

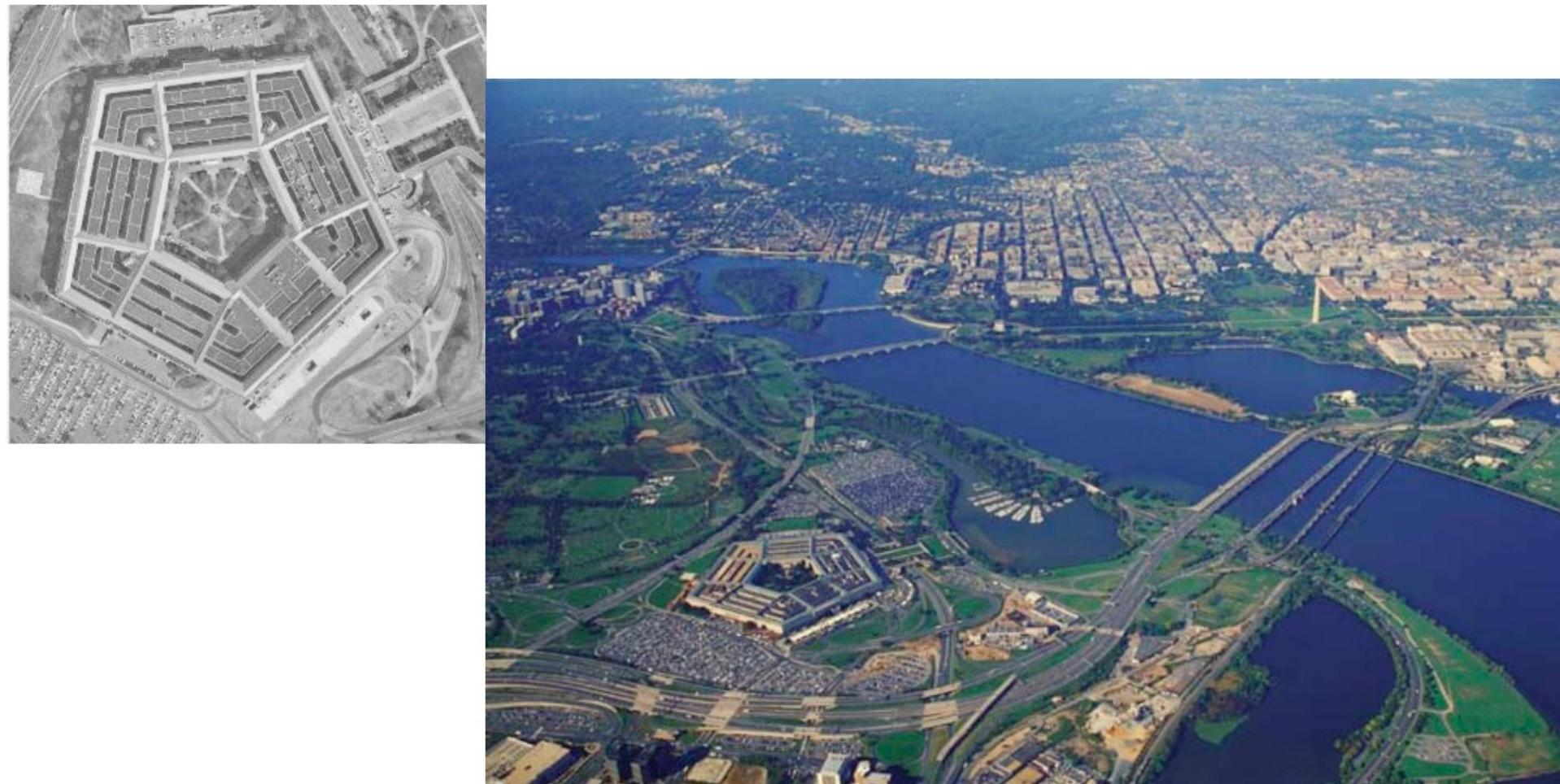
Feature Detection and Matching

Feature Point

Motivation

Requirements

Image Matching



Slide credit: Ranjay Krishna

Image Matching



by [Diva Sian](#)



by [swashford](#)

Slide credit: Steve Seitz

Image Matching

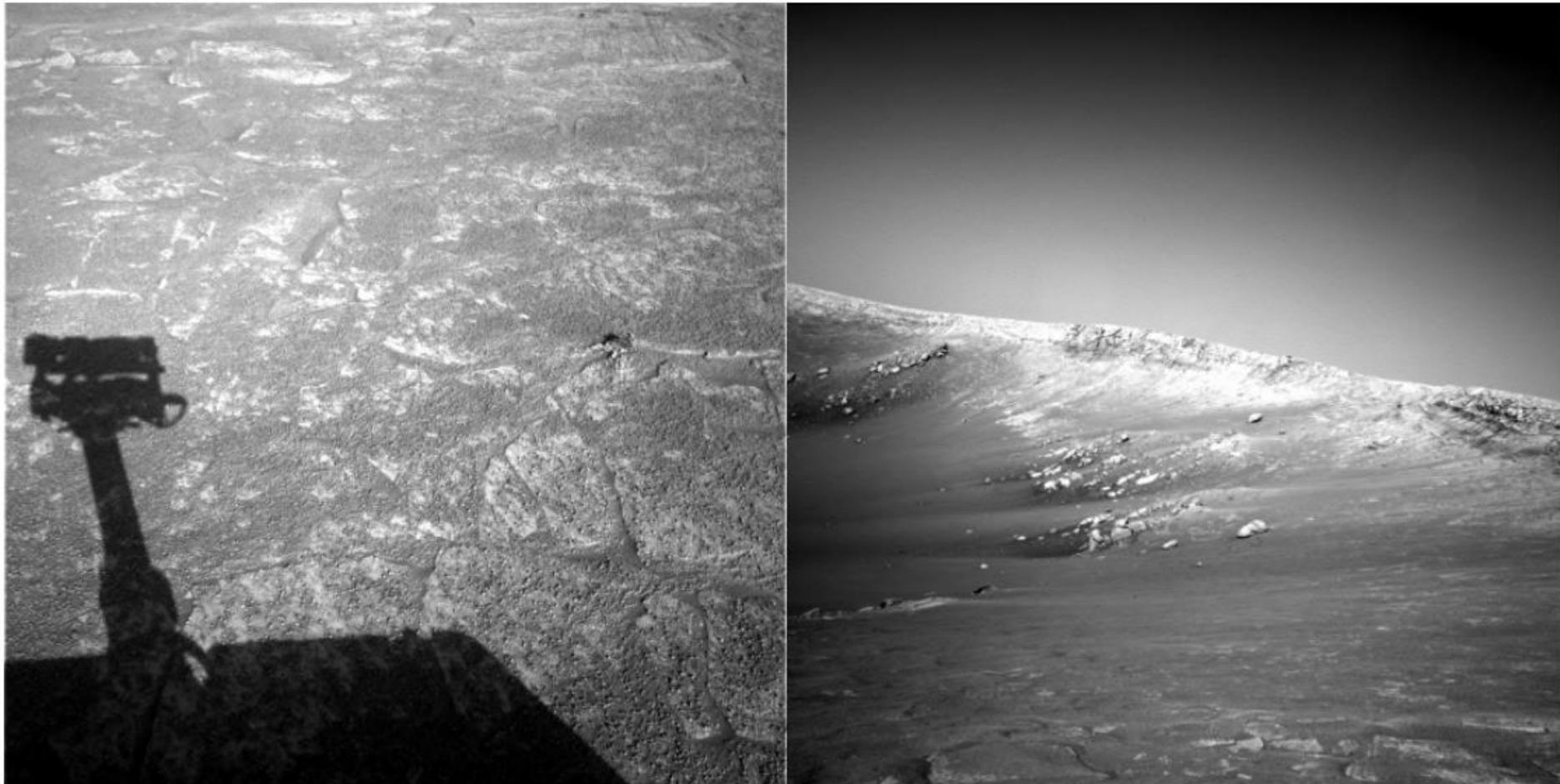


by [Diva Sian](#)



by [scgbt](#)

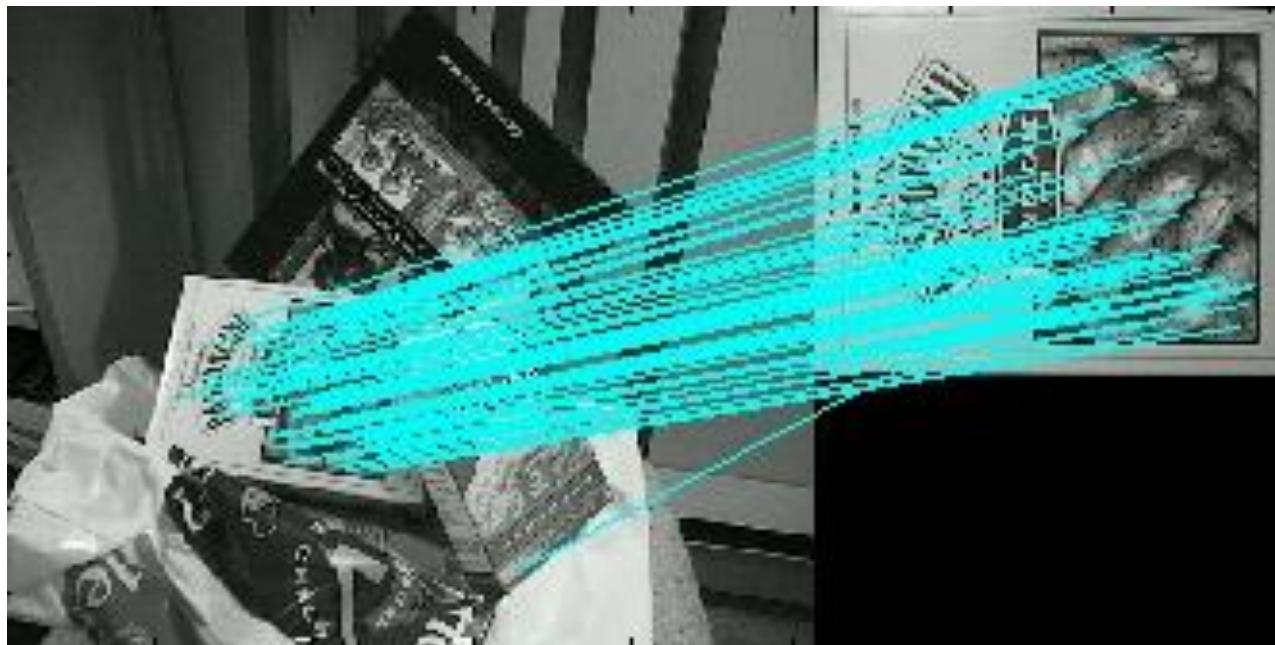
Can you match two images?



NASA Mars Rover images

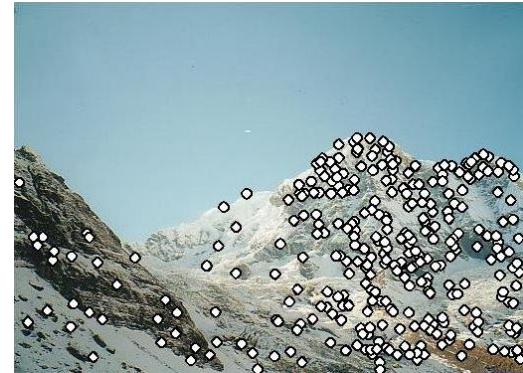
Slide credit: Steve Seitz

Feature Points



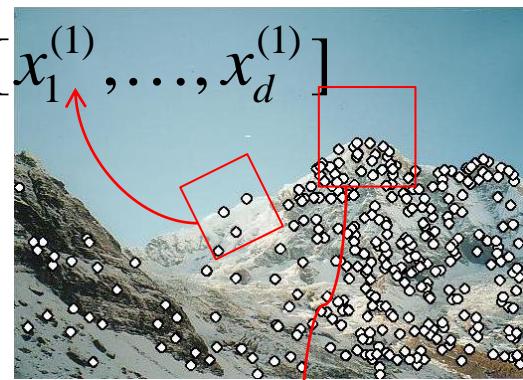
Local Features

- 1) Detection: Identify the interest points



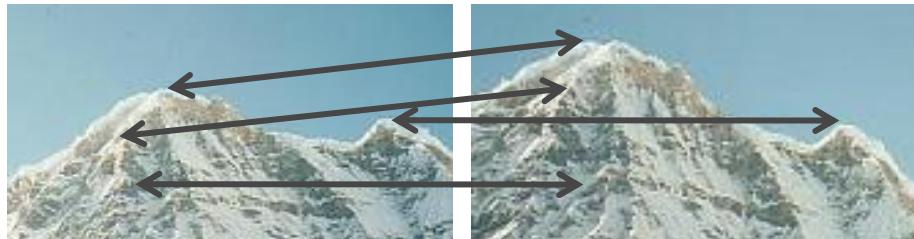
- 2) Description: Extract vector feature descriptor surrounding each interest point.

$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$



- 3) Matching: Determine correspondence between descriptors in two views

$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

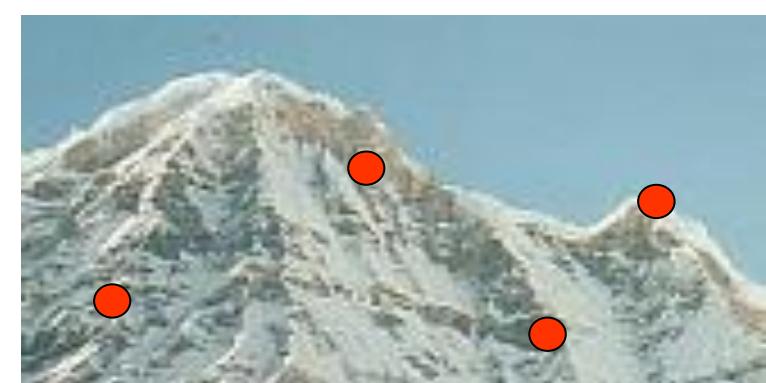


Properties for Local Features

- ▶ **Repeatability**
 - The same feature can be found in several images despite geometric and photometric transformations
- ▶ **Saliency**
 - Each feature has a distinctive description
- ▶ **Compactness and efficiency**
 - Many fewer features than image pixels
- ▶ **Locality**
 - A feature occupies a relatively small area of the image; robust to clutter and occlusion

Repeatability (1 / 2)

- ▶ We want to detect (at least some of) the same points in both images.

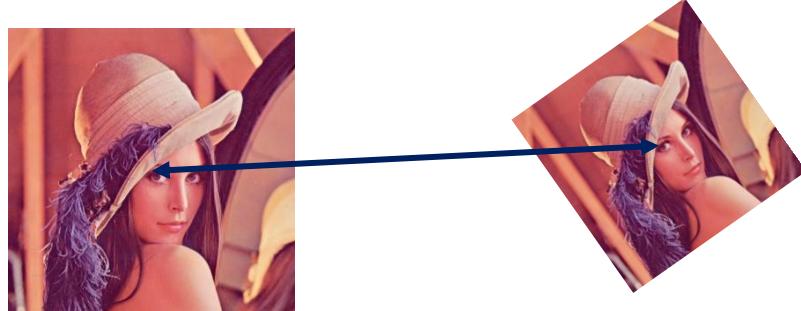


No chance to find true matches!

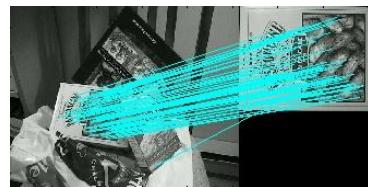
- ▶ Yet we have to be able to run the detection procedure *independently* per image.

Repeatability (2/2)

- ▶ Invariant to translation, rotation, and scale



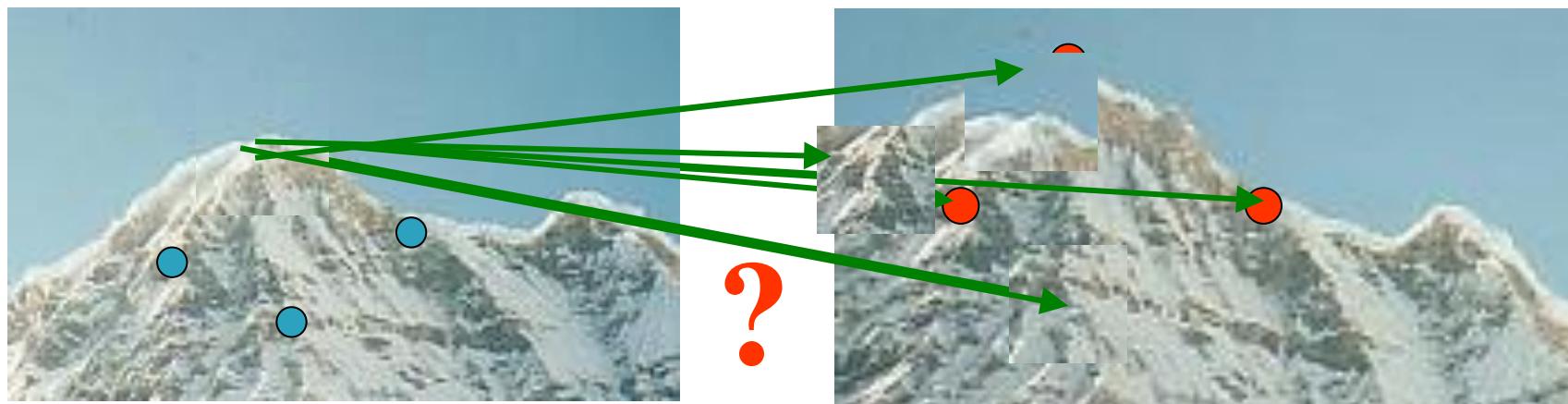
- ▶ Robust to transformation



- ▶ Robust to lighting and noise

Distinctiveness

- ▶ We want to be able to reliably determine which point goes with which.



- ▶ Must provide some invariance to geometric and photometric differences between the two views.

Local Invariant Features

- ▶ Hessian & **Harris** [Beaudet '78], [Harris '88]
- ▶ Laplacian, DoG [Lindeberg '98], [Lowe '99]
- ▶ Harris-/Hessian-Laplace [Mikolajczyk & Schmid '01]
- ▶ Harris-/Hessian-Affine [Mikolajczyk & Schmid '04]
- ▶ EBR and IBR [Tuytelaars & Van Gool '04]
- ▶ MSER [Matas '02]
- ▶ Salient Regions [Kadir & Brady '01]
- ▶ Others...

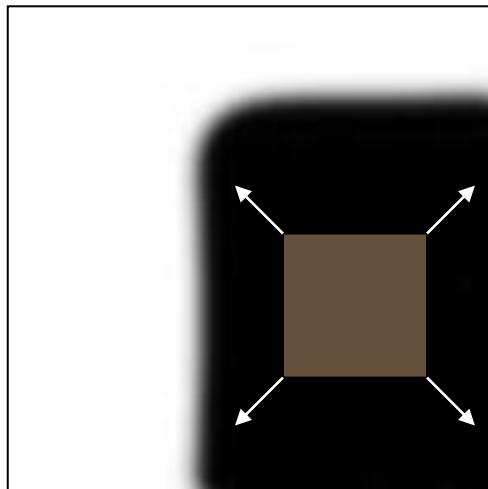
- ▶ Those detectors have become a basic building block for many applications in Computer Vision.

Feature Point Detection

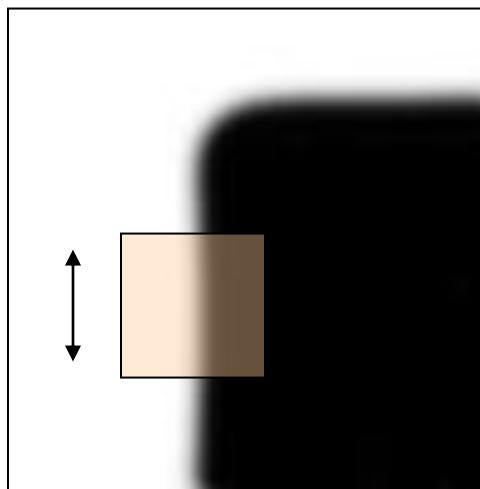
Harris Corner

Corners as distinctive interest points

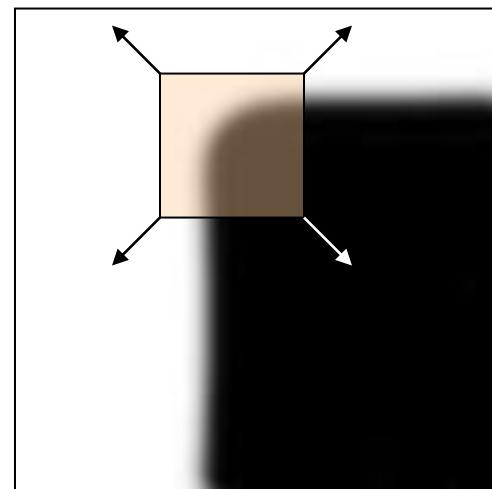
- ▶ Shifting a window in *any direction* should give *a large change* in intensity



“flat” region:
no change in all
directions

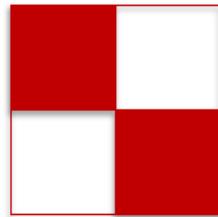


“edge”:
no change along th
e edge direction



“corner”:
significant change
in all directions

Corners versus edges

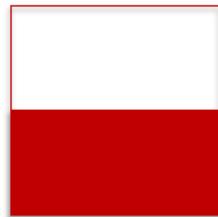


$$\sum I_x^2 \longrightarrow \text{Large}$$

$$\sum I_y^2 \longrightarrow \text{Large}$$

Corner

$$I_x \Leftrightarrow \frac{\partial I}{\partial x}$$

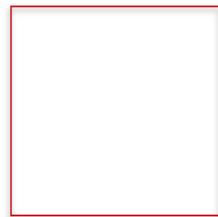


$$\sum I_x^2 \longrightarrow \text{Small}$$

$$\sum I_y^2 \longrightarrow \text{Large}$$

Edge

$$I_y \Leftrightarrow \frac{\partial I}{\partial y}$$

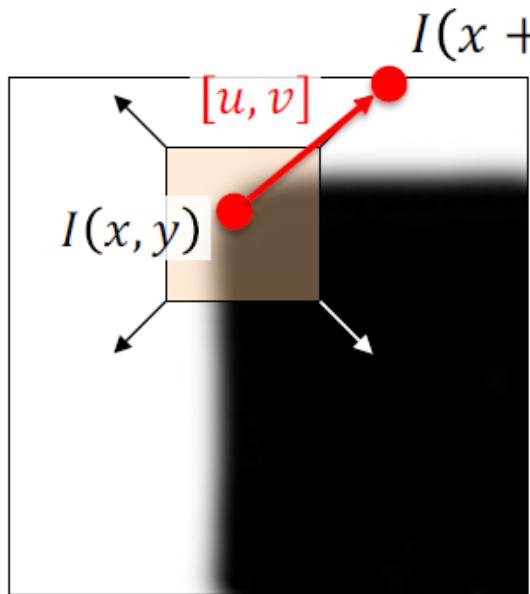


$$\sum I_x^2 \longrightarrow \text{Small}$$

$$\sum I_y^2 \longrightarrow \text{Small}$$

Nothing

Measure change in all directions



“corner”:
significant change
in all directions

Measure change as intensity difference:

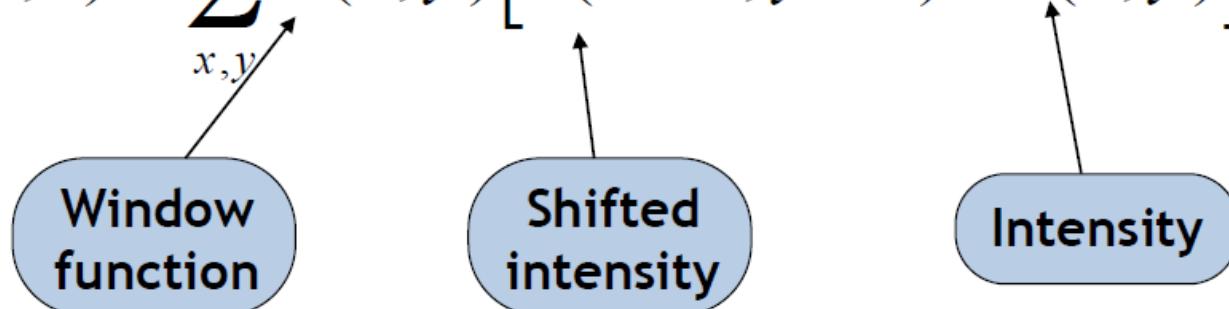
$$I(x + u, y + v) - I(x, y)$$

That's for a single point, but we have to accumulate over a "small window" around that point...

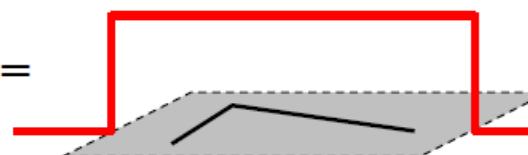
Harris Detector Formulation

- Change of intensity for the shift $[u,v]$:

$$E(u,v) = \sum w(x,y) [I(x+u, y+v) - I(x, y)]^2$$

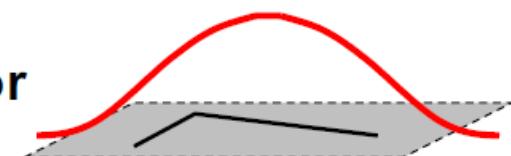


Window function $w(x,y) =$



1 in window, 0 outside

or



Gaussian

Harris Detector Formulation

- This measure of change can be approximated by (Taylor expansion):

$$E(u, v) \approx [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

where M is a 2×2 matrix computed from image derivatives:

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

↑
Sum over image region – the area we are
checking for corner

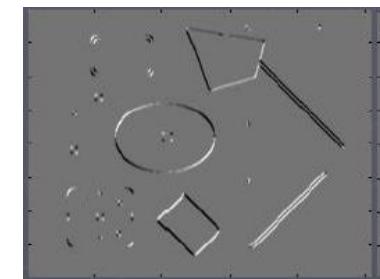
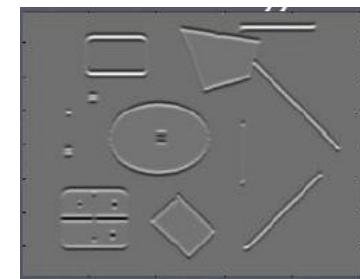
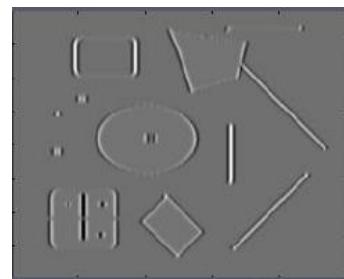
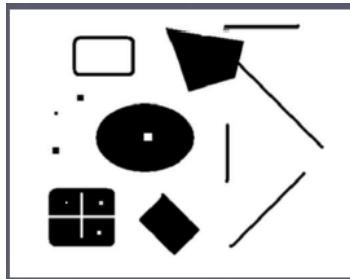
**Gradient with
respect to x ,
times gradient
with respect to y**

$$M = \begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} = \sum \begin{bmatrix} I_x \\ I_y \end{bmatrix} [I_x \ I_y]$$

Harris Detector Formulation

$$M = \sum w(x, y) \begin{bmatrix} I_x I_x & I_x I_y \\ I_x I_y & I_y I_y \end{bmatrix}$$

2 x 2 matrix of image derivatives



Notation:

$$I_x \Leftrightarrow \frac{\partial I}{\partial x}$$

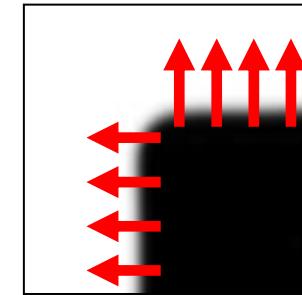
$$I_y \Leftrightarrow \frac{\partial I}{\partial y}$$

$$I_x I_y \Leftrightarrow \frac{\partial I}{\partial x} \frac{\partial I}{\partial y}$$

What does this matrix reveal?

- ▶ First, consider an axis-aligned corner:

$$M = \sum \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$$



- ▶ This means dominant gradient directions align with x or y axis
- ▶ Look for locations where both λ 's are large.
- ▶ If either λ is close to 0, then this is not corner-like.

What if we have a corner that is not aligned with the image axes?

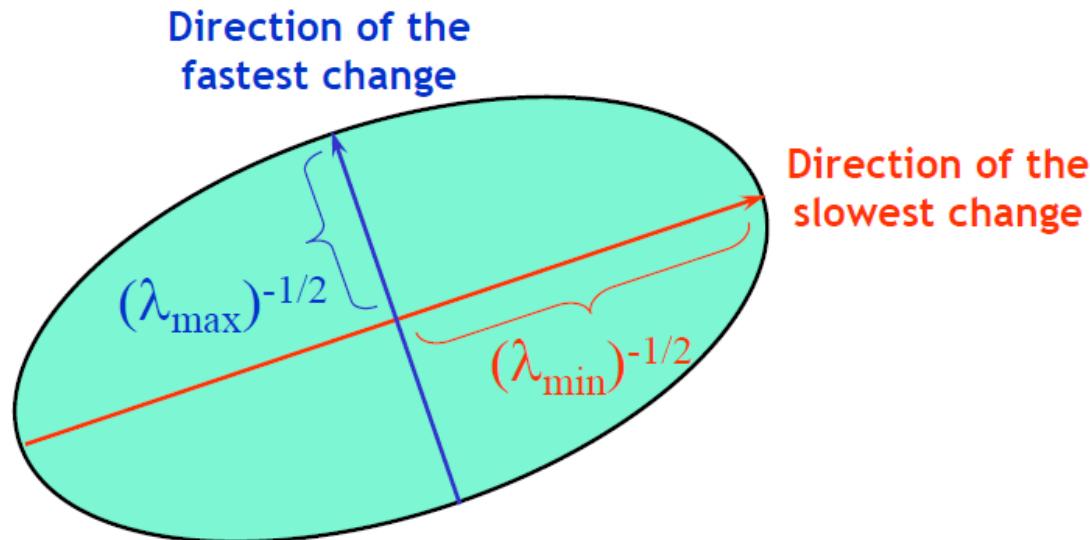
General Case

- Since M is symmetric, we have

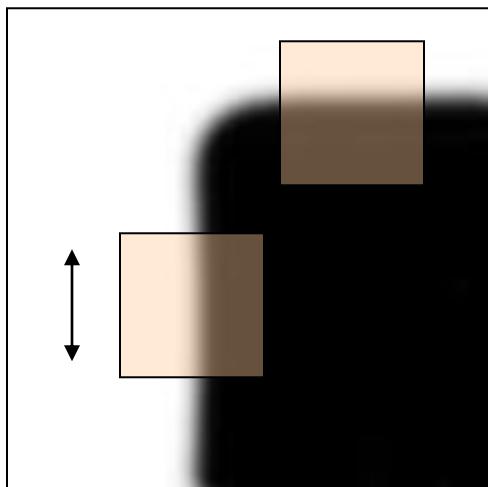
$$M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

(Eigenvalue decomposition)

- We can think of M as an ellipse with axis lengths determined by the eigenvalues and orientation determined by R

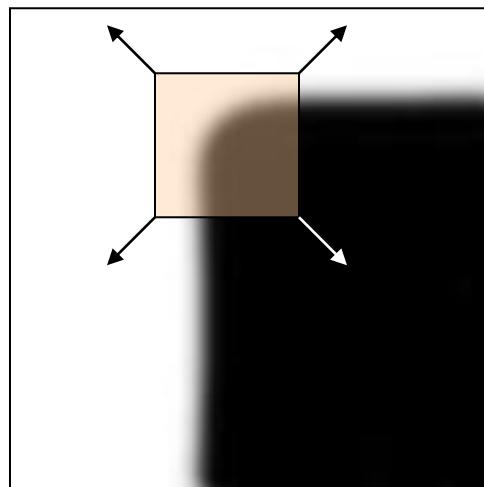


Example



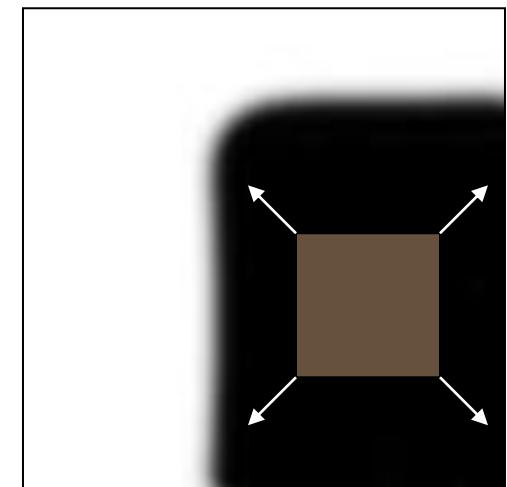
“edge”:

$$\begin{aligned}\lambda_1 &>> \lambda_2 \\ \lambda_2 &>> \lambda_1\end{aligned}$$



“corner”:

λ_1 and λ_2 are large,
 $\lambda_1 \sim \lambda_2$;

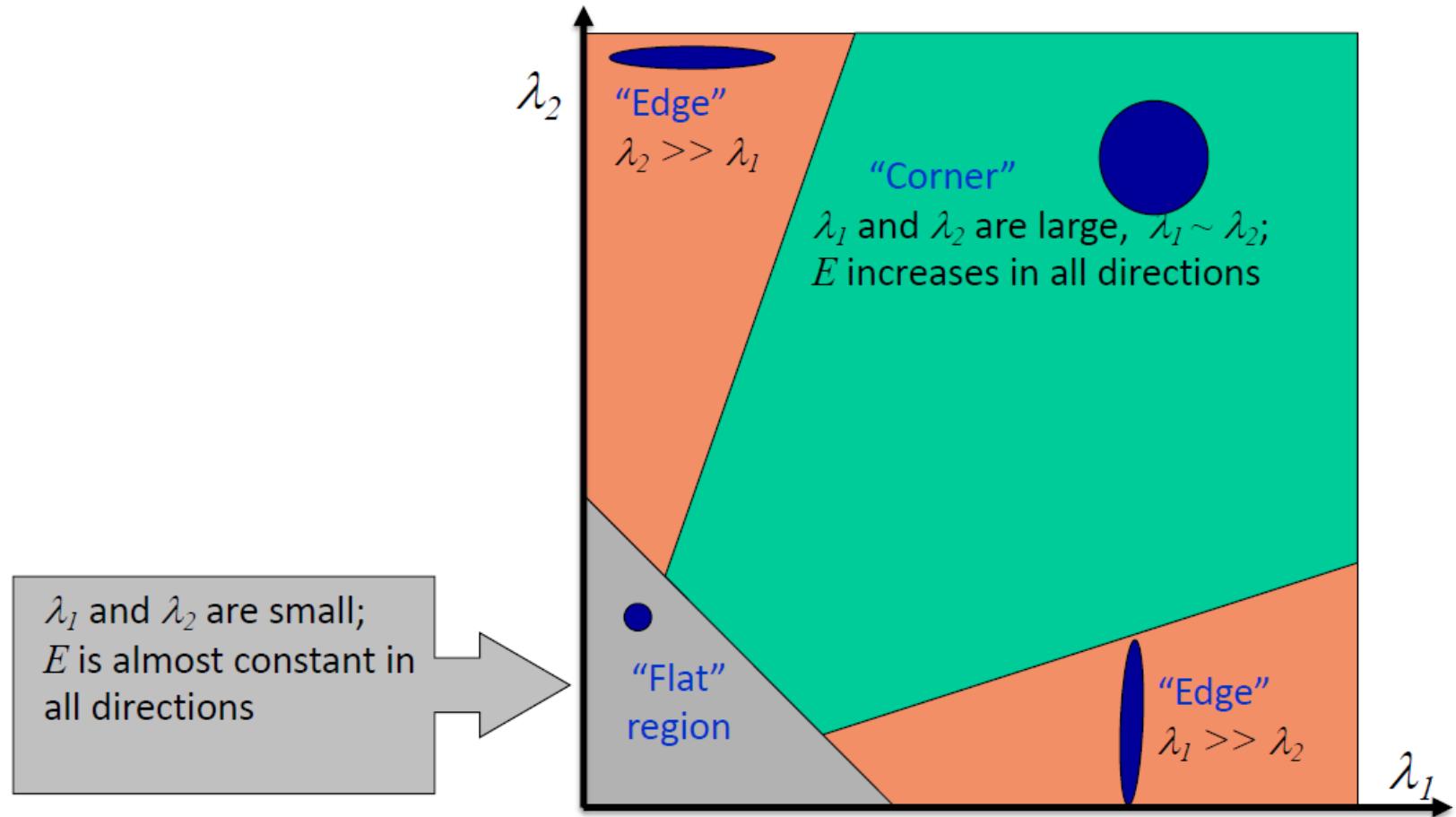


“flat” region

λ_1 and λ_2 are
small;

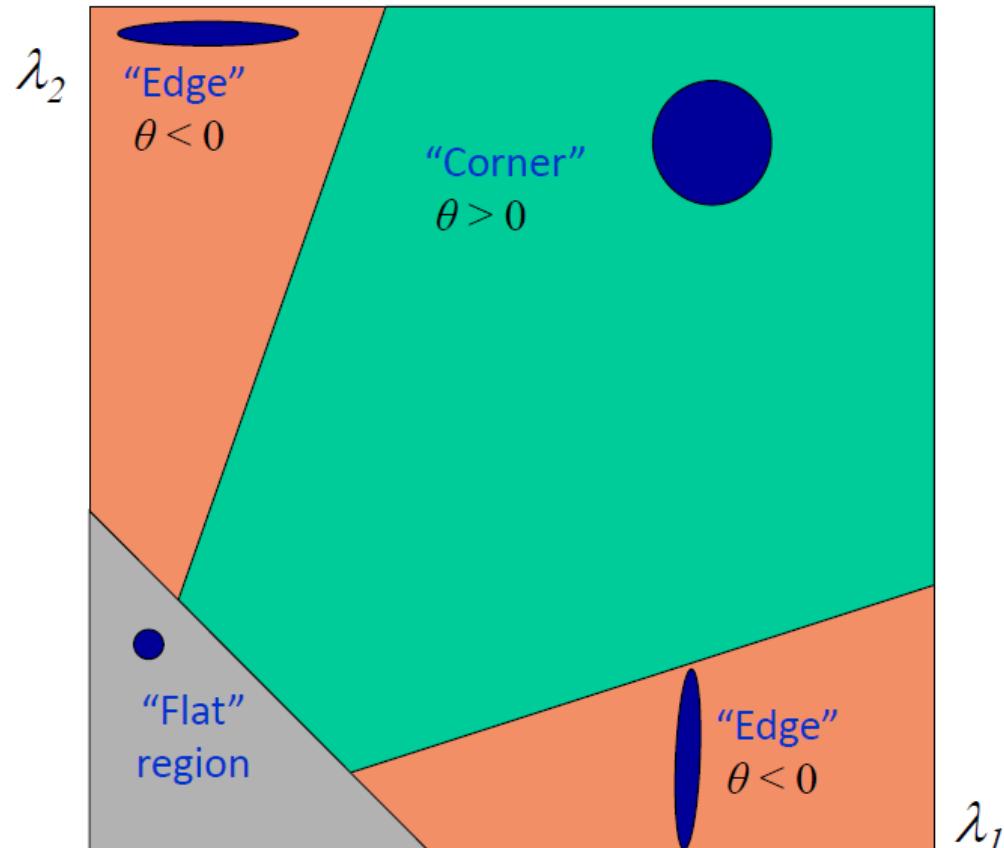
Interpreting the Eigenvalues

- Classification of image points using eigenvalues of M :



Corner Response Function

$$\theta = \det(M) - \alpha \operatorname{trace}(M)^2 = \lambda_1 \lambda_2 - \alpha(\lambda_1 + \lambda_2)^2$$



- Fast approximation
 - Avoid computing the eigenvalues
 - α : constant (0.04 to 0.06)

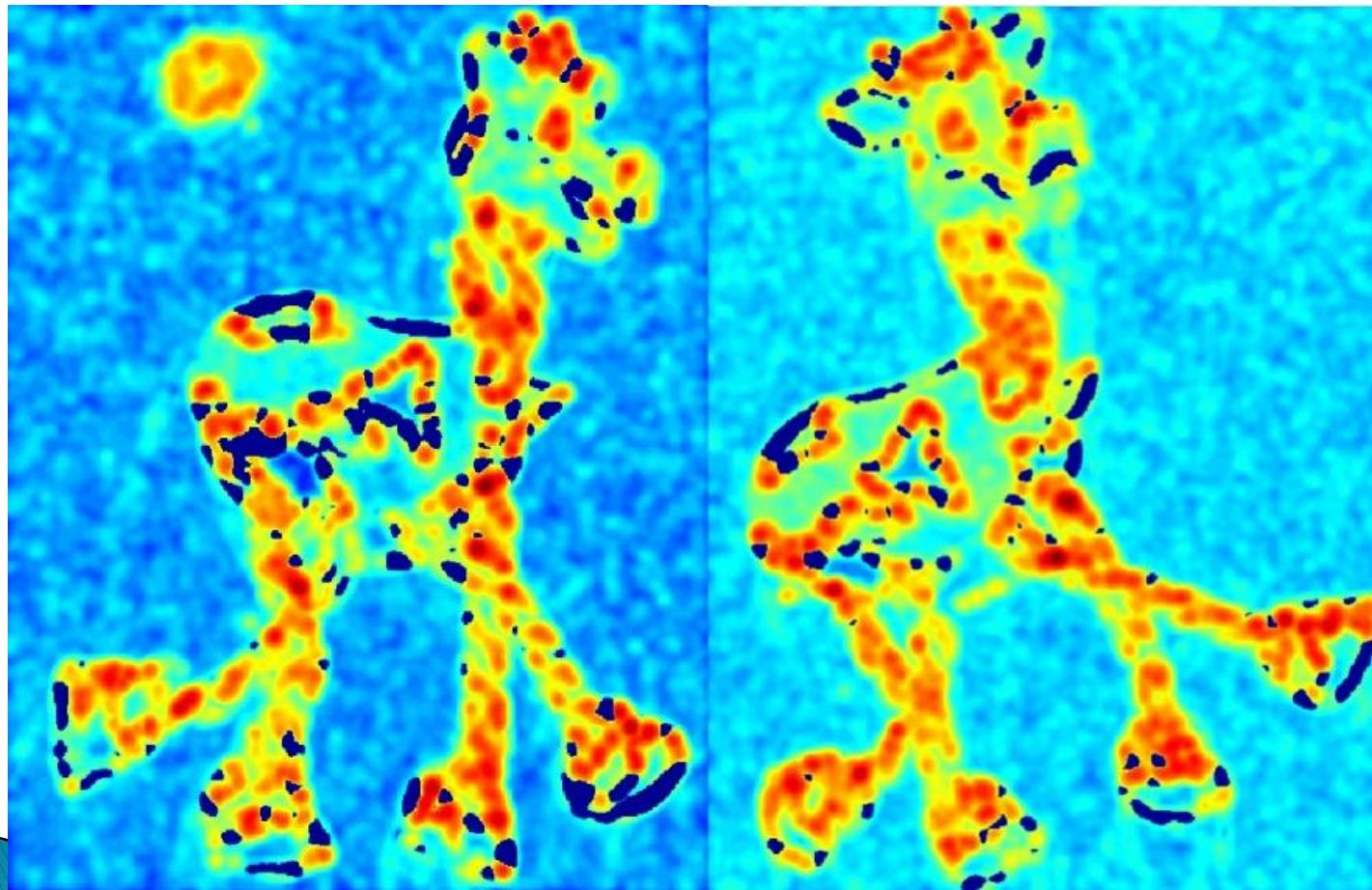
Harris Detector: Steps



Slide credit: Kristen Grauman

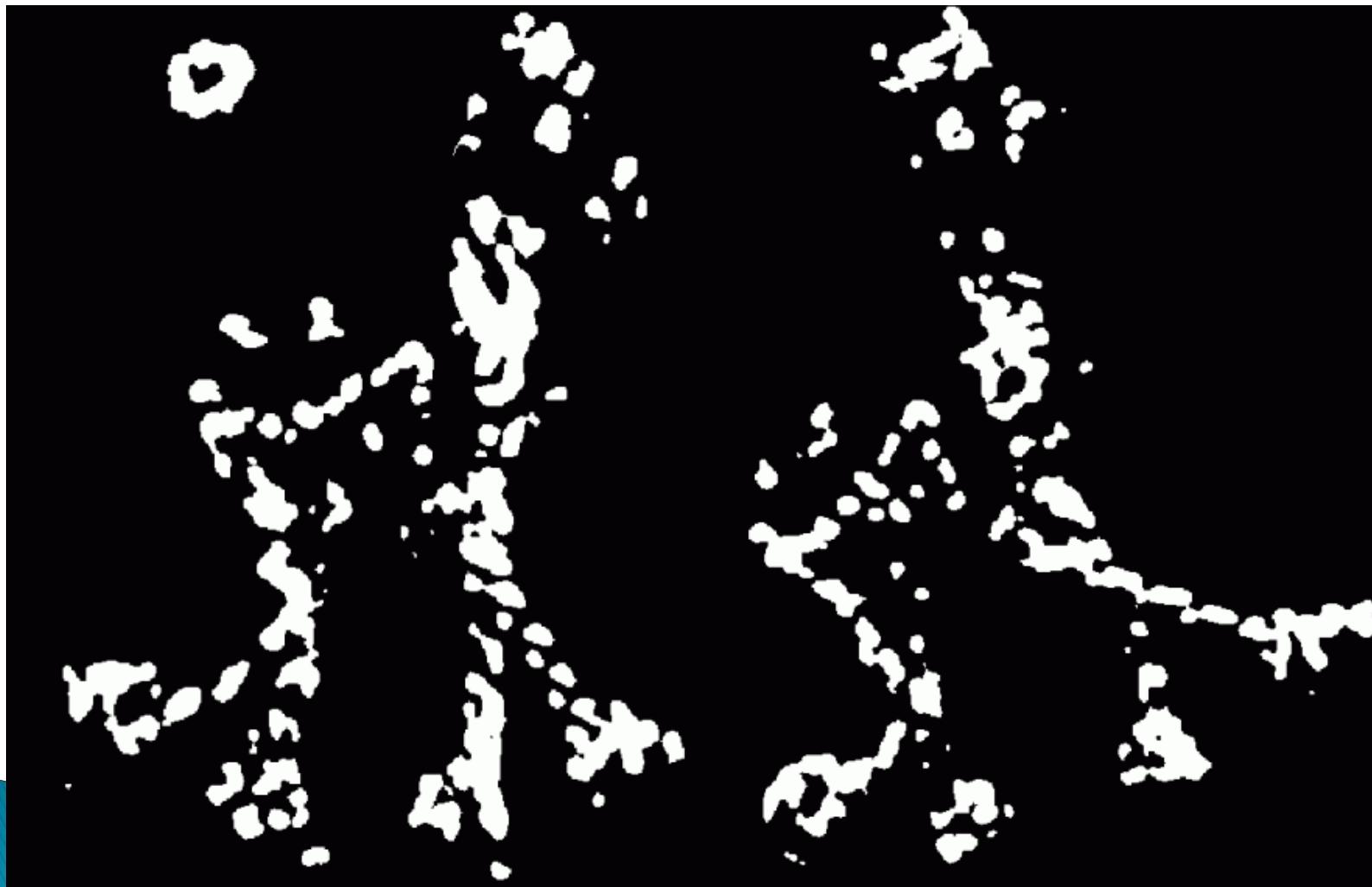
Harris Detector: Steps

Compute corner response f



Harris Detector: Steps

Find points with large corner response: $f > \text{threshold}$

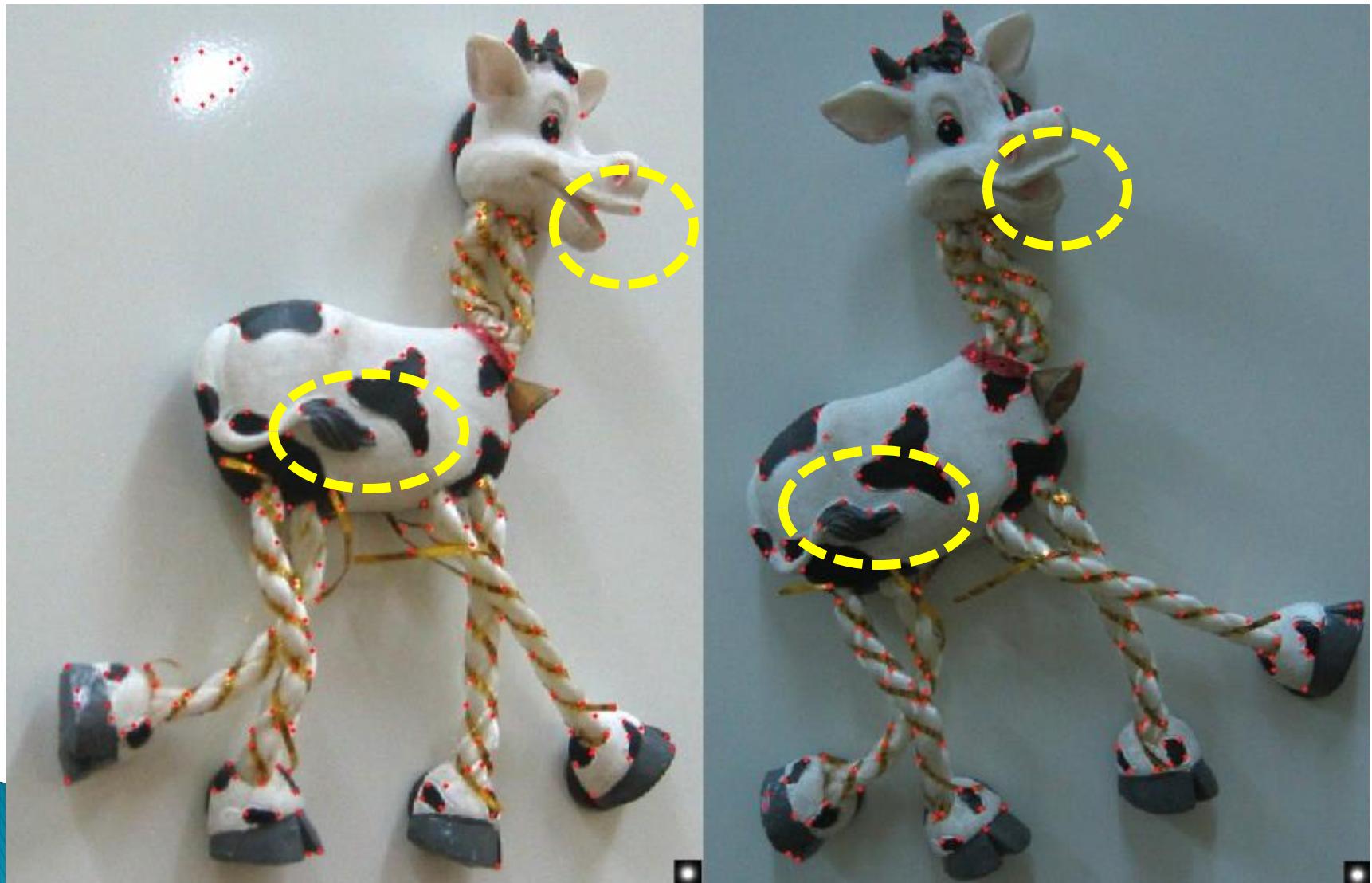


Harris Detector: Steps

Take only the points of local maxima of f

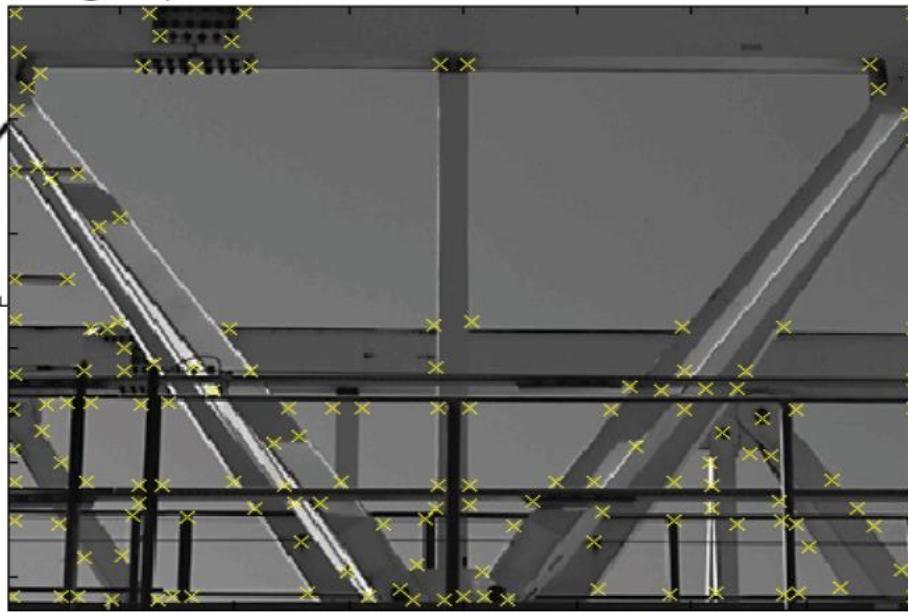
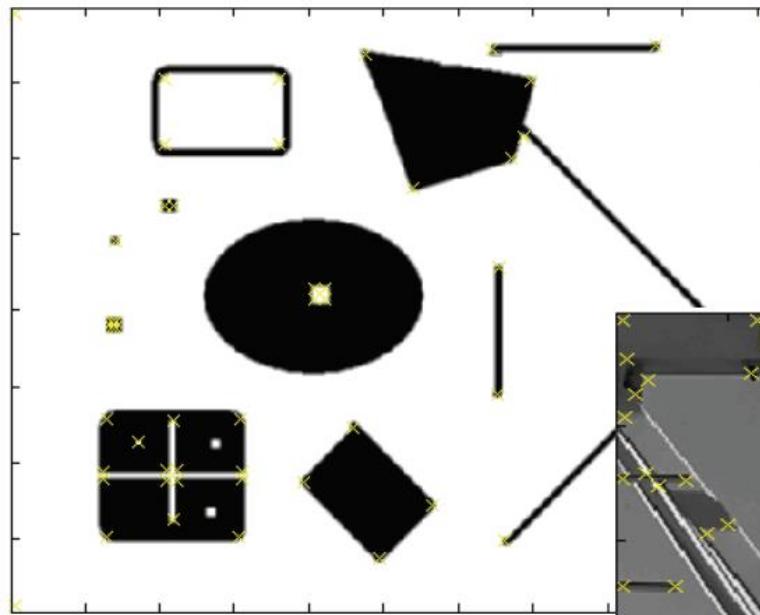


Harris Detector: Steps



Slide credit: Kristen Grauman

Harris Detector – Responses

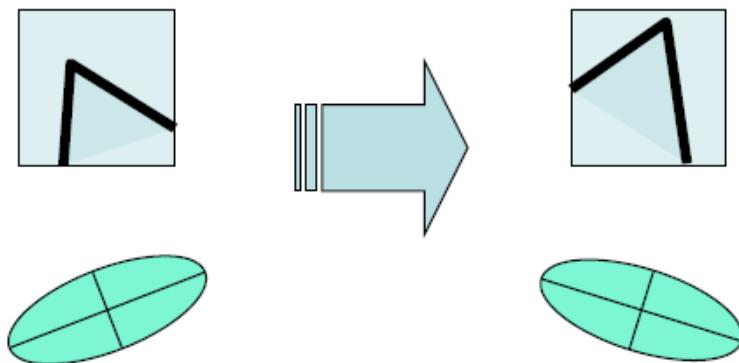


Effect: A very precise corner detector.

Slide credit: Krystian Mikolajczyk

Properties of Harris Corner Detector

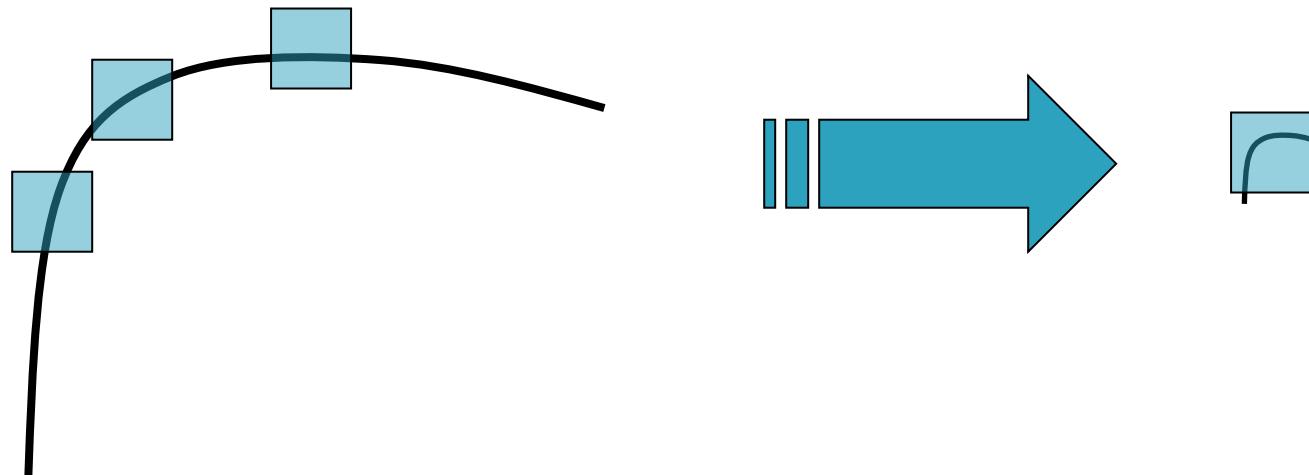
- ▶ Translation invariant?
- ▶ Rotation Invariant?



$$M = X \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} X^T$$

Properties of Harris Corner Detector

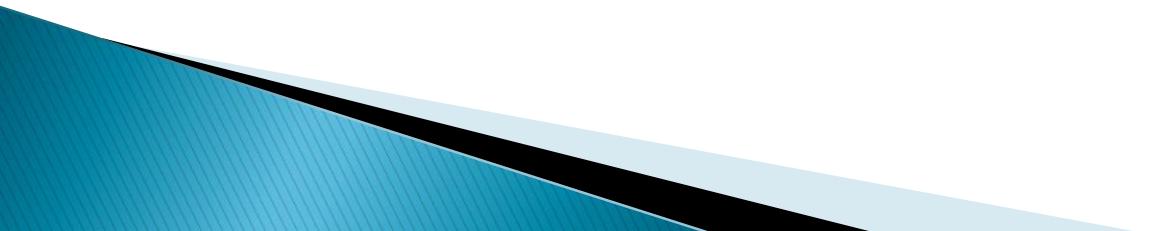
- ▶ Scale invariant?



All points will be
classified as edges

Corner
!

Scale Invariant Keypoint Detection



Automatic Scale Selection

- ▶ How do we find corresponding patch sizes?



Automatic scale selection

Intuition:

- Find scale that gives local maxima of some function f in both position and scale.

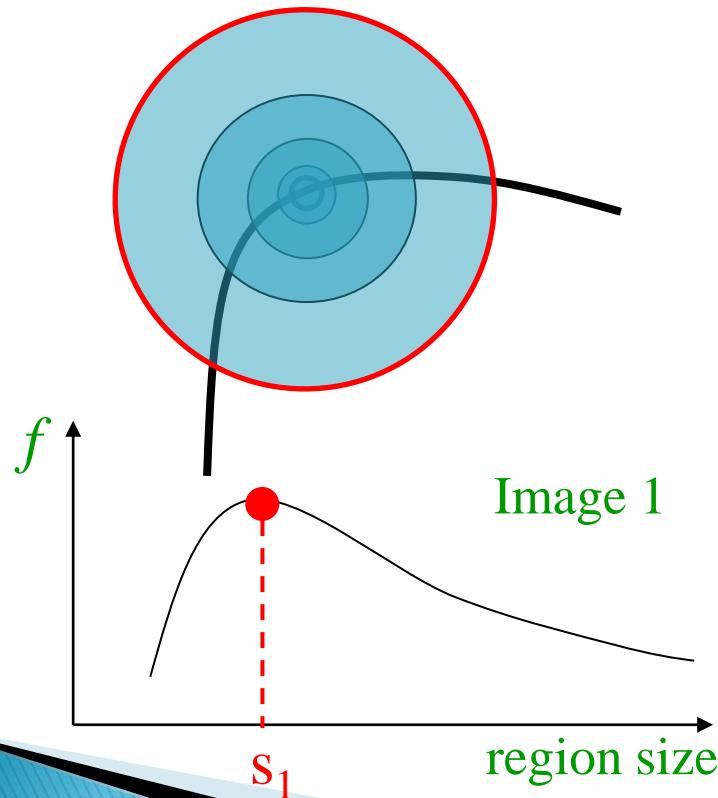


Image 1

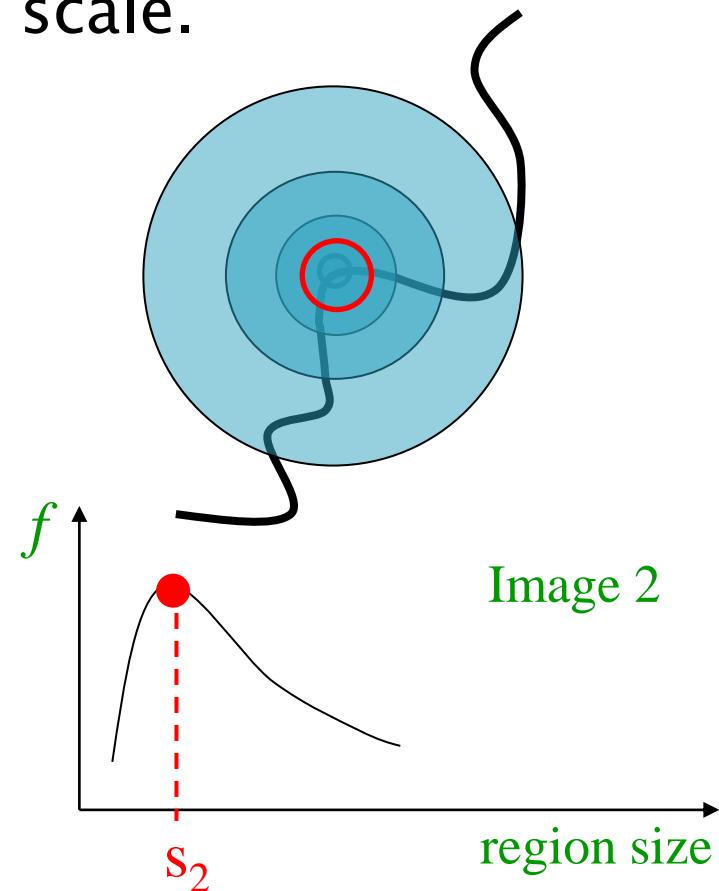
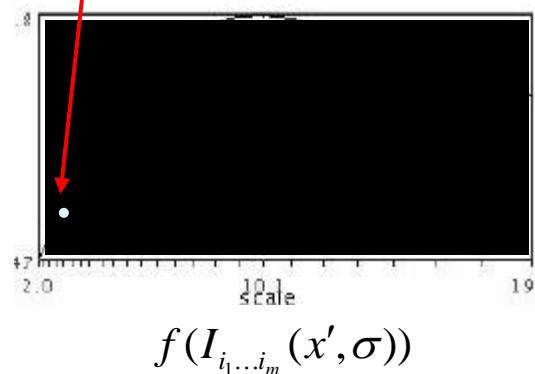
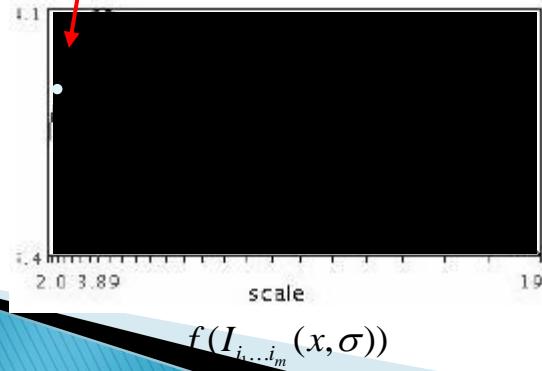
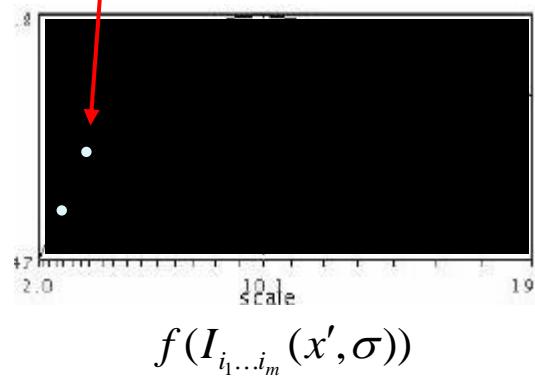
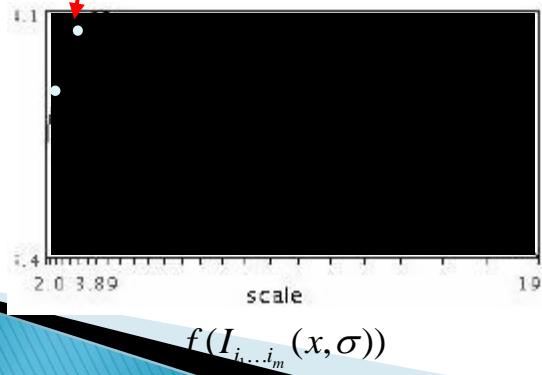


Image 2

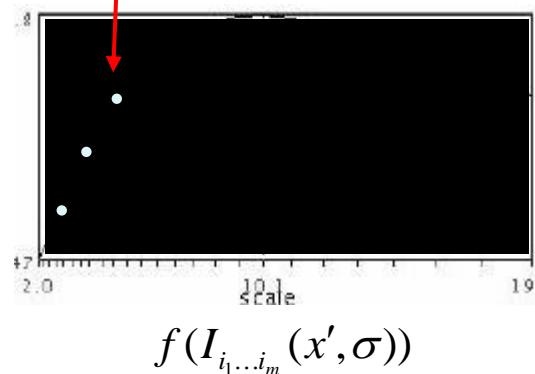
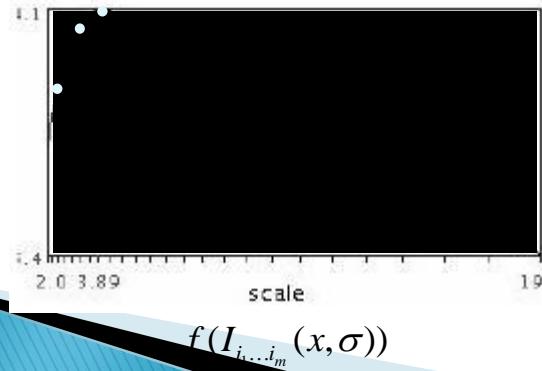
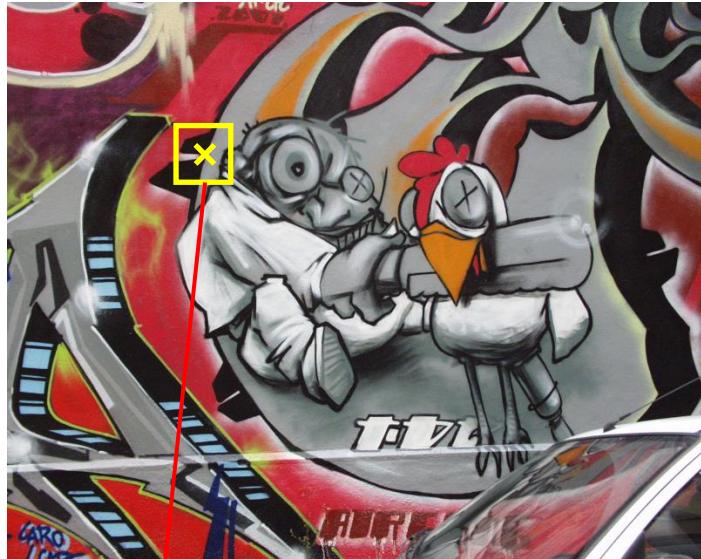
Automatic Scale Selection



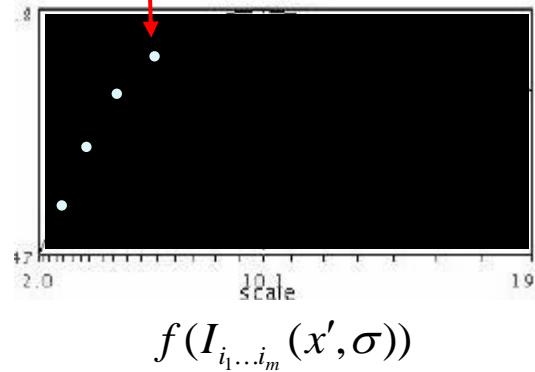
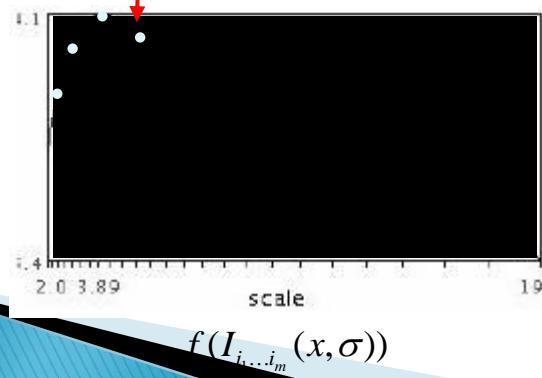
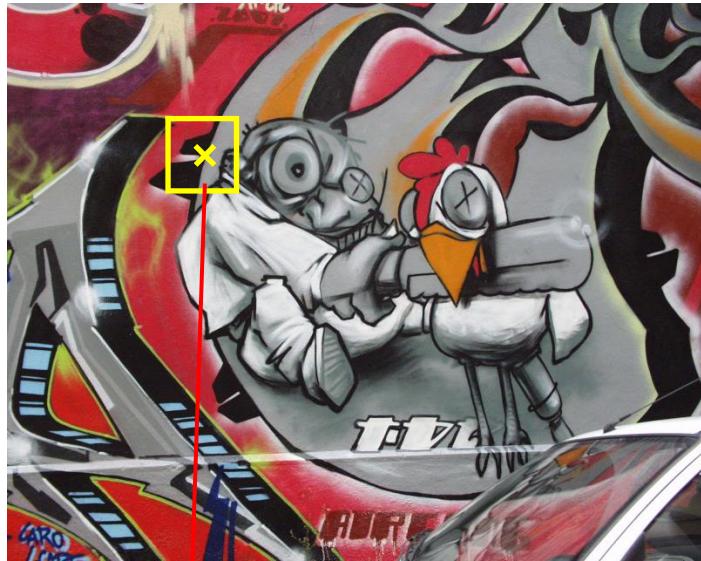
Automatic Scale Selection



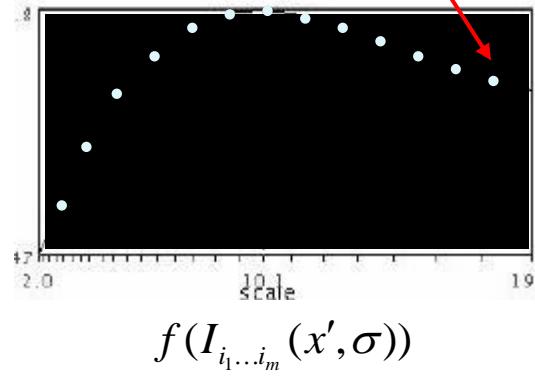
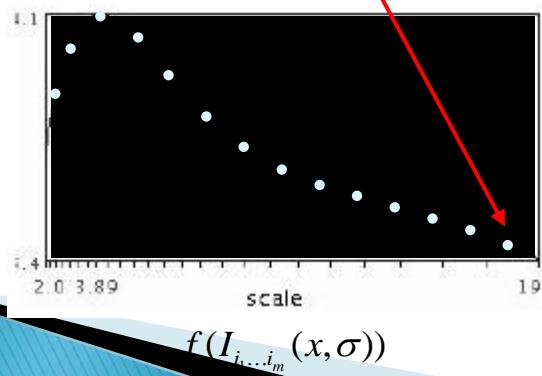
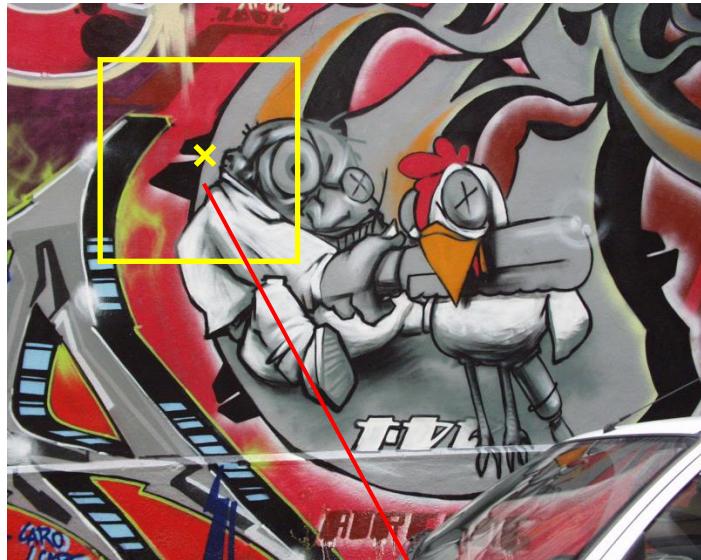
Automatic Scale Selection



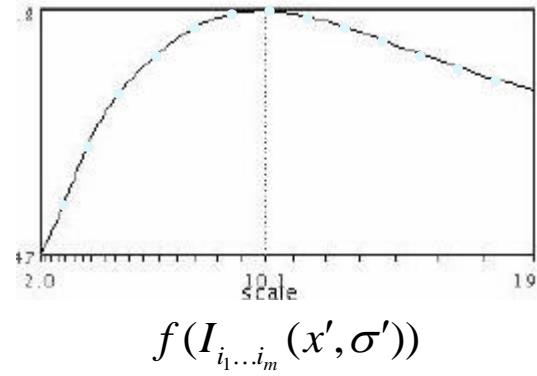
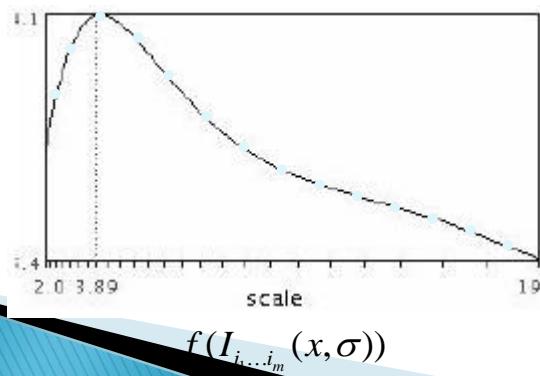
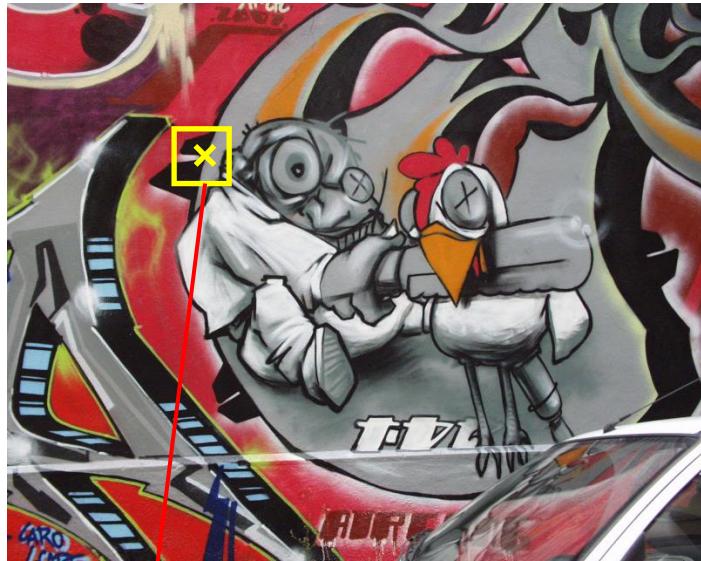
Automatic Scale Selection



Automatic Scale Selection

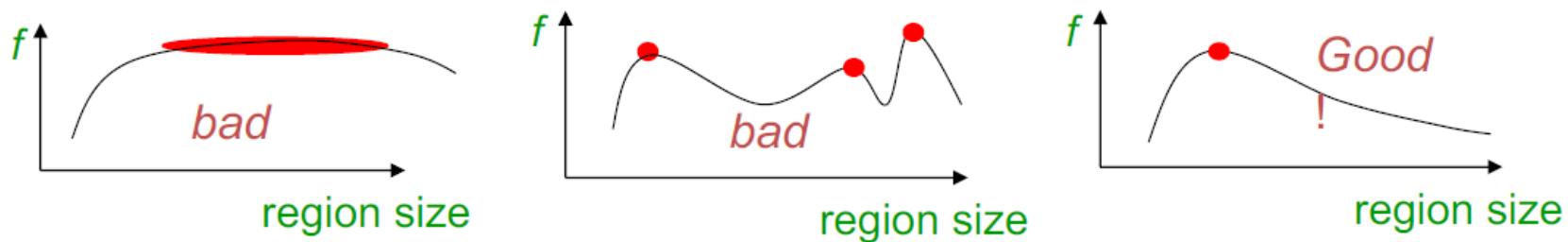


Automatic Scale Selection



What is a good function for scale invariant detection?

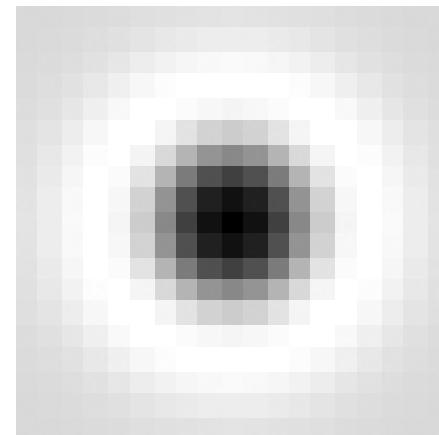
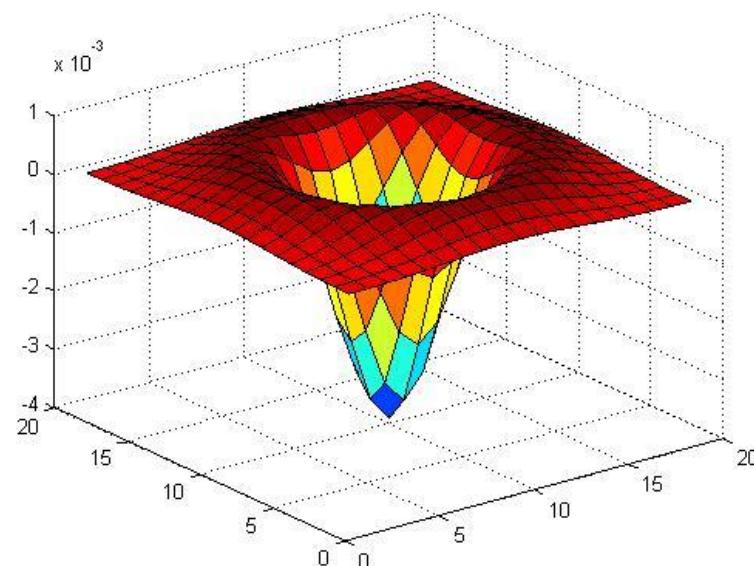
- A “good” function for scale detection:
has one stable sharp peak



- For usual images: a good function would be one which responds to contrast (sharp local intensity change)

Blob detection in 2D

- ▶ Laplacian of Gaussian: Circularly symmetric operator for blob detection in 2D

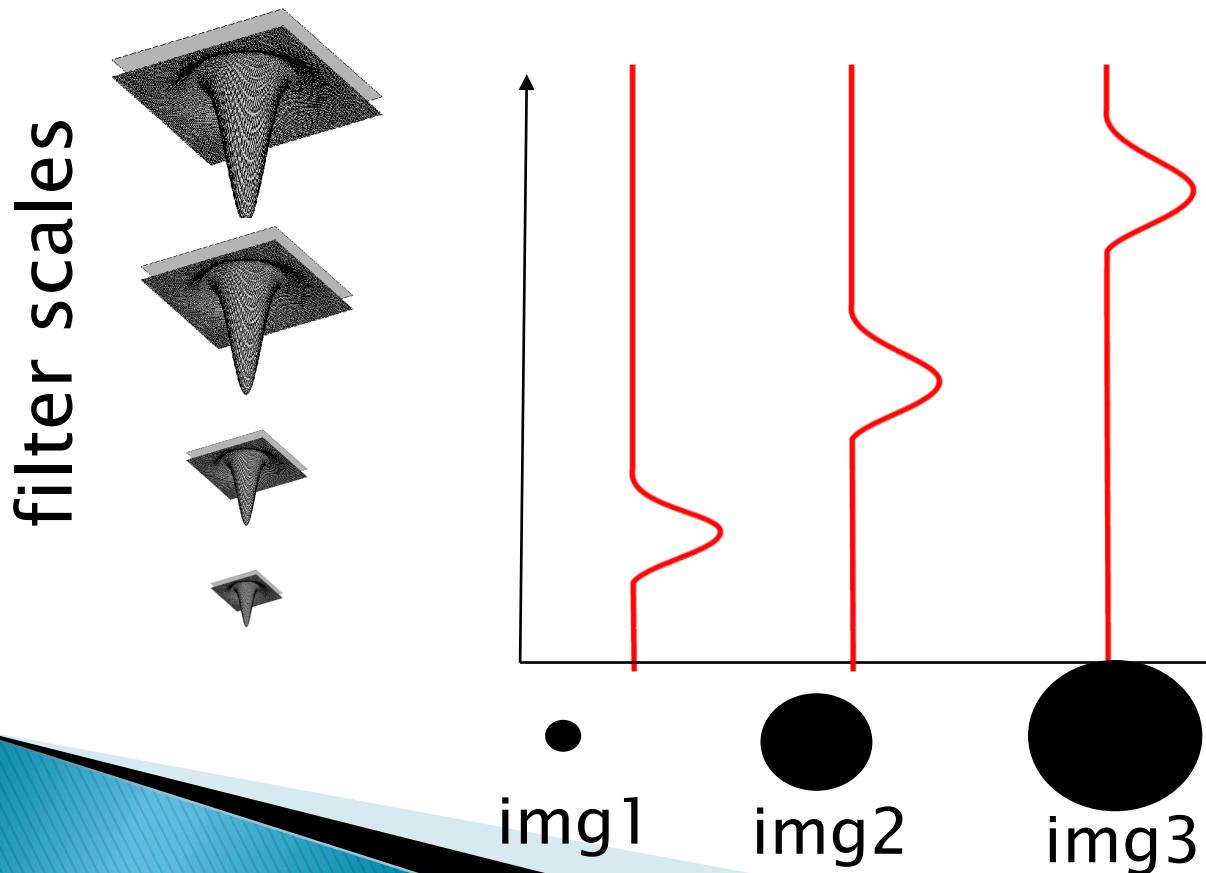


$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$

Blob detection in 2D: scale selection

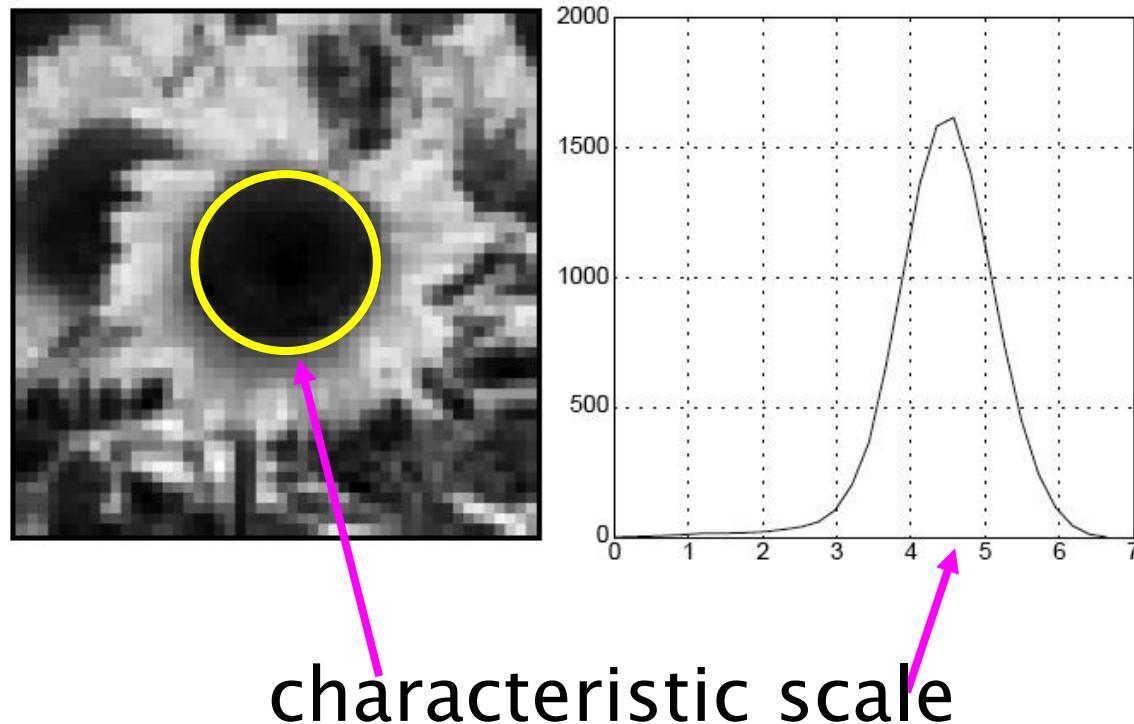
- ▶ Laplacian-of-Gaussian = “blob” detector

$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$



Blob detection in 2D

- ▶ We define the *characteristic scale* as the scale that produces peak of Laplacian response

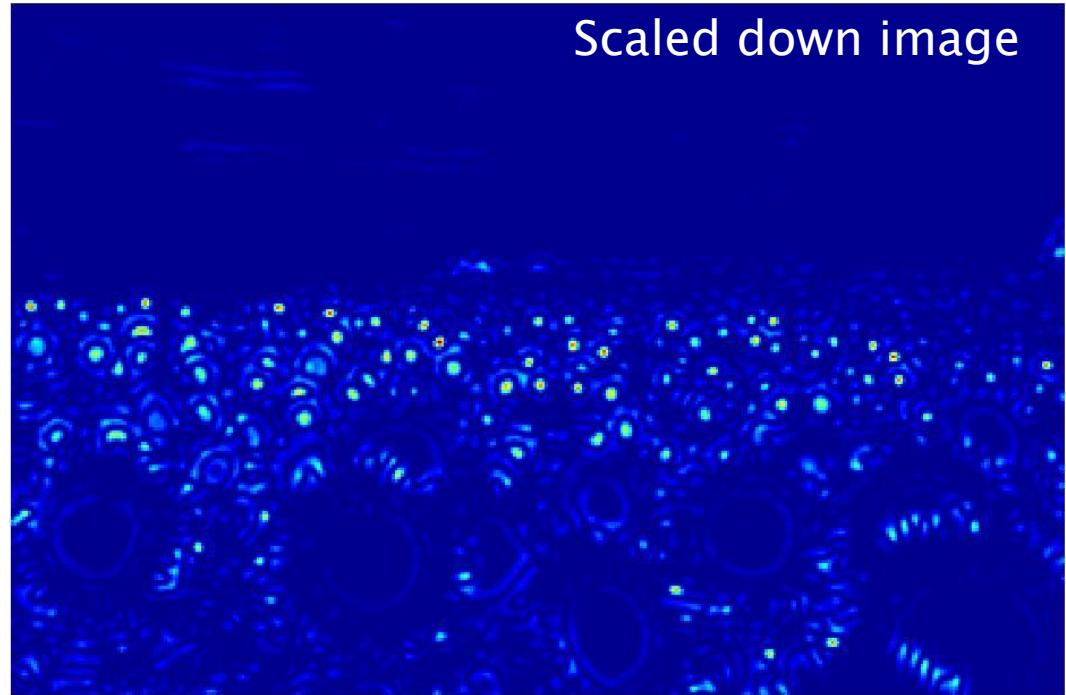


Example

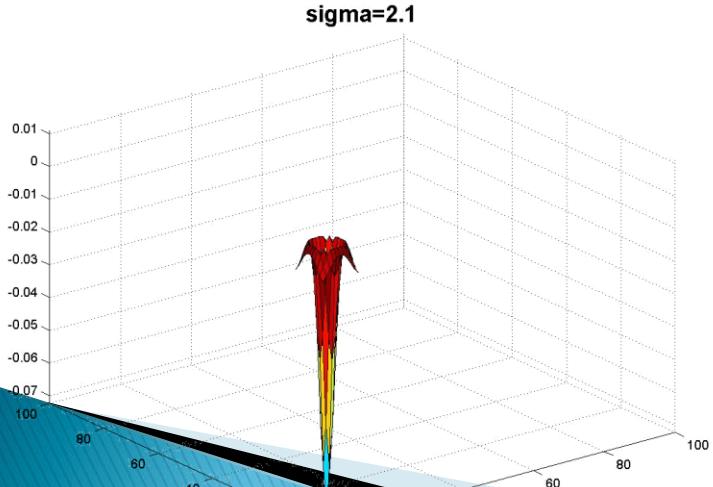
Original image
at $\frac{3}{4}$ the size



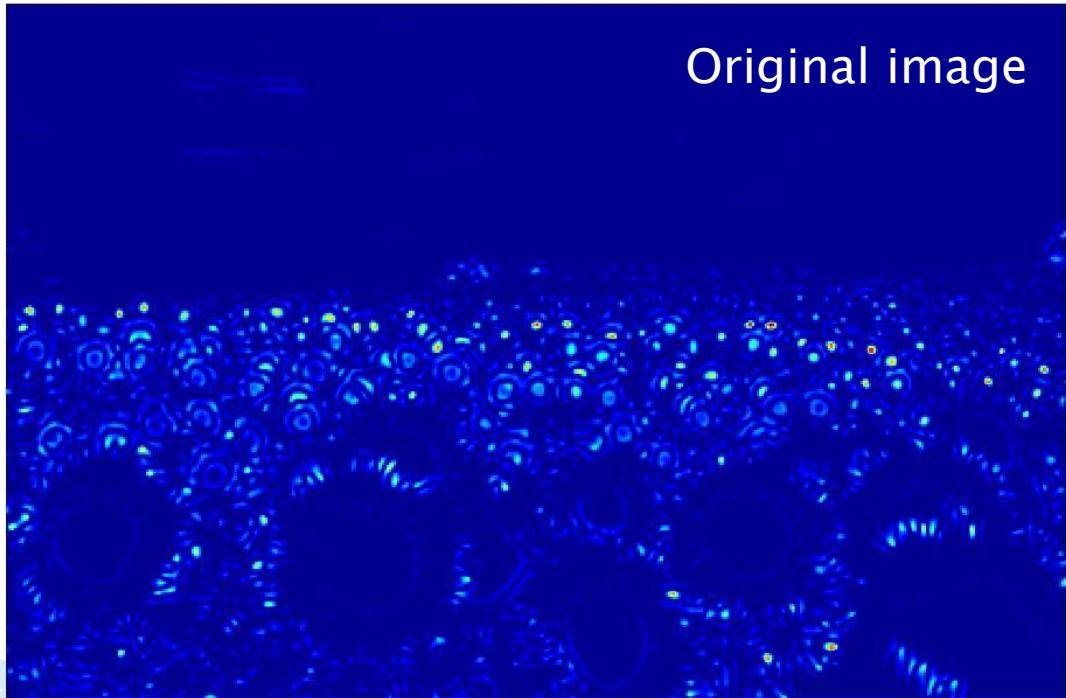
Original image
at $\frac{3}{4}$ the size



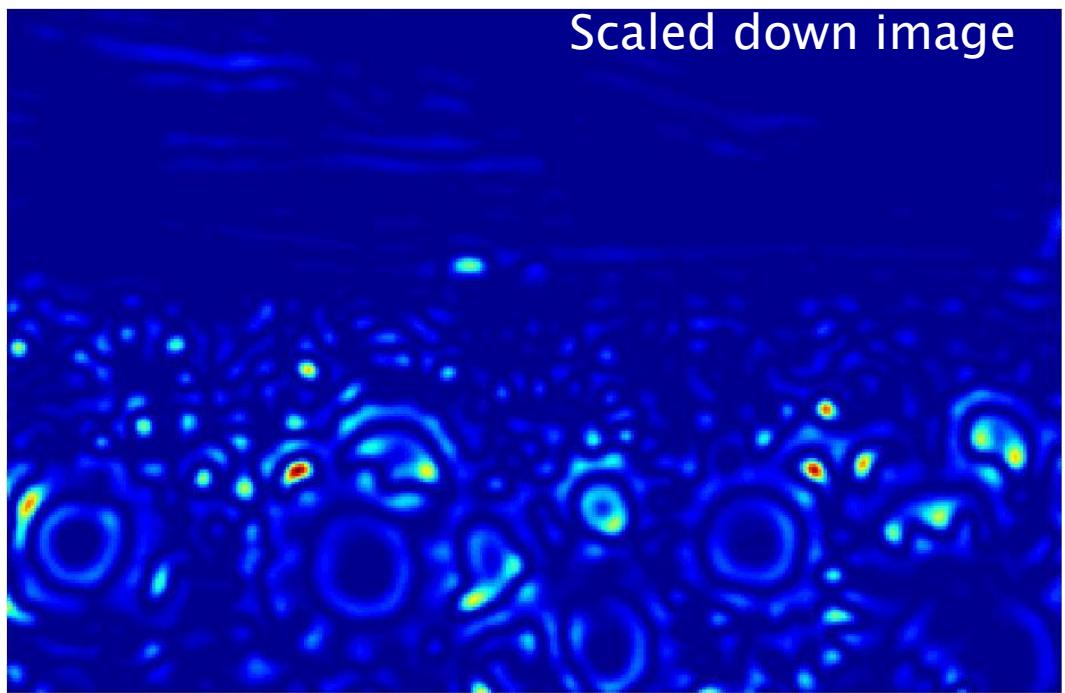
sigma=2.1



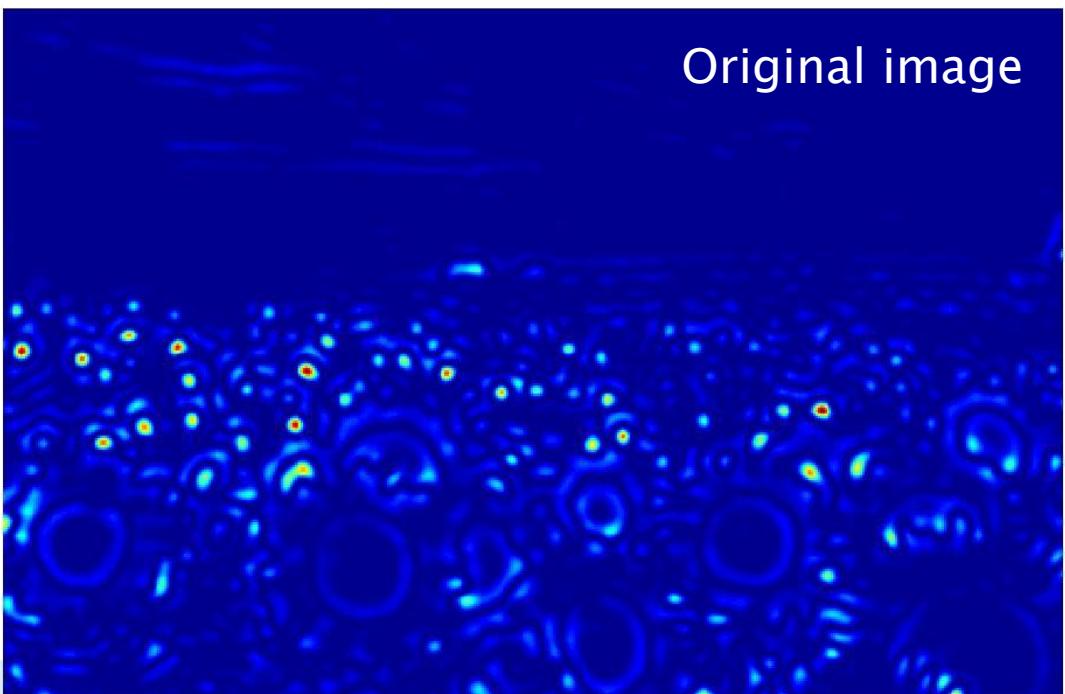
Original image



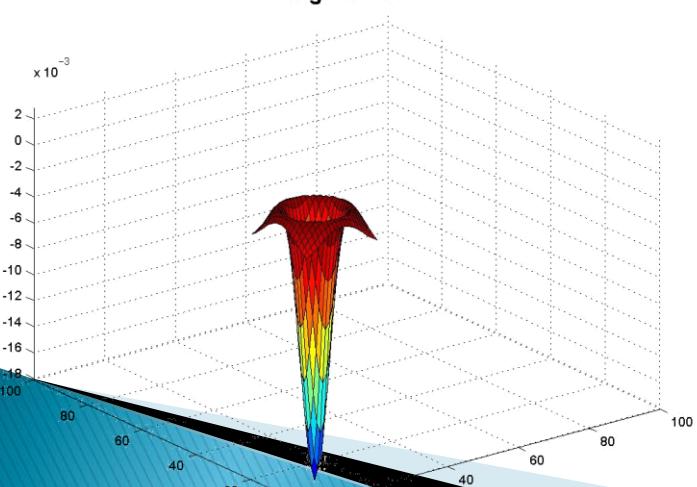
Scaled down image



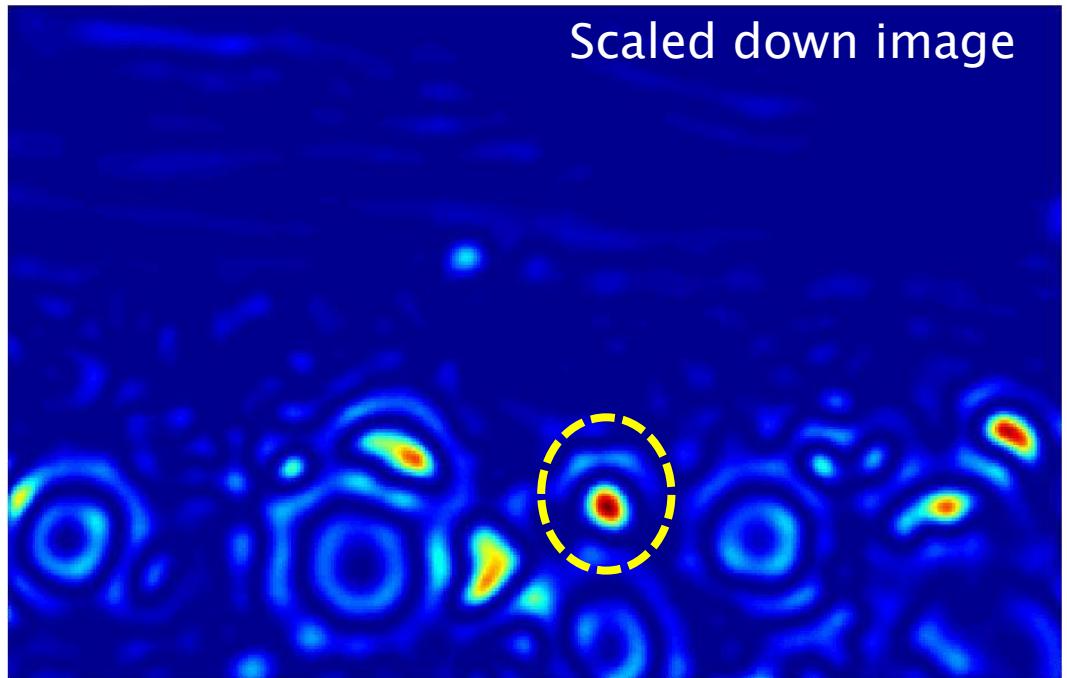
Original image



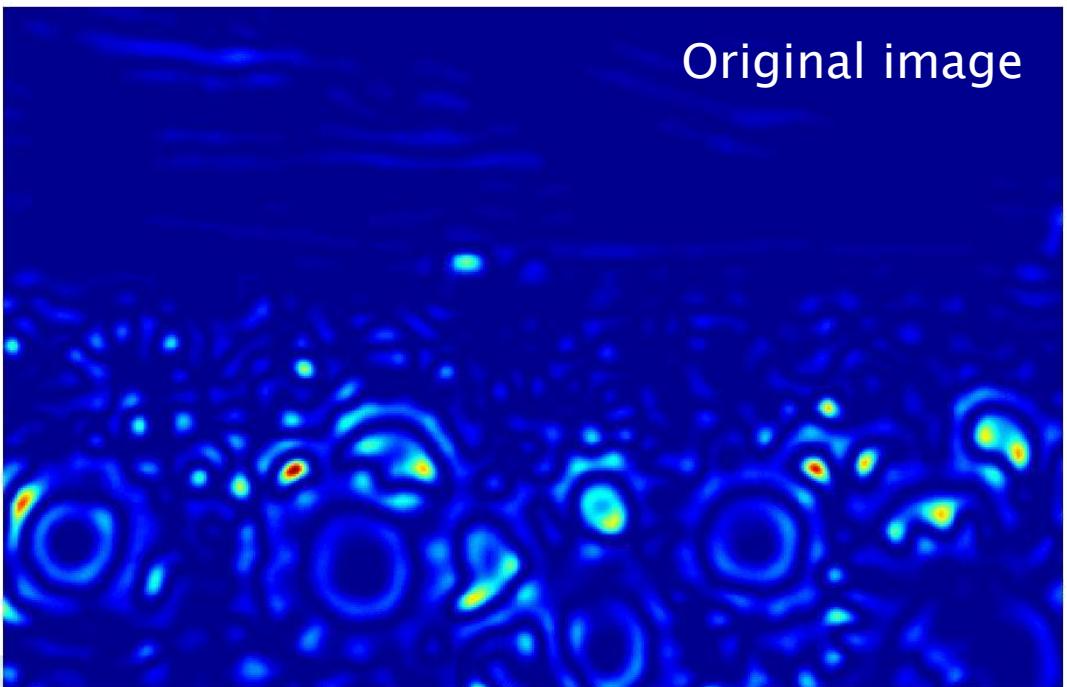
$\sigma = 4.2$



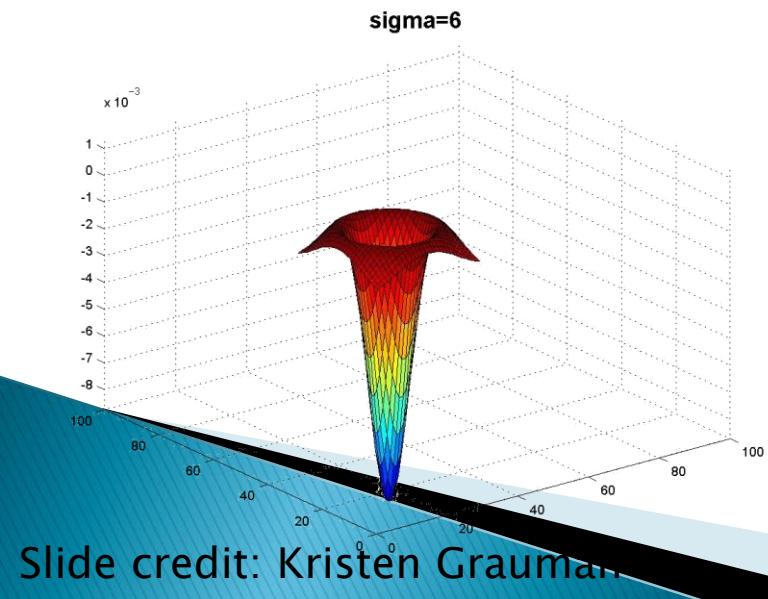
Scaled down image



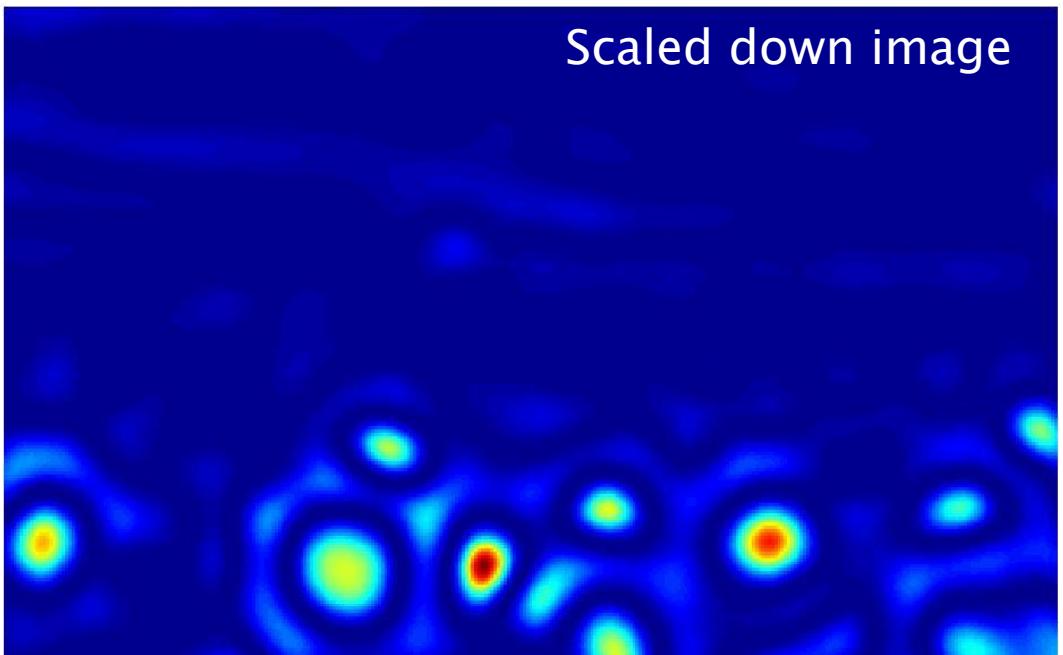
Original image



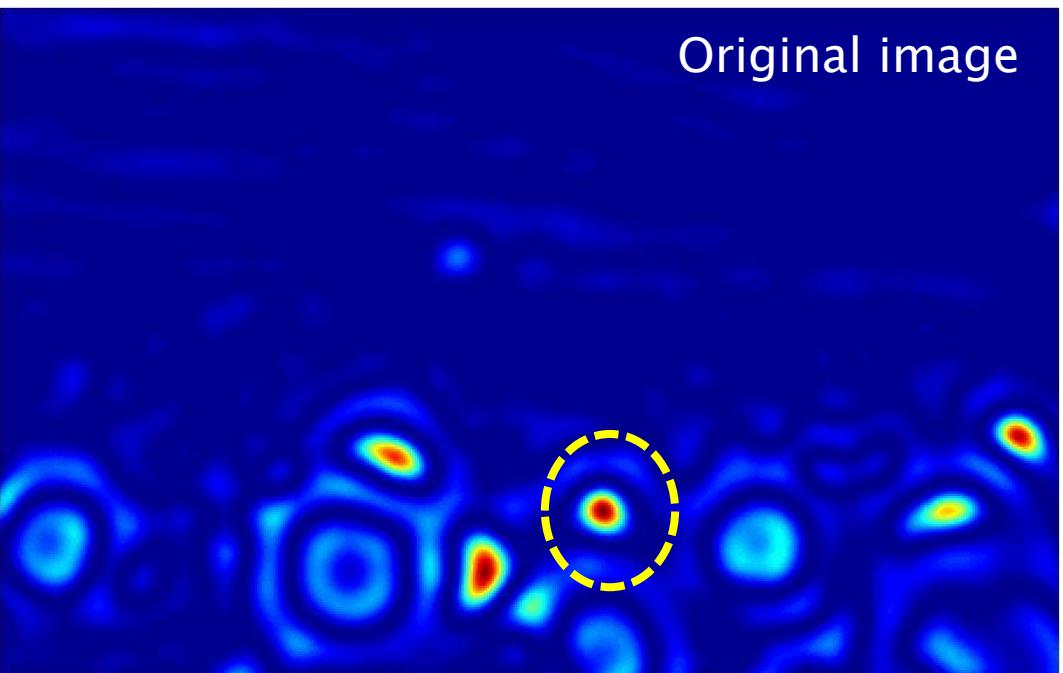
$\sigma=6$



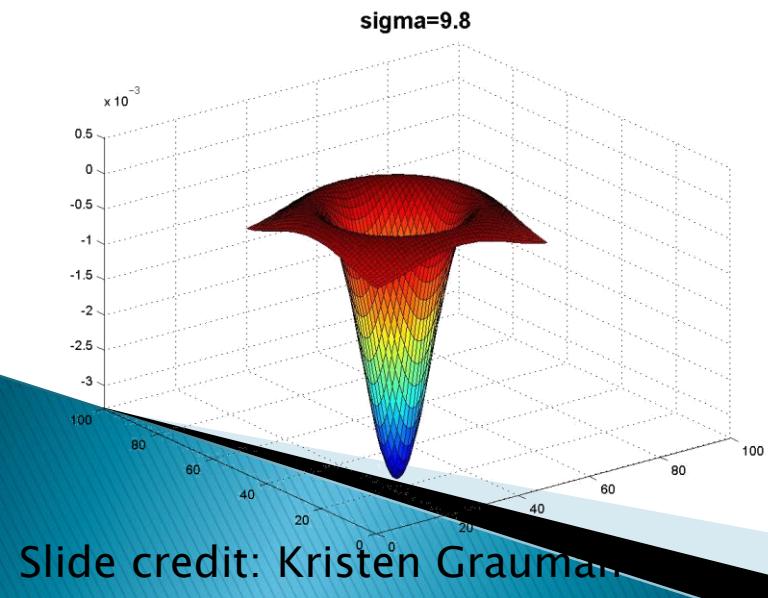
Scaled down image



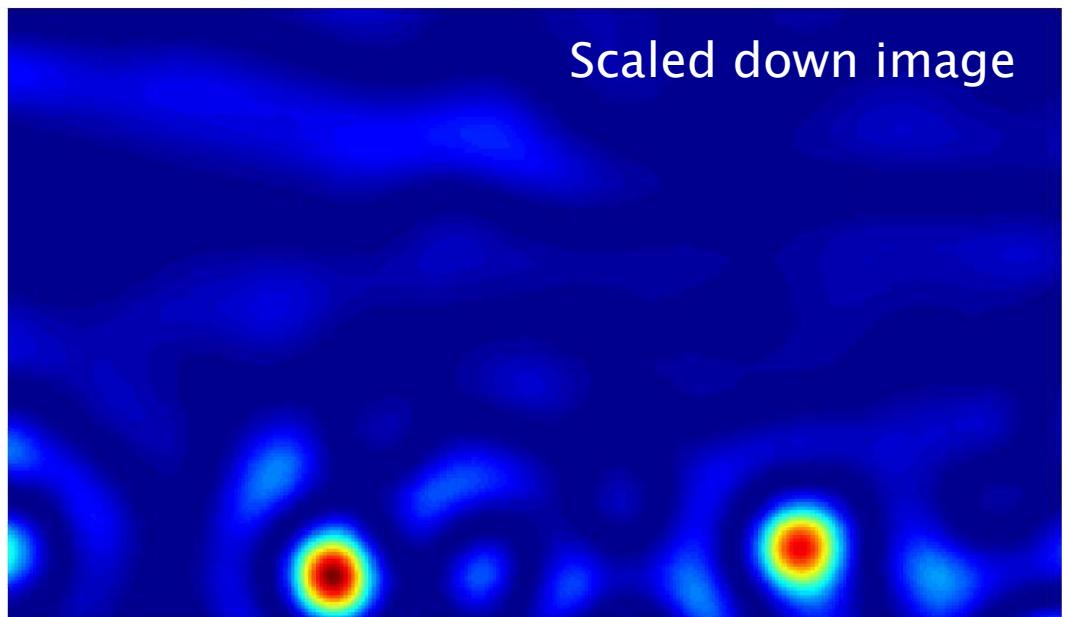
Original image



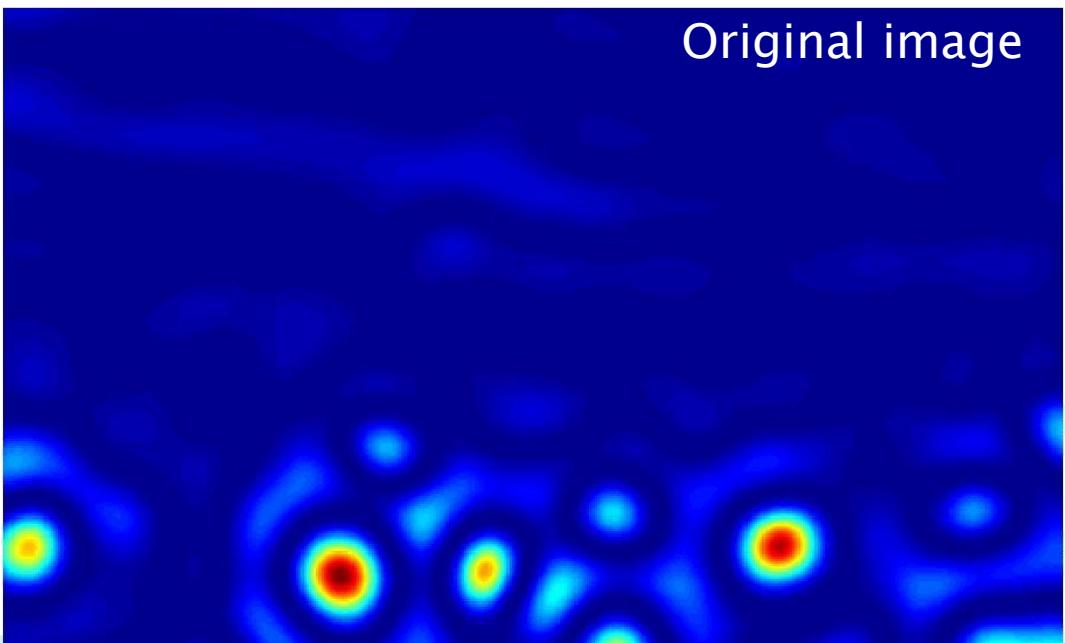
$\sigma = 9.8$



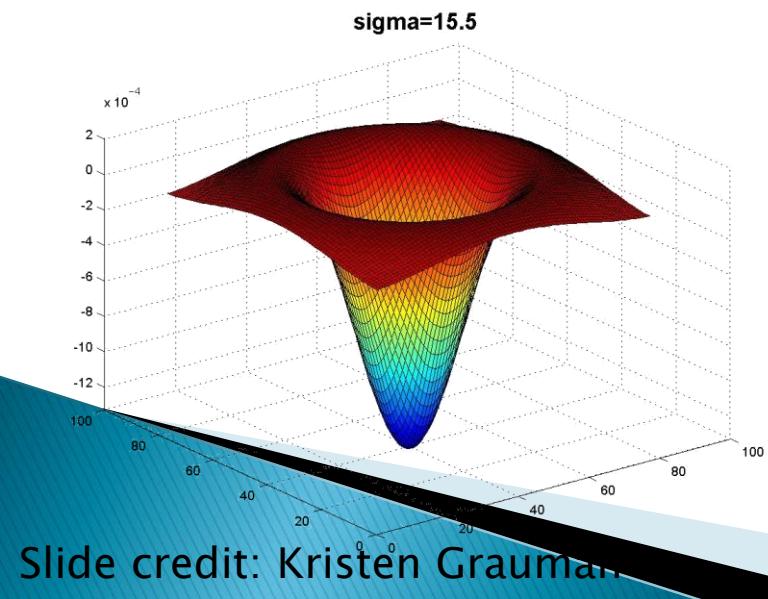
Scaled down image



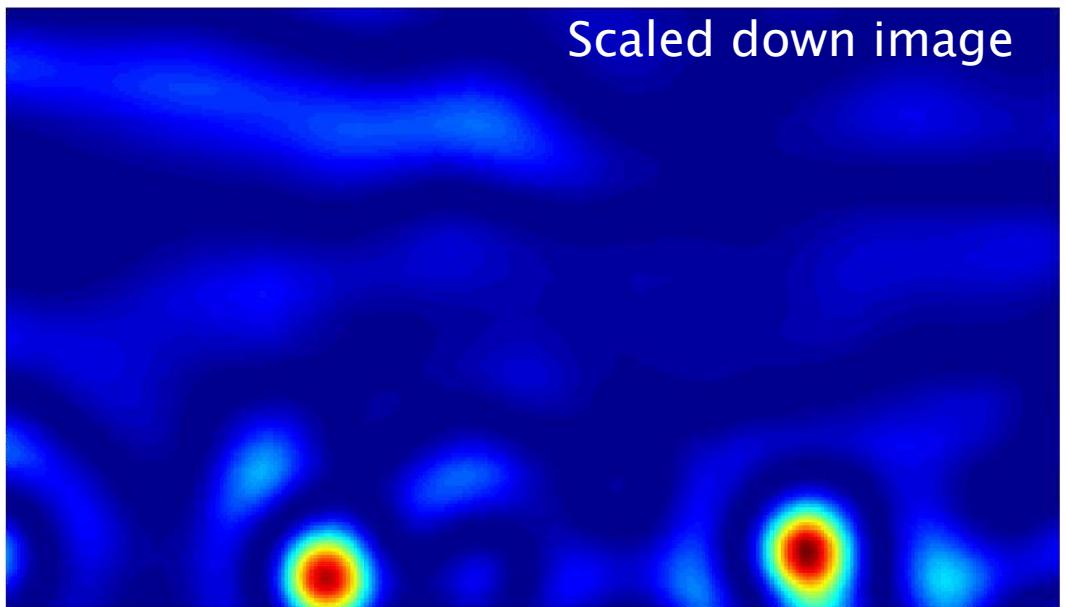
Original image



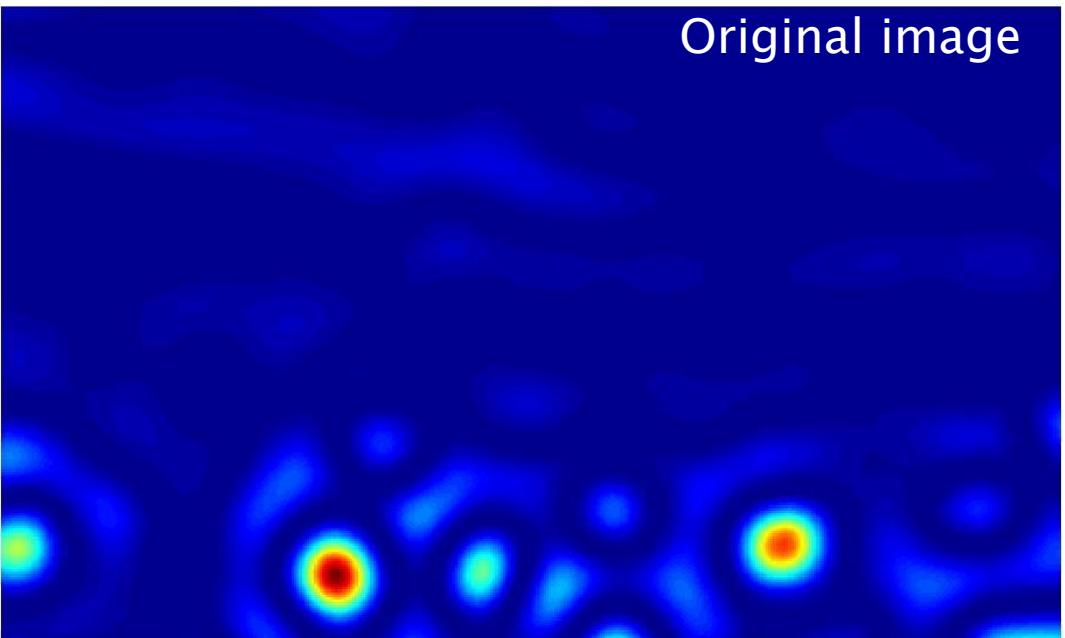
$\sigma = 15.5$



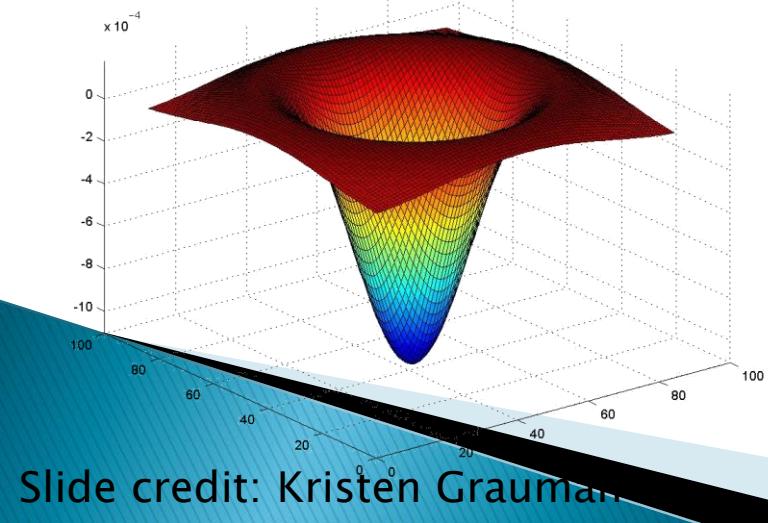
Scaled down image



Original image



$\sigma = 17$

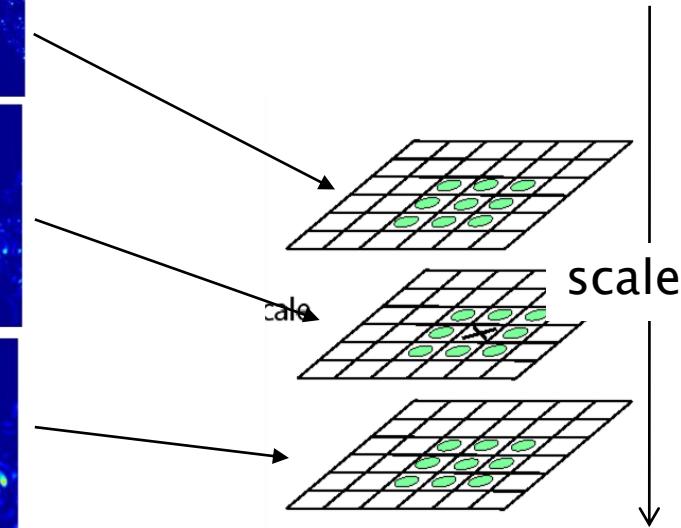
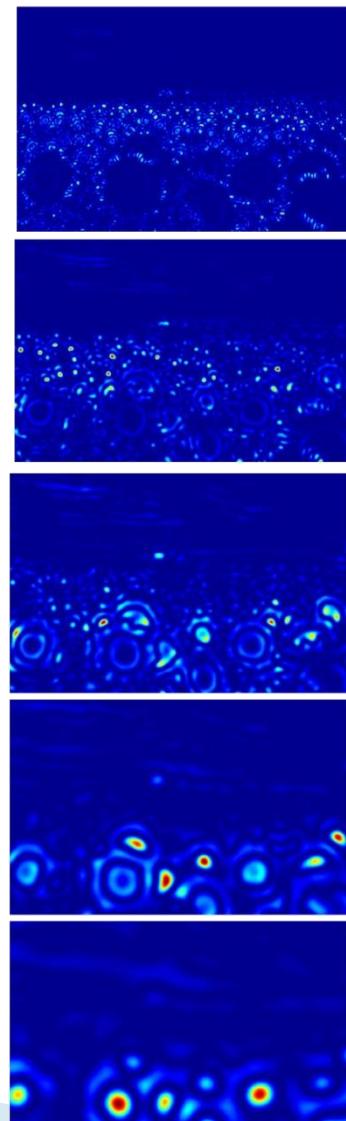


Scale invariant interest points

Interest points are local maxima in both position and scale.



$$L_{xx}(\sigma) + L_{yy}(\sigma) \rightarrow \sigma_1, \sigma_2, \sigma_3, \sigma_4, \sigma_5$$



⇒ List of
 (x, y, σ)

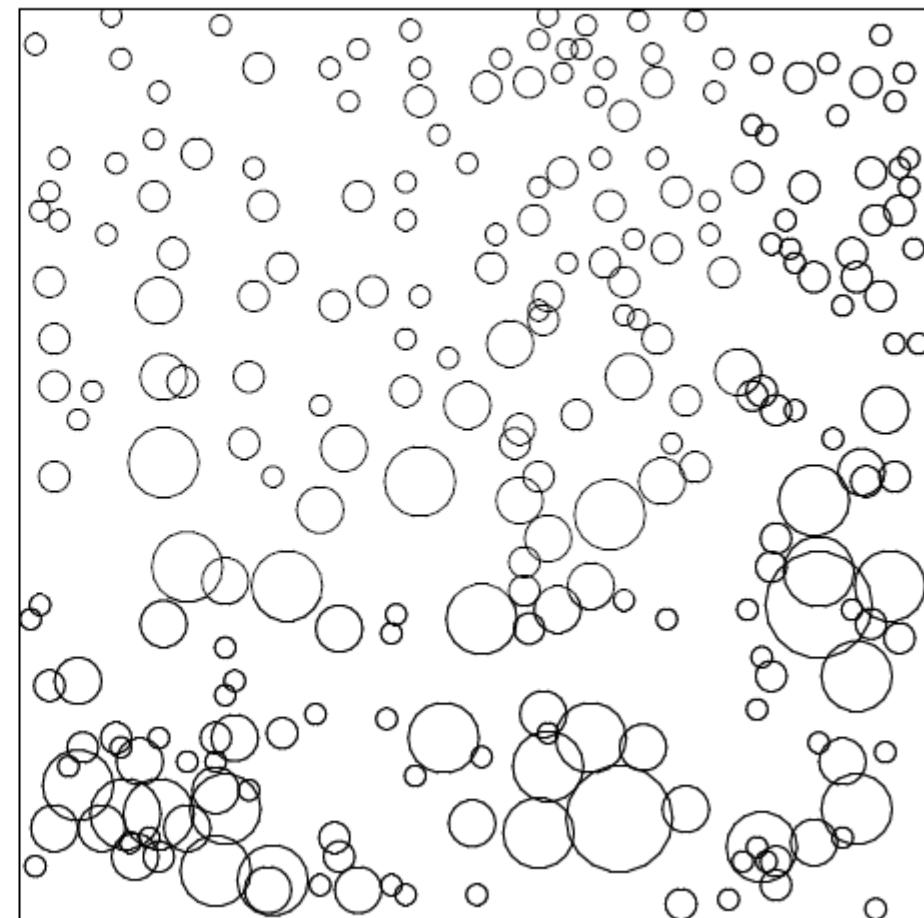
Squared filter
response map
 s

Scale-space blob detector: Example

original image



scale-space maxima of $(\nabla_{norm}^2 L)^2$



Scale-space blob detector: Example



Image credit: Lana Lazebnik

Technical detail

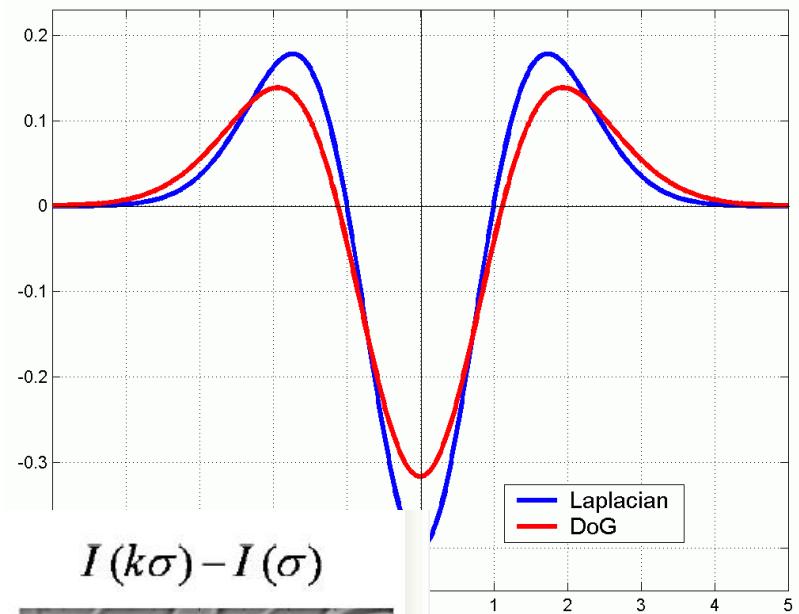
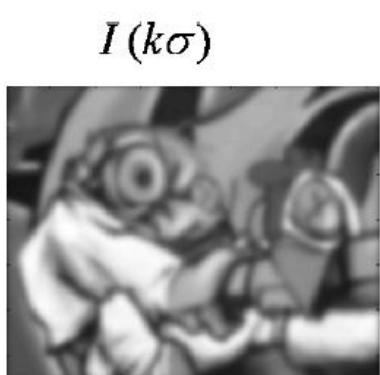
- ▶ We can approximate the Laplacian with a difference of Gaussians; more efficient to implement.

$$L = \sigma^2 \left(G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma) \right)$$

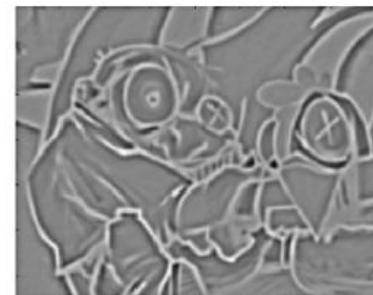
(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)



$$I(k\sigma) - I(\sigma)$$



Slide credit: Kristen Grauman

Feature Point Description

- ▶ Now we have feature points.
- ▶ How do we describe feature points for matching?

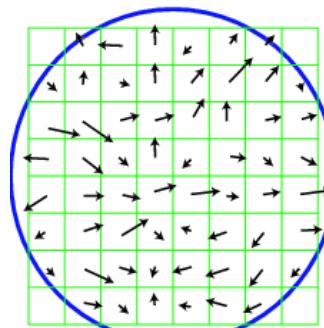


Descriptor

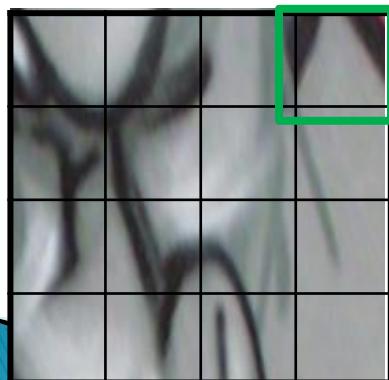
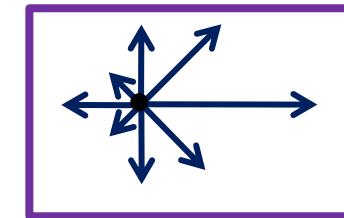
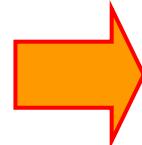


Scale Invariant Feature Transform (SIFT) descriptor

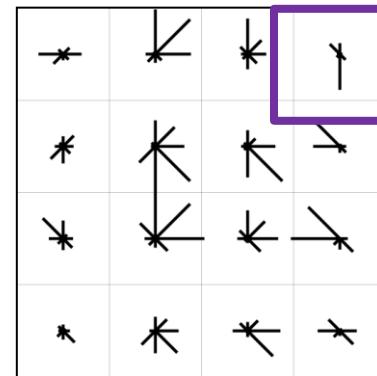
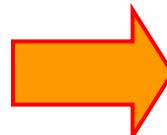
- ▶ Use histograms to bin pixels within sub-patches according to their orientation.



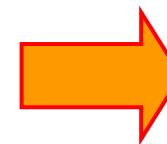
gradients



subdivided local patch

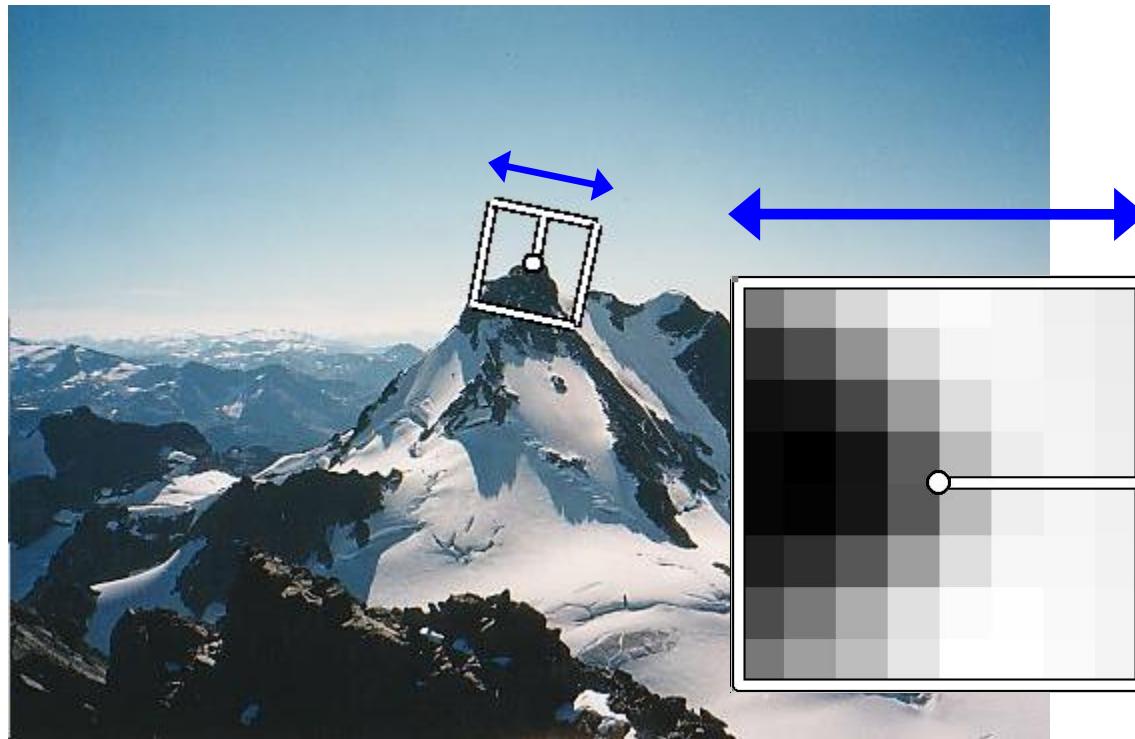


histogram per grid cell



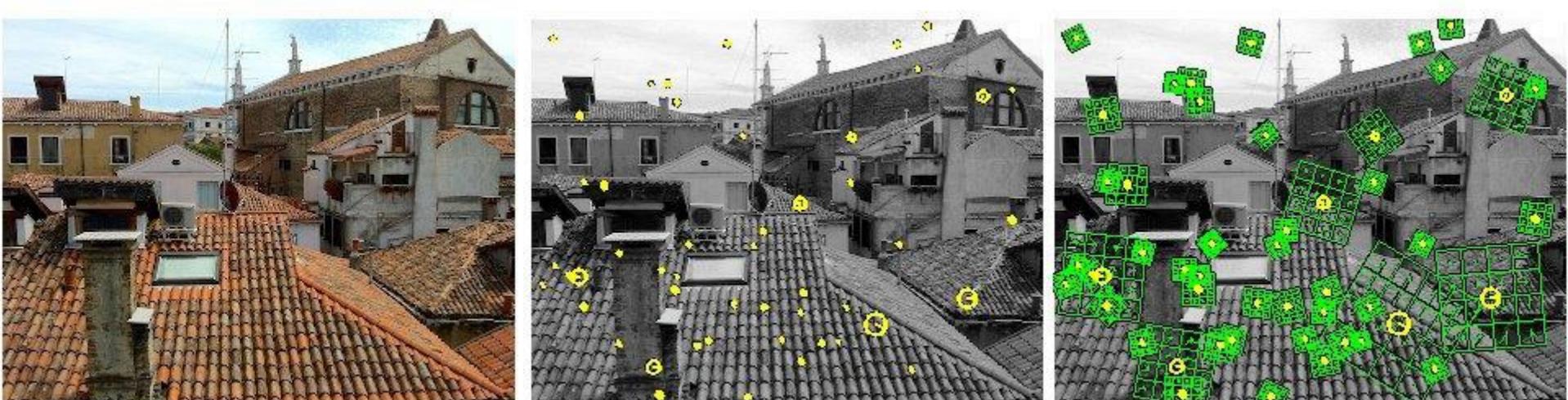
Final descriptor = concatenation of all histograms, normalize

Making descriptor rotation invariant



- Rotate patch according to its dominant gradient orientation
- This puts the patches into a canonical orientation.

Scale Invariant Feature Transform (SIFT) descriptor [Lowe 2004]



Interest points and their
scales and orientations
(random subset of 50)

SIFT descriptors

Feature Points Matching

Matching local features



Slide credit: Kristen Grauman

Matching local features



Image 1



Image 2

To generate **candidate matches**, find patches that have the most similar appearance

Simplest approach: compare them all, take the closest (or closest k , or within a thresholded distance)

SIFT (preliminary) matches

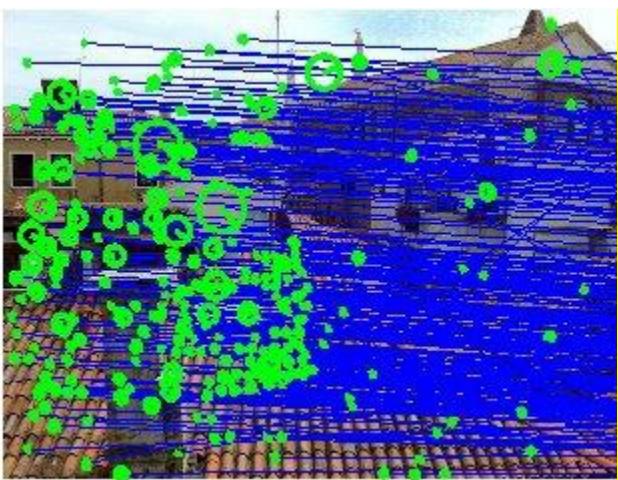
img1



img2



img1



img2

