

Input: $\mathcal{X}, k, \mathcal{L}, d$

Step 1 *Preprocessing, Section 5.1*

1: Construct $G(\mathcal{X}, E)$ by connecting each element in \mathcal{X} with its k -nearest neighbors.

2: **for all** $x \in \mathcal{X}$ **do**

3: $N_x = \{y \in \mathcal{X} : (x, y) \in E\}$ *Compute neighborhoods*

4: $[N_x^0] = USV^T$

where $[N_x^0]$ is the data matrix formed by the elements in N_x shifted to the origin of \mathbb{R}^N and U, S, V are the results of its d-rank SVD.

5: $M_x = U$ *Compute tangent spaces*

6: **end for**

Step 2 *Greedy computation of partition $\mathbf{C}_{\mathcal{L}}^*$ *

7: $n = |\mathcal{X}|, \lambda = 0, \mathbf{C}_{\mathcal{L}}^* = \{\{x\} : x \in \mathcal{X}\}$ *Initialization*

8: **for** $\lambda < n - \mathcal{L}$ **do** *Greedy merging, Section 5.2*

9 $(C'_i, C'_j) = \underset{\substack{C_i, C_j \in \mathbf{C}_{n-\lambda}^* \\ \psi(C_i, C_j) \text{ is true}}}{\text{argmin}} \tilde{d}(C_i, C_j)$ *Eq. (23)*

10: $\mathbf{C}_{n-\lambda+1}^* = (\mathbf{C}_{n-\lambda}^* \setminus \{C'_i, C'_j\}) \cup \{C'_i \cup C'_j\}$

11: Compute $M_{C'_i \cup C'_j}$ *Eq. (3)*

12: $\lambda = \lambda + 1$

13: **end for**

14: **for** $C_i \in \mathbf{C}_{\mathcal{L}}^*$ **do** * Compute the final flats F_i *

15: $[C_{m_i}^0] = USV^T$

where m_i is the sample mean of C_i , $[C_{m_i}^0]$ is the data matrix formed by the samples in C_i shifted by m_i and U, S, V are the results of its d-rank SVD.

16: $F_i = U$

17: **end for**

Output: $\mathbf{C}_{\mathcal{L}}^*, \mathbf{F}$