

HW #6

Brian Hert  
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csc 137

6.1 Calculate the required maximum clock frequency for each of the following data Paths:

a) Single-Cycle data Path in Fig. 6.2.

$$\begin{aligned} &= \text{Adder} + \text{Adder} + \text{Adder/Subtractor} + T_{sa} + T_{ca} + T_{cs} \\ &= 0.8 \text{ ns} + 0.8 \text{ ns} + 1.1 \text{ ns} + 0.05 \text{ ns} + 0.05 \text{ ns} + 0.05 \text{ ns} \\ &= 2.85 \text{ ns} \end{aligned}$$

$$\begin{aligned} \text{maximum} &= 1 / \text{Longest Path Delay} \\ \text{Frequency} &= 1 / 2.85 \text{ ns} \cdot 10^9 \text{ ns} / \text{Hz} \\ &= 350,877,192.987 \text{ Hz} \\ &= \boxed{350 \text{ MHz}} \end{aligned}$$

b) multi-cycle Path in Fig. 6.3

$$\begin{aligned} &= \text{max } 1 + \text{adder} + 1 \text{ Subtractor} + \text{max } 2 + T_{sa} + T_{ca} + T_{cs} \\ &= 0.6 \text{ ns} + 1.1 \text{ ns} + 0.3 \text{ ns} + (0.05 \text{ ns} \times 3) \\ &= 2.15 \text{ ns} \end{aligned}$$

$$\begin{aligned} \text{c) maximum frequency} &= 1 / 2.15 \text{ ns} \\ &= 1 / 2.15 \text{ ns} \cdot 10^9 \text{ ns} / \text{Hz} \\ &= 465,116,279.06977 \text{ Hz} \\ &= \boxed{465.12 \text{ MHz}} \end{aligned}$$

c) Pipelined data Path in Fig 6.4

= Adder / Subtractor + Register

=  $1.1\text{ns} + 0.15\text{ns}$

=  $1.25\text{ns}$

$$\begin{aligned}\text{Maximum Frequency} &= 1 / 1.25\text{ns} \\ &= 1 / 1.25\text{ns} \cdot 10^9\text{ns} / \text{Hz} \\ &= 800,000,000 \text{ Hz} \\ &= \boxed{800 \text{ MHz}} \quad \checkmark\end{aligned}$$

6.2 Estimate the speedup between the following data paths when generating  $W=1000$  quantities  $A_i + B_i + C_i \pm D_i$  for  $i=0, 1, 2, \dots, 999$ .  $K=3$ ; Ignore the data reading and writing delays.

a) Problem 6.1a vs 6.1c

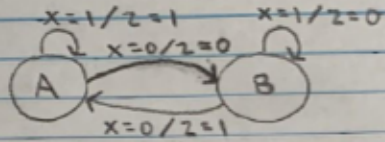
$$\text{Speedup} = \frac{N \cdot K}{K + (N-1)}$$

$$= \frac{1000 \cdot 3}{3 + (1000-1)}$$

$$= \frac{3000}{1002}$$

$$= \boxed{2.994} \quad \checkmark$$

5.1



Number of Bits =  $\log_2(2) = 1$

	A	$q_0$	X	$d_0$	Z
0	A	0	0	1	0
1	B	0	1	0	1
2	B	1	0	0	1
3	A	1	1	1	0



$$d_0 = \overline{q_0} \overline{X} + q_0 X = q_0 \oplus X$$

$$z = \overline{q_0} X + q_0 \overline{X} = q_0 \oplus X$$

