

# Assignment11

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## 1 Information

Writer : Junhyuck Woo

Std.ID : 20145337

Project : Build a binary classifier to classify digit 0 against all the other digits at MNIST dataset.

## 2 import library

```
In [1]: import numpy as np
import pandas as pd
```

## 3 Load files

Training data, Testing data

```
In [2]: file_data = "mnist_train.csv"
        handle_file = open(file_data, "r")
        train_data = handle_file.readlines()
        handle_file.close()

        file_data = "mnist_test.csv"
        handle_file = open(file_data, "r")
        test_data = handle_file.readlines()
        handle_file.close()

        num_train = len(train_data)
        num_test = len(test_data)
        train_image = np.zeros((28 * 28, num_train), dtype=float)
        train_label = np.zeros(num_train, dtype=int)
        test_image = np.zeros((28 * 28, num_test), dtype=float)
        test_label = np.zeros(num_test, dtype=int)

        count = 0
        for line in train_data:
            line_data = line.split(',')
```

```

label = line_data[0]
train_label[count] = label
im_vector = np.asfarray(line_data[1:])
train_image[:,count] = im_vector
count += 1
count = 0
for line in test_data:
    line_data = line.split(',')
    label = line_data[0]
    test_label[count] = label
    im_vector = np.asfarray(line_data[1:])
    test_image[:,count] = im_vector
    count += 1

```

```

In [3]: class classifier:
    def __init__(self, k=64):
        self.k = k
        self.filter = self.generate_filter(k)

    def normalize(self, data):
        data_normalized = (data - np.min(data)) / (np.max(data) - np.min(data))
        return(data_normalized)

    def calculate_average(self, data):
        size_x, size_y = data.shape
        size = size_x*size_y
        average = sum(sum(data))/size
        return(average)

    def calculate_standard(self, average, data):
        variance = self.calculate_average(data*data) - (average*average)
        std = np.sqrt(variance)
        return(std)

    def whitening(self, data):
        avgerage = self.calculate_average(data)
        standard = self.calculate_standard(avgerage, data)
        whiten_data = (data - avgerage) / standard
        return(whiten_data)

    def generate_filter(self, k=64):
        data_filter = np.random.normal(0, 1, (k, 28*28))
        return(np.asmatrix(data_filter))

    def extract_feature(self, data, f):
        feature = f * data
        size_x, size_y = feature.shape
        for i in range(size_x):

```

```

        for j in range(size_y):
            feature[i,j] = max(0, feature[i,j])
    return(feature)

def reshape_data(self, data):
    num = max(data.shape)
    reshape_data = np.zeros((self.k + 1, num), dtype=float)
    for i in range(num):
        reshape_data[:,i] = np.insert(data[:,i], 0, 1)
    return(reshape_data)

def reshape_label(self, label, select):
    num = len(label)
    reshape_label = np.zeros(num, dtype=int)
    for i in range(num):
        if(int(label[i])==select):
            reshape_label[i] = 1
        else:
            reshape_label[i] = -1
    return(reshape_label)

def train(self, train_data, label, num_digit=10):
    count = 0
    normalized_data = self.normalize(train_data)
    whiten_data = self.whitening(normalized_data)
    self.x = np.zeros((num_digit, self.k+1), dtype=float)
    feature = self.extract_feature(whiten_data, self.filter)
    train_image = self.reshape_data(feature)
    A = np.asmatrix(train_image.transpose())
    pinv_A = np.linalg.pinv(A)

    for i in range(num_digit):
        train_label = self.reshape_label(label, i)
        y = np.asmatrix(train_label)
        buf = np.array(pinv_A * y.transpose())
        self.x[i,:]= buf.T
    self.x = np.asmatrix(self.x)
    #return(self.x)

def predict(self, test_data):
    normalized_data = self.normalize(test_data)
    whiten_data = self.whitening(normalized_data)
    feature = self.extract_feature(whiten_data, self.filter)
    test_image = self.reshape_data(feature)
    A = np.asmatrix(test_image.transpose())
    y = A * self.x.T
    label = []
    for i in range(max(test_data.shape)):

```

```

        label.append(np.argmax(y[i,:]))
    label = np.array(label)
    return(label)

def evaulation(self, prediction, label):
    tp = 0
    error = 0
    result = np.zeros((11,11), dtype=int)
    for i in range(len(prediction)):
        result[prediction[i]][label[i]] +=1
        if(prediction[i] == label[i]):
            tp += 1
        else:
            error += 1

    for i in range(10):
        result[10][i] = sum(result.T[:,i])
        result[i][10] = sum(result[:,i])
    result[10][10] = sum(result[:,10])

    # Plot
    print("True Possitive: ", tp/result[10][10])
    print("Error Rate: ", error/result[10][10])
    chart = pd.DataFrame(result.T)
    return(chart)

```

```

In [4]: binary_classifier = classifier(64)
        binary_classifier.train(train_image, train_label)

```

```

In [5]: y = binary_classifier.predict(train_image)
        binary_classifier.evaulation(y, train_label)

```

```

True Possitive:  0.77035
Error Rate:  0.22965

```

```

Out [5]:

```

	0	1	2	3	4	5	6	7	8	9	10
0	5355	22	91	70	14	99	144	65	38	25	5923
1	2	6415	89	50	35	24	27	20	69	11	6742
2	131	335	4279	169	163	32	417	204	160	68	5958
3	133	219	209	4674	48	285	87	131	171	174	6131
4	43	204	68	68	4470	79	173	141	89	507	5842
5	373	337	70	515	163	3218	216	115	224	190	5421
6	141	312	201	60	113	88	4917	15	51	20	5918
7	71	222	98	52	190	26	15	5332	19	240	6265
8	133	338	206	425	130	221	145	139	3879	235	5851
9	84	153	62	160	806	112	73	706	111	3682	5949
10	6466	8557	5373	6243	6132	4184	6214	6868	4811	5152	60000

```
In [6]: y = binary_classifier.predict(test_image)
        binary_classifier.evaulation(y, test_label)
```

True Possitive: 0.7766  
Error Rate: 0.2234

```
Out [6]:
```

	0	1	2	3	4	5	6	7	8	9	10
0	881	2	12	17	2	18	28	15	4	1	980
1	0	1086	11	13	2	2	3	0	14	4	1135
2	30	83	718	27	30	7	64	34	32	7	1032
3	29	30	24	804	5	37	11	22	25	23	1010
4	3	30	7	6	758	17	35	23	17	86	982
5	56	40	19	79	26	559	27	24	34	28	892
6	39	35	33	6	26	15	787	3	11	3	958
7	5	49	25	6	26	3	4	853	3	54	1028
8	37	32	24	76	16	30	29	31	668	31	974
9	14	18	6	22	150	18	17	91	21	652	1009
10	1094	1405	879	1056	1041	706	1005	1096	829	889	10000

```
In [7]: binary_classifier = classifier(256)
        binary_classifier.train(train_image, train_label)
```

```
In [8]: y = binary_classifier.predict(train_image)
        binary_classifier.evaulation(y, train_label)
```

True Possitive: 0.88595  
Error Rate: 0.11405

```
Out [8]:
```

	0	1	2	3	4	5	6	7	8	9	10
0	5645	2	15	23	16	49	101	11	50	11	5923
1	1	6600	28	21	15	20	12	15	24	6	6742
2	67	169	5087	124	95	31	99	118	138	30	5958
3	49	92	182	5222	26	150	56	101	158	95	6131
4	12	70	31	4	5205	21	85	19	21	374	5842
5	115	74	45	287	106	4355	155	60	136	88	5421
6	56	58	42	7	47	115	5562	6	22	3	5918
7	36	132	66	24	128	18	11	5583	17	250	6265
8	49	247	86	198	70	204	66	44	4750	137	5851
9	41	47	23	95	259	42	17	220	57	5148	5949
10	6071	7491	5605	6005	5967	5005	6164	6177	5373	6142	60000

```
In [9]: y = binary_classifier.predict(test_image)
        binary_classifier.evaulation(y, test_label)
```

True Possitive: 0.8955  
Error Rate: 0.1045

```
Out [9]:
```

	0	1	2	3	4	5	6	7	8	9	10
0	945	1	6	1	0	9	10	2	5	1	980
1	0	1120	2	3	0	2	4	0	4	0	1135
2	16	24	879	25	12	5	19	16	35	1	1032
3	4	9	27	892	2	21	7	18	22	8	1010
4	0	10	6	0	876	2	22	4	3	59	982
5	12	10	6	47	12	718	27	24	26	10	892
6	14	10	4	0	14	15	899	1	1	0	958
7	3	27	21	4	6	0	2	912	4	49	1028
8	9	25	11	23	15	34	16	6	823	12	974
9	13	11	3	14	42	2	3	21	9	891	1009
10	1016	1247	965	1009	979	808	1009	1004	932	1031	10000

```
In [10]: binary_classifier = classifier(1024)
         binary_classifier.train(train_image, train_label)
```

```
In [11]: y = binary_classifier.predict(train_image)
         binary_classifier.evaulation(y, train_label)
```

True Possitive: 0.9479666666666666  
Error Rate: 0.052033333333333334

```
Out [11]:
```

	0	1	2	3	4	5	6	7	8	9	10
0	5801	2	14	5	7	9	31	5	44	5	5923
1	0	6636	36	13	16	5	2	9	16	9	6742
2	31	34	5588	50	48	6	35	62	84	20	5958
3	8	21	83	5698	8	95	16	49	99	54	6131
4	6	31	15	3	5551	5	33	7	20	171	5842
5	33	19	17	96	30	5024	86	13	63	40	5421
6	32	18	9	2	15	53	5754	0	35	0	5918
7	15	58	47	12	57	7	4	5938	14	113	6265
8	15	66	53	78	30	94	44	15	5389	67	5851
9	25	13	12	73	118	39	4	118	48	5499	5949
10	5966	6898	5874	6030	5880	5337	6009	6216	5812	5978	60000

```
In [12]: y = binary_classifier.predict(test_image)
         binary_classifier.evaulation(y, test_label)
```

True Possitive: 0.9443  
Error Rate: 0.0557

```
Out [12]:
```

	0	1	2	3	4	5	6	7	8	9	10
0	961	0	2	0	0	3	7	3	4	0	980
1	0	1122	2	3	1	0	3	0	4	0	1135
2	9	1	958	13	5	1	9	11	22	3	1032
3	0	0	10	951	1	12	1	11	17	7	1010
4	1	5	4	0	921	1	8	2	4	36	982

5	3	2	0	24	6	826	10	5	10	6	892
6	7	2	1	0	7	7	927	1	6	0	958
7	1	16	15	2	11	0	2	952	4	25	1028
8	5	2	6	22	3	11	9	8	901	7	974
9	7	7	1	7	23	14	2	16	8	924	1009
10	994	1157	999	1022	978	875	978	1009	980	1008	10000

In [ ]: