

Q1 APPROXIMATION: Independent Set

Give an algorithm that attempts to find an approximation to the maximum independent set in a graph $G = (V, E)$ where the maximum degree of any vertex is d . Think of a simple greedy solution with a good heuristic.

Show that the algorithm runs in polynomial time.

Justify the correctness of the algorithm.

What is the bound on the approximation ratio of your algorithm?

Can you construct a graph instance that would show your approximation analysis to be tight.

Q2 APPROXIMATION: TSP

The input to the traveling salesman problem (TSP) is an undirected graph with edge weights, and the optimal output is a cycle that visits every vertex exactly once (a tour) with minimum total weight. This problem is known to be NP-complete.

Can you use the MinimumSpanningTree algorithm to produce a constant k -approximation algorithm for the TSP.

What is the constant k ?

What assumptions if any does your algorithm make of the edge weights?