

HW 4
CS 381

Tian Qiu

1.

(a). (b).

	j	0	1	2	3	4	5	6	7	8	9
I		Y	M	I	N	N	E	S	O	T	A
0	X	0	0	0	0	0	0	0	0	0	0
1	W	0	↑0	↑0	↑0	↑0	↑0	↑0	↑0	↑0	↑0
2	A	0	↑0	↑0	↑0	↑0	↑0	↑0	↑0	↑0	↖ 1
3	S	0	↑0	↑0	↑0	↑0	↑0	↖ 1	↑ 1	↑ 1	↑ 1
4	H	0	↑0	↑0	↑0	↑0	↑0	↑ 1	↑ 1	↑ 1	↑ 1
5	I	0	↑0	↖ 1	← 1	← 1	← 1	↑ 1	↑ 1	↑ 1	↑ 1
6	N	0	↑0	↑ 1	↖ 2	↖ 2	← 2	← 2	← 2	← 2	← 2
7	G	0	↑0	↑ 1	↑ 2	↑ 2	↑ 2	↑ 2	↑ 2	↑ 2	↑ 2
8	T	0	↑0	↑ 1	↑ 2	↑ 2	↑ 2	↑ 2	↑ 2	↖ 3	← 3
9	O	0	↑0	↑ 1	↑ 2	↑ 2	↑ 2	↑ 2	↖ 2	↑ 3	↑ 3
10	N	0	↑0	↑ 1	↖ 2	↖ 3	← 3	← 3	↑ 3	↑ 3	↑ 3

(c).

Another subsequence "INO" "INT" are not discovered.

Because in the algorithm,

if $c[i-1, j] \geq c[i, j-1]$

then go up

We miss the "O".

Because the 4th N in MINNESOTA first matching the 6th N in WASHINGTON.

The second N missed.

Our goal is to find one LCS but not all LCS. So the algorithm makes sense.

2.

First come up to the brain. But time is $O(2^n)$ which is because do not use memorizing method.

```
Count = 0
Function wordbreak(string, N) // N is the size of string
  For I to N:
    Prefix = string.substring(0,I)
    If prefix is a word:
      If I == N:
        Count ++
        Return
      WordBreak( string.substring(I, N-I), N - 1)
    End
  End
End
```

So redo the problem by another way of thinking.

Step1: Characterize the structure of optimal solution

Set function $F[i]$ which means how many ways that substring 0 to index “i” can be separated perfectly

Step2: Recursively define the value of optimal solution

```
If string.substring(j, I) is a word &&  $F[j] \neq 0$ :
   $F[I] += F[j]$ 
```

Step3: Compute the value by bottom-up way

```
For I from 1 to N:
  For j from 0 to I-1:
    If string.substring(j, I) is a word &&  $F[j] \neq 0$ :
       $F[I] += F[j]$ 
  End
End
```

Step4: Construct the solution from step 3

$F[n]$ is exactly how many ways one could break the string into a sequence of words.

Pseudo code:

Function WordBreak (string)

N = length of string

 // initial array F to record how many ways that string can be separated to word

 For $l = 1$ to $N + 1$:

$F[l] = 0$

 End

 // for prefix start from 0

$F[0] = 1$

 For l from 1 to N :

 For j from 0 to $l-1$:

 If string.substring(j, l) is a word && $F[j] \neq 0$:

$F[l] += F[j]$

 End

 End

 Return $F[n]$

Time analyze:

 Because it has two loops and inside the loop, the time is constant. Also the initialization time is constant.

$T(n) = O(N^2)$