
    while (!stack.empty())
    {
        s = stack.top(); // Pop a vertex from stack and print it
        stack.pop();
        // Print the popped item only if it is not visited.
        if (!visited[s]) { cout << s << " "; visited[s] = true; }
        for (auto i = adj[s].begin(); i != adj[s].end(); ++i)
            if (!visited[*i])
                stack.push(*i);
    }
}
```

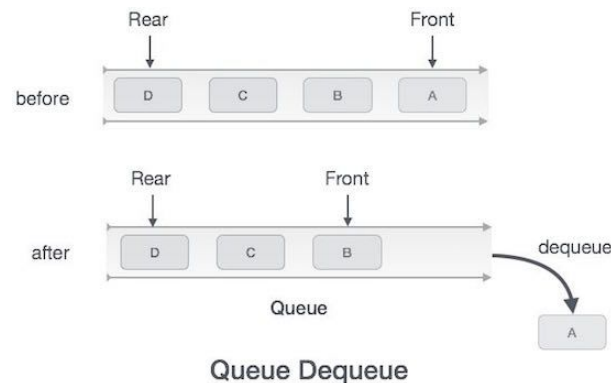
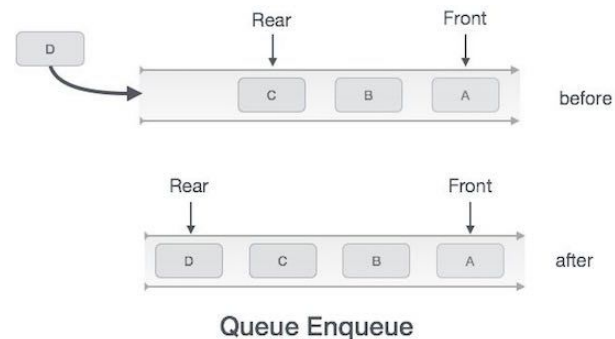
Note: Get all adjacent vertices of the popped vertex s. If the adjacent has not been visited, then push it to stack .

Queue: FIFO

Review: Basics



- **FIFO: First In, First Out**
- **Basic methods:**
 - `enqueue()` , `dequeue()`
 - `front()` , `back()`
 - `count()`
- **Applications**
 - Data streams
 - Process scheduling (DMV service request)
 - Breadth-first graph search
- **How to implement queue with linked lists or dynamic arrays?**



```
class Deque
{
    public:
        bool push_front(const ItemType& item);
        bool push_back(const ItemType& item);
        bool pop_front(const ItemType& item);
        bool pop_back(const ItemType& item);
        bool empty() const; // true if empty
        int count() const; // number of items
    private:
        int size // Some data structure that keeps the items.
};
```

Question: How to implement `class Deque` with linked lists?

Inheritance & Polymorphism

What's the next?



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- **Inheritance**

- Motivation & Definition: Deriving a class from another
- Construction & Destruction
- Override a member function

- **Polymorphism**

- Virtual functions
- Examples of polymorphism
- Abstract base class



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Thank you!

Q & A

Exercise problems from Worksheet 1 & 2 (see “LA worksheet” tab in CS32 website).

Topics today:

- Linked List (Worksheet 1, Question 5-12)

Answers will be posted after discussions.