

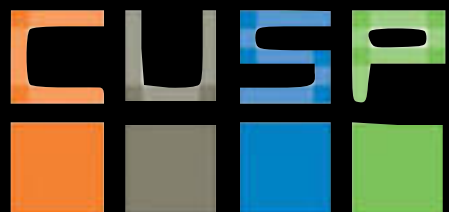
Urban Informatics

Fall 2018

dr. federica bianco fbianco@nyu.edu



@fedhere



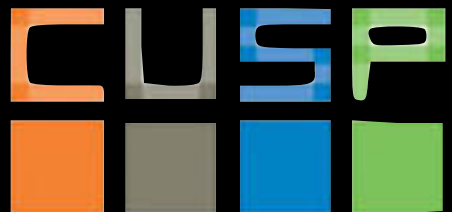
X: decision trees

Recap:

- Good practices with data: falsifiability, reproducibility
- Basic data retrieving and munging: APIs, Data formats
- SQL
- Basic statistics: distributions and their moments
- Hypothesis testing: p -value, statistical significance
- Statistical and Systematic errors
- Visualizations
- Geospatial analysis
- OLS
- Goodness of fit tests
- Likelihood

Today:

- decision and regression trees (CART)
- topics in Time Series Analysis



X: decision trees

machine learning

models with parameters that are “learned” from the data



machine learning

models with parameters that are “learned” from the data

parameters that are optimized based on the data



machine learning

algorithms that can learn from and make predictions on data.

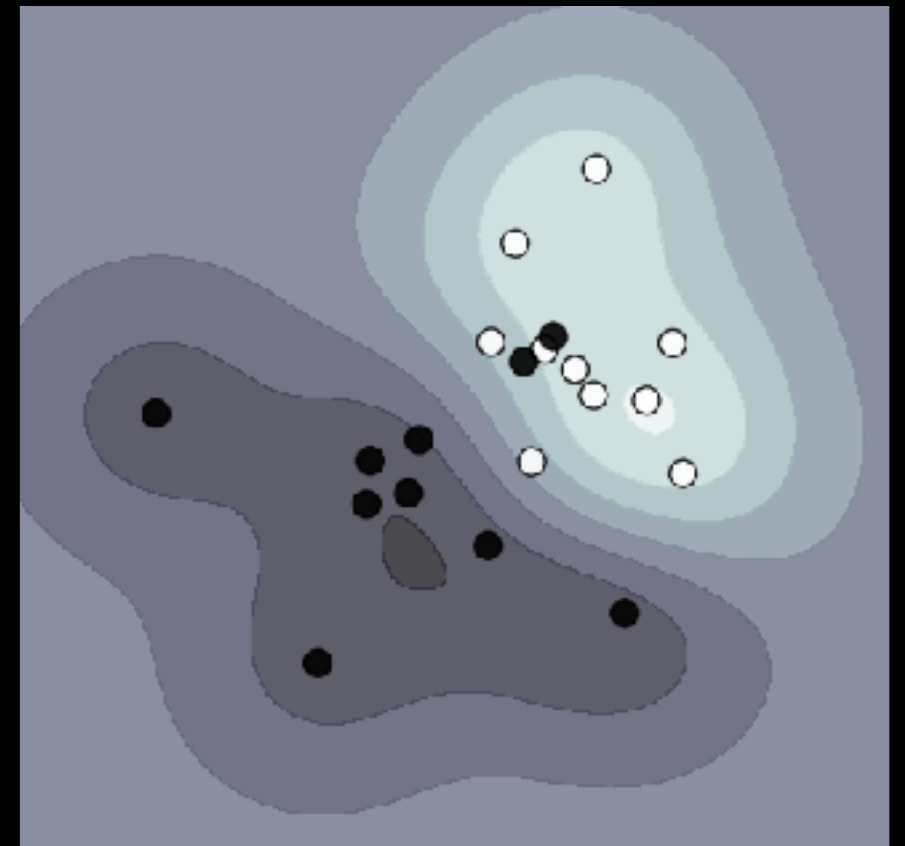
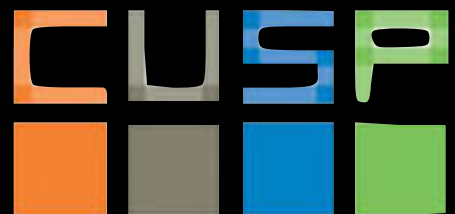


machine learning

algorithms that can learn from and make predictions on data.



supervised learning
extract features and create
models that allow
prediction where the
correct answer is known for
a subset of the data



XI: Clustering

machine learning

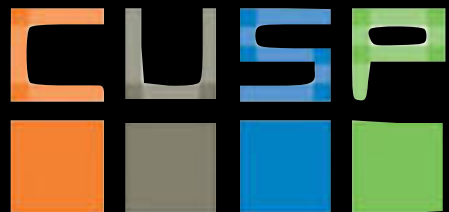
algorithms that can learn from and make predictions on data.



supervised learning
extract features and create
models that allow
prediction where the
correct answer is known for
a subset of the data



unsupervised learning
identify features and create
models that allow to
understand structure in the
data



machine learning

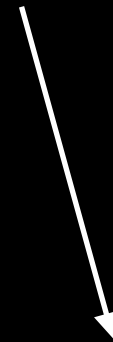
algorithms that can learn from and make predictions on data.



supervised learning

classification

prediction

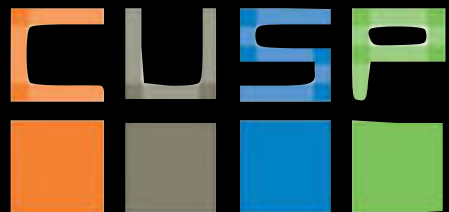


unsupervised learning

understanding structure

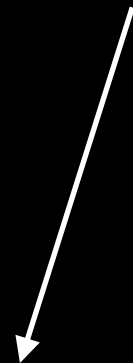
organizing + compressing data

(classification, feature learning)



machine learning

algorithms that can learn from and make predictions on data.



supervised learning

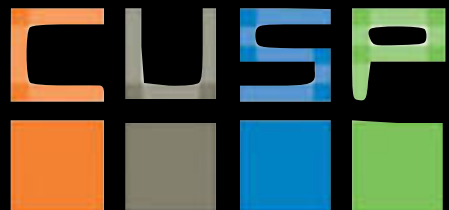
classification

prediction

LR, SVM

CART

DL



unsupervised learning

understanding structure

organizing + compressing data

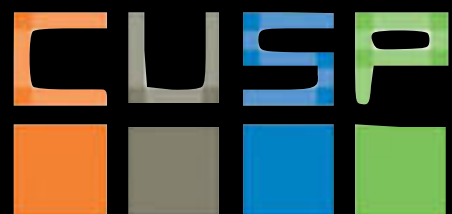
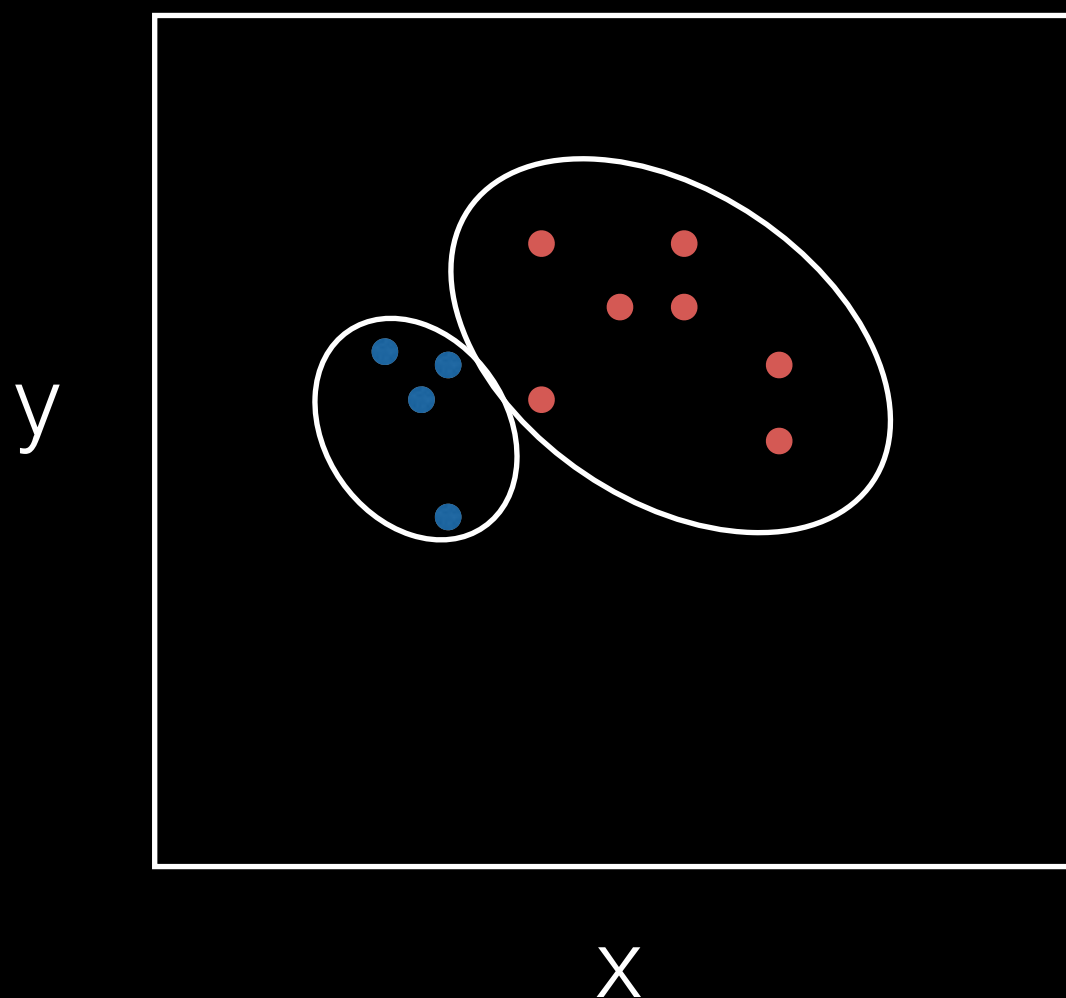
(classification, feature learning)

CLUSTERING

XI: Clustering

Supervised Learning

observed:
(x, y, color)

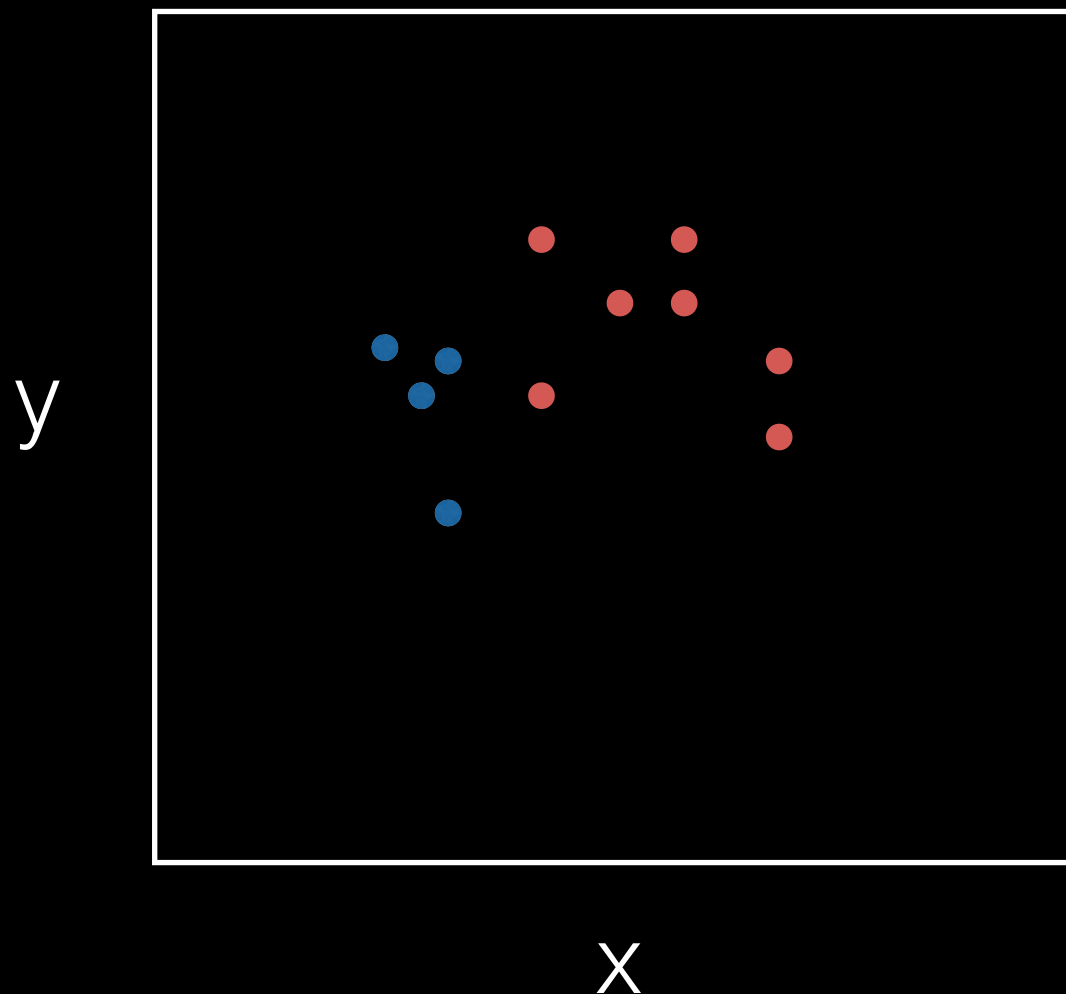


X: decision trees

Partitioning methods: classifying (SVM, CART)

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)

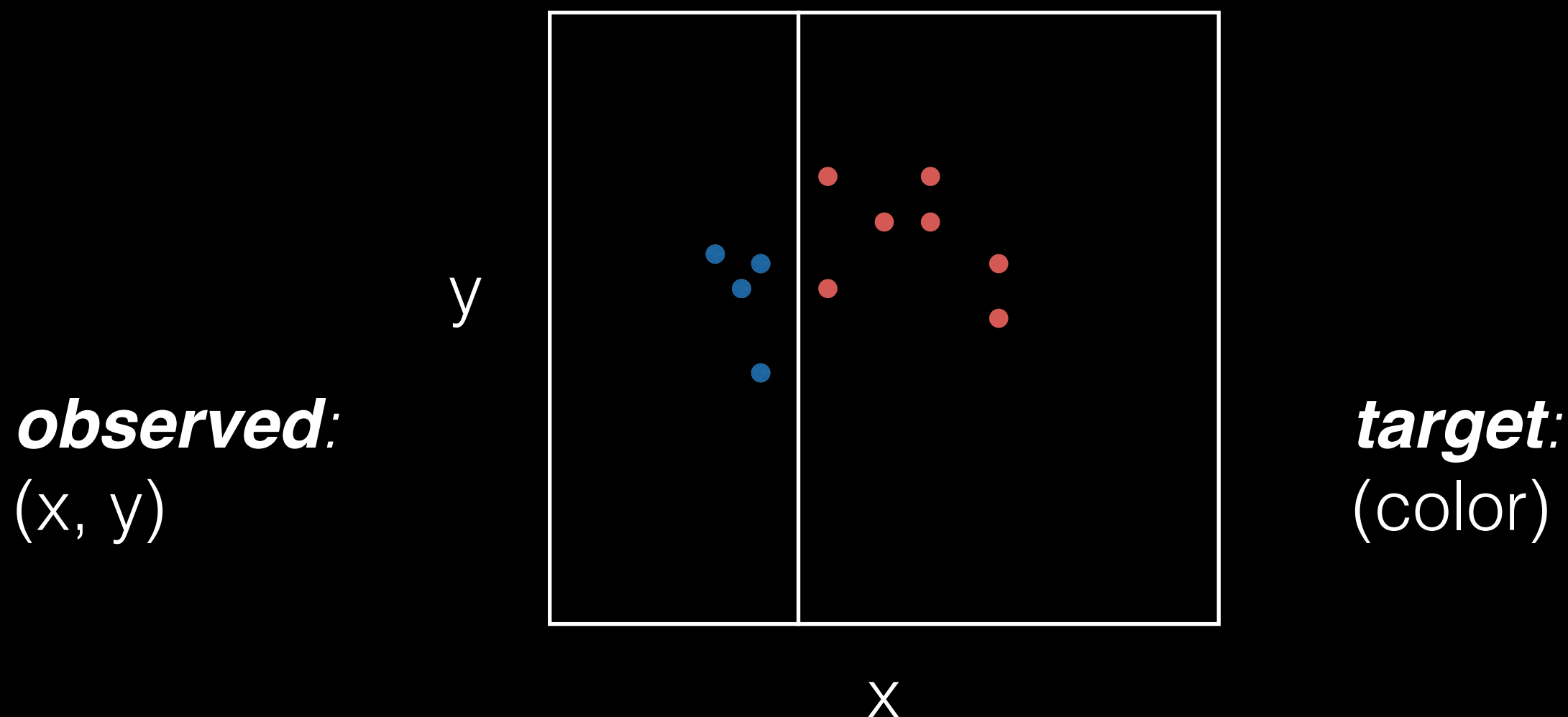
observed:
(x, y)



target:
(color)

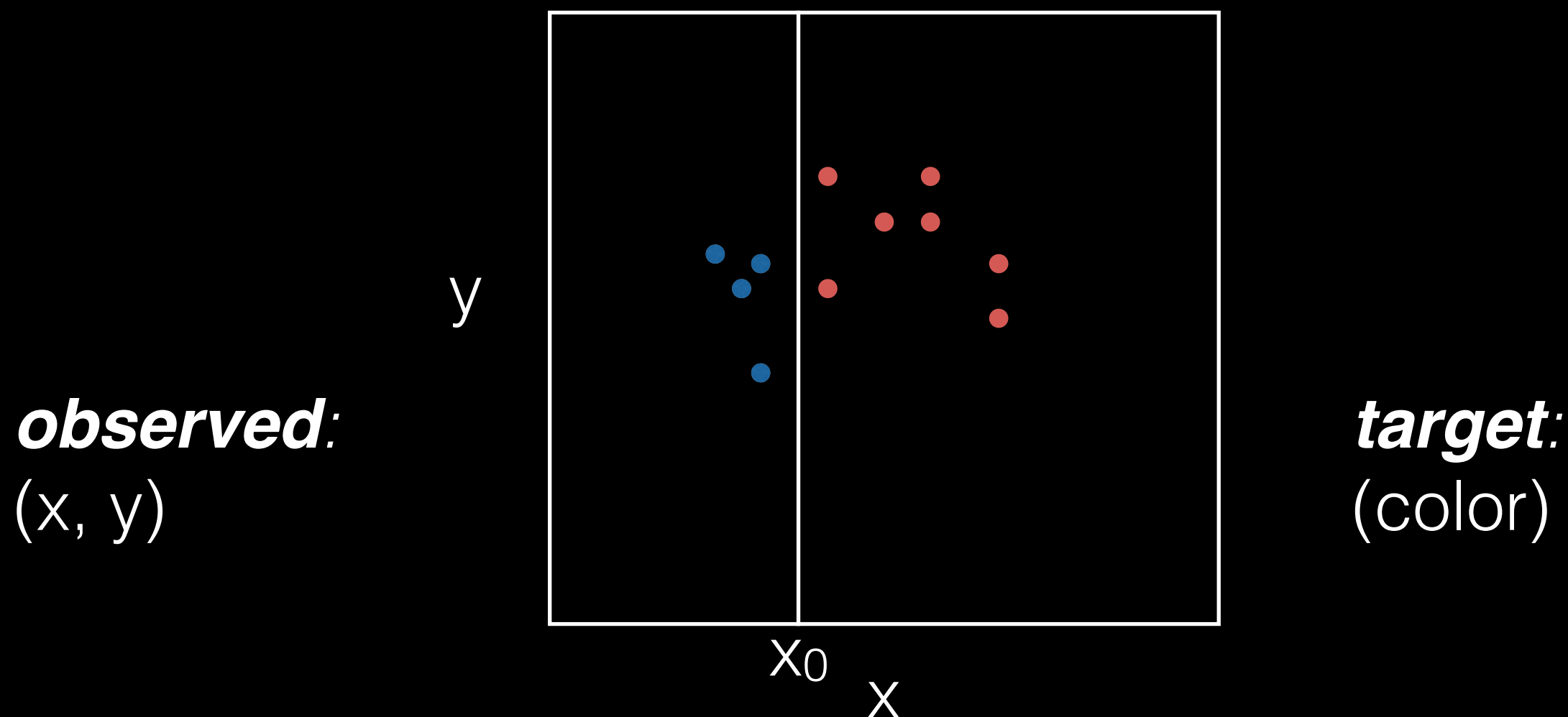
Partitioning methods: classifying

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)

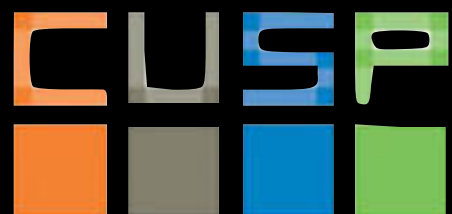


Partitioning methods: classifying

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)



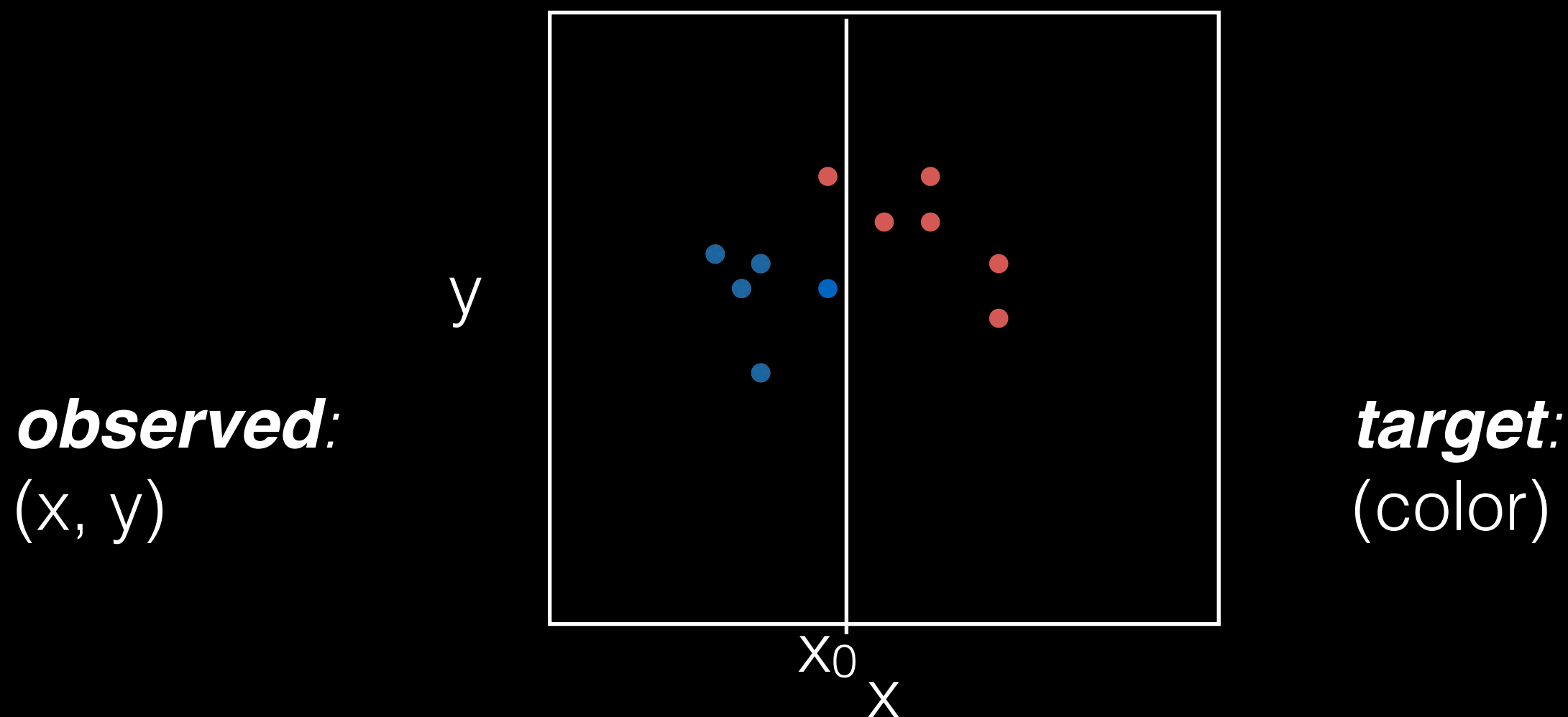
if $x > x_0 \Rightarrow$ ball is red



X: decision trees

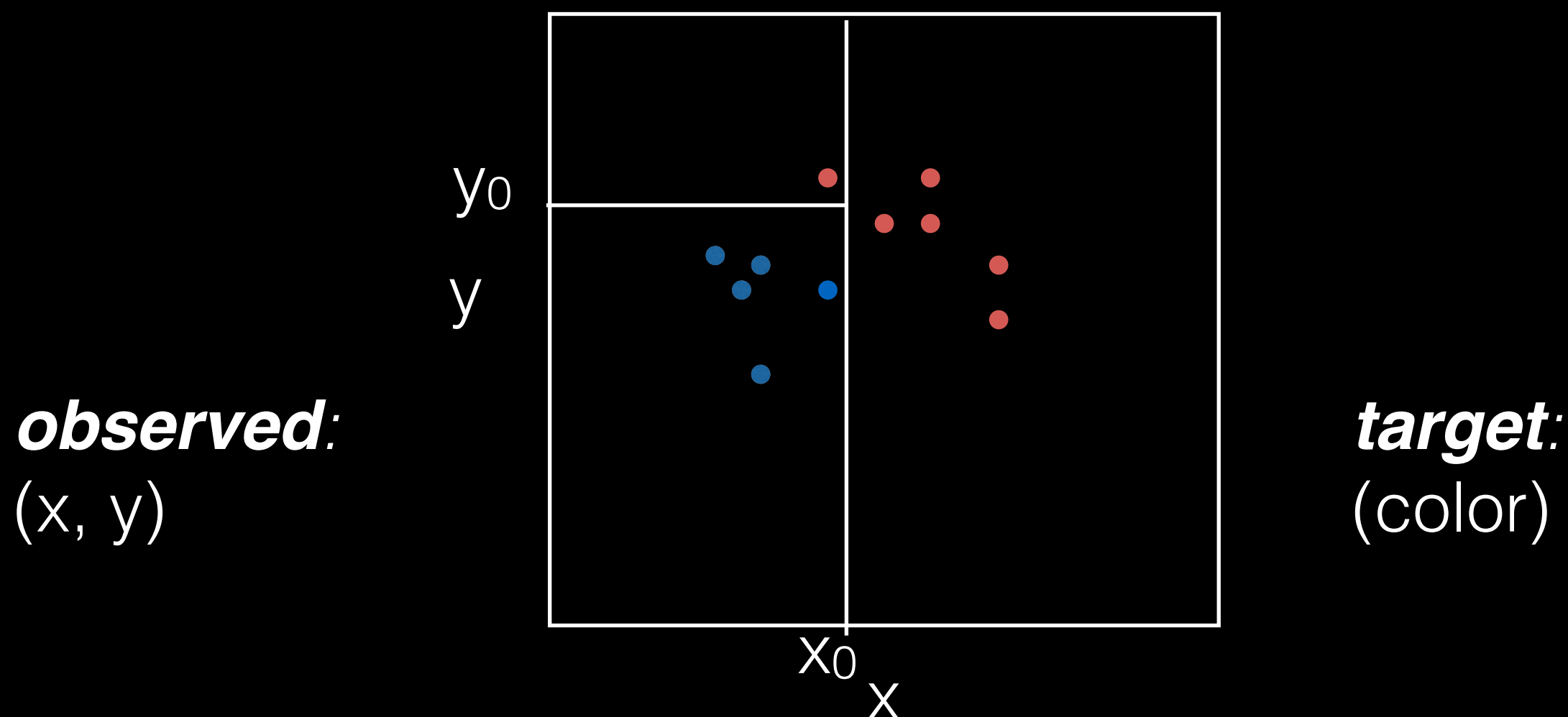
Partitioning methods: classifying

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)

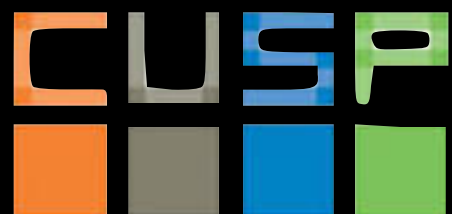


Partitioning methods: classifying

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)



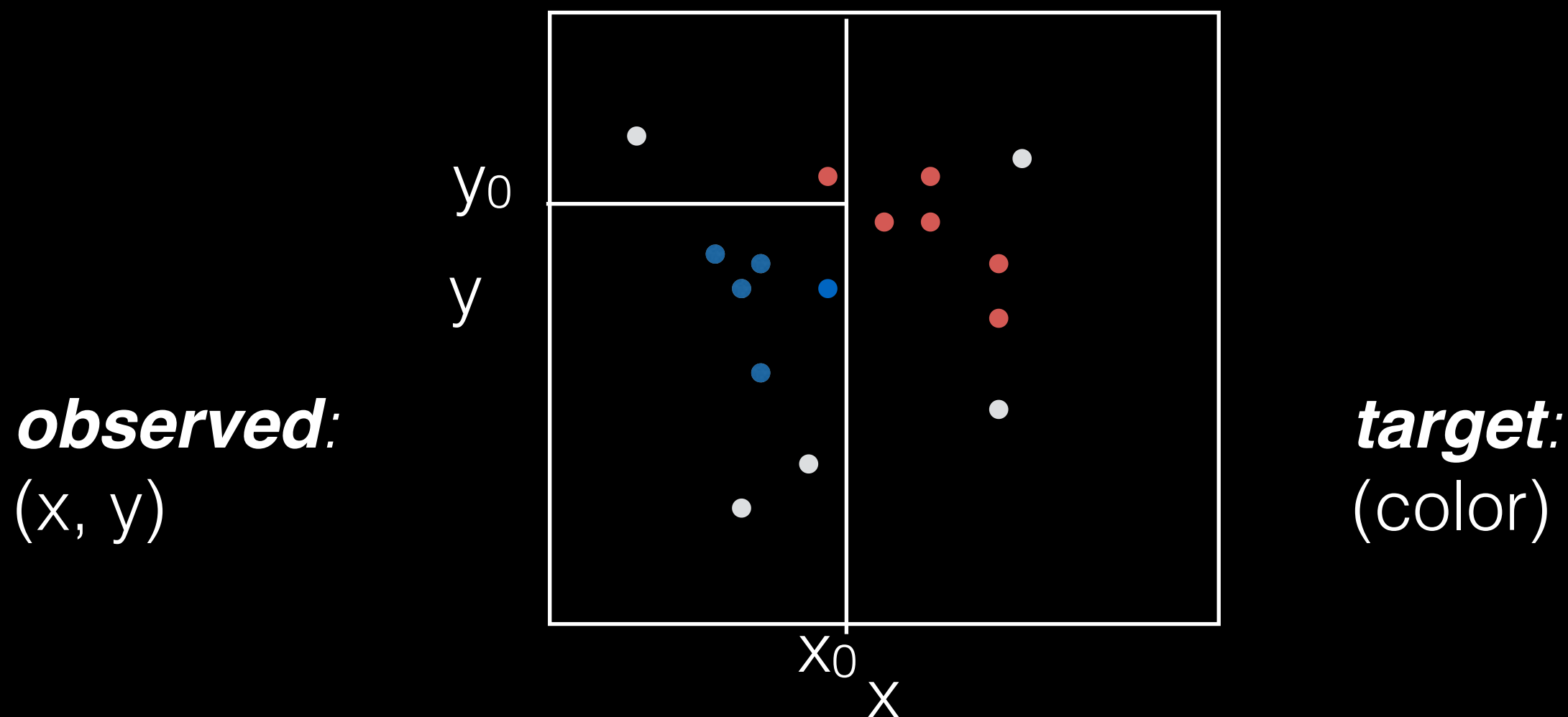
if $x > x_0$ or $y > y_0 \Rightarrow$ ball is red



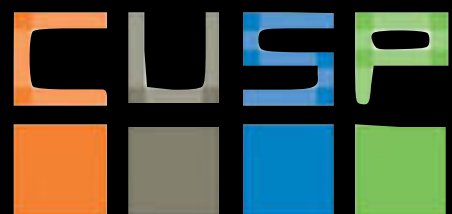
X: decision trees

Partitioning methods: classifying

goal is to partition the space of observed variables
to separate the space of unobserved (target variables)



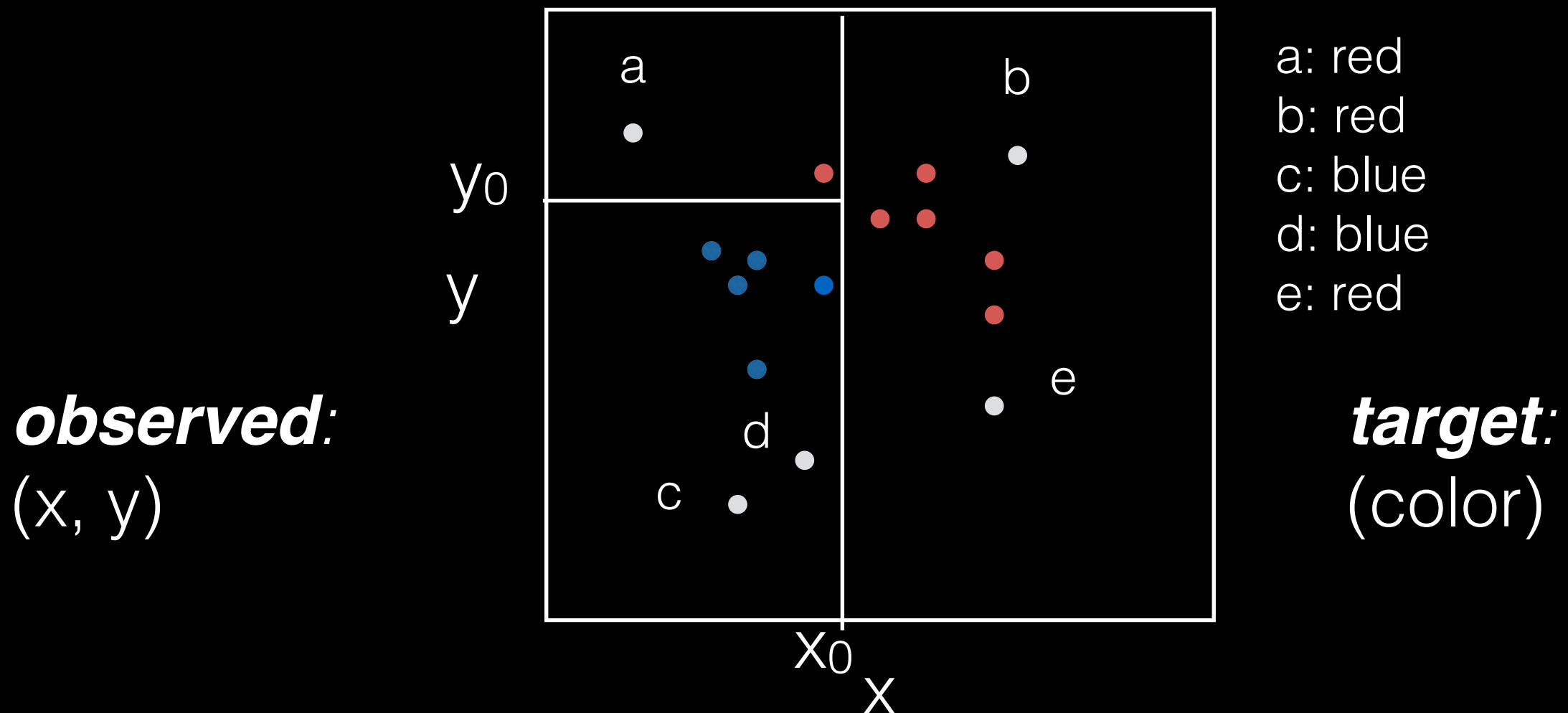
if $x > x_0$ or $y > y_0 \Rightarrow$ ball is red



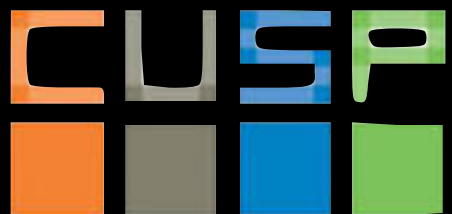
X: decision trees

Partitioning methods: classifying

goal is to partition the space of observed variables to separate the space of unobserved (target variables)

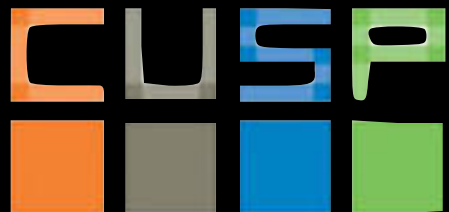


if $x > x_0$ or $y > y_0 \Rightarrow$ ball is red



X: decision trees

Decision Trees



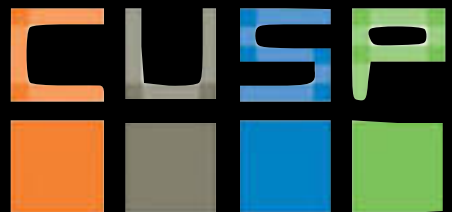
X: decision trees

The good

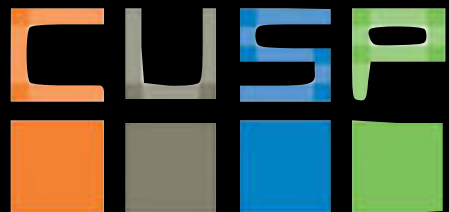
- Non-Parametric
- White-box: can be easily interpreted
- Works with any feature type and mixed feature types
- Works with missing data
- Robust to outliers

The bad

- High variability (-> use *ensemble* methods)
- Tendency to overfit
- (not as easily interpretable after all...)



a single tree



X: decision trees

714 passengers
 $N_s=424$ $N_d=290$

Application:
a robot to predict
surviving the
Titanic (Kaggle)

features:

gender

ticket class

age

target variable:

survival (y/n)

 N_s : survived
 N_d : died

714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

gender (binary)

M

Ns=93 Nd=360

F

Ns=197 Nd=64

features: purity 79%

purity 75%

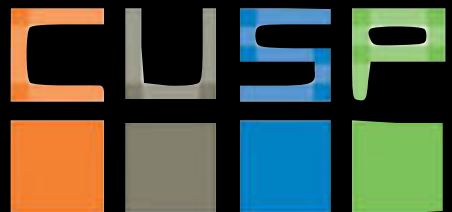
gender 79/75%

ticket class

age

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

class (categorical)

1st

Ns=471 Nd=242

2nd,3rd

Ns=335 Nd=378

features: purity 66%

purity 44%

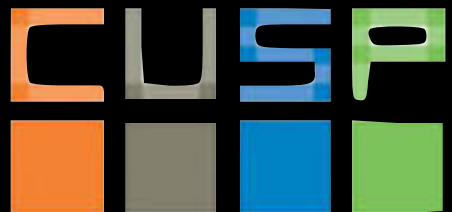
gender 79/75%

ticket class 66/44%

age

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

age (continuous)

<6.5

Ns=500 Nd=214

purity 30%

>6.5

Ns=278 Nd=435

purity 70%

features:

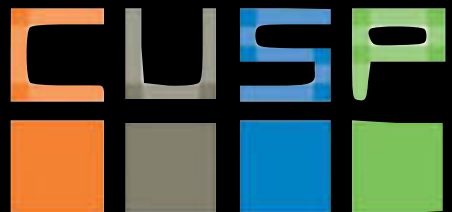
gender 79/75%

ticket class 66/44%

age 30/70%

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

age (continuous)

M

Ns=93 Nd=360

purity 79%

F

Ns=197 Nd=64

purity 75%

features:

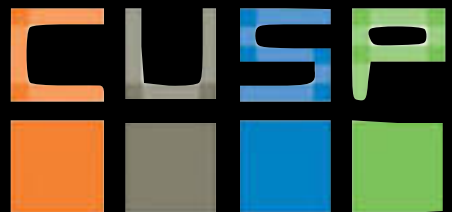
gender 79/75%

age 66/44%

ticket class 30/70%

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

gender (binary)

M

Ns=93 Nd=360

purity 79%

F

Ns=197 Nd=64

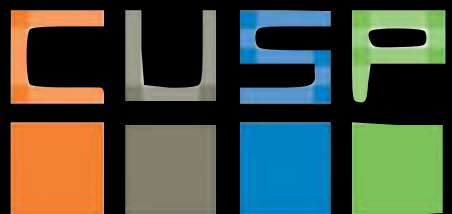
purity 75%

features:

gender 79/75%

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

gender (binary)

M

Ns=93 Nd=360

purity 79%

F

Ns=197 Nd=64

purity 75%

features:

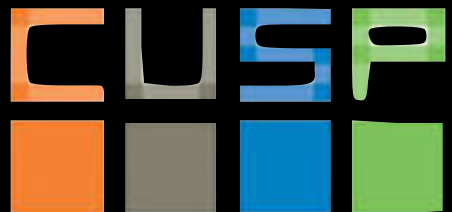
gender 79/75%

age: M 74/67% F 96/40%

ticket class: M 40/15% F 96/65%

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

gender (binary)

M

Ns=93 Nd=360

purity 79%

F

Ns=197 Nd=64

purity 75%

features:

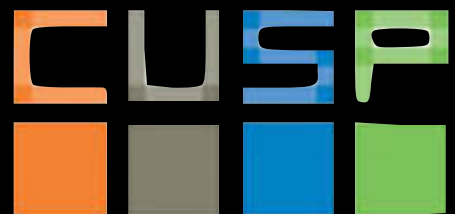
gender 79/75%

age: M 67/82% F 74/76%

ticket class: M 40/15% F 96/65%

target variable:

survival (y/n)



714 passengers
Ns=424 Nd=290

Application:
a robot to predict
surviving the
Titanic (Kaggle)

gender (binary)

M

Ns=93 Nd=360
purity 79%

F

Ns=197 Nd=64
purity 75%

age (continuous)

>6.5

Ns=77 Nd=352
purity 82%

<6.5

Ns=16 Nd=8
purity 67%

class (ordinal 1,2,3)

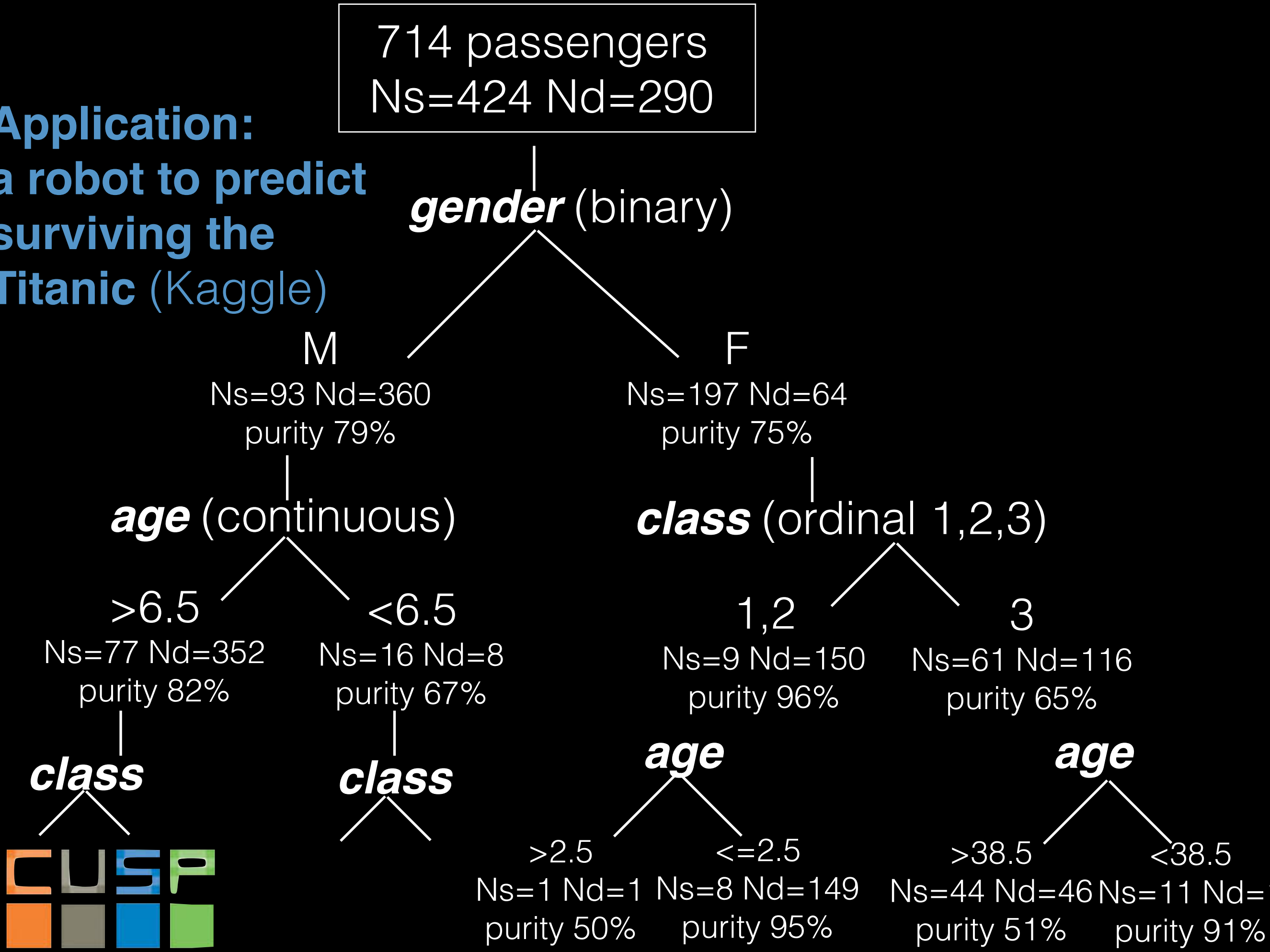
1

Ns=82 Nd=3
purity 96%

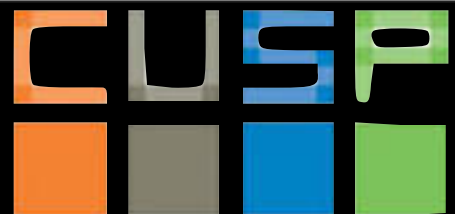
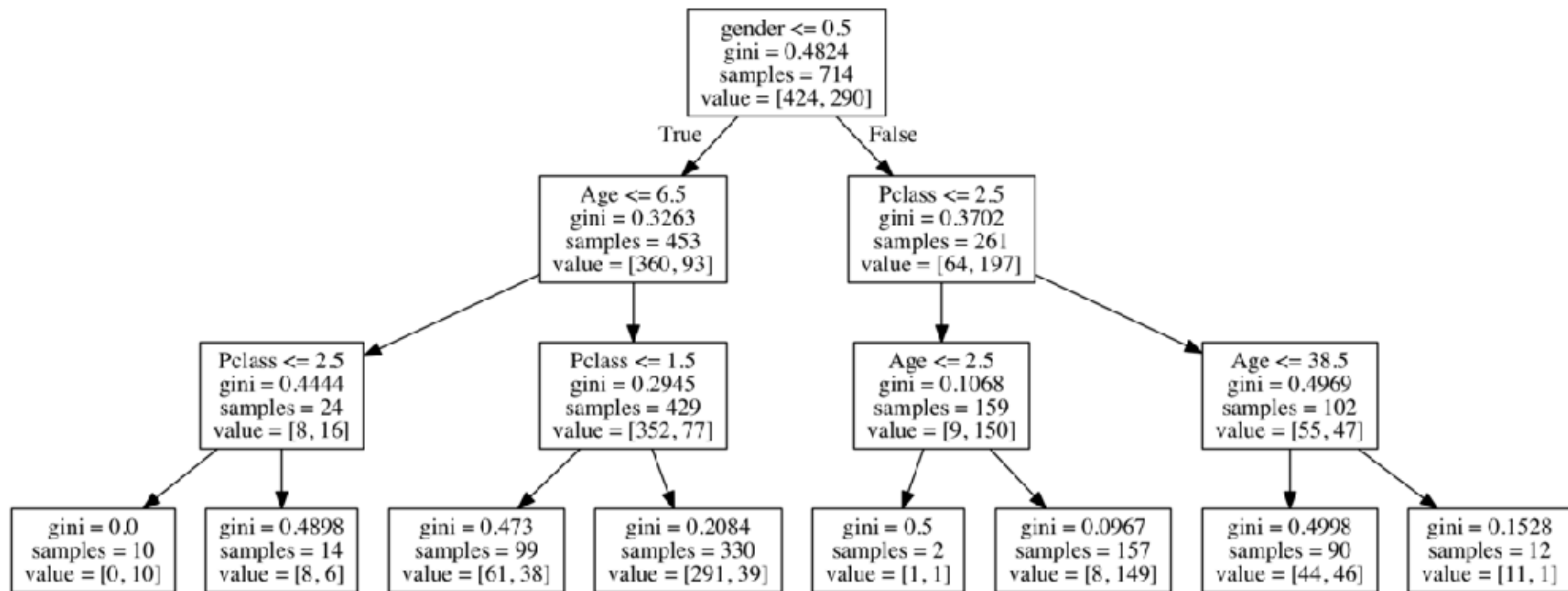
2,3

Ns=114 Nd=62
purity 65%

Application:
a robot to predict
surviving the
Titanic (Kaggle)



Application: a robot to predict surviving the Titanic (Kaggle)



https://github.com/fedhere/PUI2017_fb55/blob/master/Lab12_fb55/TitanicByCART.ipynb

Application: a robot to predict surviving the Titanic (Kaggle)

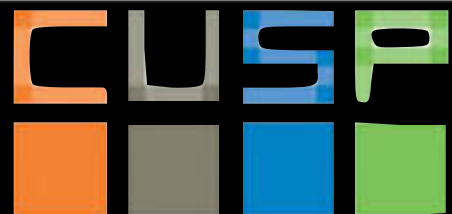
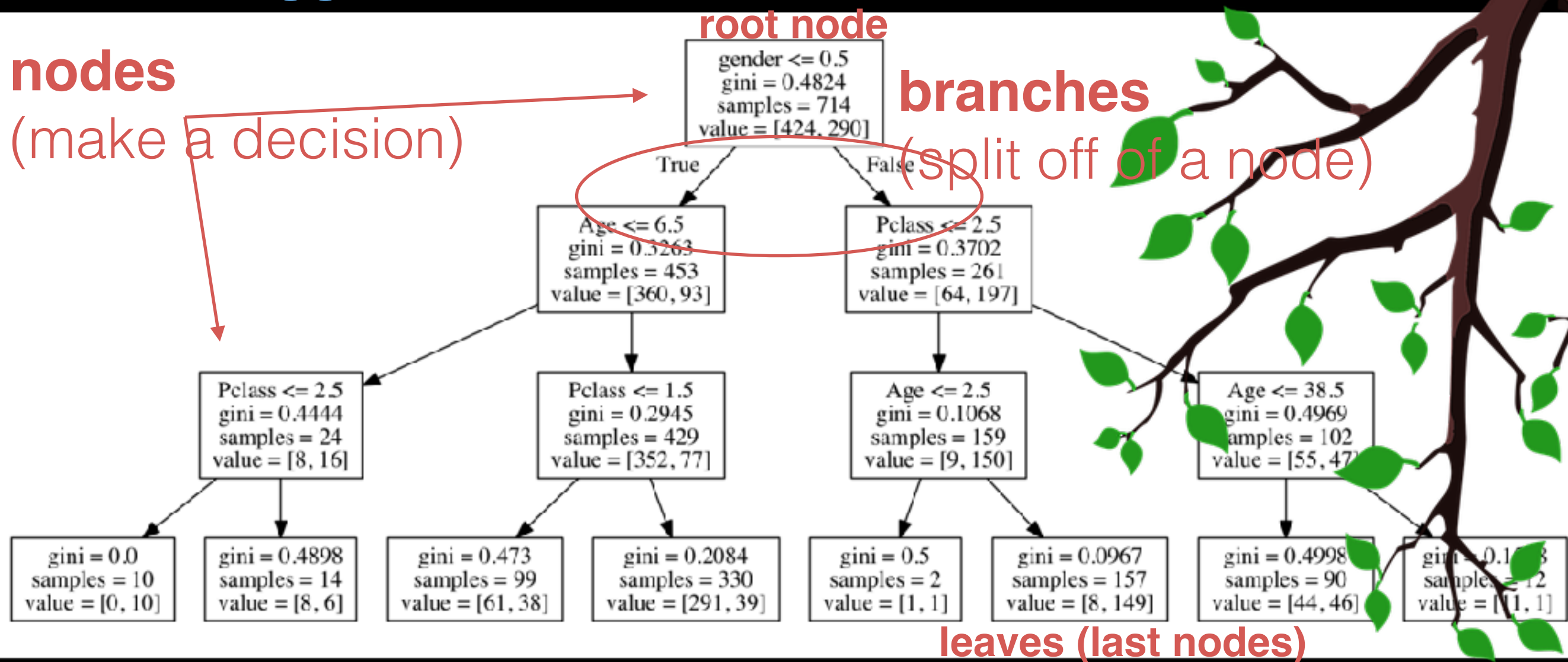
nodes

(make a decision)

root node

branches

(split off of a node)



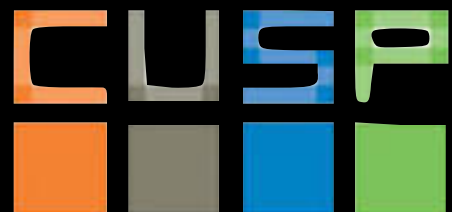
https://github.com/fedhere/PUI2017_fb55/blob/master/Lab12_fb55/TitanicByCART.ipynb

a single tree

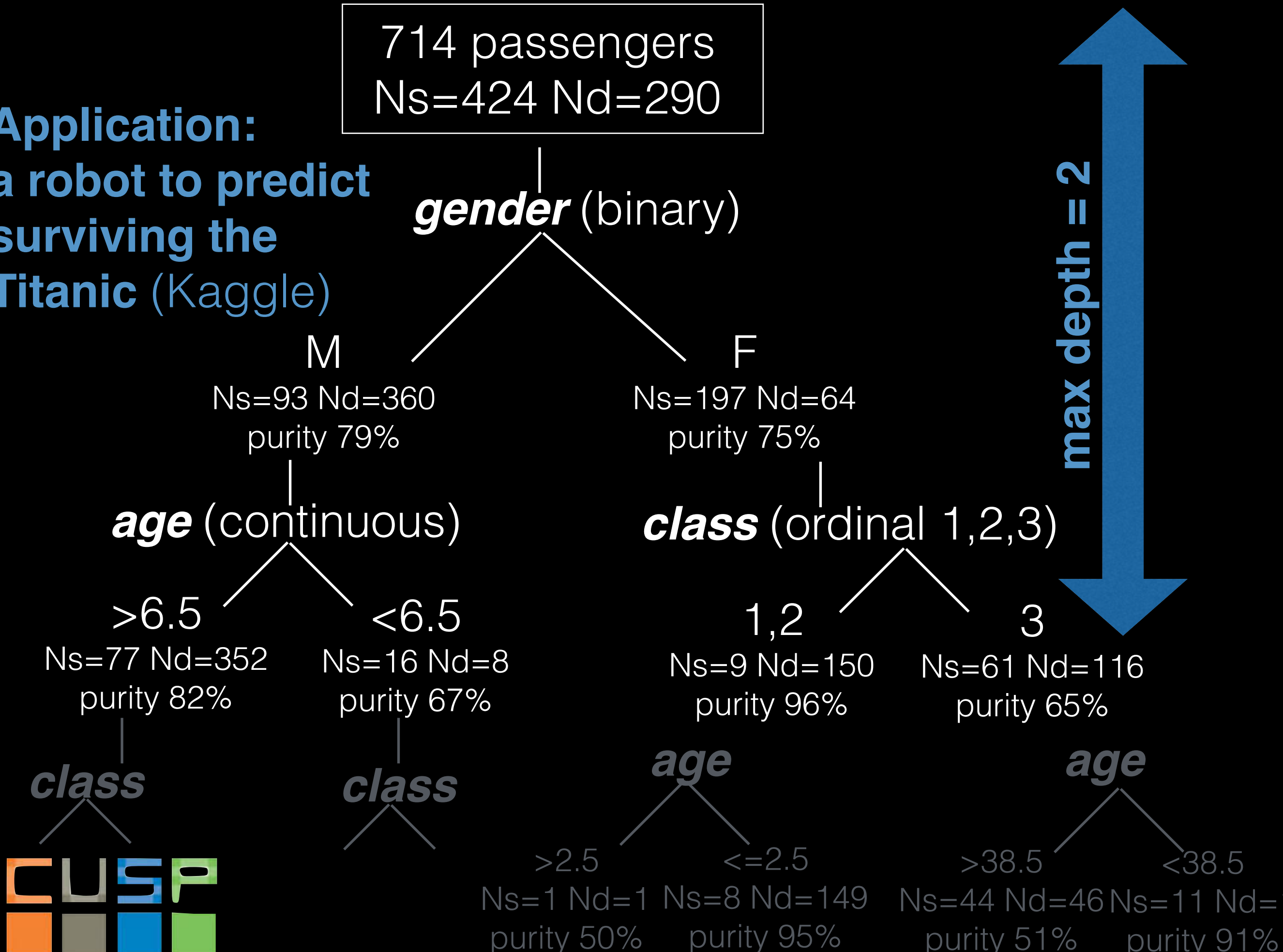
parameters:

maximum depth (controls overfitting)

maximization scheme

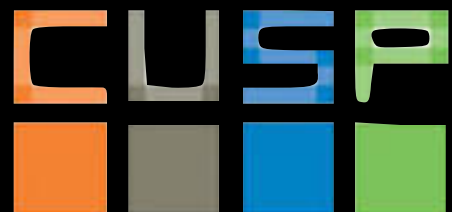


Application:
a robot to predict
surviving the
Titanic (Kaggle)



parameters:
maximum depth (controls overfitting)
maximization scheme

<https://scikit-learn.org/stable/modules/generated/sklearn.ensemble.RandomForestClassifier.html>



X: decision trees

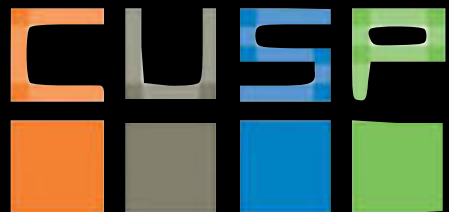
a single tree

parameters:

maximum depth (controls overfitting)

maximization scheme

gini, entropy (information content), variance...

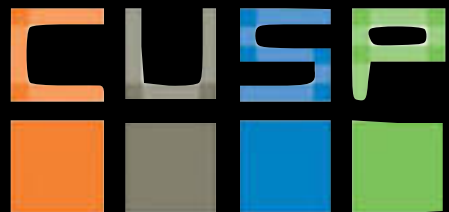


a single tree

issues :

variance - different trees lead to different results

solution : a forest



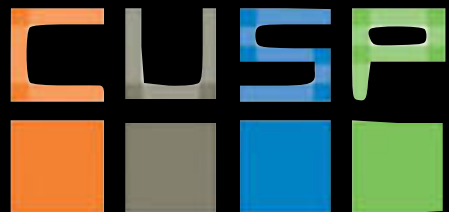
a single tree

issues :

variance - different trees lead to different results

solution : a forest

- run many tree models,
- look at the ensemble result



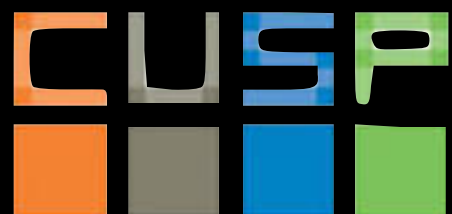
Ensemble methods:

Random forest:

- trees run in parallel (independently of each other)
- each tree uses a random subset of observations/features (bootstrap - bagging)
- class predicted by *majority vote*: what class do most trees think a point belong to?

Gradient boosted trees:

- trees run in series (one after the other)
- each tree uses different weights for the features learning the weights from the previous tree
- the last tree has the prediction



Ensemble methods:

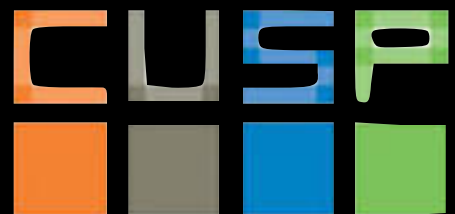
Random forest:

- trees run in parallel (independently of each other)
- each tree uses a random subset of observations/features (bootstrap - bagging)
- class predicted by *majority vote*: what class do most trees think a point belong to?

Gradient boosted trees:

- trees run in series (one after the other)
- each tree uses different weights for the features learning the weights from the previous tree
- the last tree has the prediction

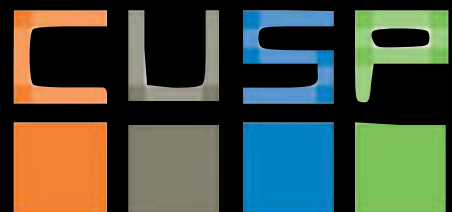
More parameters:



- BOTH: depth, criterion, min sample to split, min sample in leaf
- RF: number of trees, number of features/tree
- GB: loss function, learning rate, number of boosts

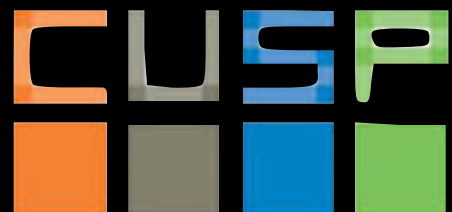
How good is my model?

https://scikit-learn.org/stable/modules/model_evaluation.html



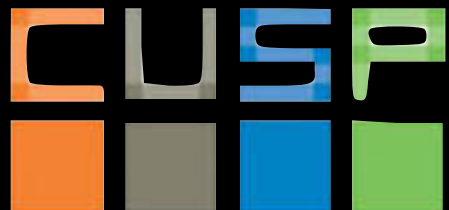
X: decision trees

	H_0 is True	H_0 is False
H_0 is falsified	Type I error False Positive important message gets spammed	True Positive
H_0 is not falsified	True Negative	Type II error False negative Spam in your Inbox



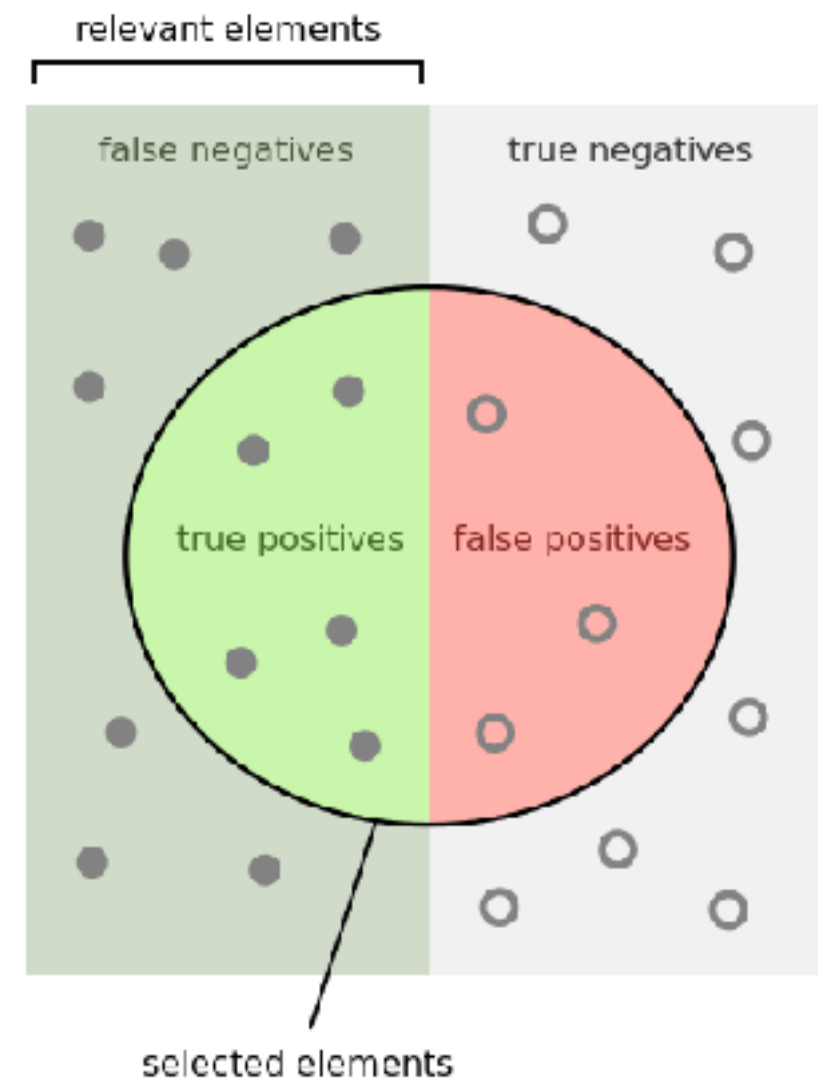
$$\text{LR} = \frac{\text{False Negative}}{\text{True Negative}}$$

	<i>H</i> ₀ is True	<i>H</i> ₀ is False
<i>H</i> ₀ is falsified	Type I error False Positive important message gets spammed	True Positive
<i>H</i> ₀ is not falsified	True Negative	Type II error False negative Spam in your Inbox

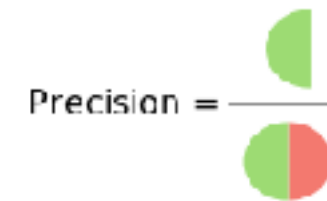


$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$



How many selected items are relevant?



$$\text{Precision} = \frac{\text{True Positives}}{\text{True Positives} + \text{False Positives}}$$

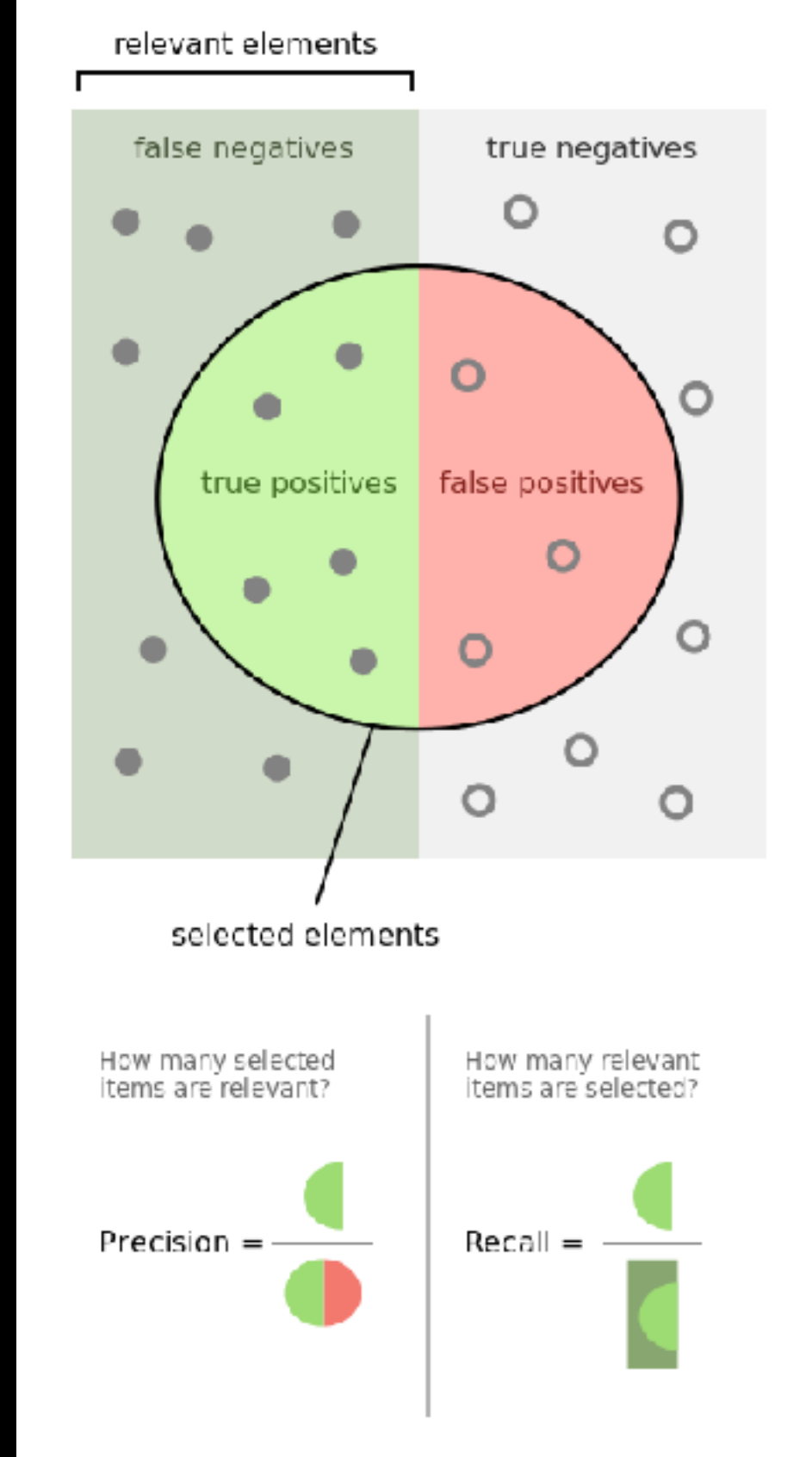
How many relevant items are selected?



$$\text{Recall} = \frac{\text{True Positives}}{\text{True Positives} + \text{False Negatives}}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$



$$\text{Accuracy} = \frac{TP+TN}{TP+TN+FP+FN}$$



1.10.7.1. Classification criteria

If a target is a classification outcome taking on values $0, 1, \dots, K-1$, for node m , representing a region R_m with N_m observations, let

$$p_{mk} = 1/N_m \sum_{x_i \in R_m} I(y_i = k)$$

Common measures of impurity are Gini

$$H(X_m) = \sum_k p_{mk}(1 - p_{mk})$$

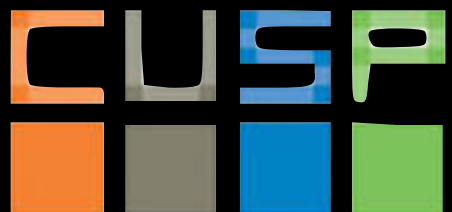
Cross-Entropy

$$H(X_m) = \sum_k p_{mk} \log(p_{mk})$$

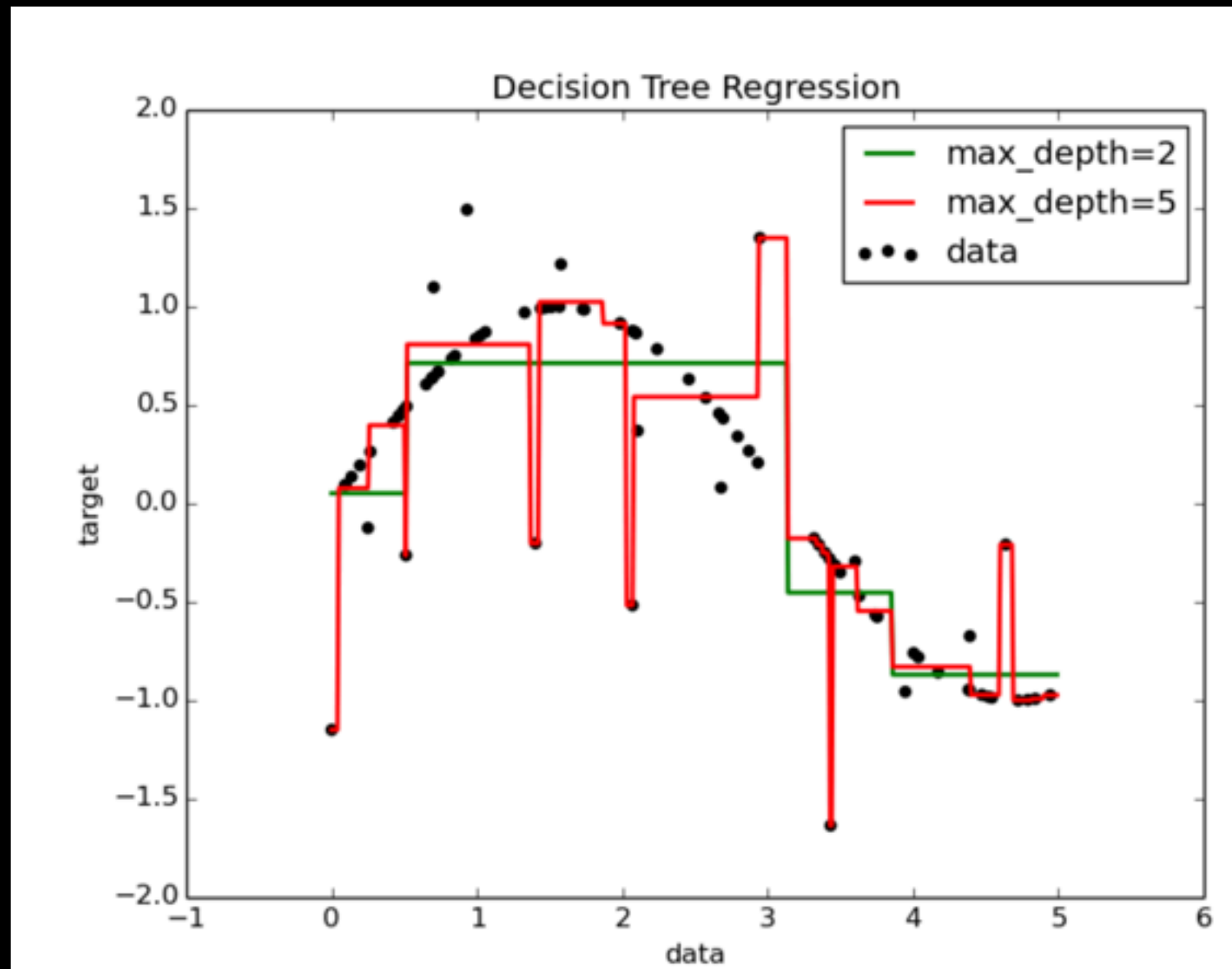
and Misclassification

$$H(X_m) = 1 - \max(p_{mk})$$

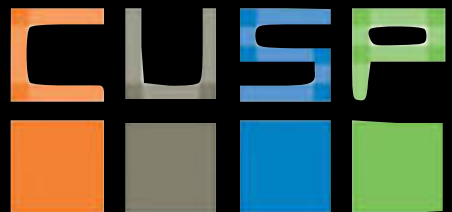
<http://scikit-learn.org/0.16/modules/tree.html#tree-algorithms-id3-c4-5-c5-0-and-cart>



Regression Trees

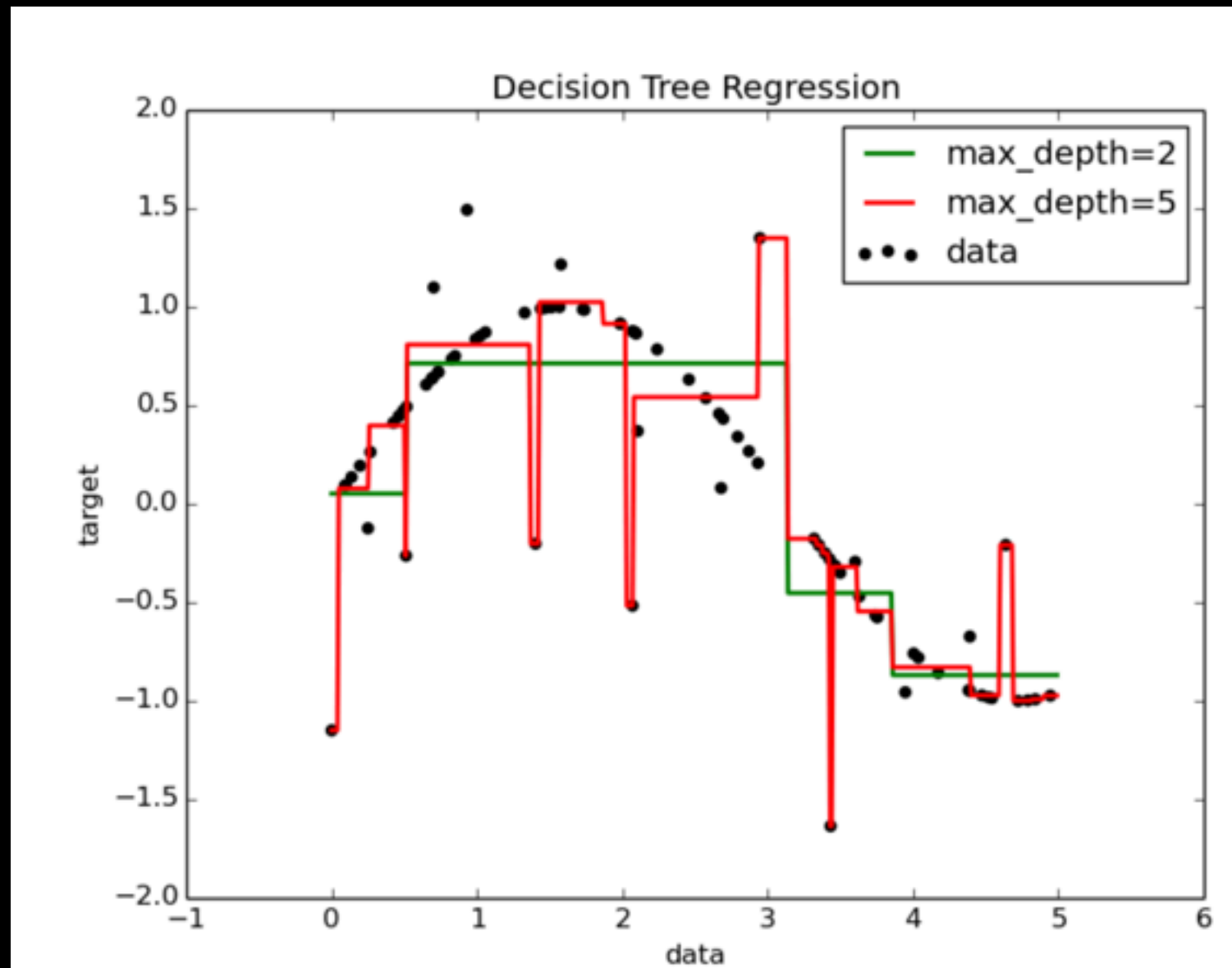


<http://scikit-learn.org/0.16/modules/tree.html#tree-algorithms-id3-c4-5-c5-0-and-cart>



Regression Trees

$$c_m = \frac{1}{N_m} \sum_{i \in N_m} y_i$$
$$H(X_m) = \frac{1}{N_m} \sum_{i \in N_m} (y_i - c_m)^2$$

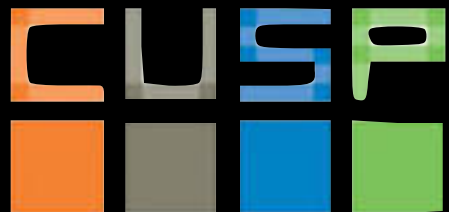


How good is my model?

https://scikit-learn.org/stable/modules/model_evaluation.html

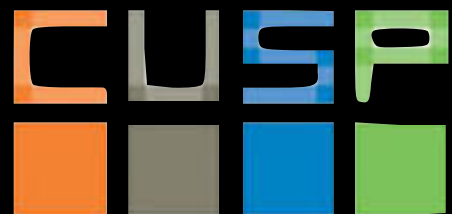
Is my model overfitting?

cross validation:



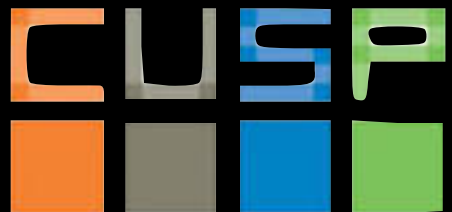
X: decision trees

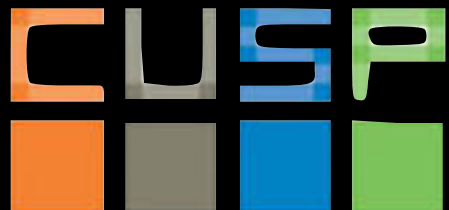
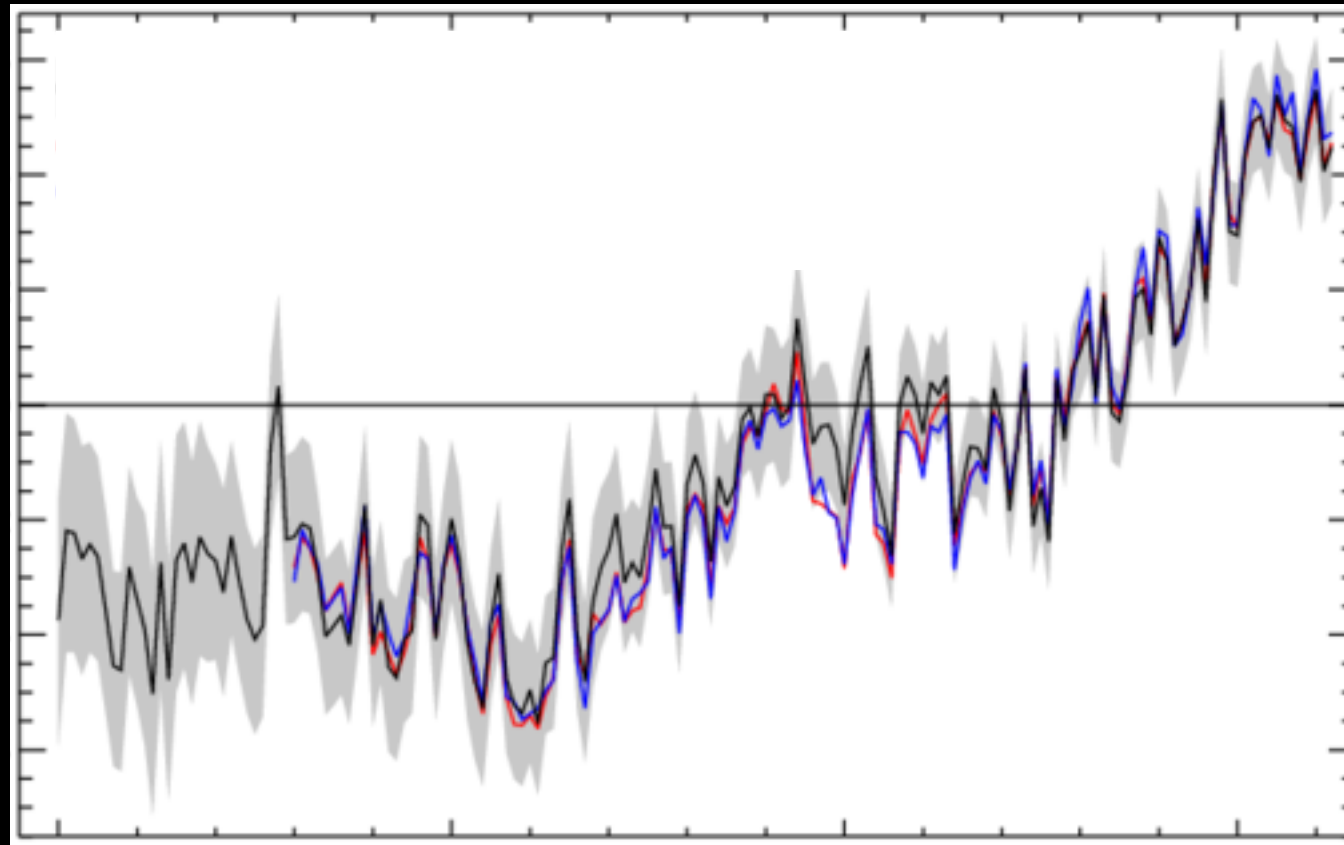
super important missing topic:
pruning!
when is my tree overfitting?

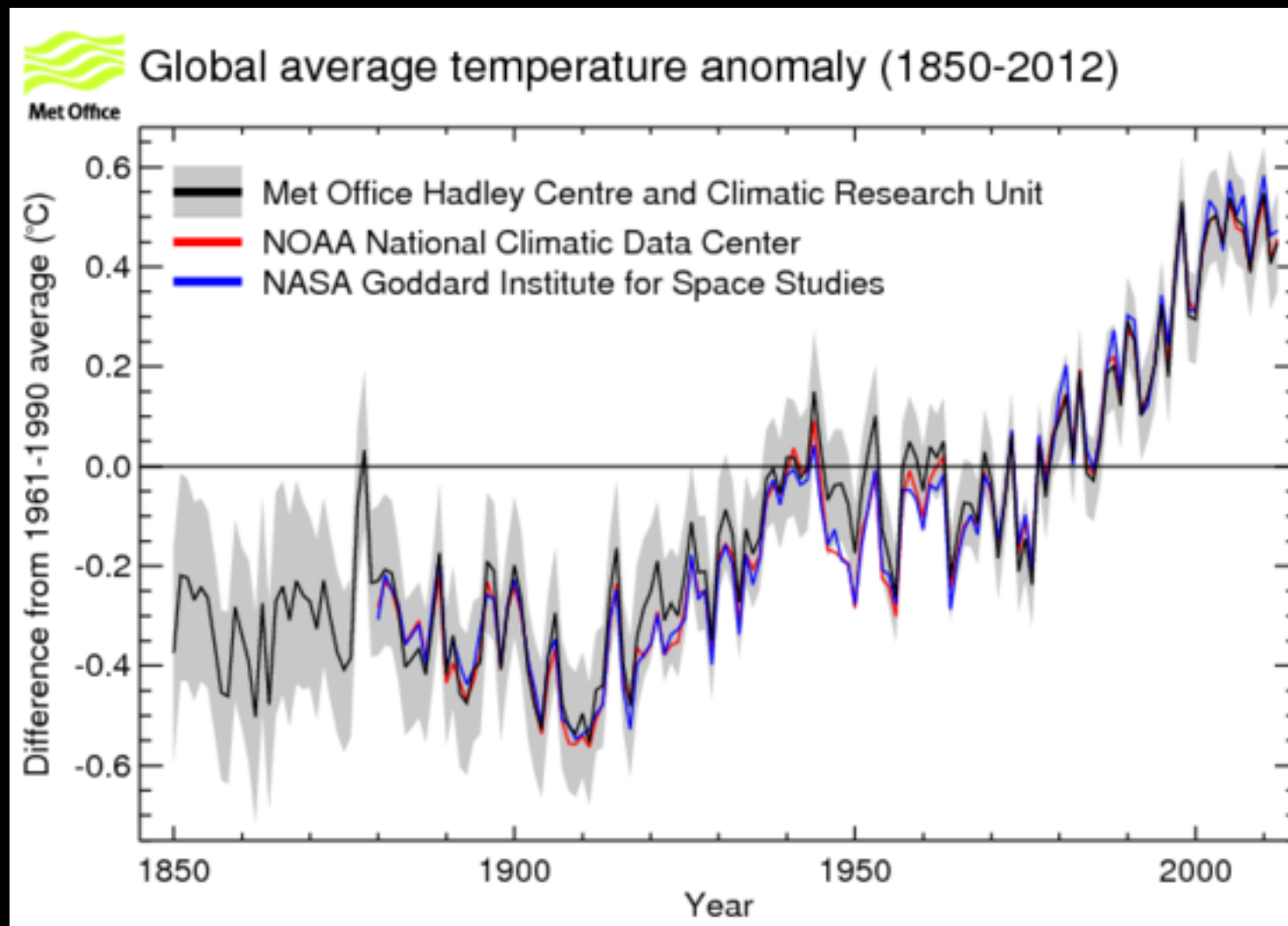


Topics in (time) series analysis

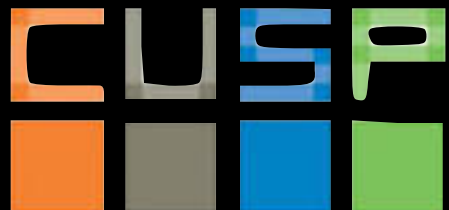
- smoothing
- de-trending
- event detection
- period finding (Fourier analysis)
- clustering (including anomaly detection)

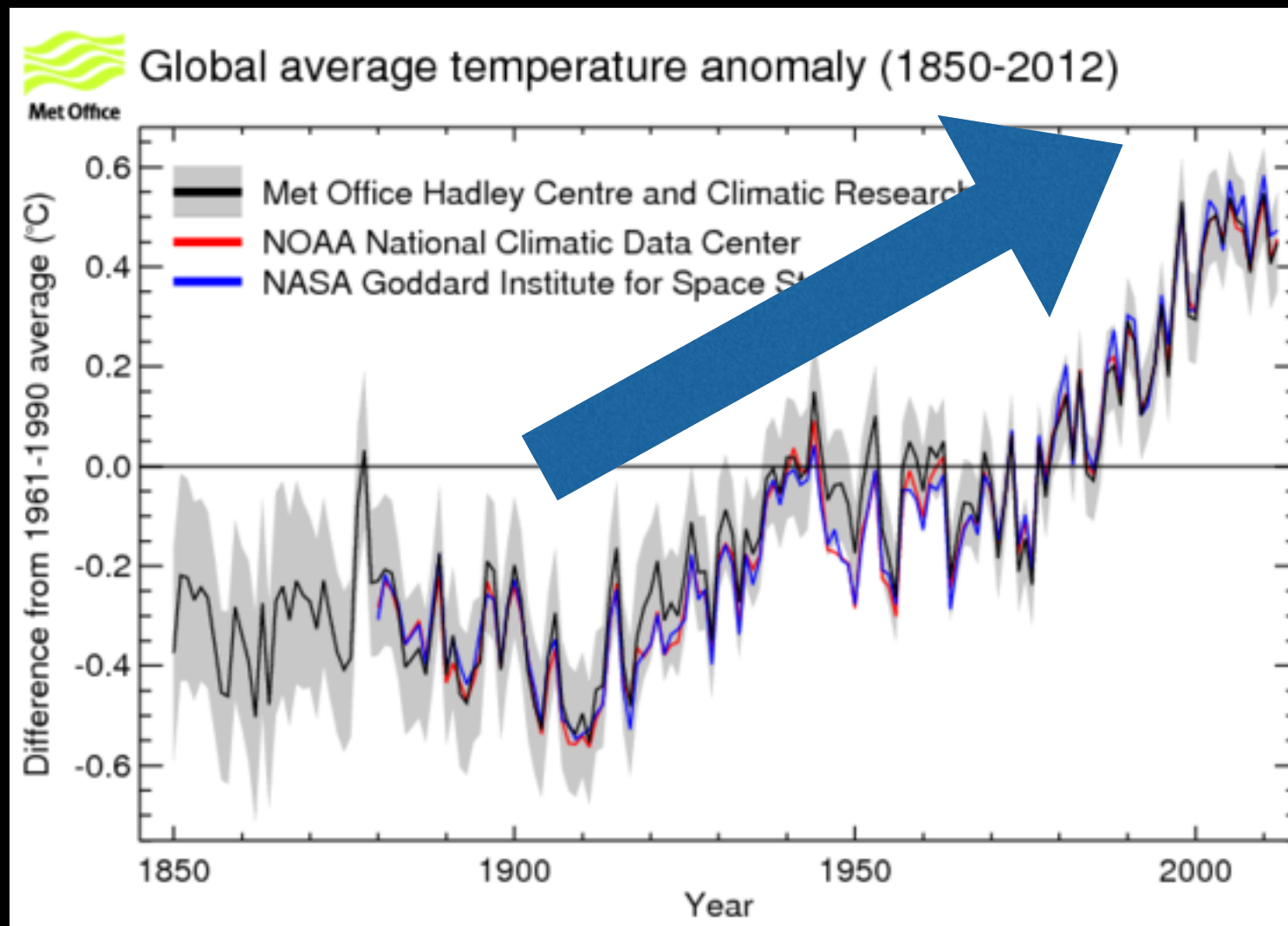




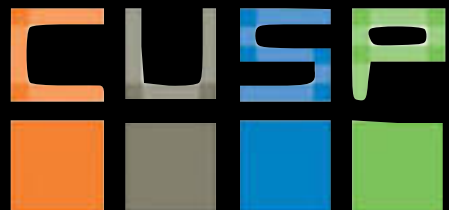


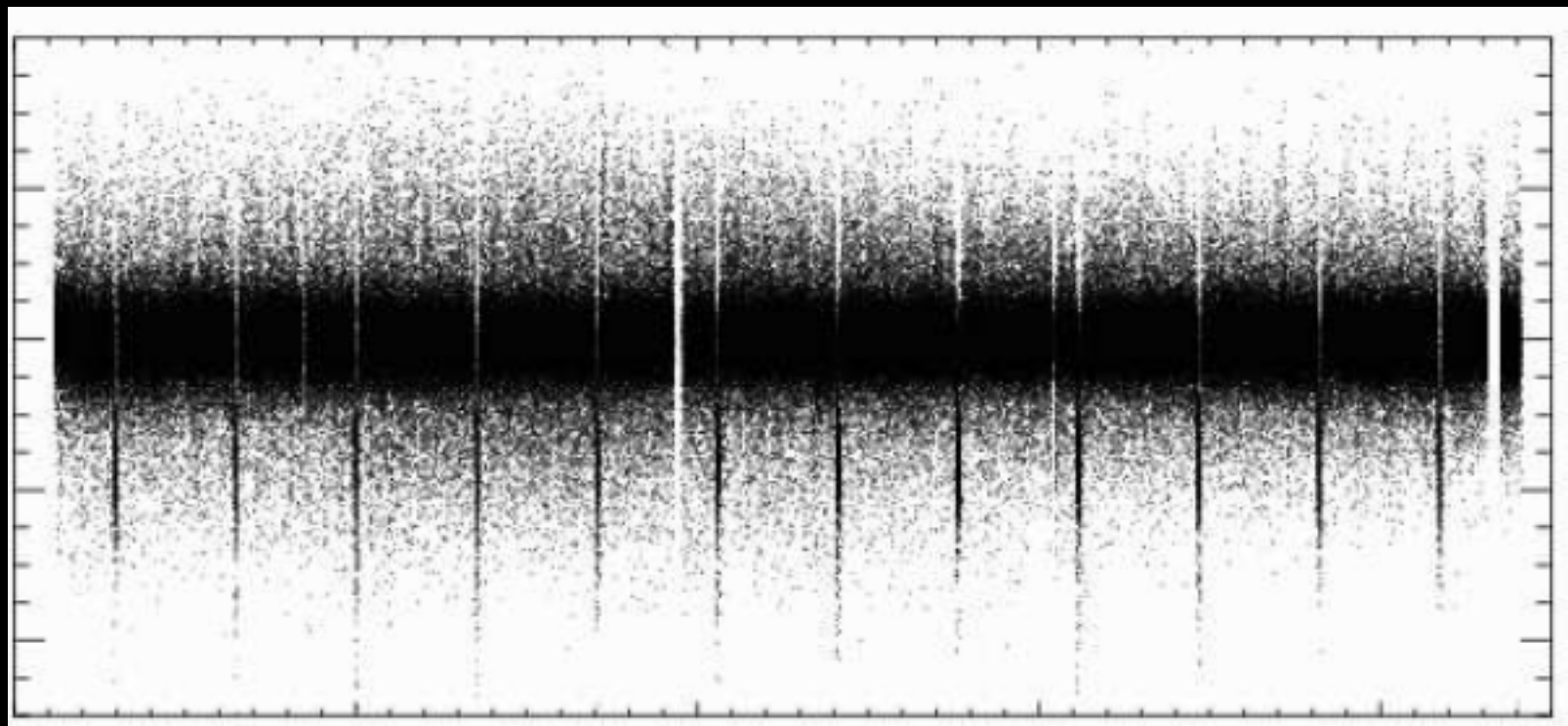
Trend

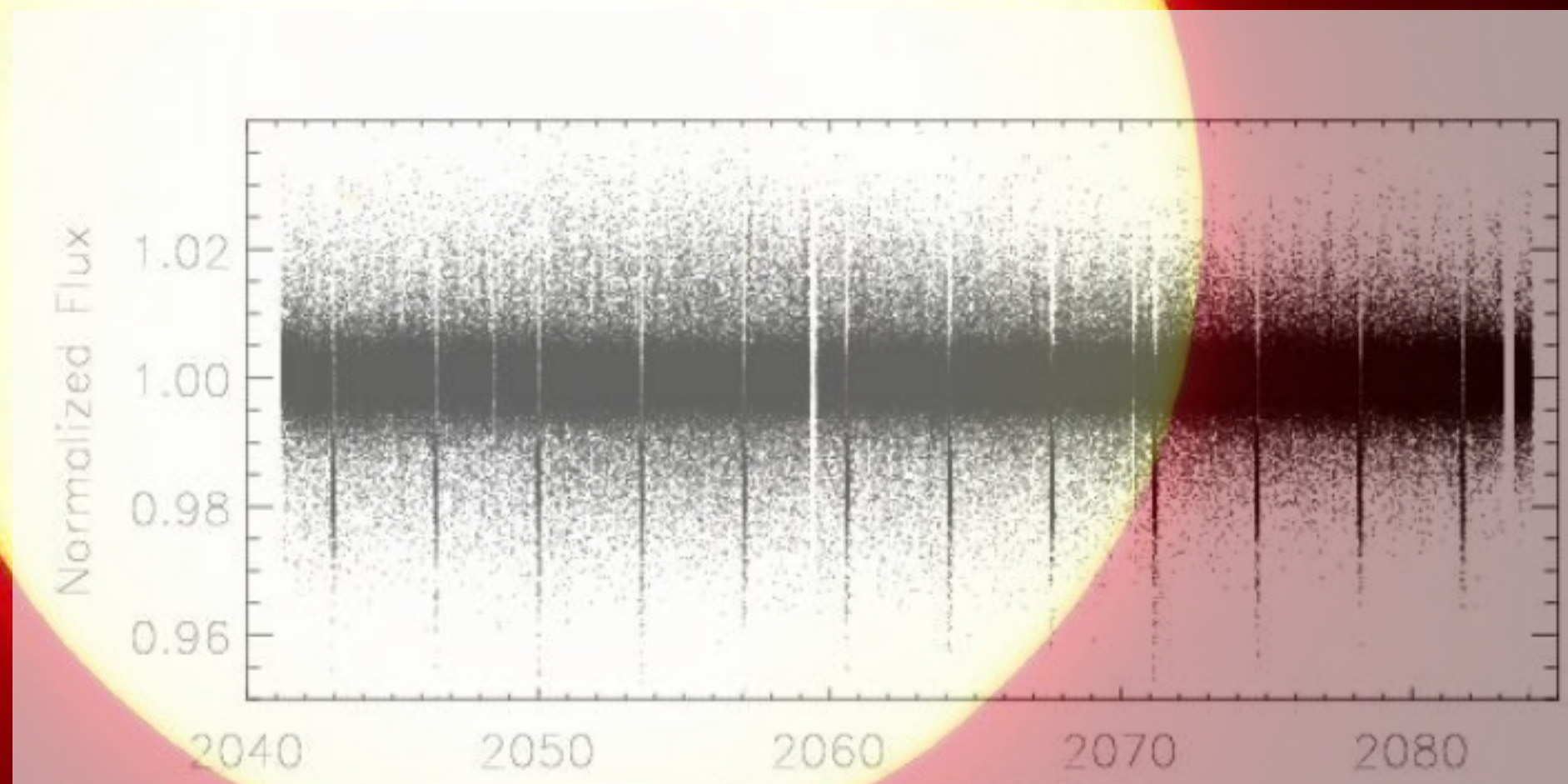




Trends

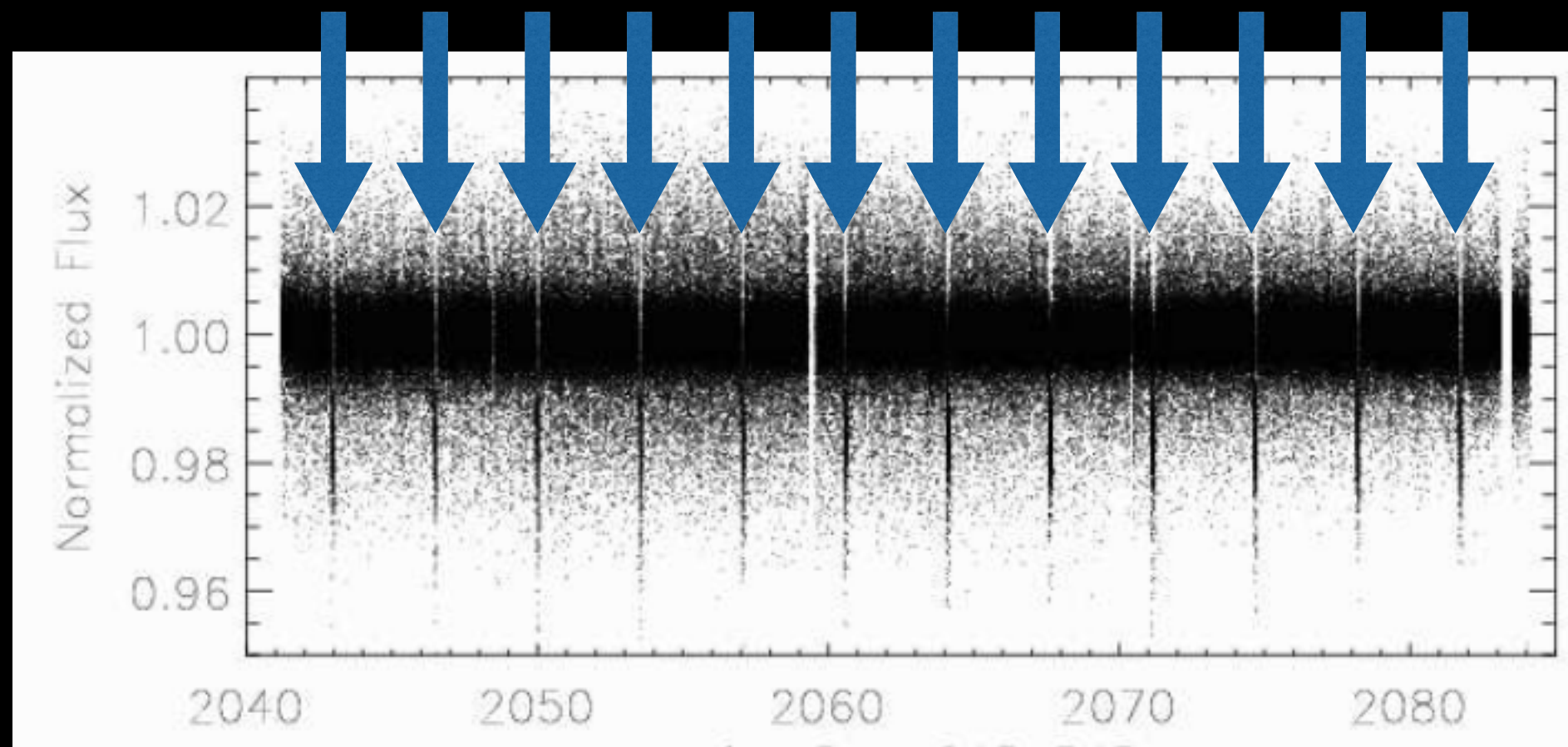




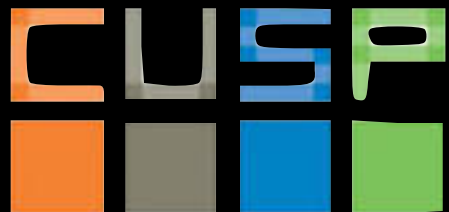


don't forget to vote!

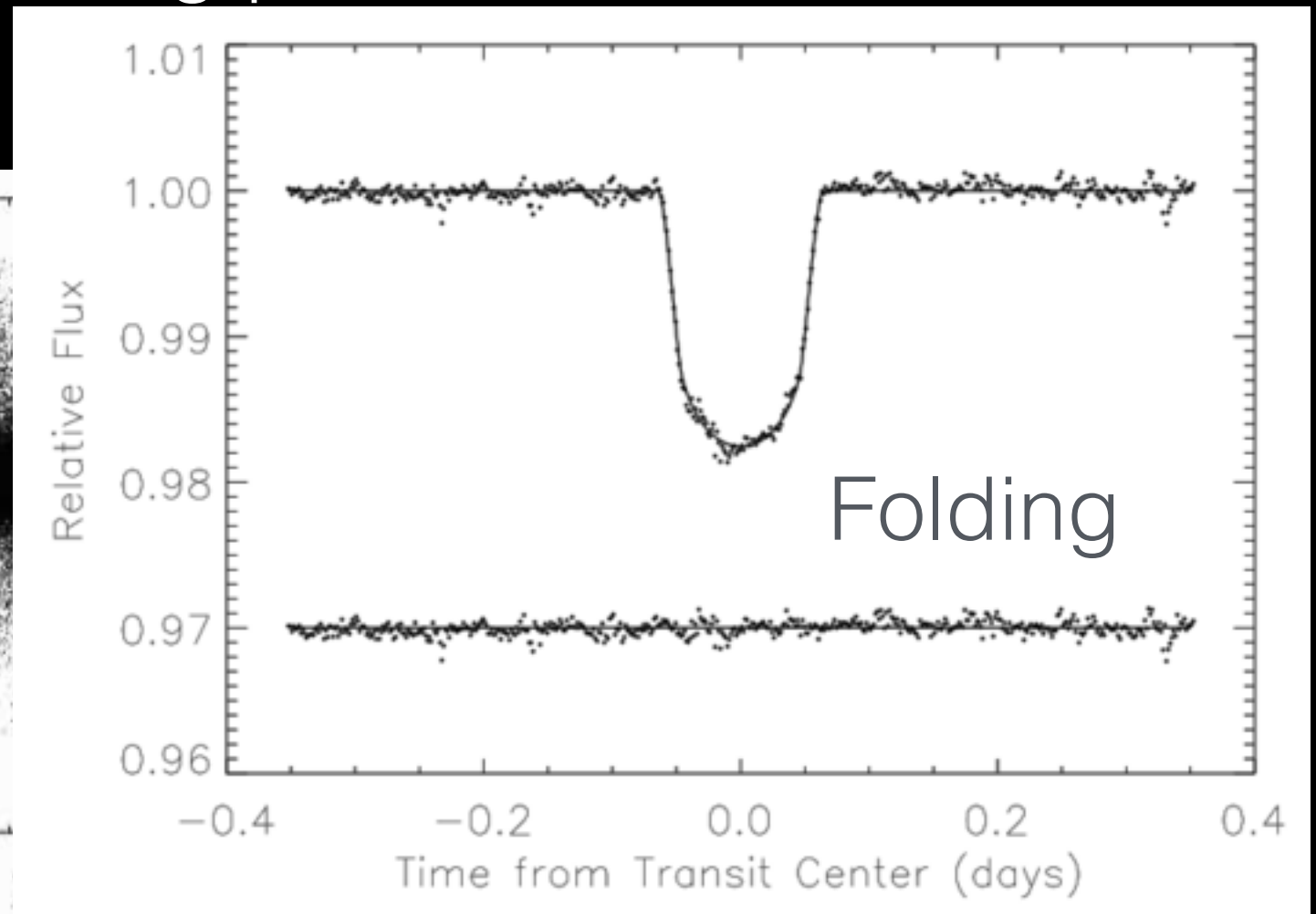
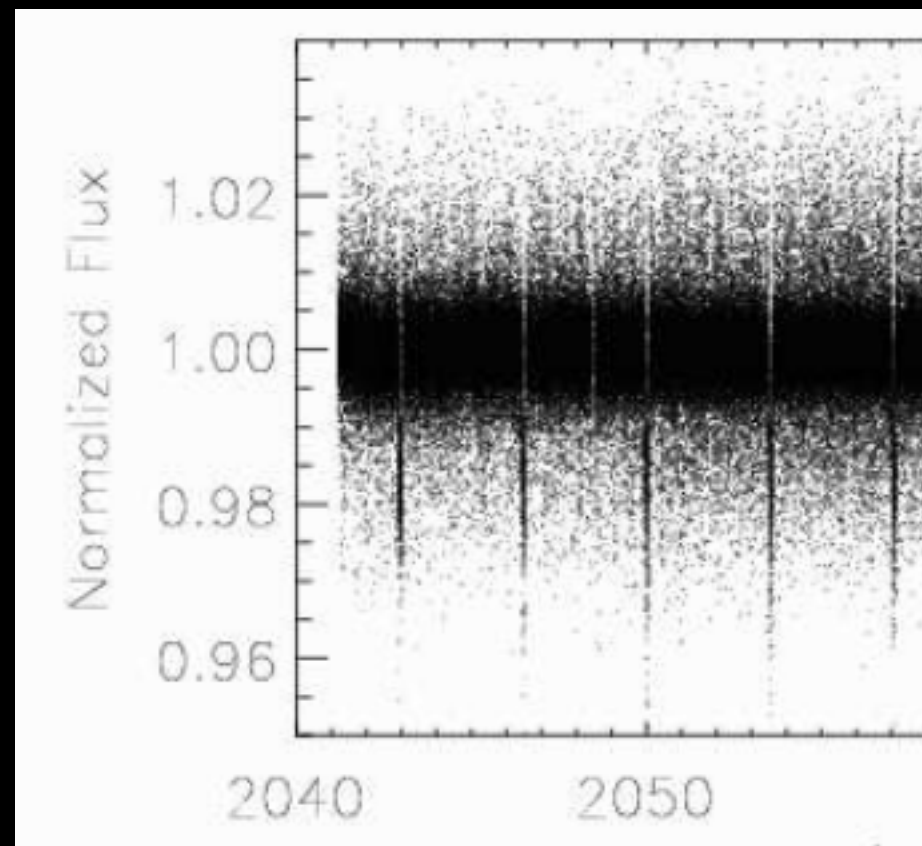
HD 209458, the first transiting planet to be discovered.



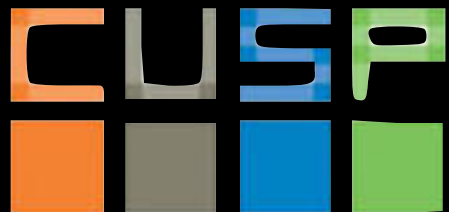
Periodicity

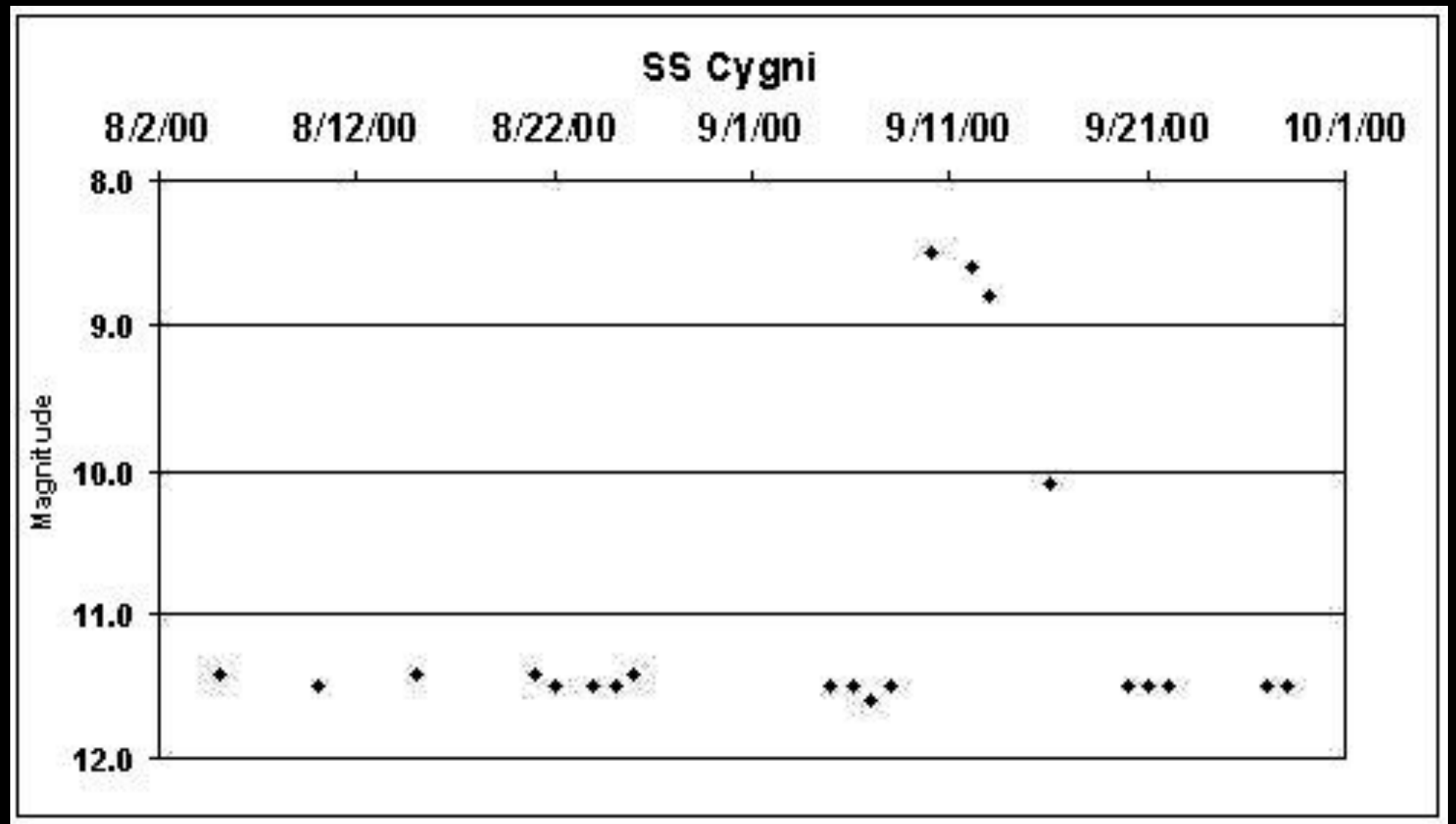


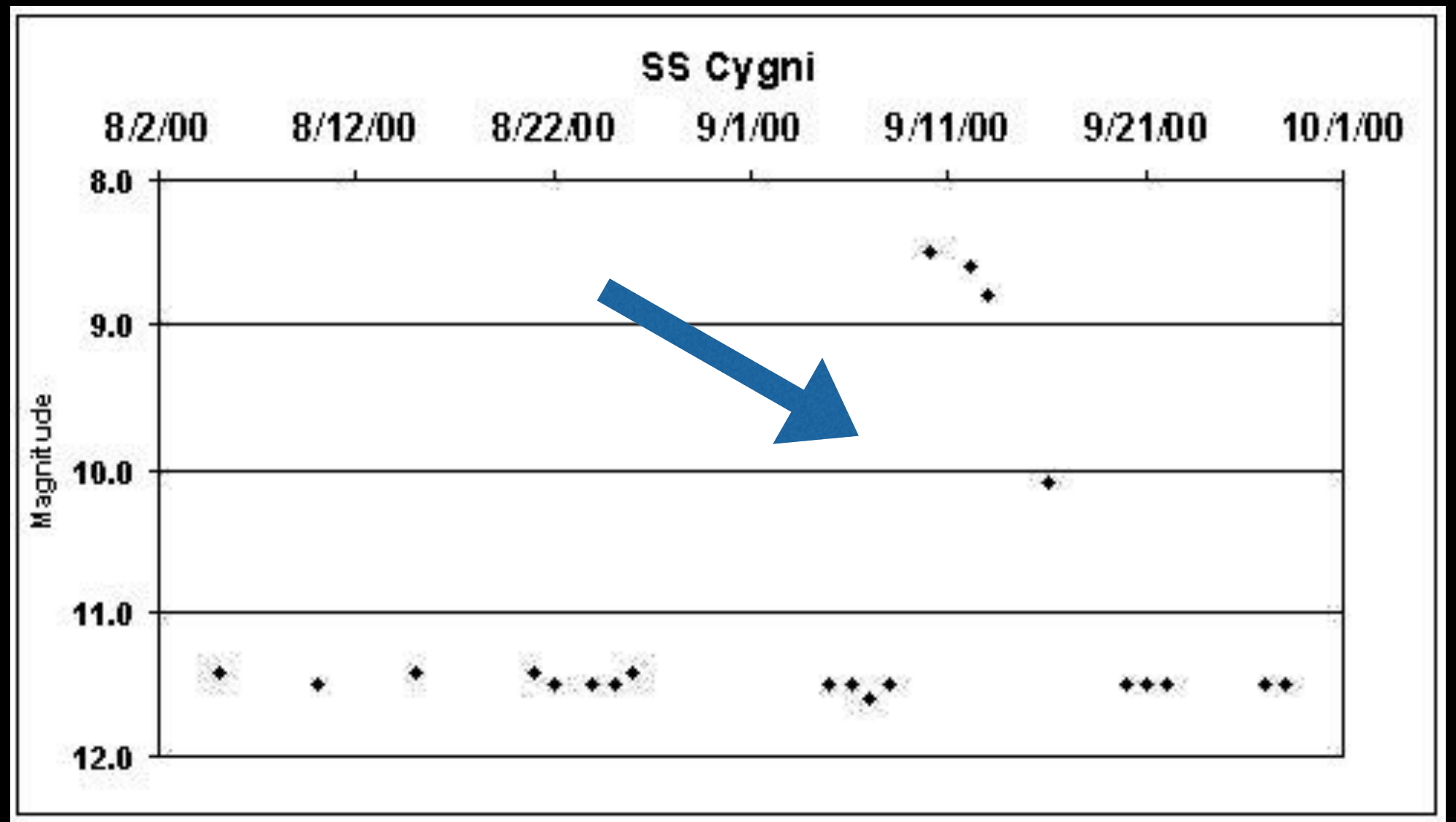
HD 209458, the first transiting planet to be discovered.



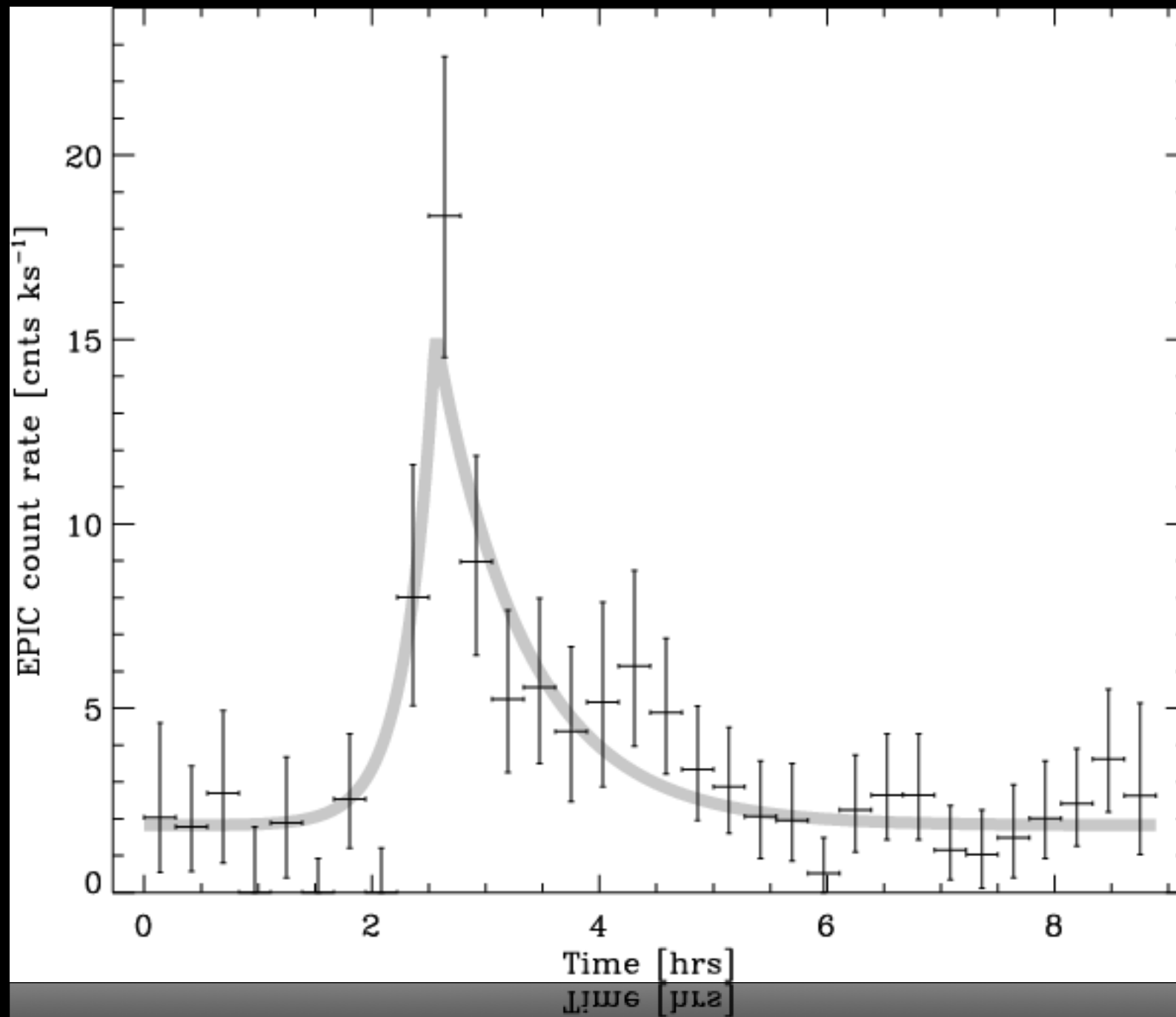
Periodicity



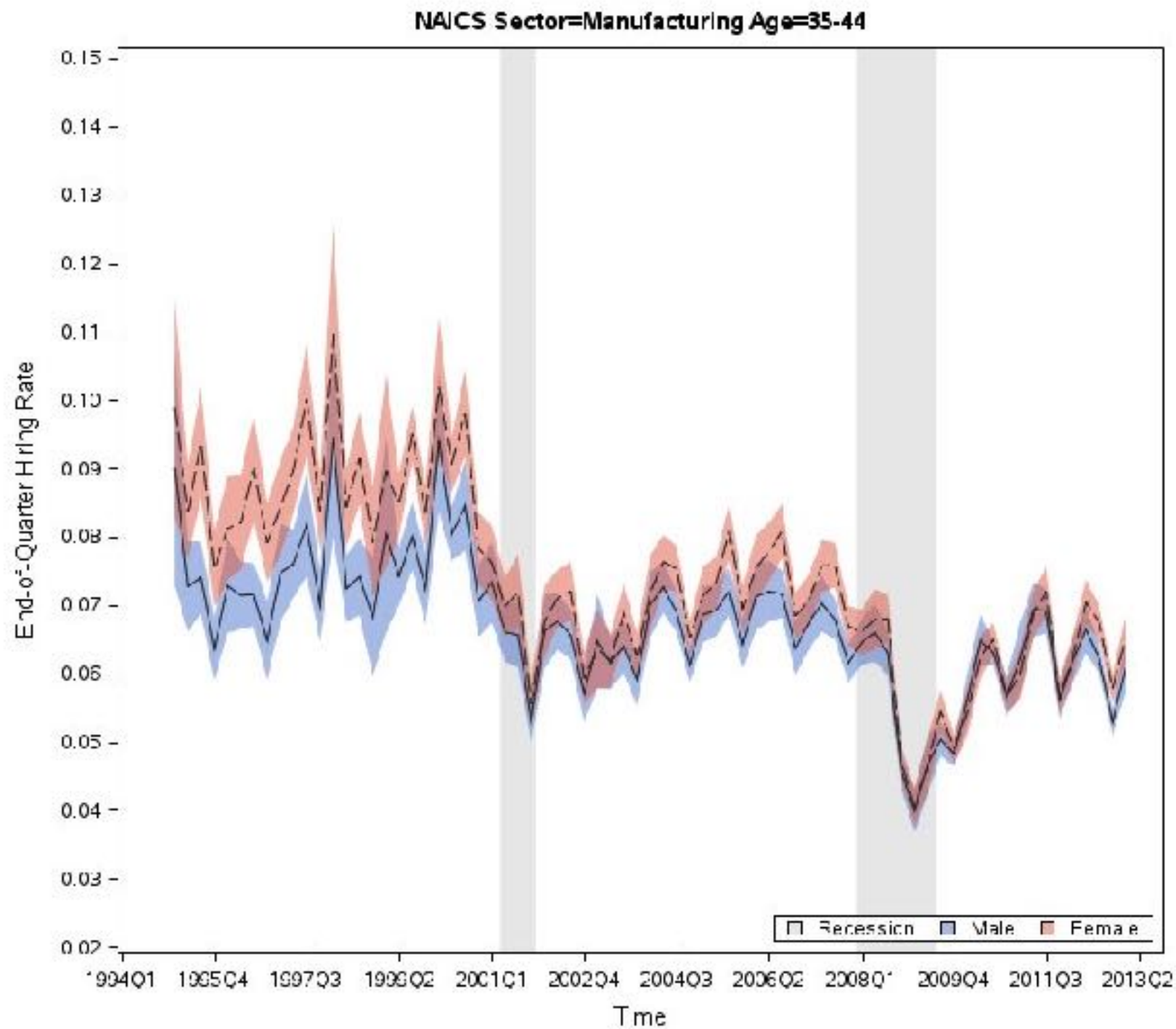




event detection

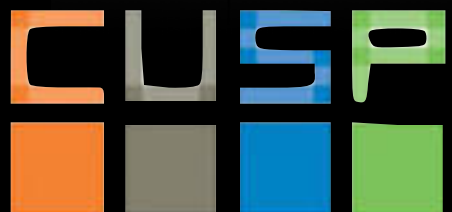


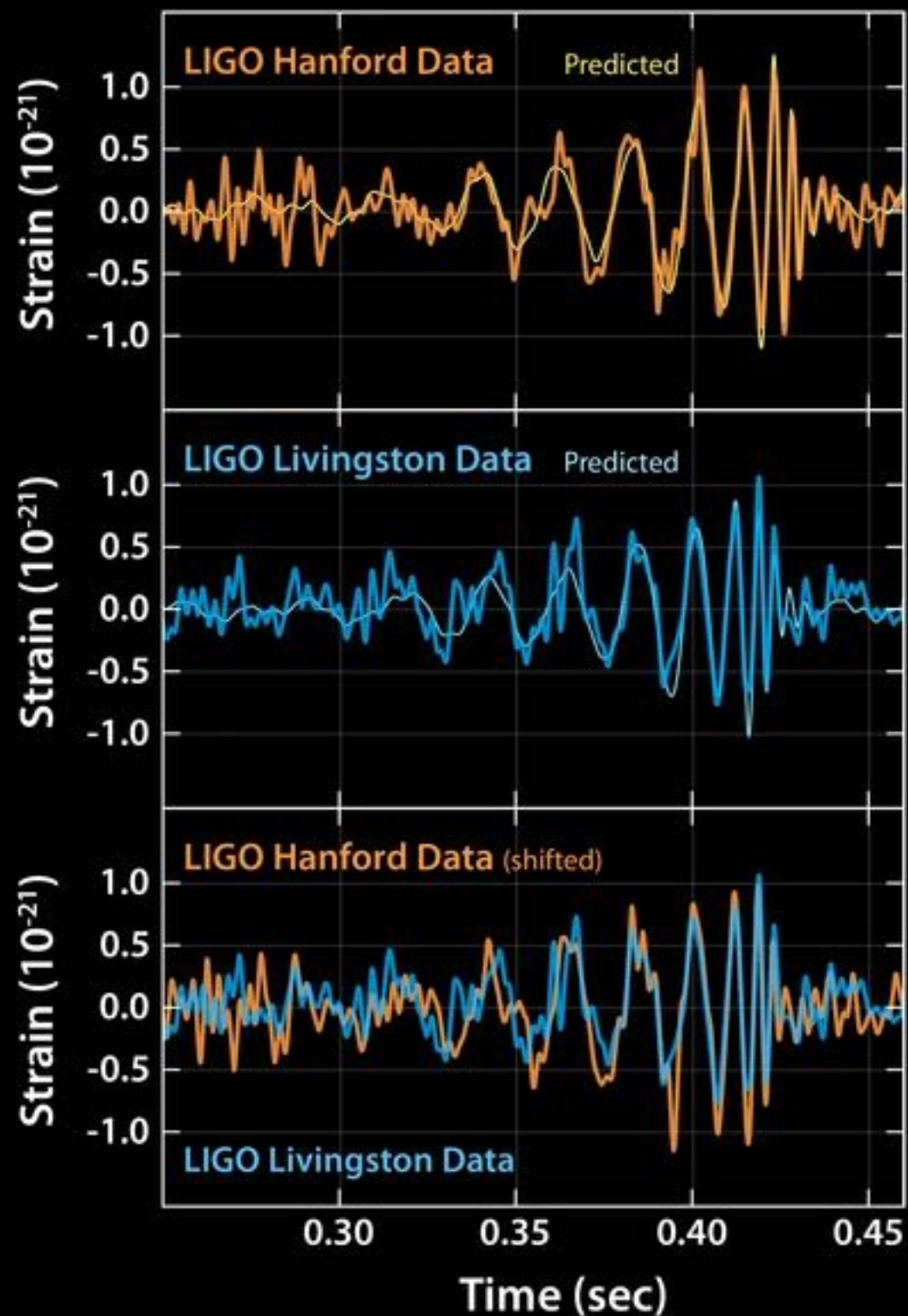
event detection



event detection

LEHD data (Prof. Julia Lane)

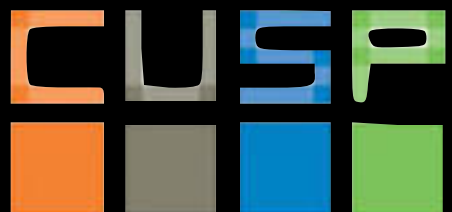




event detection

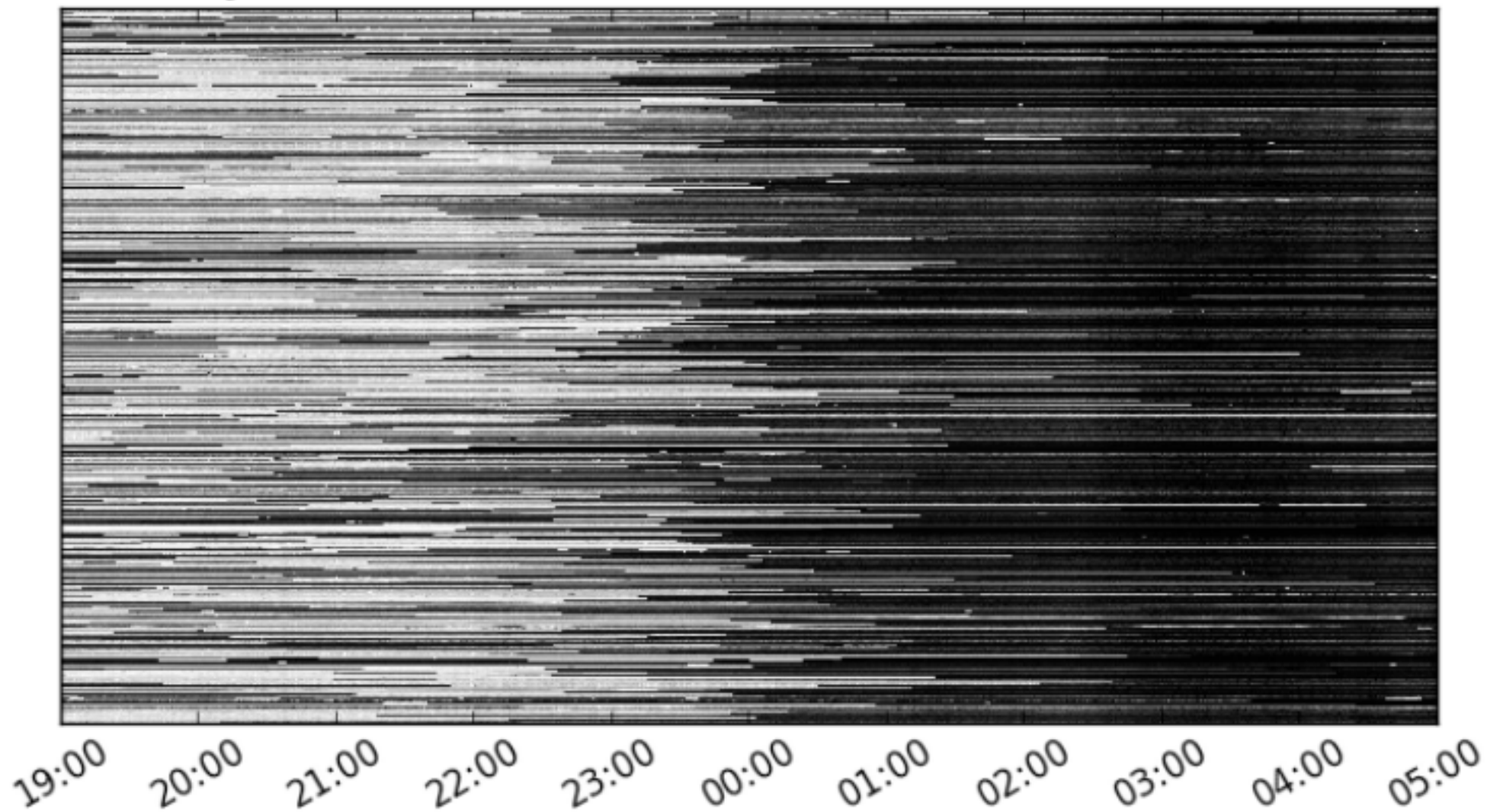
LIGO gravitational wave detection

Abbott et al. Physical Review Letters 116, 061102 (2016)



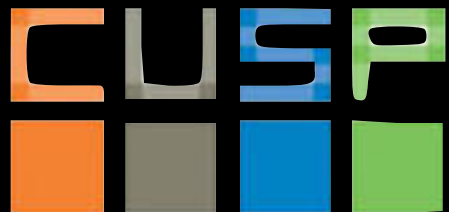
XI: Topics in Time series

Monday

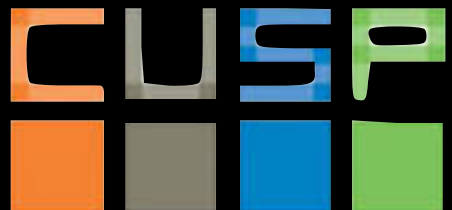
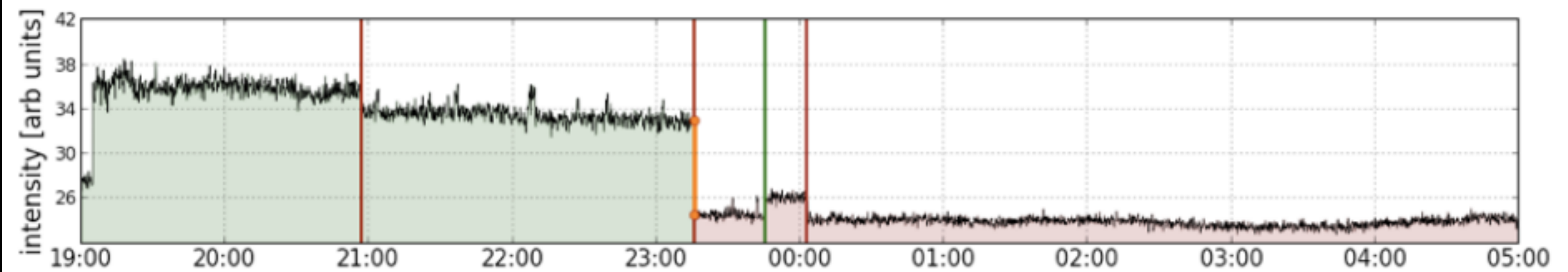
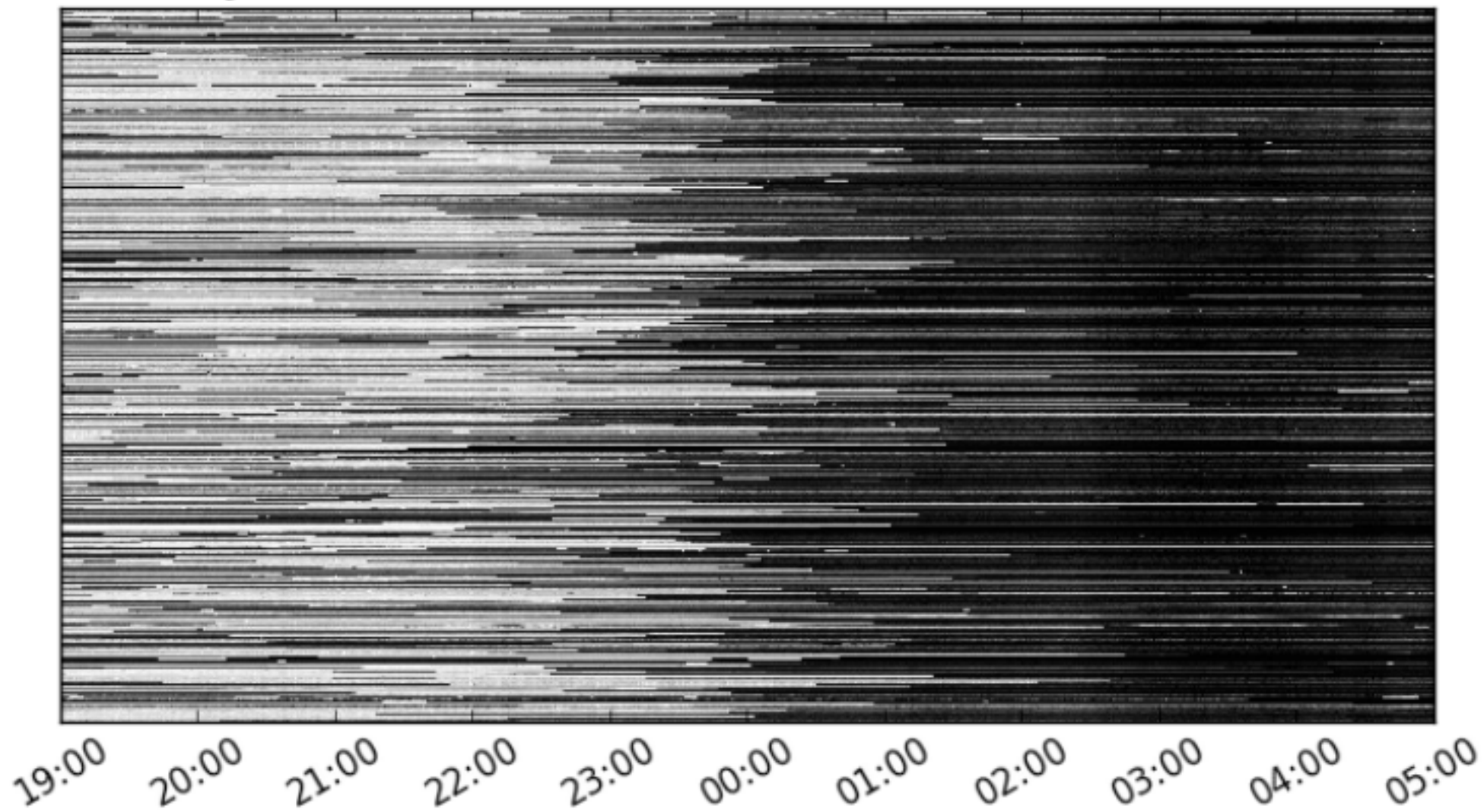


<http://www.sciencedirect.com/science/article/pii/S0306437915001167>

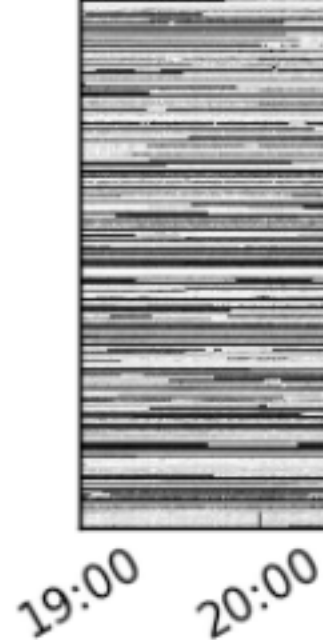
CUSP-UO



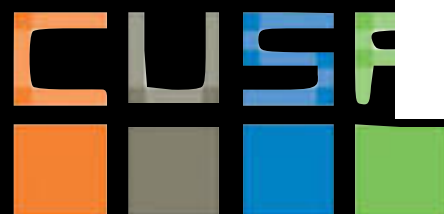
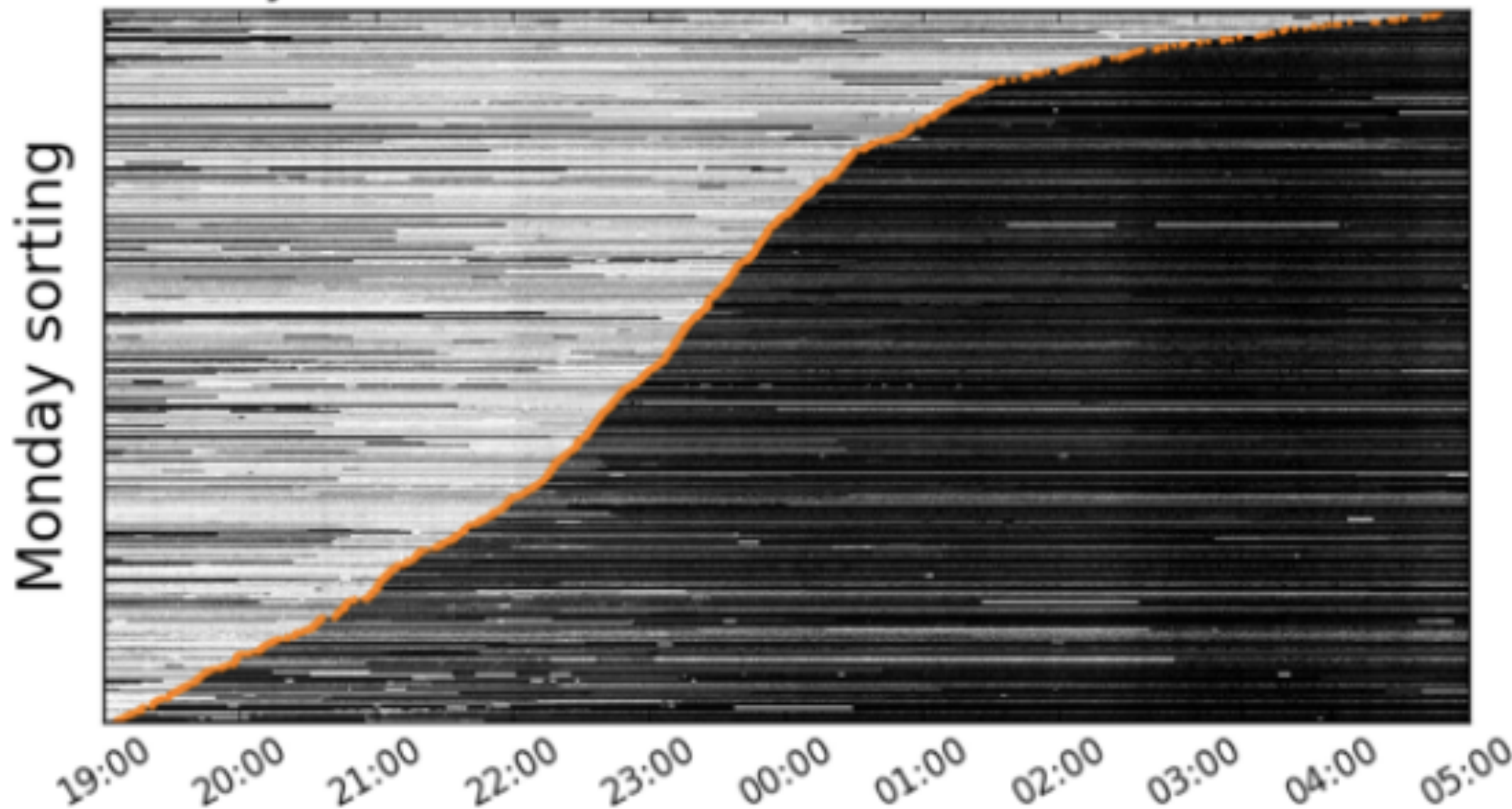
Monday

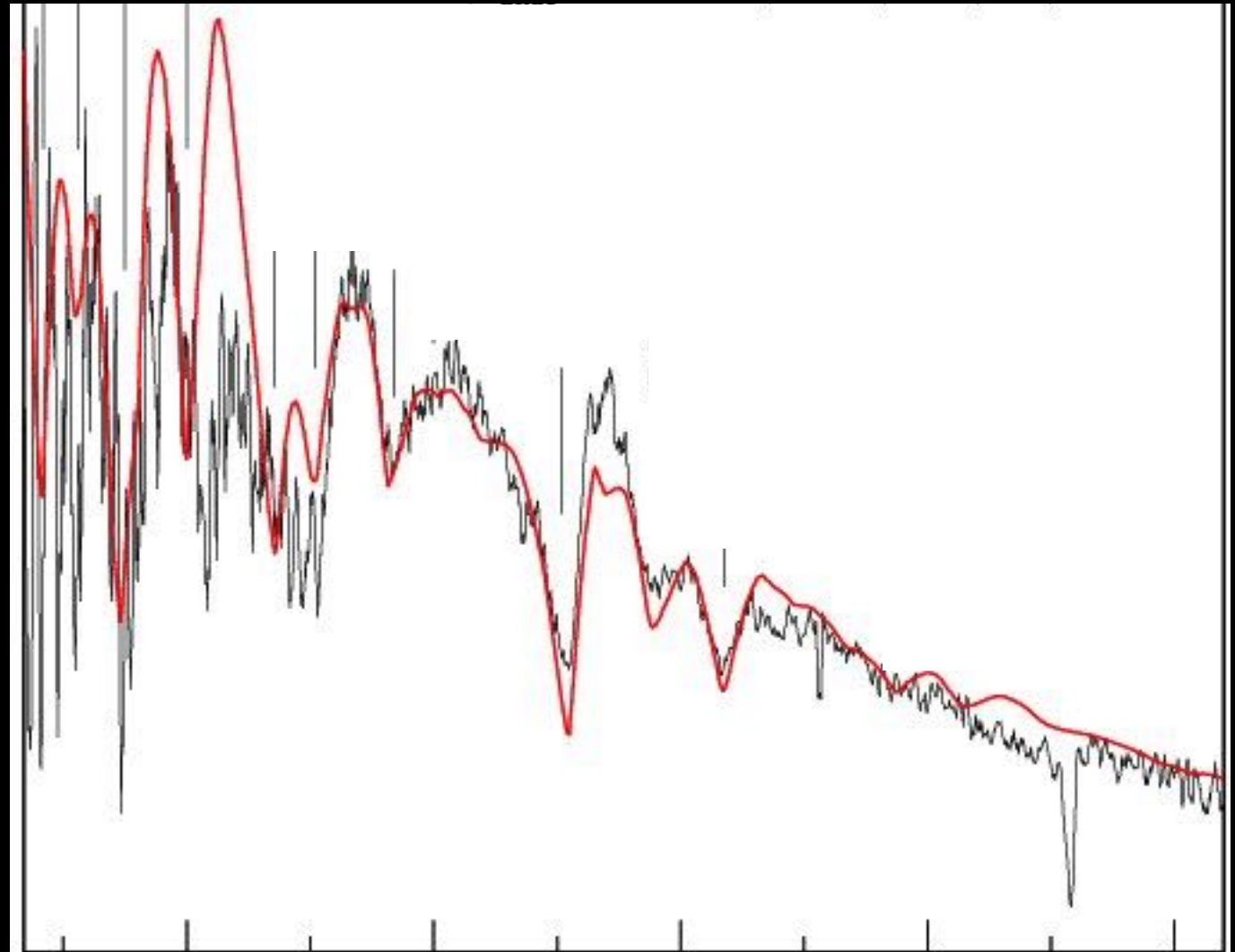


Monday

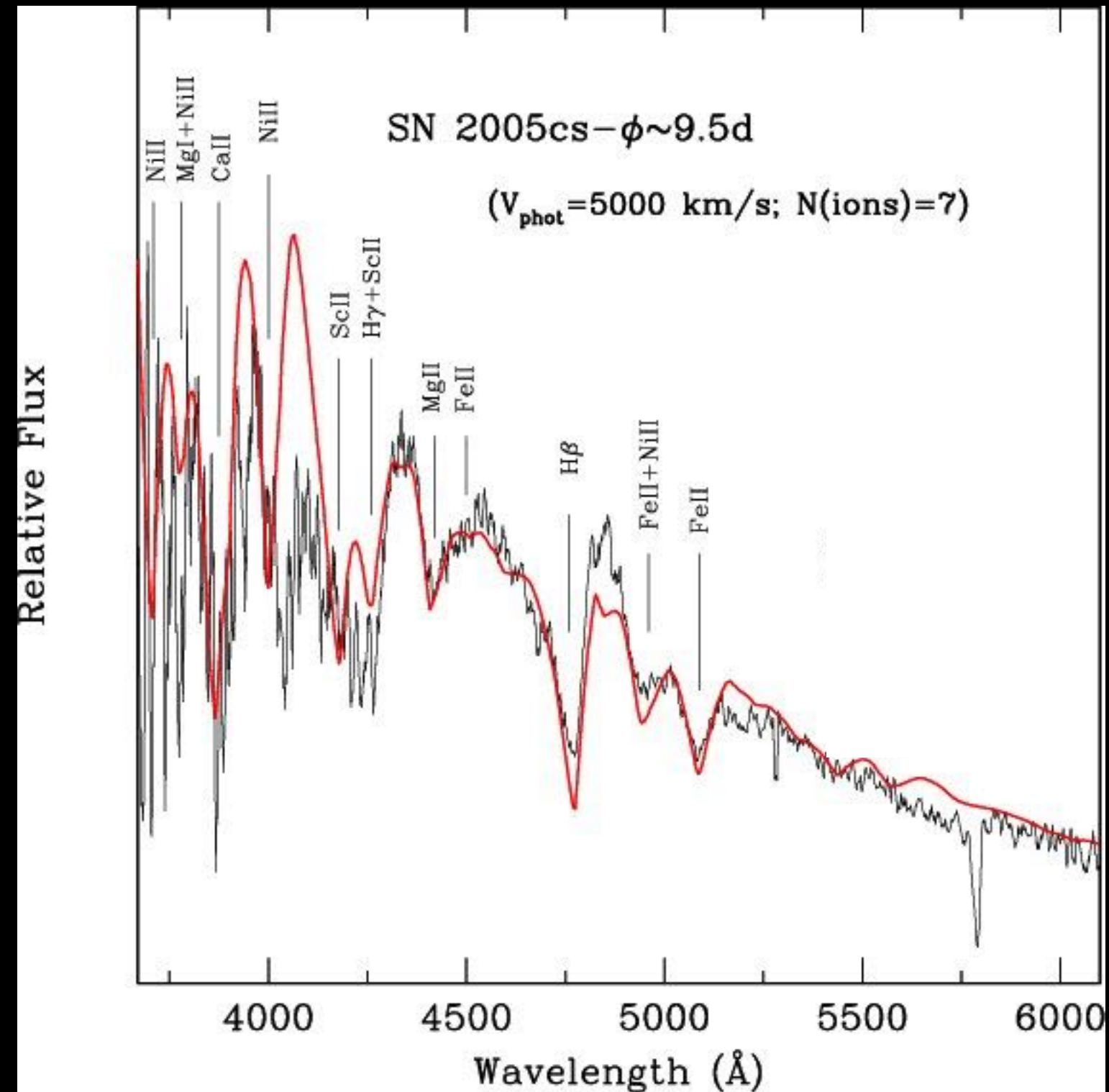


Monday

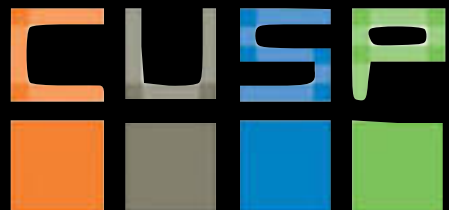
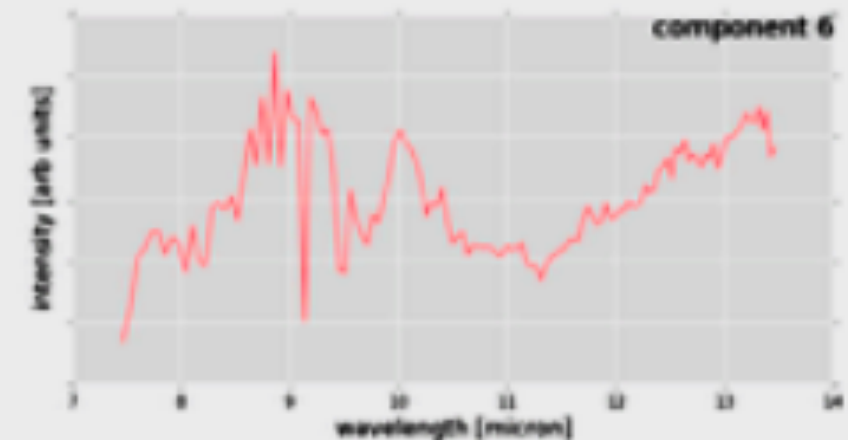
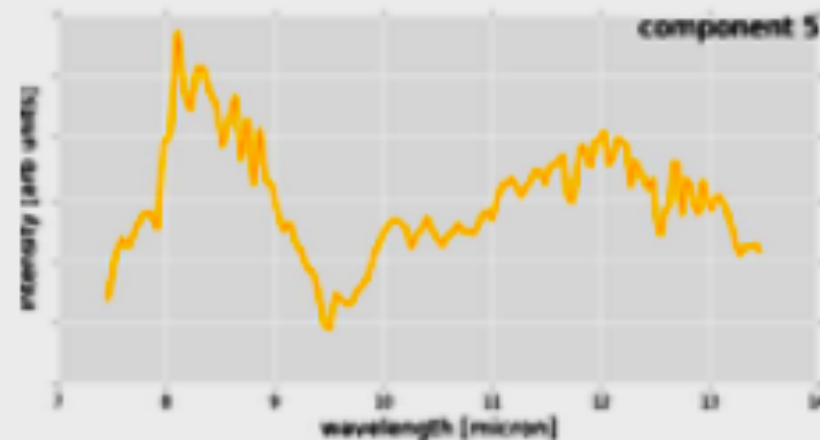
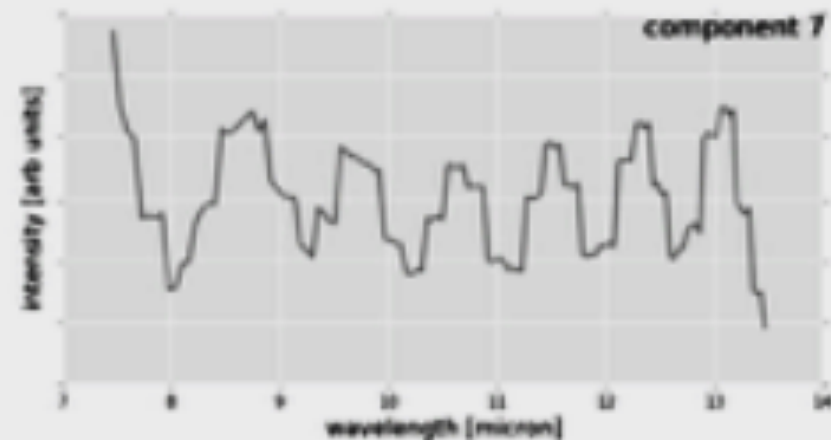
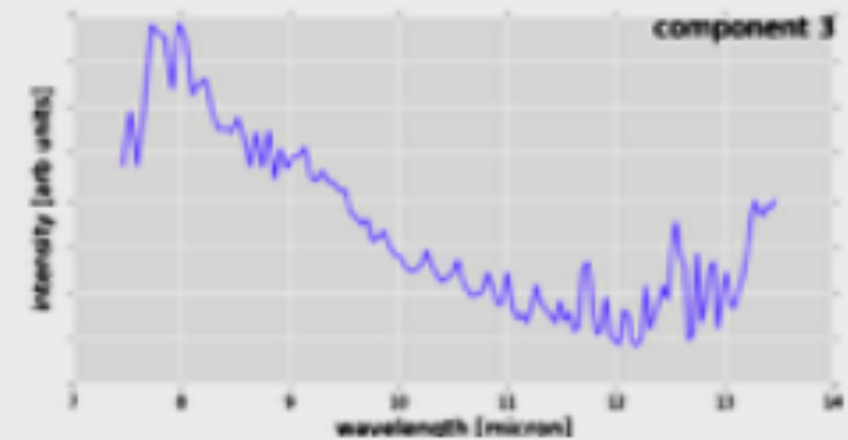
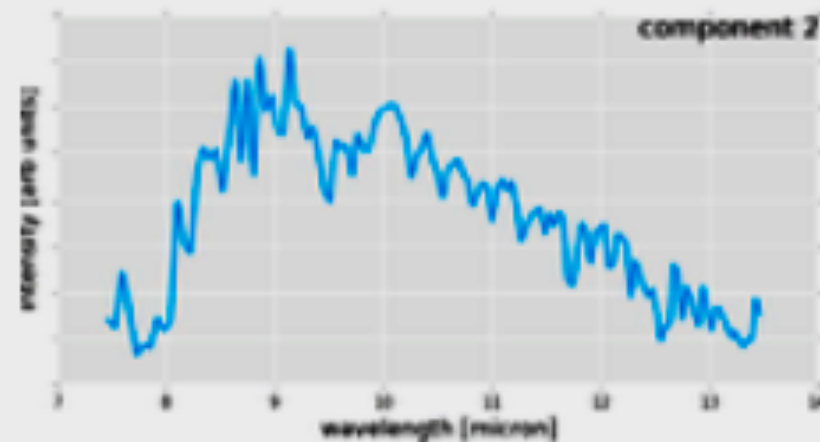
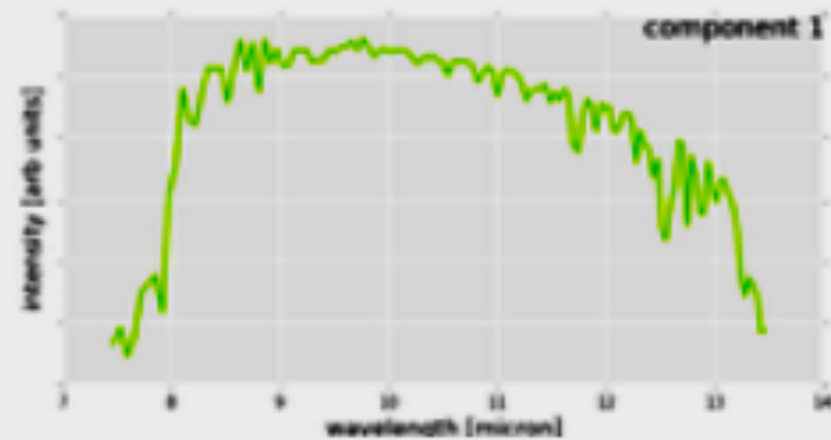




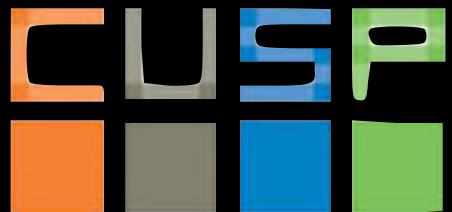
they do not have to be *TIME* series!



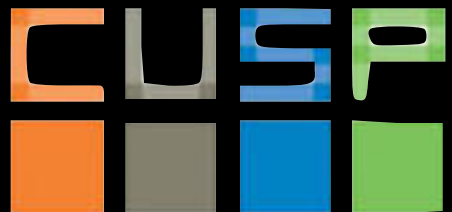
CUSP-UO spectra of urban lights for light technology assessment



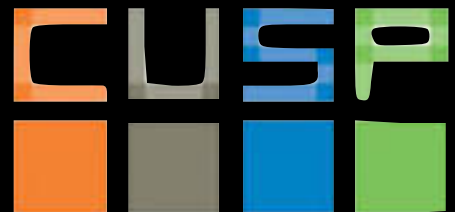
- event detection



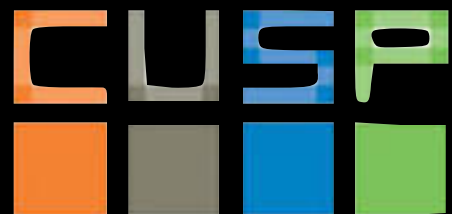
- event detection
- identification of trends



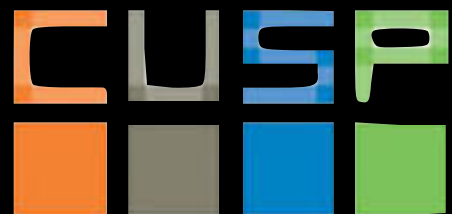
- event detection
- identification of trends
- periodicity detection



- event detection
- identification of trends
- periodicity detection
- prediction

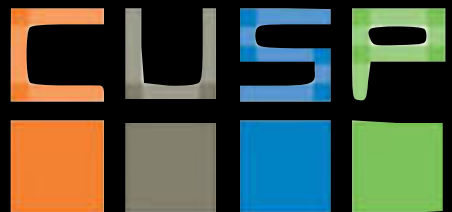


- event detection
- identification of trends
- periodicity detection
- prediction
- classification (clustering)



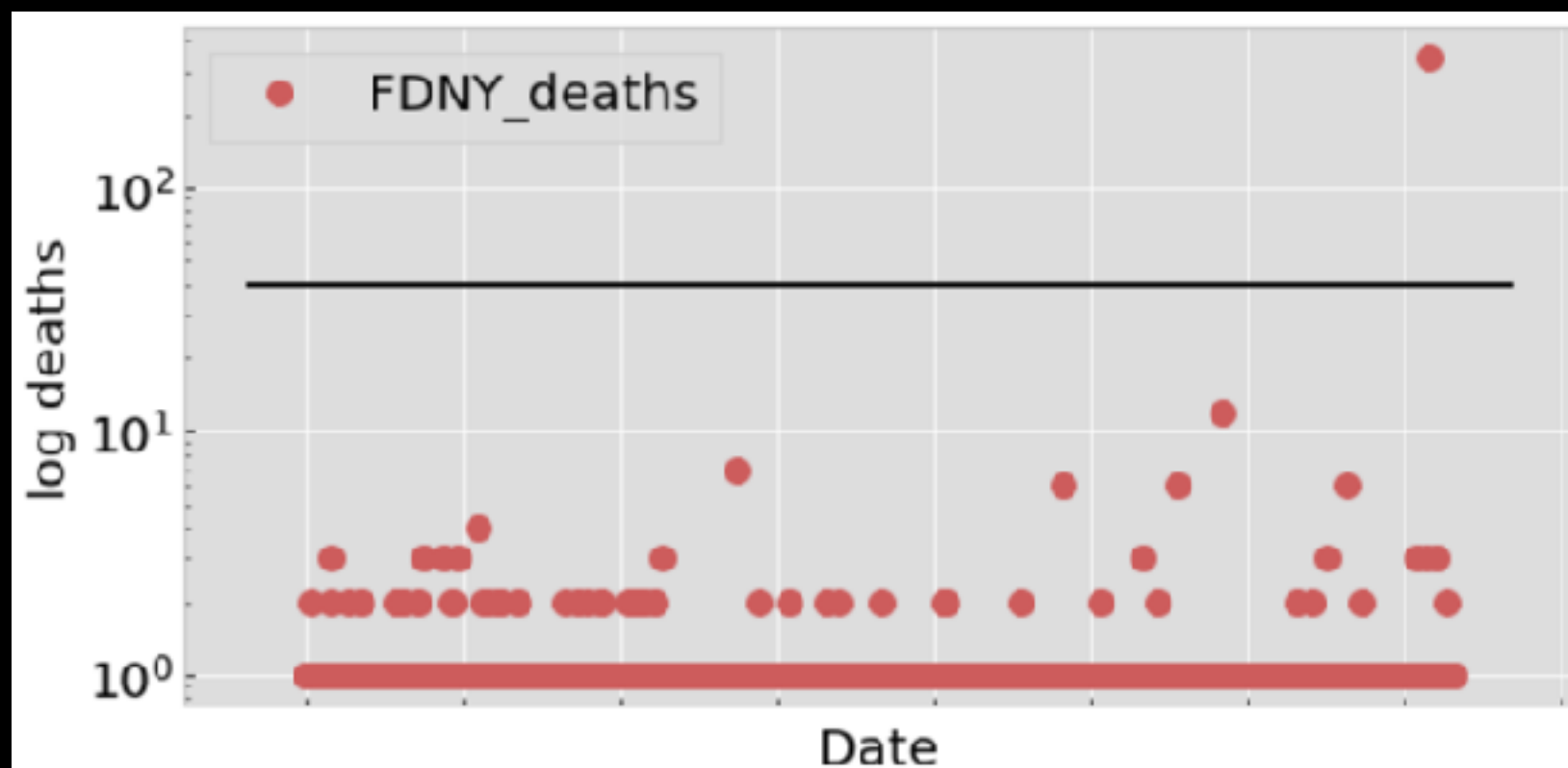
- event detection

Thresholding

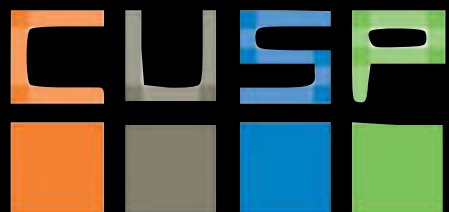


- event detection

Thresholding



[https://github.com/fedhere/Ulnotebooks/blob/master/
FDNYdeaths.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/FDNYdeaths.ipynb)



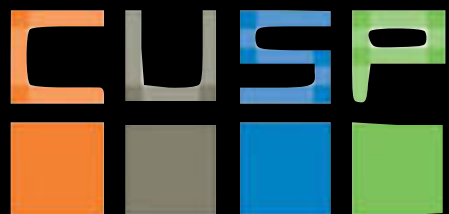
- event detection

Thresholding



- take the mean (possibly a local mean)
- take the standard deviation (possibly a local stdev)
- find points that deviate from the mean by more than N standard deviation

[https://github.com/fedhere/Ulnotebooks/blob/master/
FDNYdeaths.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/FDNYdeaths.ipynb)

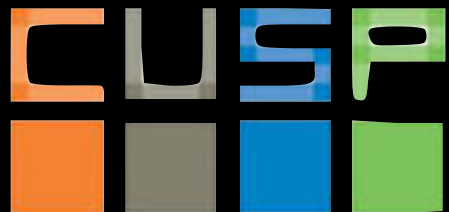


- event detection

Point of change



<https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/pointOfChange.ipynb>



- event detection
- identification of trends

Stationary data

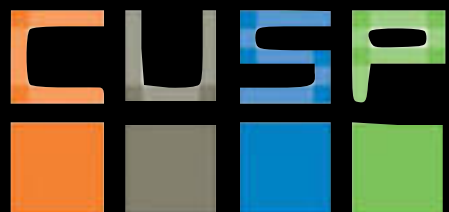
Smoothing (Rolling mean)

ADFuller test for unit root (for non-stationarity)



https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/stationarity_macroecconomicData.ipynb

https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/stationarity_syntheticData.ipynb



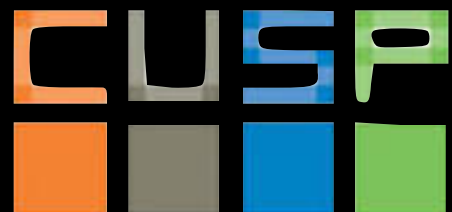
- event detection
- identification of trends
- periodicity detection

ARMA/ARIMA



<http://www.statsref.com/HTML/index.html?arima.html>

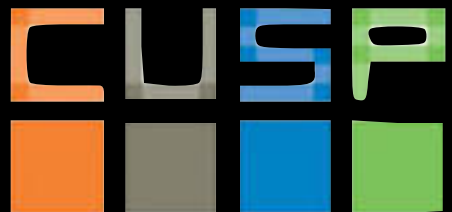
<http://www.econ.ohio-state.edu/dejong/note2.pdf>



ARIMA

Autoregression

$$x(t) = a_1 x(t-1) + \epsilon_t$$

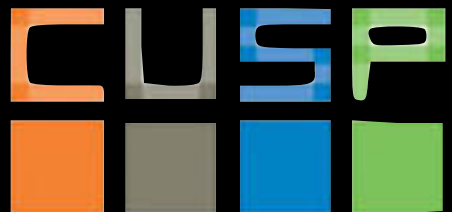


ARIMA

Autoregression

$$x(t) = a_1 x(t-1) + \epsilon_t$$

$$x(t) = a_1 x(t-1) + a_2 x(t-2) + \dots + a_n x(t-n) + \epsilon_t$$



Integration

$$x'(t) = x(t) - x(t-i)$$

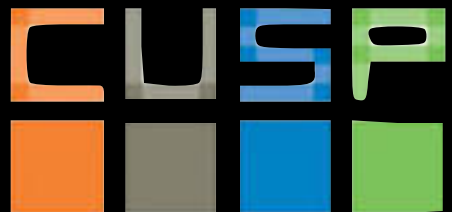
ARIMA

Autoregression

$$x(t) = \sum_{i=1}^p a_i x_{t-i} + \varepsilon_t$$

Moving Average Model

$$x(t) = \sum_{i=1}^q \theta_i \varepsilon_{t-i} + \varepsilon_t$$



ARIMA

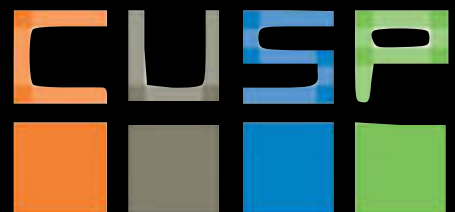
Autoregression

$$x(t) = \sum_{i=1}^p a_i x_{t-i} + \varepsilon_t$$

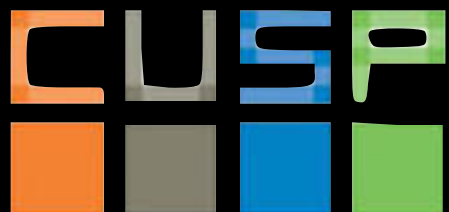
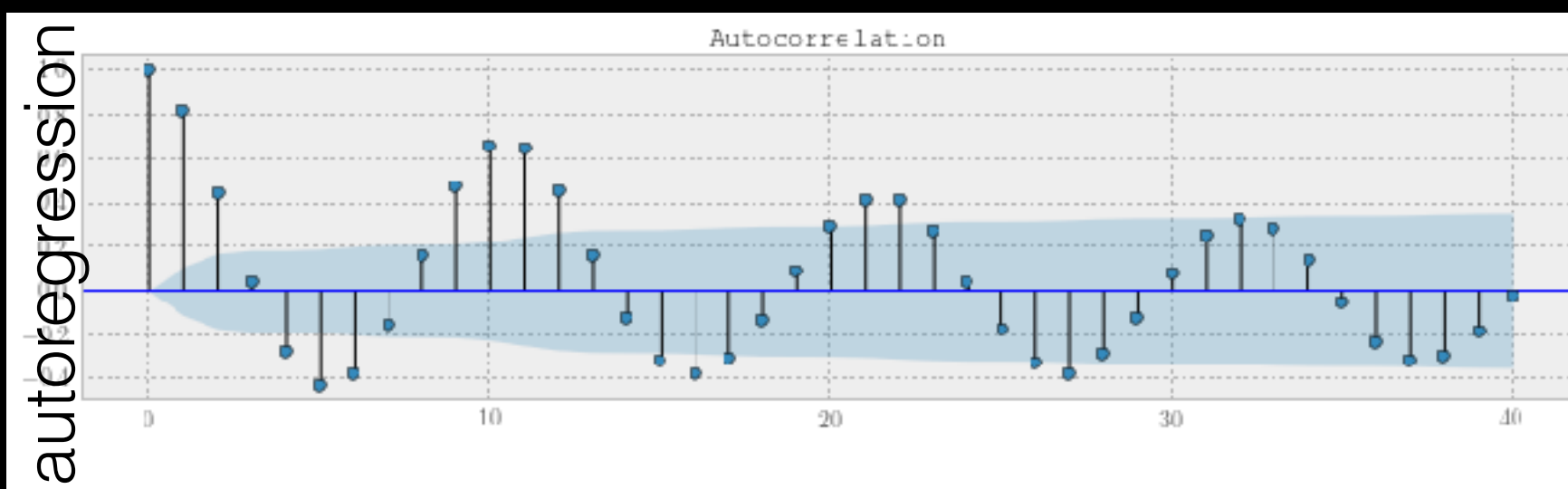
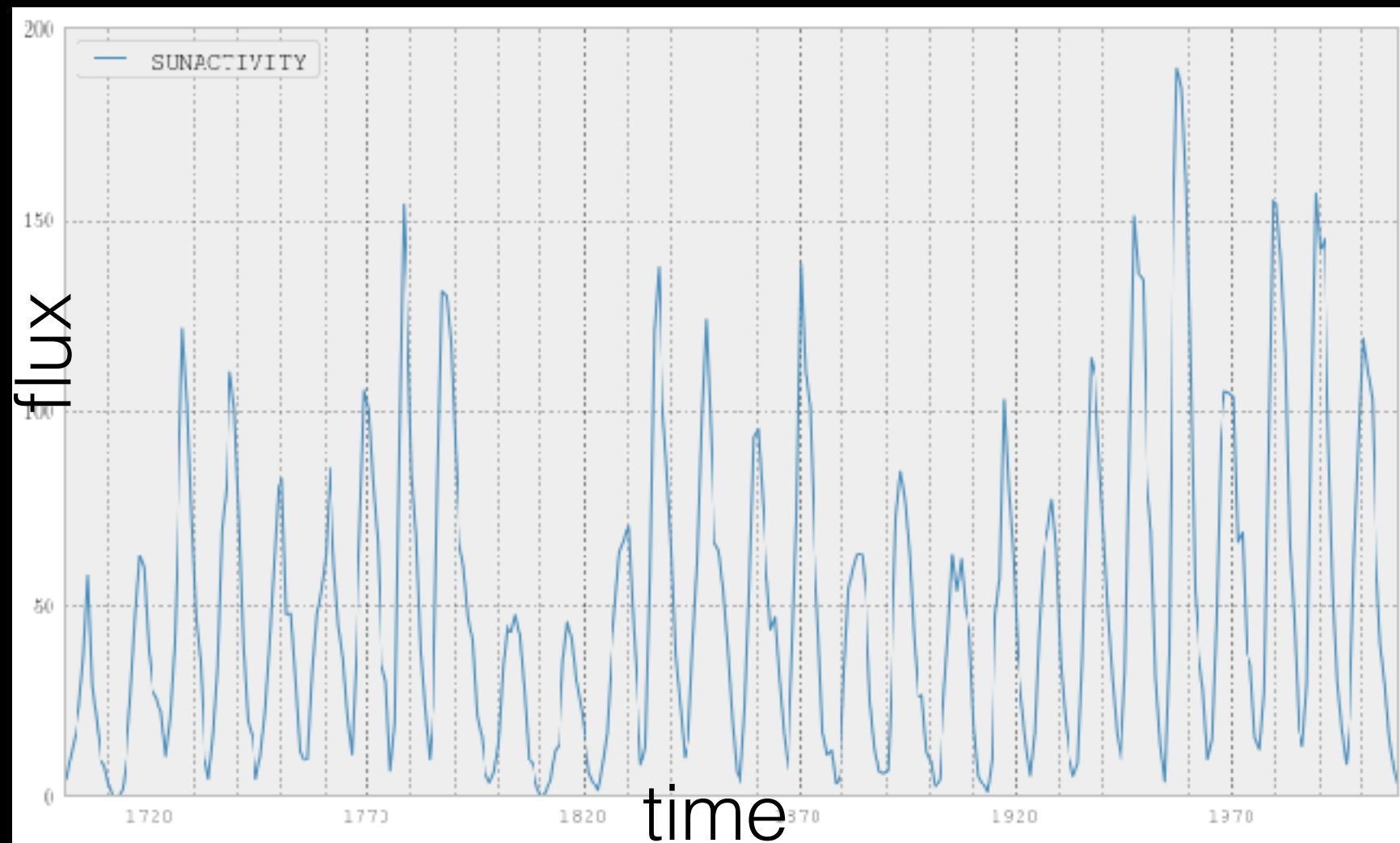
Moving Average Model

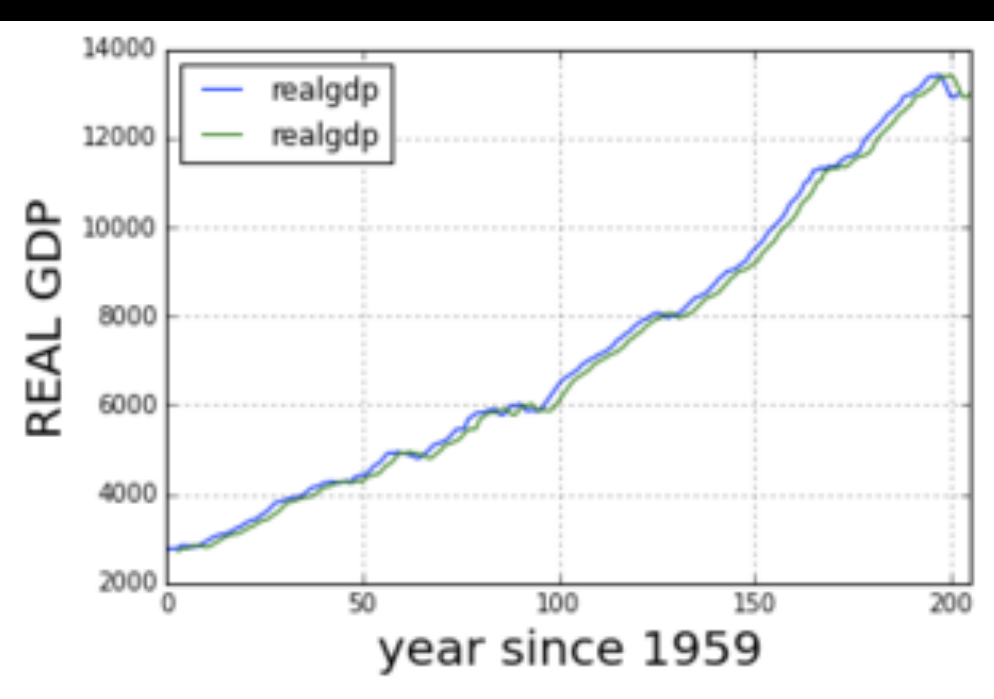
$$x(t) = \sum_{i=1}^q \theta_i \varepsilon_{t-i} + \varepsilon_t$$

 jupyter



http://statsmodels.sourceforge.net/devel/examples/notebooks/generated/tsa_arma_0.html

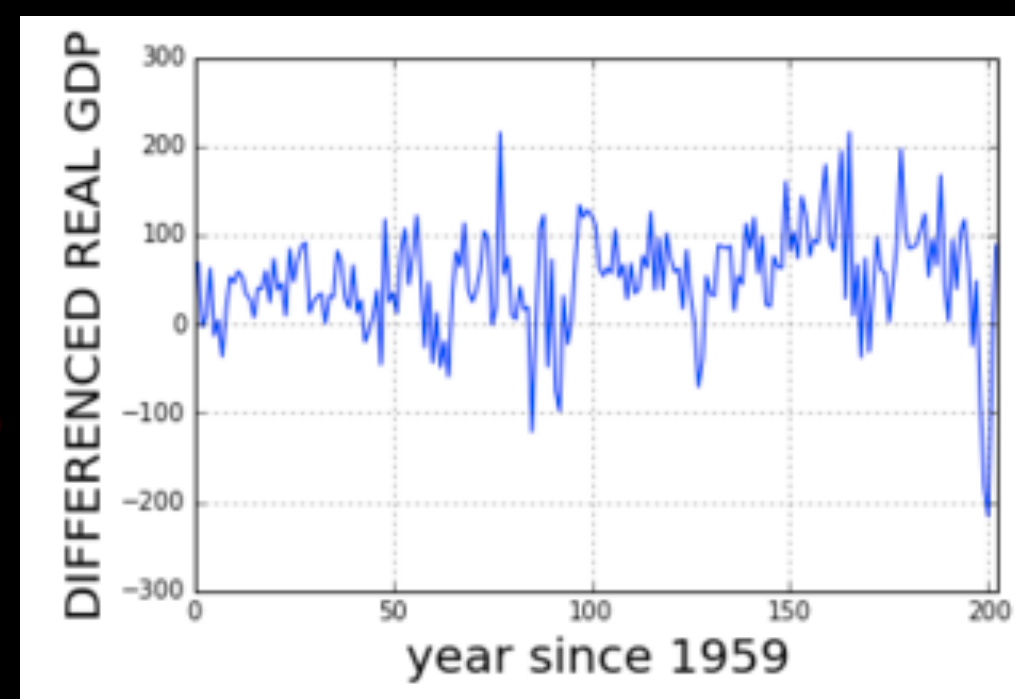




Integration

$$x'(t) = x(t) - x(t-i)$$

ARIMA



Autoregression

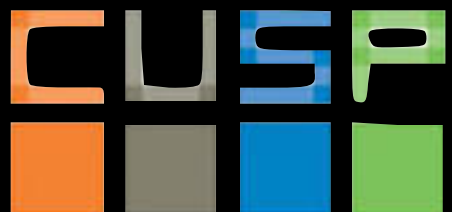
$$x(t) = \sum_{i=1}^p a_i x_{t-i} + \varepsilon_t$$

Moving Average Model

$$x(t) = \sum_{i=1}^q \theta_i \varepsilon_{t-i} + \varepsilon_t + \mu$$

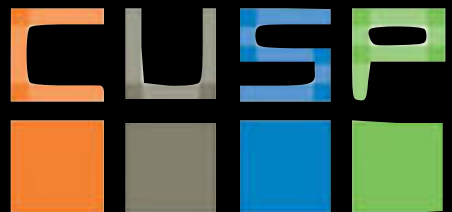
 jupyter

https://github.com/fedhere/Ulnotebooks/blob/master/ARMA_microdata.ipynb



Key points:

- Time series analysis may be done for a number of purposes: classification, prediction, event detection, period finding
- smoothing, binning, detrending (difference, regression)
- prediction tools: autoregression, ARMA, ARIMA



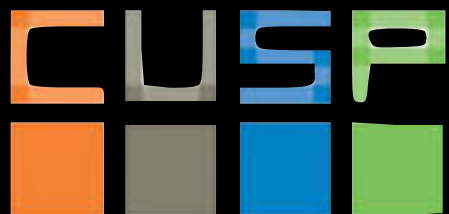
Homework:

Technical reading on SM time analysis tools. Get through ARMA

[http://conference.scipy.org/proceedings/
scipy2011/pdfs/statsmodels.pdf](http://conference.scipy.org/proceedings/scipy2011/pdfs/statsmodels.pdf)

Reading: an excellent analysis of time series
by Jake Vander Plas
(UW e-science center)

[https://jakevdp.github.io/blog/2014/06/10/is-
seattle-really-seeing-an-uptick-in-cycling/](https://jakevdp.github.io/blog/2014/06/10/is-seattle-really-seeing-an-uptick-in-cycling/)



Homework:

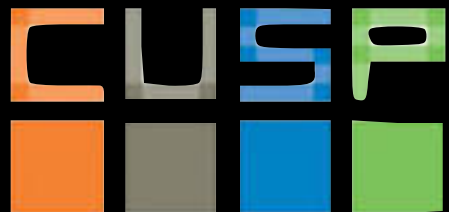
Data:

MTA subway fares. It is a complete dataset of rides logged by card swipes for 600 Manhattan stations.

It contains 23 different subway card types (e.g. monthly pass, daily pass, Act for Disability pass... i will give you this as a list)

Each time series (per station, per ticket type) contains the number of swipes per week for 194 weeks from 05/21/2010 to 02/21/2014.

it is given to you as a python data cube.
you can load it as `np.load("MTA_Fare.npy")` and you will end up with a python numpy array of shape (600,23,194)



Homework:

Goal 1:

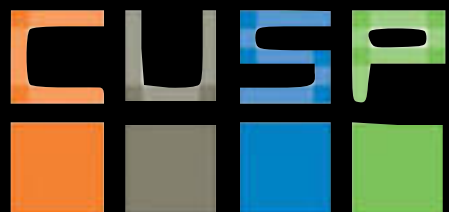
Event detection: Identify the most prominent event. There is a very significant drop (>3 -sigma) in *all* time series. Identify it and figure out what it is due to.

Goal 2:

Some of the time series are stationary, some show a downward trend: Identify the time series with the most prominent downward trend.

Goal 3:

Build a classifier that assigns a card type to a time series based on time series features



Homework Hints:

Goal 1:

Some of the time series are stationary, some show a downward trend: Identify the time series with the most prominent downward trend.

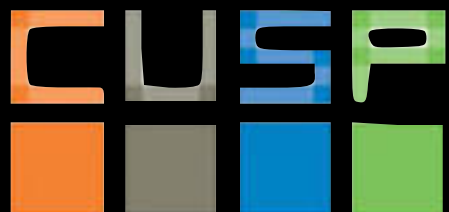
work with all time series individually. you can use the rolling mean to find trends: compare rolling mean near beginning and end of time series.

Goal 2:

Event detection: Identify the most prominent event. There is a very significant drop (>3 -sigma) in *all* time series.

Identify it and figure out what it is due to.

Since I am telling you the event is in all time series you can work with averages: for example average over all rise types per station. Since i am telling you it is a highly significant event you can find it by thresholding



Homework Hints:

Goal 3:

Build a classifier that assigns a card type to a time series based on time series features

- Clean the data from missing values (drop time series with NaNs)
- Used all the time series, the ticket type as a label.
- Calculate the mean, standard deviation, and by station and use the following features:

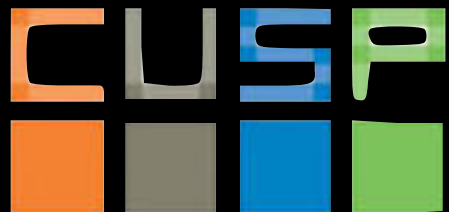
1,2 line fit coefficient to the reduced time series

$(\text{time series} - \text{mean_by_station}) / \text{stdev_of_station}$

3 mean_of_station

4 stdev_of_station

- Split the training and test data
- Build and test a random forest model that predicts the ticket type based on these 4 features.
- Build and test a random forest model that predicts the ticket type based on all datapoint in the time series (194 features)
- Plot a confusion matrix for each model (discuss)
- Compare the models w a sklearn.metrics classification_report
- Find the 2 most important features in each model

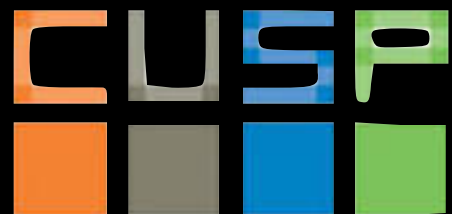


References ok Decision trees:

<http://what-when-how.com/artificial-intelligence/decision-tree-applications-for-data-modelling-artificial-intelligence/>

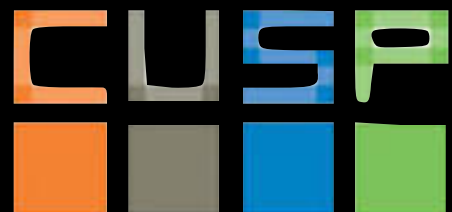
<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC4466856/>

<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC4380222/>



don't just do linear
regression!

[http://scikit-learn.org/0.16/
modules/tree.html#tree-
algorithms-id3-c4-5-c5-0-
and-cart](http://scikit-learn.org/0.16/modules/tree.html#tree-algorithms-id3-c4-5-c5-0-and-cart)



X: decision trees

References ok Decision trees:

Statistical Analysis Handbook

<http://www.statsref.com/HTML/index.html>

Stationary and non stationary time series

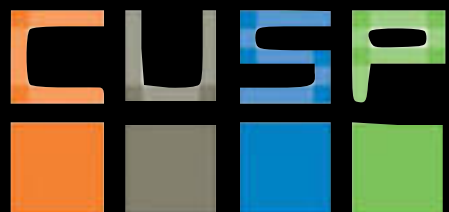
<http://www.cas.usf.edu/~cconnor/geolsoc/html/chapter11.pdf>

ARMA & ARIMA

<http://www.econ.ohio-state.edu/dejong/note2.pdf>

Time series classification in python, not covered but you should read about it!

<http://alexminnaar.com/time-series-classification-and-clustering-with-python.html>

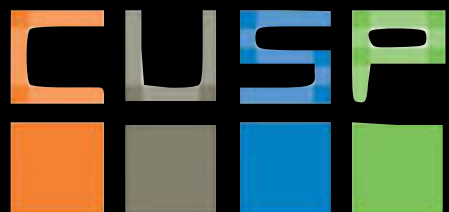


Reading:

*An excellent use of viz for data exploration
and transition to inferential analysis*

<https://blog.data.gov.sg/how-we-caught-the-circle-line-rogue-train-with-data-79405c86ab6a#.iz1r655xo>

Lee Shangqian, Daniel Sim & Clarence Ng



X: decision trees