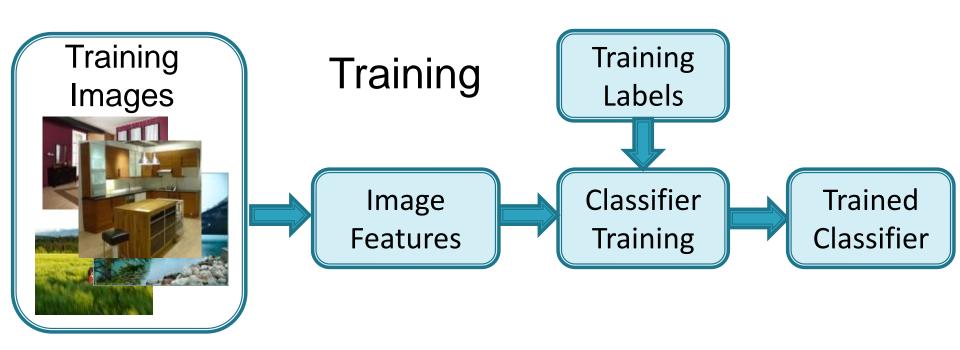
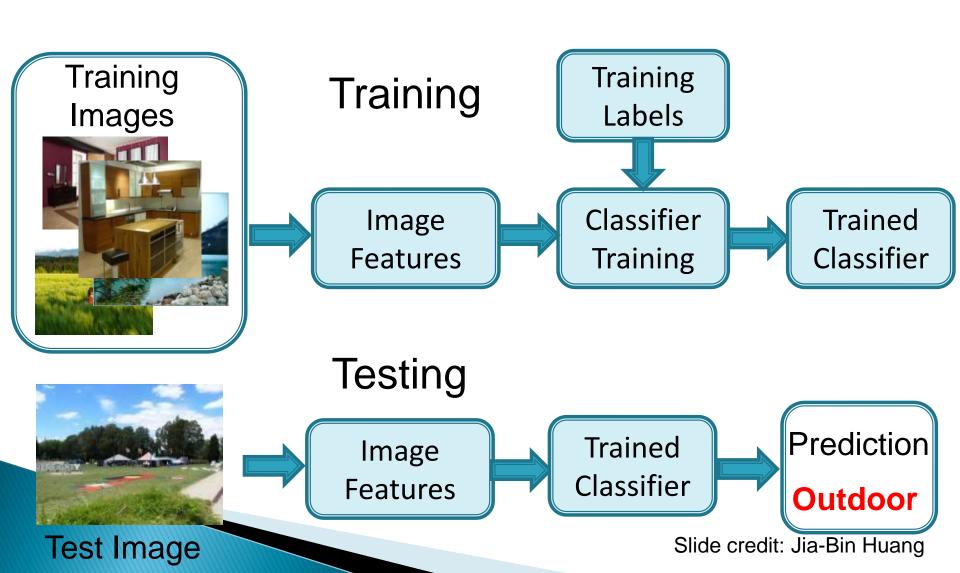
# Deep Learning for Visual Recognition

## Introduction

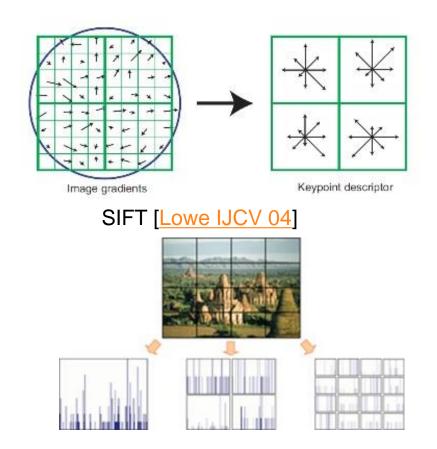
# Traditional Image Categorization: Training phase



# Traditional Image Categorization: Testing phase

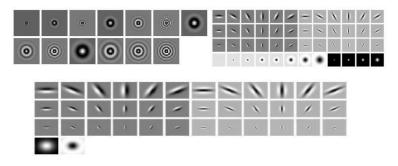


# Feature Design





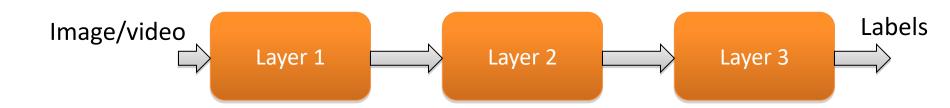
Harris Corner



**Textons** 

# Hierarchy of Feature Extractors

- Each layer of hierarchy extracts features from output of previous layer
- All the way from pixels → classifier
- Layers have the (nearly) same structure

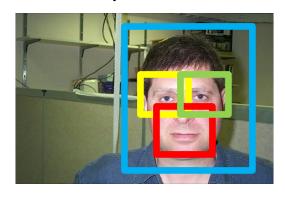


Train all layers jointly

### **Learning Feature Hierarchy**

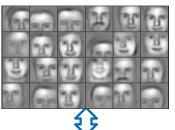
#### Goal: Learn useful higher-level features from images

Input data

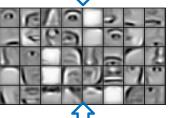




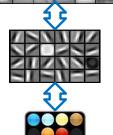
Lee et al., ICML 2009; CACM 2011 Feature representation



3rd layer "Objects"



2nd layer "Object parts"

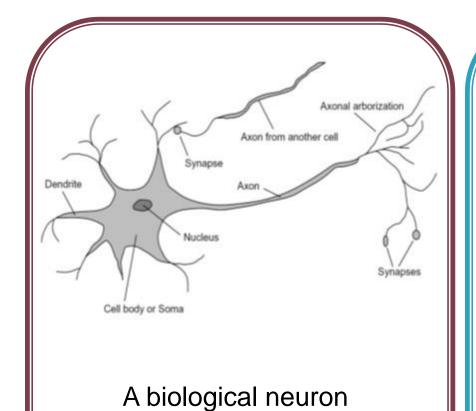


1st layer "Edges"

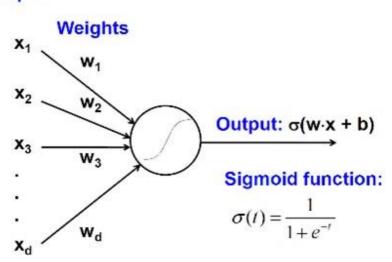
**Pixels** 

Slide: Rob Fergus

### Biological neuron and Perceptrons



Input

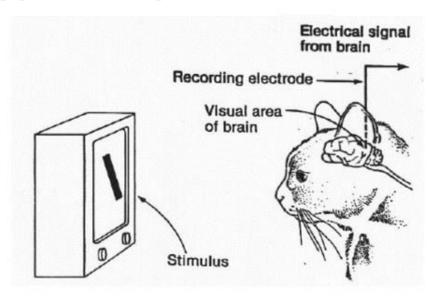


An artificial neuron (Perceptron)
- a linear classifier

#### Simple, Complex and Hypercomplex cells

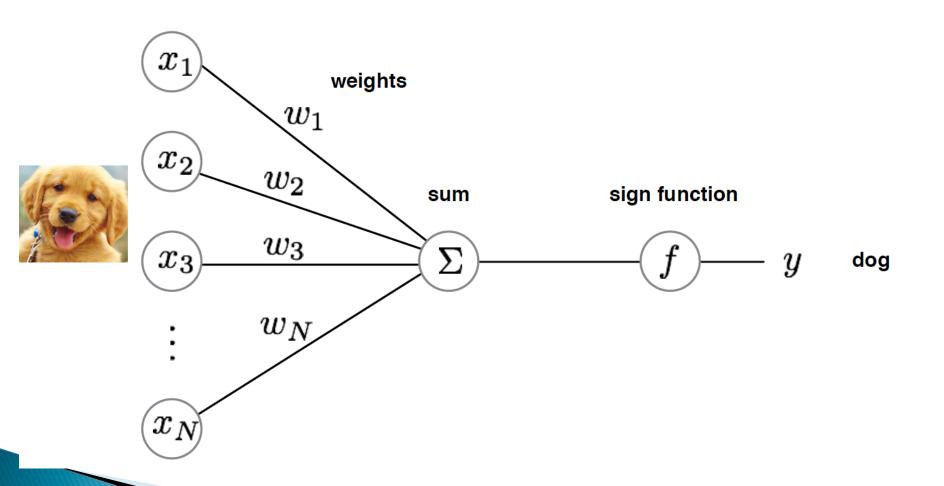






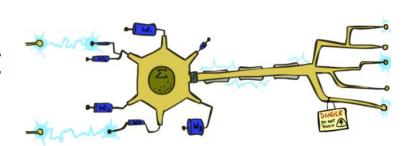
Suggested a **hierarchy** of **feature detectors** in the visual cortex, with higher level features responding to patterns of activation in lower level cells, and propagating activation upwards to still higher level cells.

# Perceptron: for image classification



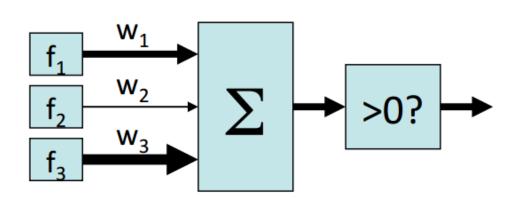
# Neuron: Linear Perceptron

- Inputs are feature values
- Each feature has a weight
- Sum is the activation



$$activation_w(x) = \sum_i w_i \cdot f_i(x) = w \cdot f(x)$$

- If the activation is:
  - Positive, output +1
  - Negative, output -1



# Perceptron training algorithm

- Initialize weights w randomly
- Cycle through training examples in multiple pa sses (epochs)
- For each training example x with label y:
  - Classify with current weights:

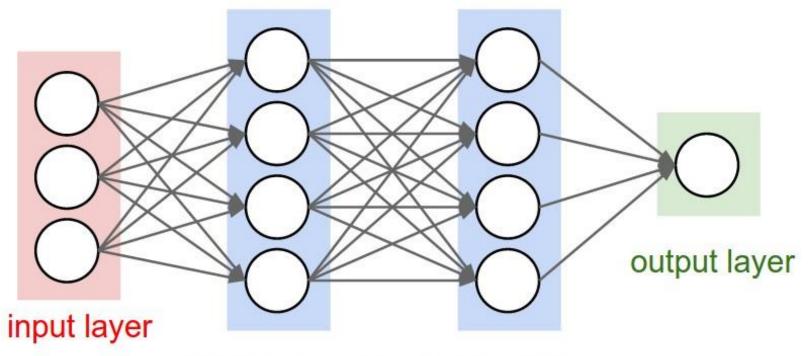
$$y' = \operatorname{sgn}(\mathbf{w} \times \mathbf{x})$$

• If classified incorrectly, update weights:

$$\mathbf{w} - \mathbf{w} + \partial(y - y') \mathbf{x}$$
  
( $\alpha$  is a positive *learning rate* that decays over time)

# Multi-layer perceptrons

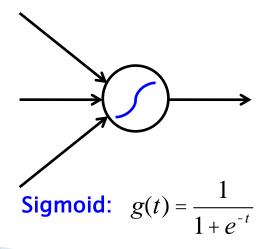
- To make nonlinear classifiers out of perceptrons, build a multi-layer neural network!
  - This requires each perceptron to have a nonlinearity

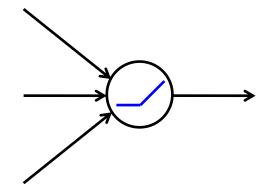


hidden layer 1 hidden layer 2

# Multi-layer perceptrons

- To make nonlinear classifiers out of perceptrons, build a multi-layer neural network!
  - This requires each perceptron to have a nonlinearity
  - To be trainable, the nonlinearity should be differentiable





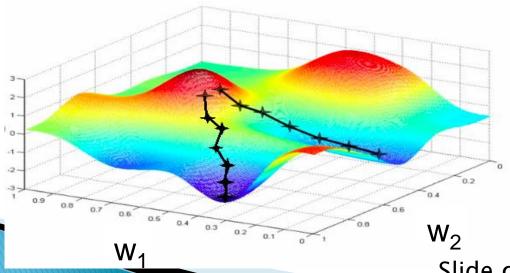
**Rectified linear unit (ReLU):** g(t) = max(0,t)

# Training of multi-layer networks

Find network weights to minimize the error between true and estimated labels of training examples:

$$E(\mathbf{w}) = \mathop{\tilde{\mathbf{o}}}_{j=1}^{N} \left( y_j - f_{\mathbf{w}}(\mathbf{x}_j) \right)^2$$

• Update weights by gradient descent:  $\mathbf{w} \leftarrow \mathbf{w} - \alpha \frac{\partial E}{\partial \mathbf{w}}$ 



# Training of multi-layer networks

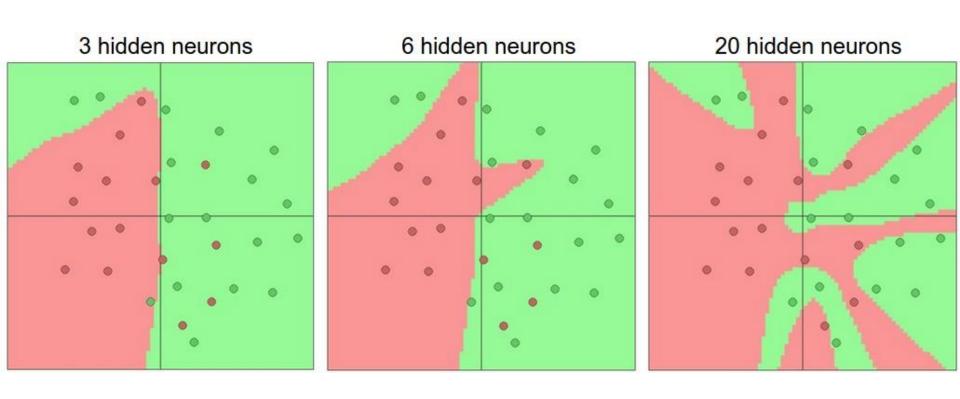
Find network weights to minimize the error between true and estimated labels of training examples:

$$E(\mathbf{w}) = \mathop{\text{a}}_{j=1}^{N} \left( y_j - f_{\mathbf{w}}(\mathbf{x}_j) \right)^2$$

- Update weights by gradient descent:  $\mathbf{w} \leftarrow \mathbf{w} \alpha \frac{\partial E}{\partial \mathbf{w}}$
- Back-propagation: gradients are computed in the direction from output to input layers and combined using chain rule
- Stochastic gradient descent: compute the weight update w.r.t. one training example (or a small batch of examples) at a time, cycle through training examples in random order in multiple epochs

### Network with a single hidden layer

Hidden layer size and network capacity:



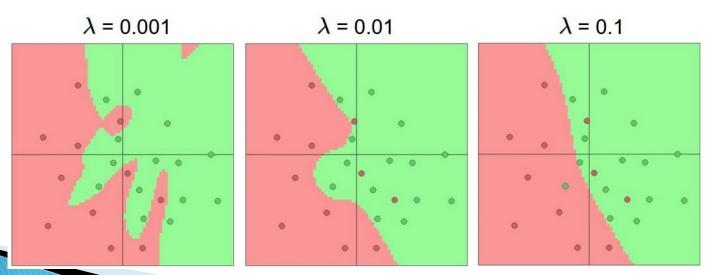
Source: <a href="http://cs231n.github.io/neural-networks-1/">http://cs231n.github.io/neural-networks-1/</a>

# Regularization

It is common to add a penalty on weight magnitudes to the objective function:

$$E(f) = \mathop{\text{a}}_{i=1}^{N} \left( y_i - f(\mathbf{x}_i) \right)^2 + \frac{1}{2} \mathop{\text{a}}_{j} w_j^2$$

 This encourages network to use all of its inputs "a little" rather than a few inputs "a lot"



http://cs231n.github.io/neural-networks-1/

#### Neural networks: Pros and cons

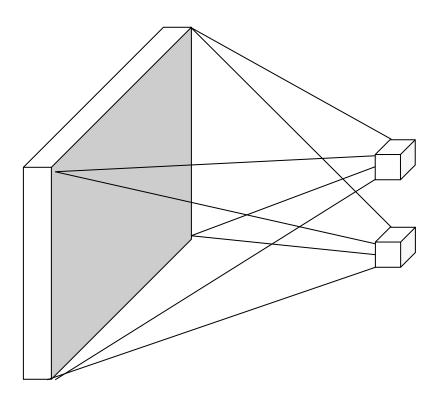
#### Pros

- Flexible and general function approximation fram ework
- Can build extremely powerful models by adding more layers

#### Cons

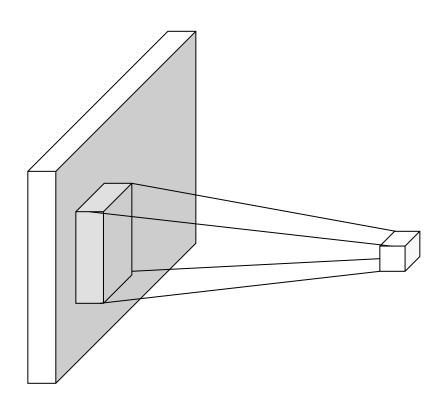
- Hard to analyze theoretically (e.g., training is pro ne to local optima)
- Huge amount of training data, computing power may be required to get good performance
- The space of implementation choices is huge (net work architectures, parameters)

### Convolutional Neural Network



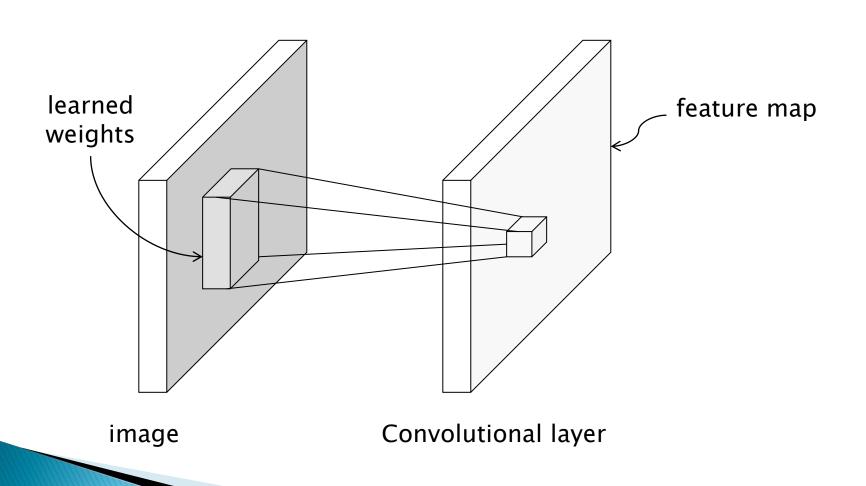
image

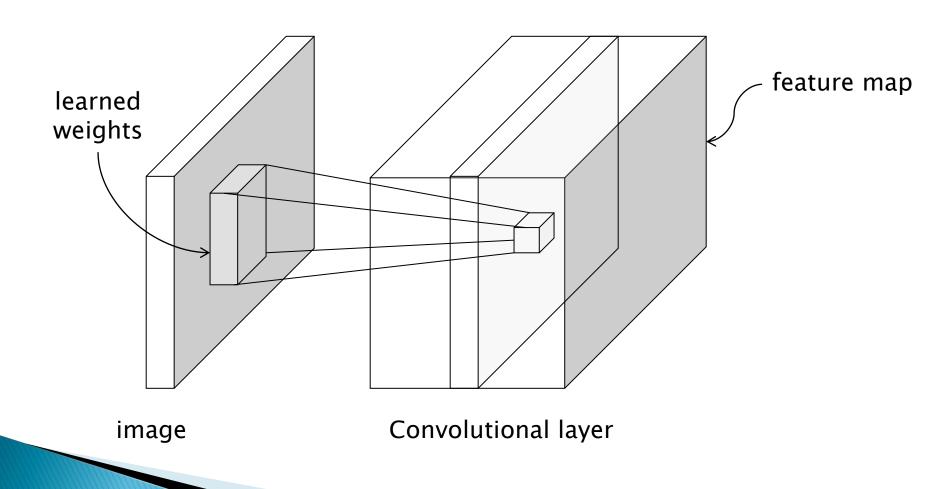
Fully connected layer



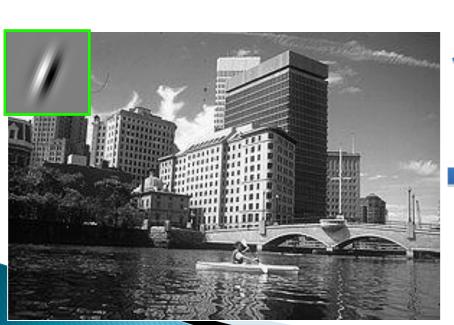
image

Convolutional layer





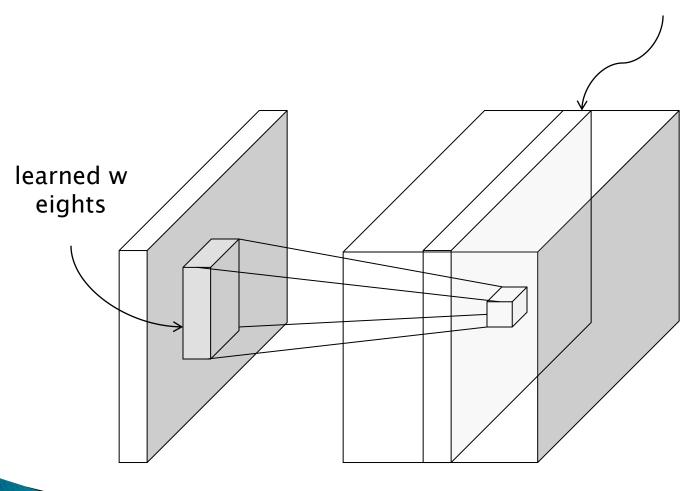
#### Convolution as feature extraction





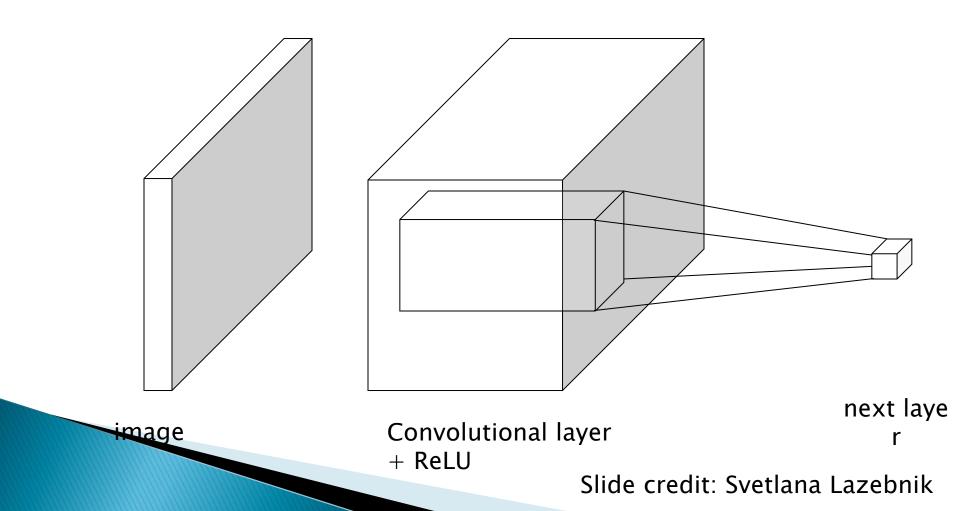
Feature Map Slide credit: Svetlana Lazebnik

# Neural networks for images feature map

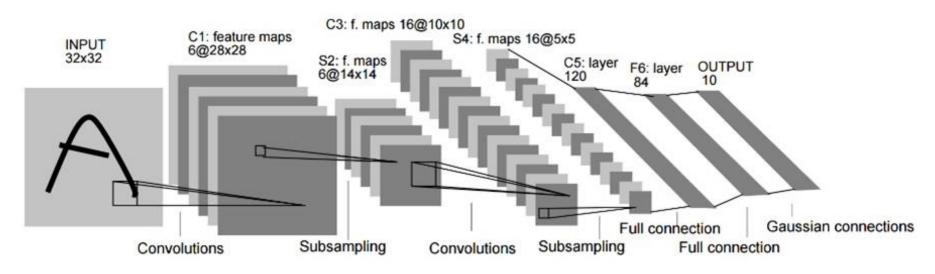


mage

Convolutional layer



# LeNet [LeCun et al. 1998]

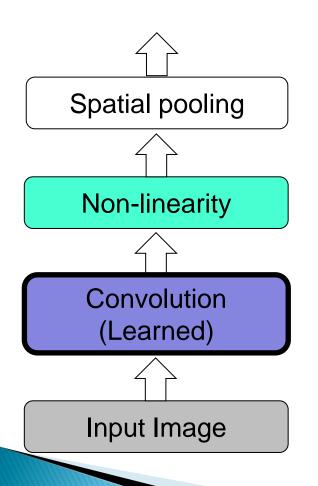




LeNet-1 from 1993

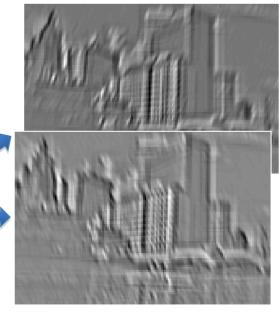
Gradient-based learning applied to document recognition [LeCun, Bottou, Bengio, Haffner 1998]

### Key operations in a CNN



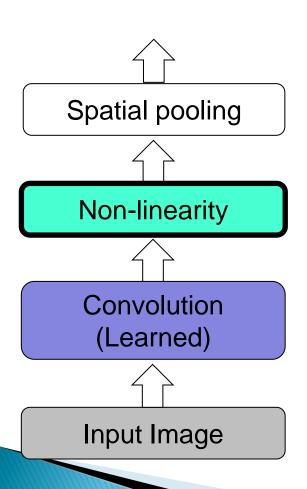




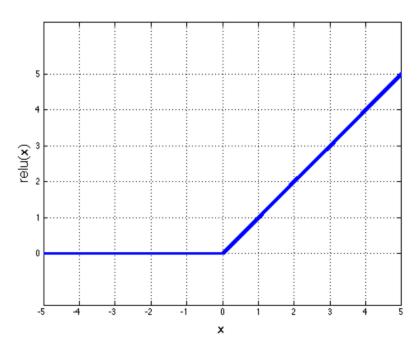


Feature Map

## Key operations in a CNN

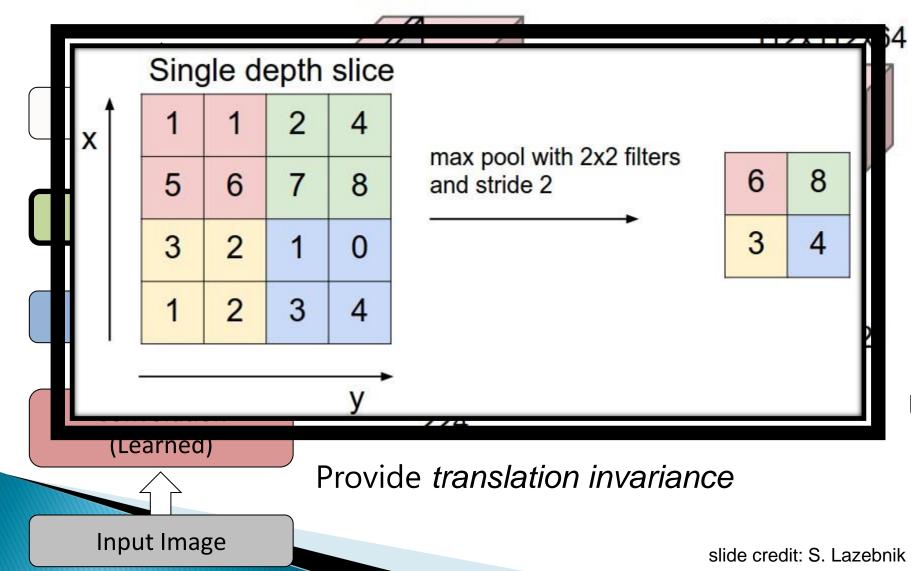


#### Rectified Linear Unit (ReLU)



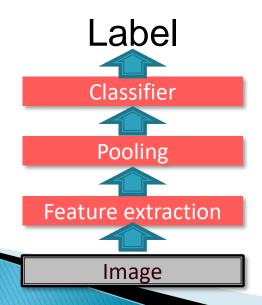
### Key operations in a CNN

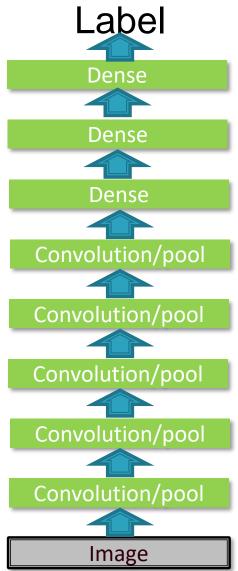
224x224x64



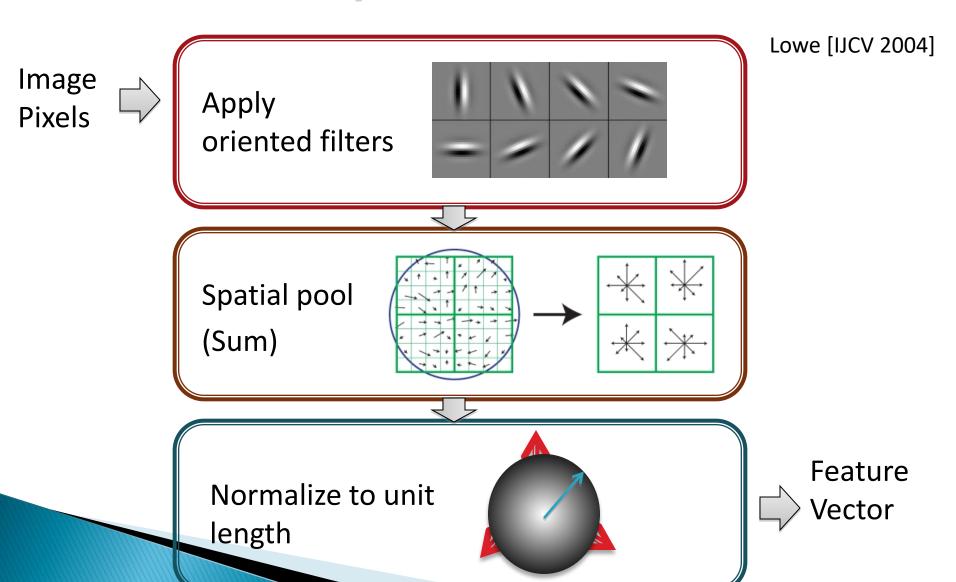
# Engineered vs. learned features

Convolutional filters are trained in a supervised manner by back-propagating classification error



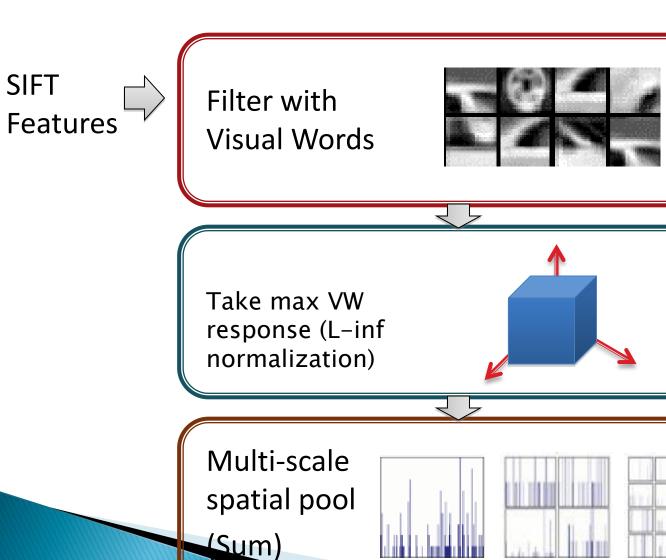


# SIFT Descriptor



slide credit: R. Fergus

# Spatial Pyramid Matching



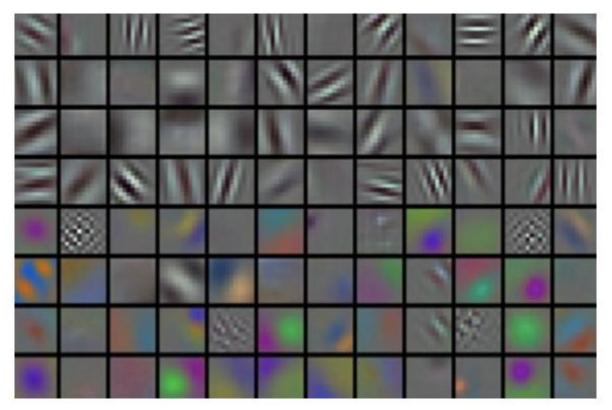
Lazebnik, Schmid, Ponce [CVPR 2006]

Classifier

slide credit: R. Fergus

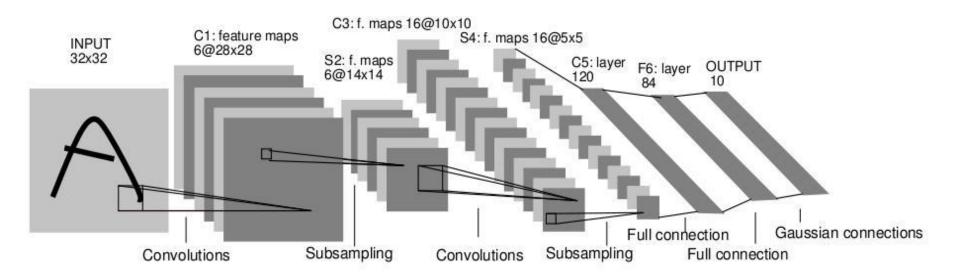
# Visualizing what was learned

What do the learned filters look like?



Typical first layer filters

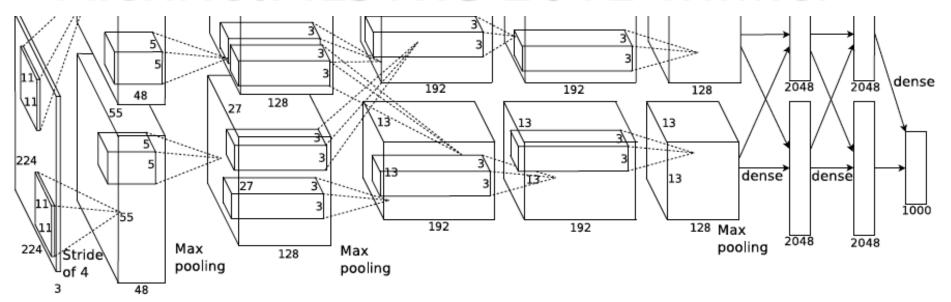
# History of CNNs: LeNet-5



- Average pooling
- Sigmoid or tanh nonlinearity
- Fully connected layers at the end
- Trained on MNIST digit dataset with 60K training examples

Y. LeCun, L. Botte: Y. Bengio, and P. Haffner, Gradient-based learning applied to document recognition, Proc. IEEE 86(11): 2278-2324, 1998.

### AlexNet: ILSVRC 2012 winner



- Similar framework to LeNet but:
  - Max pooling, ReLU nonlinearity
  - More data and bigger model (7 hidden layers, 650K units, 60M pa rams)
  - GPU implementation (50x speedup over CPU)
    - Trained on two GPUs for a week
- Dropout regularization

  A. Krizhevsky, L. Sutskever, and G. Hinton, <u>ImageNet Classification with Deep Co</u>