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1.  $P(C) = 0.8$       C Event: has chains  
 $P(S|C) = 0.6$       S Event: has shovel  
 $P(S|C') = 0.15$        $P(C') = 0.2$

(1)  $P(S|C) = \frac{P(S \cap C)}{P(C)} = \frac{0.6}{0.8} = \frac{3}{4}$

(2)  $P(S|C') = \frac{P(S \cap C')}{P(C')} = \frac{0.15}{0.2} = \frac{3}{4}$

2.  $P(R) = 0.02$       Event R: Rain on wedding  
 $P(WR|R) = .92$       WR: weather man predicts Rain  
 $P(WR|R') = 4\%$

$$P(R|WR) = \frac{P(R \cap WR)}{P(WR)} = \frac{P(WR|R) \cdot P(R)}{P(WR|R) \cdot P(R) + P(WR|R') \cdot P(R')}$$
$$= \frac{.92 \cdot 0.02}{.92 \times 0.02 + .04 \times 0.98} = 0.319$$

3. (a)  $P(HHH) = 0.78 \times 0.77 \times 0.75 = 0.45$   
Event HHH: All hits

(b)  $P(FFF) = (1-0.78)(1-0.77)(1-0.75) = 0.01265$   
Event FFF: All Fail

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HW3

$$4. (a) P(X=0) = 0.9$$

$$(b) P(X \leq 2) = 0.9 + 0.055 + 0.025 = 0.98$$

$$(c) P(2 \leq X \leq 4) = P(2) + P(3) + P(4) \\ = 0.025 + 0.015 + 0.004 = 0.044$$

$$(d) P(2 < X < 4) = P(3) = 0.015$$

$$5. (a) \text{Var}(X) = E([X - E(X)]^2) \quad \text{let } E(X) = \mu_X \\ = E(X^2 - 2X\mu_X + \mu_X^2) \\ = E(X^2) - 2E(X\mu_X) + E(\mu_X^2) \\ = E(X^2) - 2E(X) \cdot \mu_X + E(\mu_X^2) \\ = E(X^2) - 2\mu_X^2 + \mu_X^2 \\ = E(X^2) - \mu_X^2 = E(X^2) - [E(X)]^2 \quad \text{proved}$$

$$6. E(g(X)) = E(ax + b) \\ = aE(X) + b \\ = a \sum x \cdot p(x) + \sum p(x) \cdot b \\ = \sum p(x) \cdot (ax + b) \\ = \sum p(x) g(x) \quad \text{proved}$$



$$7. (a). E(X) = \sum X \cdot p(x) = 2 \times 0.2 + 3 \times 0.05 + 5 \times 0.25 + 7 \times 0.3 + 11 \times 0.15 + 13 \times 0.05$$

$$= 8$$

$$(b) \text{Var}(X) = E(X - \mu)^2$$

$$= (2-8)^2 \times 0.2 + (3-8)^2 \times 0.05 + 3^2 \times 0.25 + 1^2 \times 0.3 + 3^2 \times 0.15$$

$$+ (13-8)^2 \times 0.05$$

$$= 13.6$$

$$\sigma_X = \sqrt{\text{Var}(X)} = 3.687$$

$$(c) Y = 2X + 1$$

$$E(Y) = 2E(X) + 1 = 17$$

$$(d) \text{Var}(Y) = \text{Var}(2X + 1) = 4\text{Var}(X) = 4 \times 13.6 = 54.4$$

$$(e) \sigma_Y = \sqrt{54.4} = 7.376$$

$$(f) E(W) = E(X^2) + 1 = 4 \times 0.2 + 9 \times 0.05 + 25 \times 0.25 + 49 \times 0.3 + 121 \times 0.15 + 169 \times 0.05$$

$$= 49.8$$

$$8. (a). E(X) = \sum X \cdot p(x) = 0.9$$

$$(b) P(X < 0.9) = P(0) = 0.6$$

$$(c) P(X \geq 4 \cap X \geq 4) = P(X \geq 4) = (0.075)^2 = 0.005625$$