Use a frequentis multilevel logistic regression model (random intercept) to predict 2020 American Federal Election result and post-stratification to verify the model

Apply the frequentis multilevel logistic regression model and make diagnosis on the performance of the model

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Abstract

This report focused on using a frequentis multilevel regression model (random intercept) to predict if Donald Trump or Joe Biden can be selected as 2020 USA president. In order to build the model, we use a survey dataset (Tausanovitch, Chris and Lynn Vavreck, 2019)(Steven Ruggles, Sarah Flood, Ronald Goeken, Josiah Grover, Erin Meyer, Jose Pacas and Matthew Sobek, 2020) to build the model and a census dataset (PUMS USA, 2020) to predict who will be elected for post stratification purpose. Our model predicts that Joe Biden will be elected with significant superiority with respect to electoral votes, and we discussed the result. However, since there are some drawbacks in our model, we also discuss the weakness and how we can improve it.

key words: USA 2020 election, Donald Trump, Joe Biden, multilevel logistic regression model, post-stratification, prediction

Please click "here" to access the GitHub repository for all work.

Model

In this model, we are predicting the vote outcome of the 2020 American federal election by employing random intercept model and post-stratification technique. In the following sub-sections we will describe the logistic model regression specifics and the post-stratification calculation.

Model Specifics

We will be using a random intercept model to model the voters who will vote for Donald Trump run by R studio. We will be using sex, age_group, race, hispan, education, state, and vote_trump to model the probability of voting for Donald Trump. The logistic regression model we are using is:

$$\log \frac{p}{1-p} = \beta_0 + \beta_1 * sexmale + \beta_2 * age_group18 - 20 + ... + \beta_{18} * education tertiary (not bachelor) + \epsilon_1 + \beta_2 + \epsilon_2 + \epsilon_3 + \epsilon_4 + \epsilon_4 + \epsilon_5 +$$

Where p is the probability of Donald Trump got selected. $\log \frac{p}{1-p}$ is the odds of trump winning the election. β_0 represents intercept of the model which is 2.10152. Residual epsilon represents the error. Additionally, $\beta_1 to\beta_{18}$ represent the slope of the model, and relate to each variables. $\beta_1 = 0.41511$, $\beta_2 = -1.62472$, ...,

 $\beta_{18} = -0.45434$ respectively according to the summary data. So, for example, for everyone one unit increase in sexmale, we expect a β_1 increase in the probability of voting for Donald Trump.

```
##
                                                                     hispan
        sex
                          age_group
                                                 race
##
    Length: 3467
                        Length: 3467
                                             Length: 3467
                                                                  Length: 3467
##
    Class : character
                         Class : character
                                             Class :character
                                                                  Class :character
##
    Mode :character
                        Mode :character
                                             Mode :character
                                                                  Mode :character
##
##
##
##
     education
                            state
                                               vote_trump
##
    Length: 3467
                         Length: 3467
                                                     :0.0000
                                             Min.
##
    Class : character
                         Class : character
                                             1st Qu.:0.0000
##
    Mode :character
                        Mode :character
                                             Median :1.0000
##
                                             Mean
                                                     :0.5097
##
                                             3rd Qu.:1.0000
##
                                             Max.
                                                     :1.0000
##
        sex
                     age_group
                                                                   race
                   >= 70 :381
##
    female:1591
                                  american indian or alaska native:
                                                                        24
##
    male :1876
                   18 ~ 20: 23
                                  asian or pacific
                                                                     : 136
                   20 ~ 30:328
##
                                  black
                                                                     : 366
##
                   30 ~ 40:697
                                                                     : 174
                                  other
                   40 ~ 50:701
##
                                  white
                                                                     :2767
                   50 ~ 60:590
##
                   60 ~ 70:747
##
##
              hispan
                                             education
                                                                state
##
                    19
                          at most high school
                                                           CA
                                                                   : 376
    cuban
                                                   : 584
                 : 238
                                                           NY
##
    mexican
                          bachelor
                                                   :1620
                                                                   : 314
                                                           FL
    not hispanic:3059
                          graduate
                                                   : 757
##
                                                                   : 292
                 : 148
##
    other
                          tertiary (not bachelor): 506
                                                           TX
                                                                   : 226
##
    puerto rican:
                                                           IL
                                                                   : 157
##
                                                           OH
                                                                   : 155
##
                                                            (Other):1947
##
      vote_trump
##
            :0.0000
    1st Qu.:0.0000
##
##
    Median :1.0000
##
    Mean
            :0.5097
    3rd Qu.:1.0000
##
##
            :1.0000
    Max.
##
## # A tibble: 1 x 1
##
     prop_vote_trump
##
                <dbl>
## 1
                0.510
```

Logistic: p-value, AIC, BIC

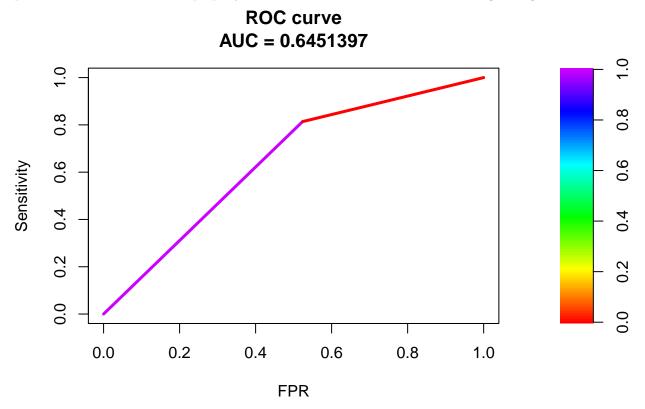
According to the summary of the model, the p-value of sexmale, raceasian or pacific, raceblack, raceother, hispanmexican, hispannot hispanic, hispanother, and education backgrounds are less than 0.05, therefore, these factors are rejecting the null hypothesis. The other factors have p-value that greater than 0.05, which means that there are evidence of not rejecting the null hypothesis. The AIC and BIC are 4335.9 and 4458.9 respectively. AIC and BIC are used to indicate the accuracy after considering the complexity. However, they

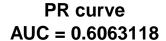
are usually used to compare between two models. We only have one model presented in this case. Therefore, AIC and BIC are meaningless without the model selection step. It can be meaningful when there are other models exists. The model with less AIC and BIC is better than the other one.

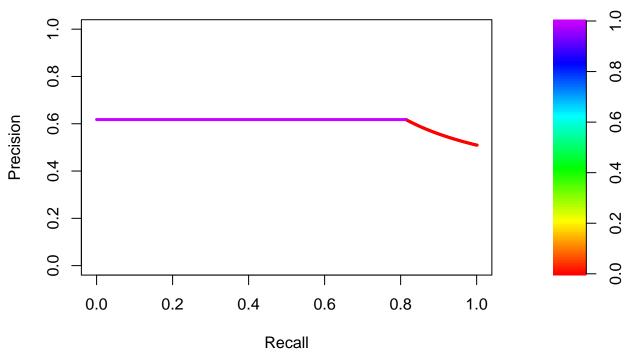
```
## Generalized linear mixed model fit by maximum likelihood (Laplace
##
     Approximation) [glmerMod]
   Family: binomial (logit)
## Formula: vote_trump ~ sex + age_group + race + hispan + education + (1 |
##
       state)
##
     Data: survey_set
##
##
        AIC
                 BIC
                       logLik deviance df.resid
##
     4335.9
              4458.9 -2147.9
                                4295.9
                                           3447
##
## Scaled residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
  -2.2688 -1.0089 0.5580 0.8129
                                    4.6751
##
## Random effects:
                       Variance Std.Dev.
## Groups Name
## state (Intercept) 0.0565
                                0.2377
## Number of obs: 3467, groups: state, 51
## Fixed effects:
                                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                     2.10152
                                                0.73666
                                                          2.853 0.004334 **
## sexmale
                                                0.07578
                                                          5.478 4.30e-08 ***
                                     0.41511
## age_group18 ~ 20
                                    -1.62472
                                                0.66708 -2.436 0.014868 *
## age_group20 ~ 30
                                    -0.23053
                                                0.17010 -1.355 0.175340
## age group30 ~ 40
                                    -0.01900
                                                0.13696 -0.139 0.889689
## age_group40 ~ 50
                                    0.20558
                                                0.13742
                                                          1.496 0.134634
## age_group50 ~ 60
                                    0.15819
                                                0.14086
                                                          1.123 0.261423
## age_group60 ~ 70
                                                0.13392
                                    0.02292
                                                          0.171 0.864082
## raceasian or pacific
                                    -1.50903
                                                0.49078 -3.075 0.002107 **
## raceblack
                                    -3.21613
                                                0.49016 -6.561 5.33e-11 ***
## raceother
                                    -1.00184
                                                0.48213
                                                         -2.078 0.037715 *
## racewhite
                                    -0.48299
                                                0.45368 -1.065 0.287054
## hispanmexican
                                    -1.74771
                                                0.58520 -2.987 0.002822 **
## hispannot hispanic
                                                0.56529 -1.978 0.047908 *
                                    -1.11824
## hispanother
                                    -1.30600
                                                0.59093 -2.210 0.027100 *
## hispanpuerto rican
                                    -1.54304
                                                1.45366 -1.061 0.288470
                                                0.10938 -4.498 6.86e-06 ***
## educationbachelor
                                    -0.49200
## educationgraduate
                                    -0.46929
                                                0.12589
                                                         -3.728 0.000193 ***
## educationtertiary (not bachelor) -0.45434
                                                0.13576 -3.347 0.000818 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 19 > 12.
## Use print(x, correlation=TRUE)
       vcov(x)
                      if you need it
## convergence code: 0
## Model failed to converge with max|grad| = 0.00781382 (tol = 0.002, component 1)
```

Logistic: ROC and PR curve

ROC (Receiver Operating Characteristics) curve plot is a visualization of the sensitivity and FPR. The larger the area under the curve (AUC, $\max=1$) is, the better the curve is. In this model, the AUC is 0.6451397, which means that the performance of this model is moderately credible. PRC (Precision-recall Curve) is used for showing the relation between precision and recall. The AUC is 0.6063118. Therefore, this model can have predictive value if the value is properly set, which is more accurate than random guessing.







Logistic: Confusion Matrix and Accuracy

The confusion matrix is used for summarizing predicted result and check the true positive and true negative rate of the model. It also gives an accuray about 0.6484, which is not bad in terms of true positive and true negative rate. Also seen from the confusion matrix below, the false positive rate is more than half of the true positive rate (ratio: $\frac{890}{1438}$), and the false negative rate is nearly half of the true negative rate (ratio: $\frac{329}{810}$). Therefore, the model performs terribly with respect to false positive rate and not well with respect to false negative rate.

```
Confusion Matrix and Statistics
##
##
             Reference
##
  Prediction
                 0
                      1
##
            0
               810 329
##
               890 1438
##
##
                  Accuracy: 0.6484
                    95% CI: (0.6322, 0.6643)
##
       No Information Rate: 0.5097
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.2921
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
##
               Sensitivity: 0.4765
##
               Specificity: 0.8138
            Pos Pred Value: 0.7112
##
```

```
## Neg Pred Value : 0.6177
## Prevalence : 0.4903
## Detection Rate : 0.2336
## Detection Prevalence : 0.3285
## Balanced Accuracy : 0.6451
##
## 'Positive' Class : 0
##
```

Post-Stratification

Post-stratification refers to the random sampling of a population and sampling of a sample n. After the survey, n units are divided into several layers according to certain stratification factors. Then stratified sampling estimation is carried out. In this project, post stratification is collecting the census data and applying the MR model to the census data to predict each individuals' voting result. It is useful because it is difficult to stratify the whole in a certain way beforehand. And the operation is simple, low cost, in the case of incomplete information, can be applied. In order to estimate the proportion of voters who will vote for Donald Trump we need to perform a post-stratification analysis. Here we create cells based on different states. Using the model described in the previous sub-section we will estimate the proportion of voters in each state. We will then weight each proportion estimate (within each state) by the respective population size of that state and sum those values and divide that by the entire population size. The reason why we choose "state" is because each state have electoral votes (total 538 votes this year) and who won more than 270 electoral votes wins the election [16]. Therefore, it is essential to predict according to states.

```
##
        sex
                      age_group
                                                                      race
##
    female:23559
                    >= 70 :8211
                                     american indian or alaska native:
                                                                           117
##
    male :19888
                    18 ~ 20: 596
                                     asian or pacific
                                                                        :13784
                    20 ~ 30:3203
##
                                     black
                                                                        : 3706
##
                    30 ~ 40:5419
                                                                        : 5017
                                     other
##
                    40 ~ 50:8260
                                     white
                                                                        :20823
##
                    50 ~ 60:9541
##
                    60 ~ 70:8217
##
                                               education
              hispan
                                                                   state
                                                                      :11347
##
    cuban
                 : 1474
                           at most high school
                                                    :21528
                                                              CA
                 : 6264
                           bachelor
                                                              NY
                                                                      : 4836
##
    mexican
                                                    :11340
##
    not hispanic:30272
                           graduate
                                                    : 5746
                                                              FL
                                                                      : 4710
##
    other
                           tertiary (not bachelor): 4833
                                                              TX
                                                                      : 3600
                 : 5277
##
    puerto rican:
                   160
                                                              NJ
                                                                      : 2153
##
                                                              TI.
                                                                      : 1636
##
                                                              (Other):15165
##
        perwt
##
                5.23
    Min.
    1st Qu.: 308.57
##
##
    Median: 444.55
##
            : 568.17
    3rd Qu.: 679.90
##
##
            :9607.51
##
##
   # A tibble: 51 x 2
##
      state trump_predict
##
      <fct>
                     <dbl>
                     0.468
##
    1 AK
##
    2 AL
                     0.500
```

```
3 AR
                      0.560
##
    4 A7.
                      0.484
##
    5 CA
##
                      0.402
    6 CO
                      0.487
##
##
    7
      CT
                      0.381
##
    8 DC
                      0.370
    9 DE
                      0.379
## 10 FL
                      0.545
## # ... with 41 more rows
```

Results

In this section, we will predict whether Donald Trump or Joe Biden will win the final federal election. The total number of electoral votes is 538, and the proportion of people who are willing to vote for Trump is predicted to be around 51% by using survey data. However this result has no personal weight which means that it cannot be used as the final result. It can only be used as a reference for future predictions. Therefore, we make predictions about the outcome of the general election by considering the electoral college. This model is accounted for variables of "sex" "age_group", "race", "hispan", "state" and "education". There are 51 states in America based on the dataset. We will predict the voting situation of these state voters. The prediction results show that there are 27 states where the percentage of voting Trump is between 0.4 and 0.5. For example, the state of Alaska (AK) has a 0.468 (46.8%) predicted voting rate of Trump. In the state of Alabama (AL), the number is 0.500 (50.0%). It is very balanced. Trump and Biden would do more campaigns on this kind of states to increase the possibility of winning. Moreover, the result demonstrates that in the state of California (CA) and Connecticut (CT), Trump's support is slightly weaker, with only 0.402 (40.2%) and 0.381 (38.1%) under the estimation. However, in the state of Arkansas (AR) and Montana (MT) the support rate for Trump is relatively high with rate of 0.560 (56.0%) and 0.583 (58.3%). In the state of District of Minnesota (MN) and Maryland (MD), we predict that voters' support for Trump would be the lowest, 0.353 (35.3%) and 0.345 (34.5%) respectively. According to our model's prediction result, Joe Biden will receive a total of 422 electoral votes, while Donald Trump will only receive 116 electoral votes. Joe Biden has more states in favor of voting for him, so we expect democratic presidential candidate, Joe Biden, to win the election.

Discussion

Summary

We try to build a logistic regression model to predict whether Donald Trump or Joe Biden will win the final federal election. First, we use the electoral college to predict the outcome of the general election and select the variables "sex, age_group", "race", "hispan", "education", and "state" to create our model. Then we made the final model diagnosis by judging AIC and BIC, observing p-value, roc curve, pc curve, and confusion matrix.

Then we conducted Post-Stratification, which is a random sampling of a population. In the case of insufficient information, we can use the MR model to predict census data to predict the voting result and perform a post-Stratification analysis. We will predict the proportion of voters in favour of voting in each state and calculate who won more than 270 votes at the end. Therefore, we will predict the voting situation of voters

in 51 states in the U.S. Among them, from the model prediction results, we can see that voters in Arkansas (AR) and Montana (MT) tend to vote for Trump. However, in Minnesota (MN) and Maryland (MD) states, Trump is predicted to have low approval rate, indicating that Joe Biden has a relatively high win rate in these states. By calculating total electoral votes, we estimate that Joe Biden will receive a total of 422 electoral votes, while Donald Trump will only receive 116 electoral votes; therefore, we expect the democratic presidential candidate Biden to win the final election.

Conclusion

In conclusion, we predict that Joe Biden who is the presidential nominee of democratic party would win in the election. Based on our model, Joe Biden would get 422 electoral votes in total while Donald Trump would only get 116 electoral votes. The difference is quite big because Joe Biden has much more states that in favour of voting him based on our model.

Weaknesses

Based on the above analysis, there are a few weaknesses of this model. First, the number of variables is quite small in both dataset and model. In the model, we only use 6 variables and we mainly focus on the demographic variables. We neglect variables that keep abreast of times. For example, in the 2016 US election, the Facebook marketing plays a key factor in Trump's winning [11]. However, the datasets of census and survey do not provide this kind of campaign variables. Thus, the model would be out of date for election of this year. Second, the dataset of census does not contain the information on people's party preference on democratic and republican. People who like democratic better would be more likely to vote for Joe Biden while people who like republican more would vote for Donald Trump. With this information, the model would be more precise. We could have a basic estimate on the voting of Joe Biden and Donald Trump. However, this information is not available. Third, when we build the model, we do not consider income factor. Typically, voters for Donald Trump are people who have a lower income while people who has a higher income tend to vote for Joe Biden. Although the income variable in census represents personal total income and the one in survey represents household income, we should still take income into this model. Fourth, when we clean the raw data of census, we are too general on some specific variables. For example, when we clean the variable of race, we combine Asian and Pacific Islander together for convenience. There are a lot of groups under Asian like Chinese, Korean, Japanese and so on. These groups would have some trends on voting based on their background and this may influence the result of election a lot. Nonetheless, we ignore these features in the model and this would cause a weak prediction. Furthermore, it is worth noting that education variable plays a very important role in the election. When we design the survey of election preference, we should include more people that have lower education level. In the survey dataset, it includes more people who have higher education level, and this would make the prediction in favor of Joe Biden [12]. People with higher education level would be more likely to vote for Joe Biden [12].

Next Steps

In order to make the estimation of model more accurate, we should find ways to eliminate the above weaknesses. For instance, we could clean the data in a more detailed way and include more variables in the analysis. We should also include survey that contains more people that has lower education level. Since the election result would be out on November 3rd, we could compare the actual result of election with our prediction. We need to do a post-hoc analysis. First, we could figure out if our prediction result match the real result. And then, we should know how big the difference is between the predicted total electoral votes and the actual one. If the difference is very big, we may need to switch to another model. For example, we could use Principal Component Analysis (PCA) which is an algorism that decreases dimensional space to start the model [13]. This would eliminate some unnecessary variables from the data and mainly focus on the key principles to predict the election. It is also important to figure out which factor is the key success factor on the election. If

we do not include that in the model, we definitely need to add that. After, the analysis, we could redesign the model and check if the new one provides a result that is closer to the actual result. Moreover, some machine learning technology could help us to build a better model. The use of artificial neural networks, which is a brain-spired system, would help the model a lot [14]. It would decrease the uncertainty of the model. All of these would better improve the estimation of this model in future elections.

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